

Exercise (Day 3): Testing with Properties

In today's exercise we will develop a variety of properties for testing the binary search tree implementation discussed in yesterday's lecture. The materials provided include a correct implementation in `BST.hs`, and the properties presented on the slides in `BSTSpec.hs`. `BSTSpec` uses Template Haskell and **quickCheckAll** to define **runTests**, which tests all the properties in the module. Make sure you can run these tests, and use this file as a starting point for your work. As you develop new properties, you should make sure they continue to pass for `BST.hs`. The files `BST1.hs` ... `BST8.hs` contain different buggy versions of `BST.hs`, with a different bug in each file. **Do not read these files**; we will use them later to practice diagnosing bugs by testing.



Writing Properties for BST

As you write properties to solve the next exercises, make sure you test each property as soon as you have written it, either by running `quickCheck` with the property as an argument, or by using **runTests** to test all the properties in the `BSTSpec` module. Since you are testing a *correct* implementation, all the properties you write should pass. (If a property fails, you need to correct the property, not the code!)

1. `BSTSpec` contains a *validity property* for **insert**. Add similar properties for **nil**, **delete**, and **union**.
2. `BSTSpec` contains *postcondition properties* for **find** and **insert**. Add postconditions for **delete** and **union**.
3. `BSTSpec` contains *metamorphic properties* for **size/insert** and **insert/insert**. Add further metamorphic properties to test **insert**, **delete**, and **union**.
4. `BSTSpec` contains a *model based property* for **insert**. Add model-based properties to test **find**, **nil**, **delete**, and **union**.

Diagnosing Bugs with Properties

Once you are satisfied with your properties, try using them to diagnose buggy implementations. The files `BST1.hs` ... `BST8.hs` contain different buggy versions of `BST.hs`, with a different bug in each file. **Do not read these files**. Four bugs are revealed by the original `BSTSpec.hs` provided, and four slip through. Each of these versions can be tested using `BSTSpec.hs`, by changing **import BST** to **import BST1** ... **import BST8**.

5. Run your tests on each of the buggy implementations, using **runTests**. If any implementation passes all your tests, something is wrong!
6. Which properties are most effective at revealing errors?
7. Use the counterexamples found to diagnose each bug. Which properties give the most helpful output? Once you think you know what the bug is, you may inspect the implementation to see if you are right.

Generating Equations with QuickSpec

To do this exercise, you will need to install `QuickSpec`. Assuming you are using `cabal`, you should be able to do so with the command

```
cabal install quickspec
```

If you encounter installation problems, then I suggest installing QuickSpec in an Ubuntu virtual machine instead.

The file `BST_QuickSpec.hs` runs QuickSpec to generate properties of the binary search tree API. Make sure you can compile and run this program:

```
ghci BST_QuickSpec  
main
```

You should see equations involving **find**, **nil** and **insert** generated. You may find it useful to put these functions into the background before rerunning QuickSpec, which can be done by applying **background** to a single signature entry, or a list of entries. The effect is to suppress equations that only involve background functions from the output (although they are still generated internally).

8. Add **delete** to the signature supplied to QuickSpec, and generate a new set of equations. Are the equations generated for **delete** reasonable?
9. Add **union** to the signature, and inspect the generated equations. Is there one that you might expect to see in a more general form? If so, make a note of it.
10. Define a new function **notKey k t = k `notElem` keys t**, and add it as a predicate to the QuickSpec signature. Inspect the properties discovered of **notKey**; is there a generalization of the equation you noted in the previous step?

(If you find that QuickSpec generates conditional equations with conditions involving variables that do not appear in the equation, you can usually eliminate them by adding **withMaxTests 100000** to the signature. These odd conditions sometimes appear because QuickSpec runs too few tests satisfying the condition to eliminate them; adding **withMaxTests** to the signature causes QuickSpec to run 100 times as many tests as usual—making equation generation slow, but more accurate.)