## Week 2: DFA and NFA

1. Exercise 2.2.1
2. Suppose $\Sigma=\{a, b\}$. Build a DFA that accepts exactly the words containg $b b a$ as a subword. Build then a DFA that accepts exactly the words not containing bba as a subword.
3. If $L \subseteq \Sigma^{*}$ is regular then so is $L^{R}=\{\operatorname{rev}(x) \mid x \in L\}$ (Hint: given a NFA for $L$ build a NFA for $L^{R}$ )
4. Suppose $\Sigma=\{a, b, c\}$. Build a DFA $A_{1}$ that accepts exactly the words containing $a c$ as a subword. Build a DFA $A_{2}$ that accepts exactly the words containing $a b$ as a subword. Using the product construction, build then a DFA for the words containing both $a b$ and $a c$ as subword, and one for the words containing $a c$ but not $a b$ as subword.
5. Build a DFA that recognizes exactly the word in $\{0,1\}^{*}$ ending with the string 0100 .
6. A ship attempts to transmit data to shore at random intervals. The receiver must continually listen and recognize when an actual transmission starts so that it can record the data that follows. Let us assume that the start of the transmission is signaled by the string 010010 and the end of transmission is signaled by the string 000111. Represent this behaviour with a DFA.
7. In a factory, we have the possible events $a, b, c$. A constraint $L_{1}$ is that if the event $b$ occurs after the event $a$, then the event $c$ should occur in between. Represent this constraint $L_{1}$ as a DFA $A_{1}$.
Suppose that there is another constraint $L_{2}$ that if the event $b$ occurs after the event $c$, then the event $a$ should occur in between. Explain intuitively why, if we have both constraints $L_{1}$ and $L_{2}$ then the event $b$ cannot occur after the event $a$. Represent the constraint $L_{2}$ as a DFA $A_{2}$. Do the product construction of $A_{1}$ and $A_{2}$ to have an automaton representing the conjunction of the constraint $L_{1}$ and $L_{2}$. Verify on this automaton that $b$ cannot occur after $a$ or $c$.
