Programming Language Technology

Exam, 12 April 2022 at 08.30 – 12.30 in M

Course codes: Chalmers DAT151, GU DIT231.

Exam supervision: Andreas Abel (+46 31 772 1731), visits at 09:30 and 11:30.

Grading scale: Max = 60p, VG = 5 = 48p, 4 = 36p, G = 3 = 24p.

Allowed aid: an English dictionary.

Exam review: 28 April 2022 13.30-14.30 in EDIT meeting room 6128 (6th floor).

Please answer the questions in English.

Question 1 (Grammars): Write a labelled BNF grammar that covers the following kinds of constructs of C/C++ (sublanguage of lab 2):

- Program: a sequence of function definitions.
- Function definition: type, identifier, comma-separated parameter list in parentheses, block.
- Parameter: type followed by identifier, e.g. int x.
- Block: a sequence of statements enclosed between { and }
- Statements:
 - block
 - initializing variable declaration, e.g., int x = 5;
 - return statement
 - if-else statement
- Expressions, from highest to lowest precedence:
 - parenthesized expression, identifier, integer literal
 - addition (+), left associative
 - less-than comparison (<), non-associative
 - short-circuiting conjunction (&&), left associative
- Type: int or bool

You can use the standard BNFC categories Integer and Ident and the list pragmas terminator and separator, but *not* the coercions pragma. An example program is:

```
int f (int x, bool b) {
  int z = x + x;
  if (b && z < 10) {
    int x = z + z;
    return x;
  } else return 0;
}</pre>
```

```
SOLUTION:
Program. Prg ::= [Def]
         Def ::= Type Ident "(" [Arg] ")" "{" [Stm] "}" ;
terminator Def ""
ADecl.
         Arg ::= Type Ident
separator Arg ","
          Stm ::= "{" [Stm] "}"
SBlock.
          Stm ::= Type Ident "=" Exp ";"
SInit.
SReturn. Stm ::= "return" Exp ";"
         Stm ::= "if" "(" Exp ")" Stm "else" Stm
SIfElse.
terminator Stm ""
EId.
        Exp3 ::= Ident
EInt.
        Exp3 ::= Integer
        Exp2 ::= Exp2 "+" Exp3
EPlus.
          Exp1 ::= Exp2 "<" Exp2
ELt.
EAnd.
          Exp
               ::= Exp "&&" Exp1
          Exp3 ::= "(" Exp ")"
          Exp2 := Exp3
_.
          Exp1 ::= Exp2
          Exp := Exp1
          Type ::= "int"
TInt.
TBool.
          Type ::= "bool"
```

Question 2 (Lexing): An non-nested Haskell comment starts with {- and ends with -} and can have any characters in between (but not the comment-end sequence -} of course). Also, {-} is not a valid comment.

- 1. Give a deterministic finite automaton for such comments with no more than 8 states. Remember to mark initial and final states appropriately.
- 2. Give a regular expression for such comments.

Work in the alphabet distinguishing 4 tokens: $\{,\}, -$, and c where c stands for any other character. (6p)

SOLUTION:

1. DFA:

2. RE:
$$\{-\left(\left(c \mid \{\mid\}\right)^* - + \left(c \mid \{\right)\right)^* - + \}$$

Question 3 (LR Parsing): Use your grammar from Question 1. Step by step, trace the shift-reduce parsing of the expression b & z < 10 showing how the stack and the input evolve and which actions are performed. (8p)

SOLUTION: The actions are shift, reduce with rule(s), and accept. Stack and input are separated by a dot.

```
. b && z < 10 -- shift
                       . \&\& z < 10
Ident
                                      -- reduce with rule EId
                       . \&\& z < 10
                                      -- reduce with coercion rules
Exp3
Exp
                       . \&\& z < 10
                                      -- shift 2x
                                      -- reduce with rule EId
Exp && Ident
                       . < 10
Exp && Exp3
                                      -- reduce with coercion rule
                       . < 10
Exp && Exp2
                       . < 10
                                      -- shift 2x
Exp && Exp2 < Integer .
                                      -- reduce with rule EInt
                                      -- reduce with coercion rule
Exp && Exp2 < Exp3
                                      -- reduce with rule ELt
Exp \&\& Exp2 < Exp2
Exp && Exp1
                                      -- reduce with rule EAnd
                                      -- accept
Exp
```

Question 4 (Type checking and evaluation):

1. Write syntax-directed type checking rules for the statement forms and blocks of Question 1. The form of the typing judgements should be $\Gamma \vdash_t s \Rightarrow \Gamma'$ where s is a statement or list of statements, t the return type, Γ is the typing context before s, and Γ' the typing context after s. Observe the scoping rules for variables! You can assume a type-checking judgement $\Gamma \vdash e : t$ for expressions e.

Alternatively, you can write the type checker in pseudo code or Haskell (then assume **checkExpr** to be defined). In any case, the typing environment and the return type must be made explicit. (6p)

SOLUTION: A context Γ is a stack of blocks Δ , separated by a dot. Each block Δ is a map from variables x to types t. We write $\Delta, x:t$ for adding the binding $x \mapsto t$ to the map. Duplicate declarations of the same variable in the same block are forbidden; with $x \notin \Delta$ we express that x is not bound in block Δ . We refer to a judgement $\Gamma \vdash e:t$, which reads "in context Γ , expression e has type t".

$$\frac{\Gamma. \vdash_t ss \Rightarrow \Gamma.\Delta}{\Gamma \vdash_t \{ss\} \Rightarrow \Gamma} \qquad \frac{\Gamma.\Delta, x:t' \vdash e:t'}{\Gamma.\Delta \vdash_t t' x = e \; ; \Rightarrow (\Gamma.\Delta, x:t')} \; x \not\in \Delta$$

$$\frac{\Gamma \vdash e:t}{\Gamma \vdash_t \mathsf{return}\, e; \Rightarrow \Gamma} \qquad \frac{\Gamma \vdash e:\mathsf{bool} \qquad \Gamma. \vdash_t s_1 \Rightarrow \Gamma.\Delta_1 \qquad \Gamma. \vdash_t s_2 \Rightarrow \Gamma.\Delta_2}{\Gamma \vdash_t \mathsf{if} \; (e) \; s_1 \, \mathsf{else}\, s_2 \Rightarrow \Gamma}$$

This judgement for statements is extended to sequences of statements $\Gamma \vdash_t ss \Rightarrow \Gamma'$ by the following rules (ε stands for the empty sequence):

$$\frac{\Gamma \vdash_t s \Rightarrow \Gamma' \qquad \Gamma' \vdash_t ss \Rightarrow \Gamma''}{\Gamma \vdash_t ss \Rightarrow \Gamma''}$$

2. Write syntax-directed interpretation rules for the expressions of Question 1. The form of the evaluation judgement should be $\gamma \vdash e \Downarrow v$ where e denotes the expression to be evaluated in environment γ and v the resulting value.

Alternatively, you can write the interpreter in pseudo code or Haskell. A function lookupVar can be assumed if its behavior is described. In any case, the environment must be made explicit. (6p)

SOLUTION: The evaluation judgement $\gamma \vdash e \Downarrow v$ for expressions is the least relation closed under the following rules.

Herein, environment γ is map from identifiers to integers. Boolean true is represented by integer 1, and false by 0.

Question 5 (Compilation):

1. Translate the example program of Question 1 to Jasmin. It is not necessary to remember exactly the names of the JVM instructions—only what arguments they take and how they work. Make clear which instructions come from which statement, and determine the stack and local variable limits. (8p)

```
SOLUTION:
.method public static f(ZI)I
.limit locals 4
.limit stack 2
;; int z = x + x;
iload_0
iload_0
iadd
istore_2
;; if (b \&\& z < 10)
iload_1
ifeq LElse
iload_2
bipush 10
if_icmpge LElse
;; int x = z + z;
iload_2
iload_2
iadd
istore_3
;; return x;
iload_3
ireturn
LElse:
;; return 0;
iconst_0
ireturn
.end method
```

2. Give the small-step semantics of the JVM instructions you used in the Jasmin code in part 1 (except for return instructions). Write the semantics in the form

$$i:(P,V,S)\longrightarrow(P',V',S')$$

where (P, V, S) is the program counter, variable store, and stack before execution of instruction i, and (P', V', S') are the respective values after the execution. For adjusting the program counter, you can assume that each instruction has size 1. (6p)

SOLUTION: Stack S.v shall mean that the top value on the stack is v, the rest is S. Jump targets L are used as instruction addresses, and P+1 is the instruction address following P.

```
instruction
                 state before
                                        state after
                  (P, V, S.0)
ifeq L
                                   \rightarrow (L, V, S)
                                   \rightarrow (P+1, V, S)
                  (P, V, S.v)
                                                                   if v \neq 0
ifeq L
if\_icmpge\ L\ (P, V, S.v.w)
                                   \rightarrow (L, V, S)
                                                                   if v > w
if\_icmpge\ L\ (P, V, S.v.w)
                                   \rightarrow (P+1, V, S)
                                                                   unless v \ge w
                  (P, V, S)
                                   \rightarrow (P+1, V, S.V(a))
{\tt iload} \ a
istore a
                  (P, V, S.v)
                                   \rightarrow (P+1, V[a:=v], S)
                                   \rightarrow (P+1, V, S.i)
iconst i
                  (P, V, S)
                  (P, V, S)
                                   \rightarrow (P+1, V, S.i)
bipush i
                  (P, V, S.v.w) \rightarrow (P+1, V, S.(v+w))
iadd
```

Question 6 (Functional languages):

1. The following grammar describes a tiny simply-typed sub-language of Haskell.

Application e_1 e_2 is left-associative, the arrow $t_1 \to t_2$ is right-associative. Application binds strongest, then addition, then λ -abstraction.

For the following typing judgements $\Gamma \vdash e : t$, decide whether they are valid or not. Your answer can be just "valid" or "not valid", but you may also provide a justification why some judgement is valid or invalid.

The usual rules for multiple-choice questions apply: For a correct answer you get 1 point for a wrong answer -1 points. If you choose not to give an answer for a judgement, you get 0 points for that judgement. Your final score will be between 0 and 5 points, a negative sum is rounded up to 0. (5p)

SOLUTION:

- (a) valid
- (b) valid
- (c) not valid
- (d) valid
- (e) not valid (cannot add 0 to function)

2. Write a **call-by-name** interpreter for the functional language above, either with inference rules or in pseudo code or Haskell. (5p)

```
SOLUTION:
type Var = String
data Exp
 = EInt Integer | EPlus Exp Exp
  | EVar Var | EAbs Var Exp | EApp Exp Exp
data Val = VInt Integer | VClos Var Exp Env
data Clos = Clos Exp Env
type Env = [(Var,Clos)]
eval :: Exp 
ightarrow Env 
ightarrow Maybe Val
eval e0 rho = case e0 of
 EInt n \rightarrow return (VInt n)
 EAbs x e \rightarrow return (VClos x e rho)
 EPlus e f \rightarrow do
    VInt n \leftarrow eval e rho
    VInt m \leftarrow eval f rho
    return (VInt (n + m))
 EVar x \rightarrow do
    Clos e rho' \leftarrow lookup x rho
    eval e rho'
 EApp f e \rightarrow do
    VClos x f' rho' \leftarrow eval f rho
    eval f' ((x, Clos e rho) : rho')
```