

Surface Scattering

Surface Scattering

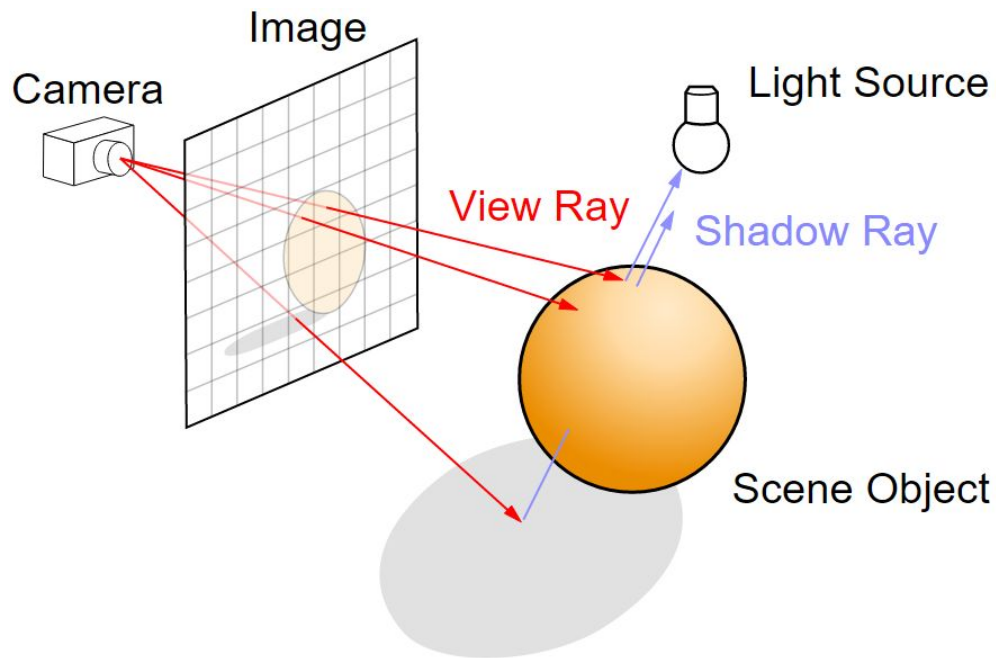
(not **sub**surface scattering)

Surface Scattering

- Ray tracing
- Materials
- B $\times$ DF Models
 - Bi-directional $\times$ Distribution Function
 - B $\mathcal{R}$ DF: Reflectance
 - B $\mathcal{T}$ DF: Transmission
 - B $\mathcal{S}$ DF: Scattering (= B $\mathcal{R}$ DF + B $\mathcal{T}$ DF)
 - B $\mathcal{SSR}$ DF - Scattering-surface reflectance
 - Subsurface scattering

Ray Tracing

- Trace rays through plane
- Camera effects
- Sampling schemes
- Speed-up techniques



Ray Tracing

- Spheres
- Diffuse, specular, (glossy)
- Reflection, refraction
- (Textures)

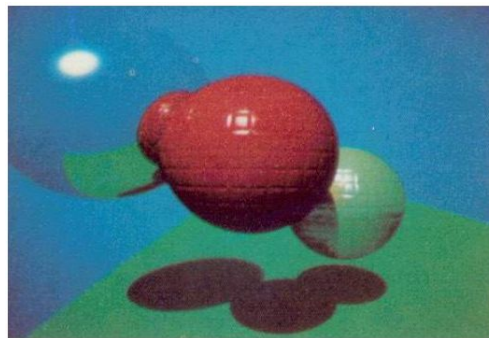


Figure 5



Figure 7

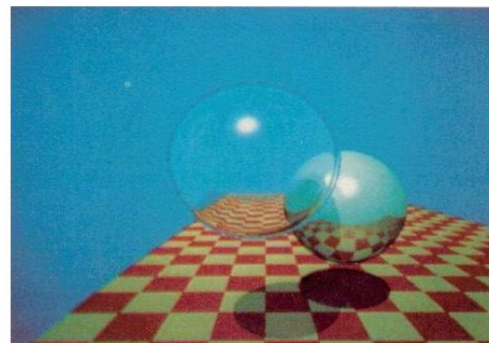


Figure 6

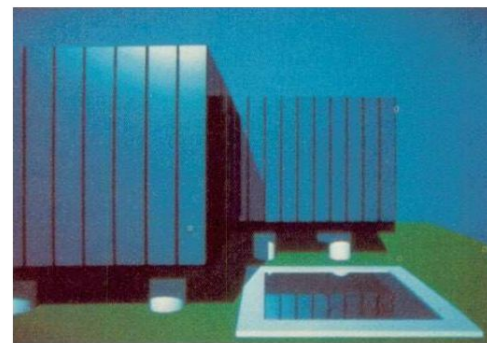


Figure 8

Turner Whitted (1980)

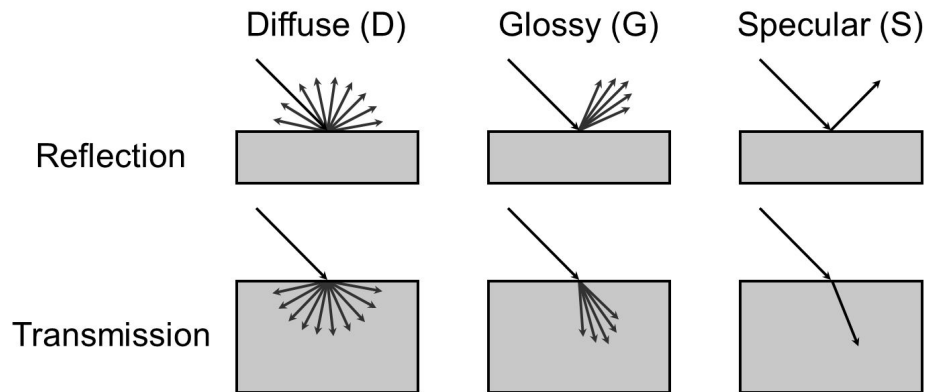
“An improved illumination model for shaded display”

Figure 5: Jim Blinn (1978)

“Simulation of wrinkled surfaces” (Bump mapping)

Ray Tracing

- Diffuse (or “Lambertian”)
 - Uniform sampling
- Specular
 - Perfect reflection
- (Glossy)
 - “glossiness” parameter



Scale

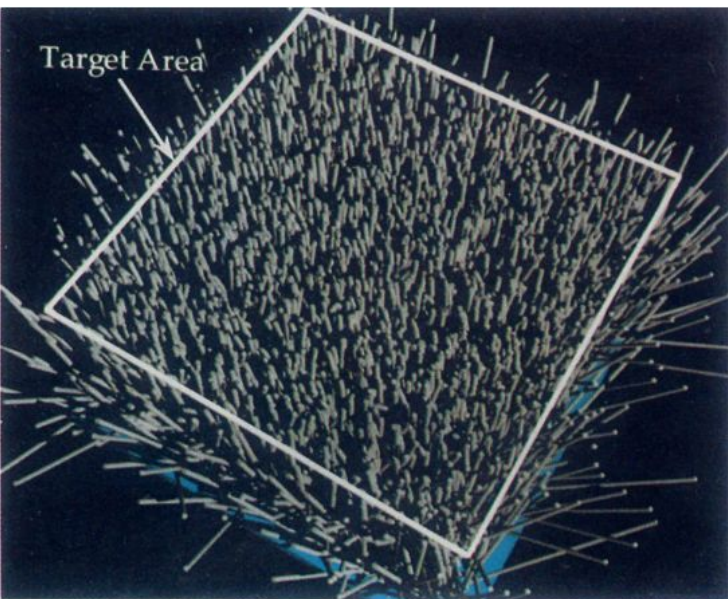


Figure 11: Microscale Geometry for Velvet

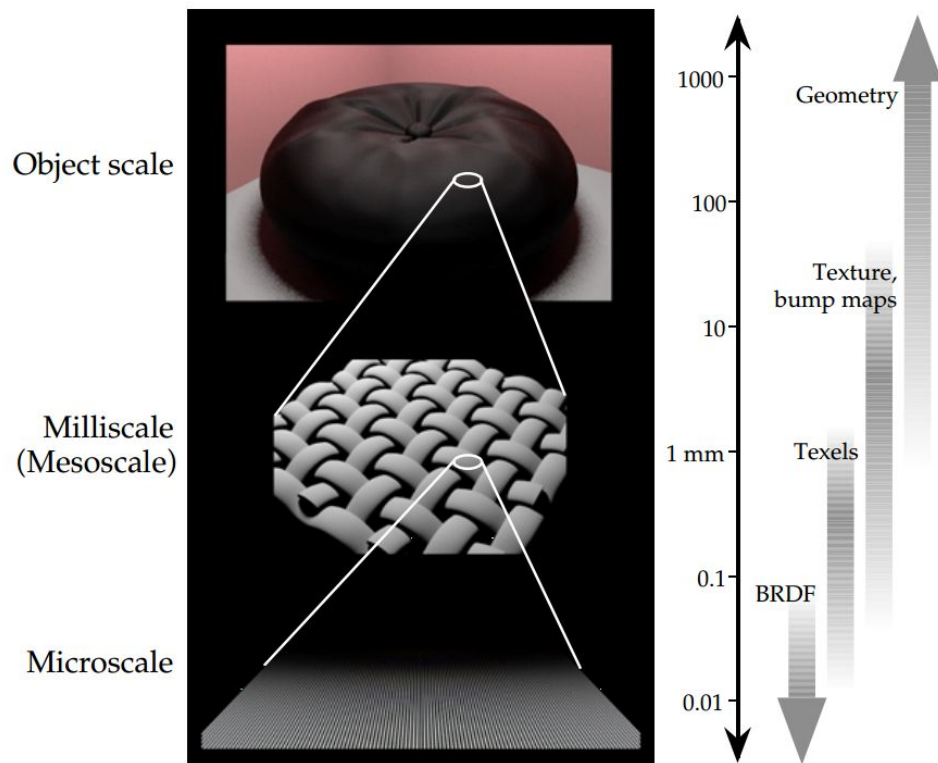
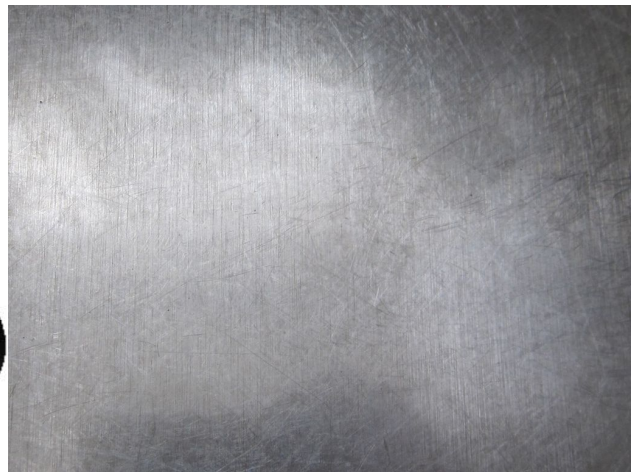
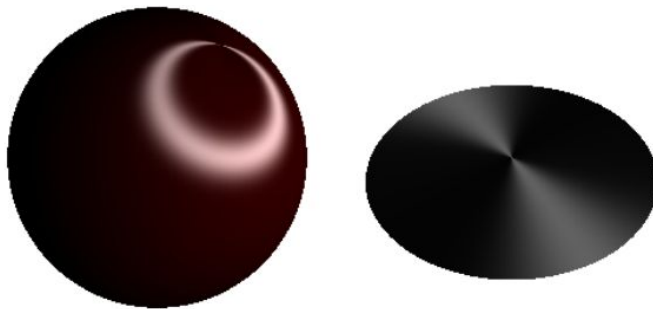
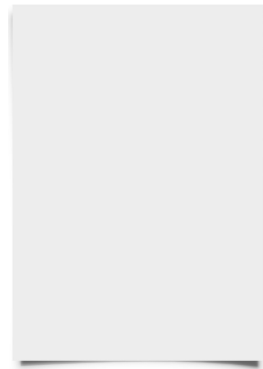


Figure 1: Applicability of Techniques

Materials

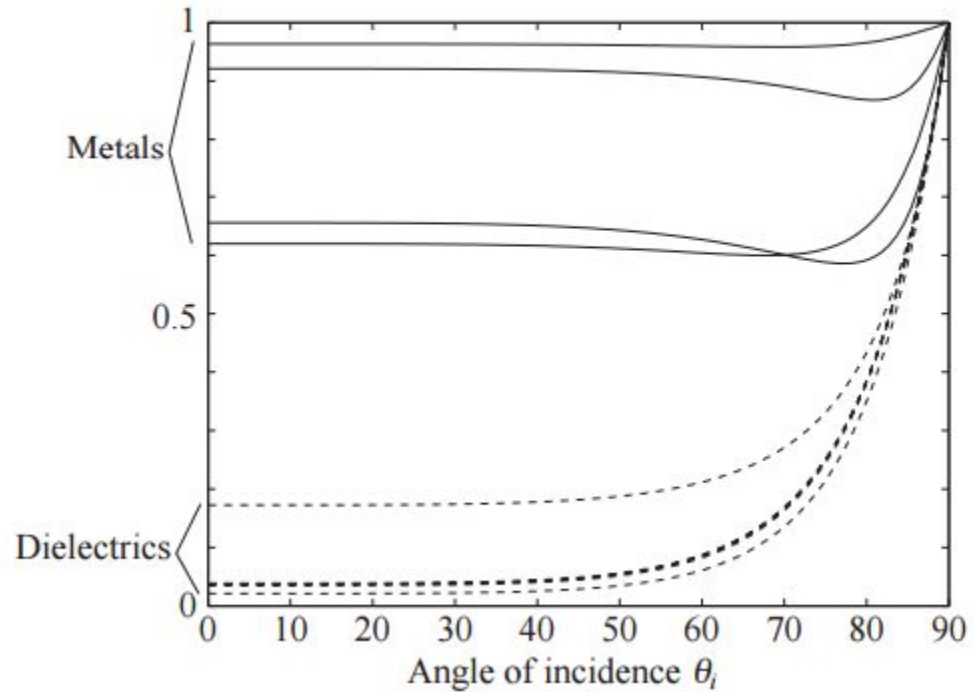
- Isotropic
 - Reflectance invariant of rotation about the surface normal
 - Paints, papers, plastics, (sandblasted) metals
- Anisotropic
 - Not isotropic
 - Roughness **biased** in some direction
 - Materials with grains, fibers, grooves, crystalline structures
 - Wood, brushed metal, marble



[Heidrich-Seidel]
*Efficient Rendering of Anisotropic Surfaces
Using Computer Graphics Hardware (1998)*

Materials

- Metals
 - Conductors
- Dielectrics
 - Insulators
 - Glass, plastic...
- (Semiconductors)
 - Rare in practice, often ignored



Specular reflectance by angle of incidence.
Perfectly smooth surfaces.

Materials

- Metals
 - Prevents subsurface scattering
 - Absorbs all energy within a fraction of one wavelength
- Dielectrics
 - **Black dielectrics** absorb all energy, but over a longer distance
 - Other dielectrics reflect significant energy by subsurface scattering
 - “**All non-metallic materials are translucent to some degree**” - Henrik Wann Jensen

Materials

Wave property of light vs. Surface roughness

- X-rays (0.01-20 nm)
- Ultraviolet light (100-400 nm)
- Visible light (400-700 nm)
- Infrared (800-1000 nm)
- microwave (1-1000 mm)

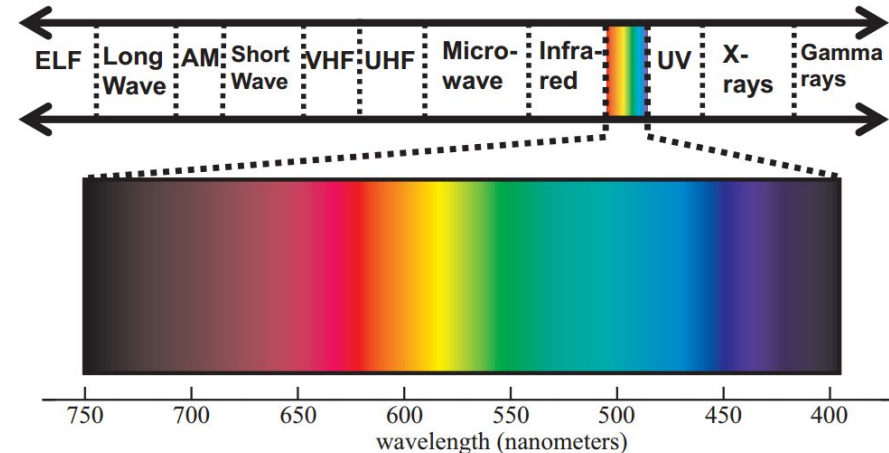


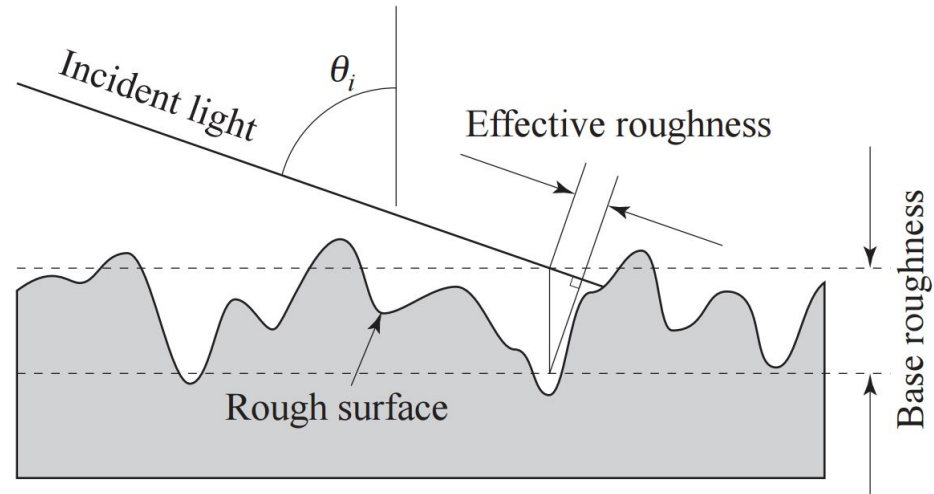
Figure 2: The visible spectrum.

Materials: Smooth surfaces

- Surfaces with low roughness:
- ρ : specular reflectance
- $F - \rho$: non-specular reflectance
- As the exponent approaches 0, all energy becomes specular reflectance

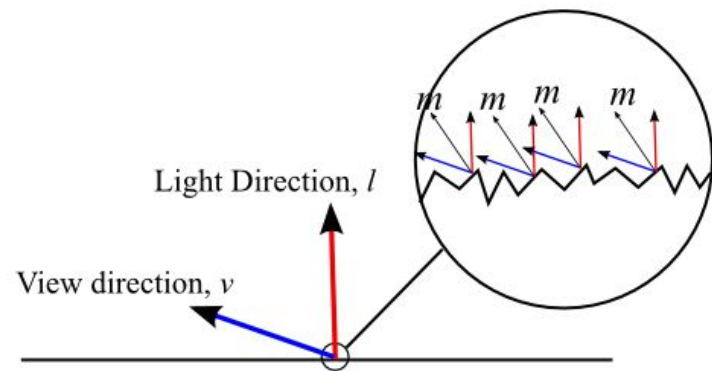
$$\rho \approx F e^{-\left(4\pi \frac{\sigma}{\lambda} \cos \theta_i\right)^2}$$

- Rough surfaces can look smooth
 - Effective roughness ≈ 0



Materials: Rough surfaces

- Roughness much greater than wavelength
- Rough surfaces:
 - “A set of faces with different slopes” or “microfacets”
 - Detectable with visible light (**millimeter** scale)
- Rough surface models
 - Phong, 1975
 - Cook & Torrance, 1982
 - Ward, 1992
 - Oren-Nayar, 1994



Reflectance models

- Lambertian (*diffusely reflecting*):

$$L_r = \frac{\rho}{\pi} \cos(\theta_i) E_0$$

- Oren-Nayar:

$$L_r = \frac{\rho}{\pi} \cos(\theta_i) S E_0$$

$$S = A + (B \max[0, \cos(\phi_i - \phi_r)] \sin \alpha \tan \beta)$$

$$A = 1 - 0.5 \frac{\sigma^2}{\sigma^2 + 0.57}$$

$$B = 0.45 \frac{\sigma^2}{\sigma^2 + 0.09}$$

$$\alpha = \max(\theta_i, \theta_r)$$

$$\beta = \min(\theta_i, \theta_r)$$



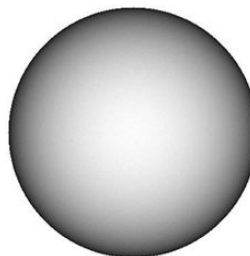
Real Image



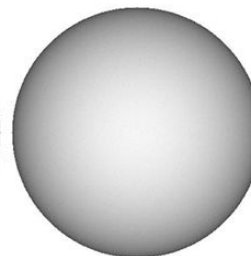
Lambertian Model



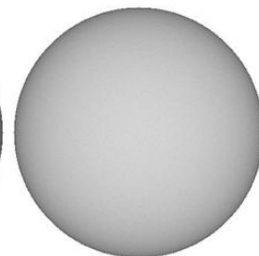
Oren-Nayar Model



$\sigma = 0$



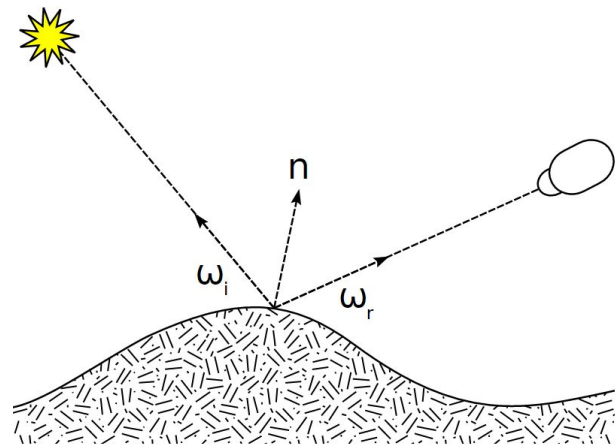
$\sigma = 0.1$



$\sigma = 0.3$

Models: BRDF

- BRDF (Bidirectional reflectance distribution function)
 - Assumes that light enters and leaves at the same point
 - Incoming direction $\mathbf{w}_i$, outgoing direction $\mathbf{w}_o$
 - BRDF: Ratio of reflected radiance exiting along $\mathbf{w}_o$ to the irradiance incident to $\mathbf{w}_i$
- Physically plausible if...
 - Always positive
 - Reciprocal: $\mathbf{w}_i$, $\mathbf{w}_o$ can be swapped for the same result
 - Energy-conserving: sum over the hemisphere is **one or less**.*
- Part of the rendering equation (...)



* Error in reading material: " $\sum f \geq 1$ "

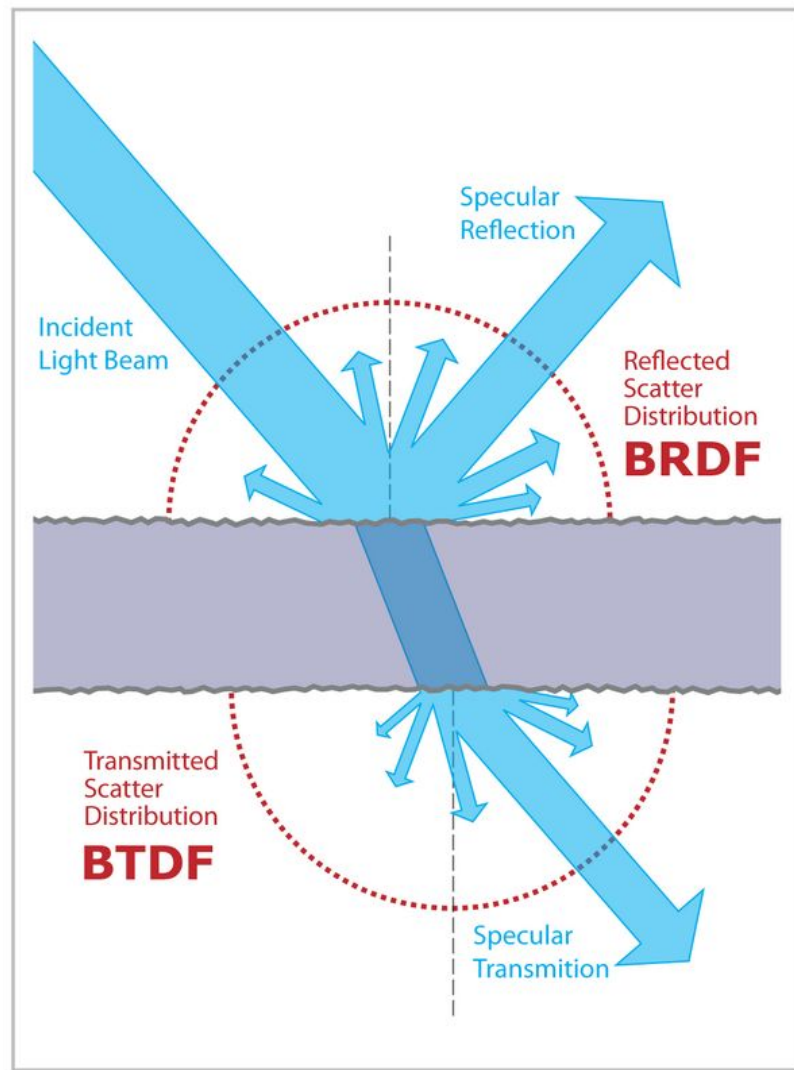
The Rendering Equation

- The radiance is...
 - **Emitted** radiance, plus
 - **Reflected** radiance, over all incoming directions $\mathbf{w}_i$ of the hemisphere Ω along $\mathbf{w}_o$

$$L_o(\mathbf{x}, \boldsymbol{\omega}_o, \lambda) = L_e(\mathbf{x}, \boldsymbol{\omega}_o, \lambda) + \int_{\Omega} \underline{f(\mathbf{x}, \boldsymbol{\omega}_i, \boldsymbol{\omega}_o, \lambda)} L_i(\mathbf{x}, \boldsymbol{\omega}_i, \lambda) \cos \theta d\boldsymbol{\omega}_i$$

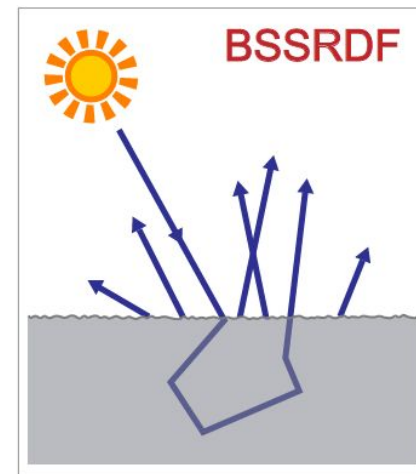
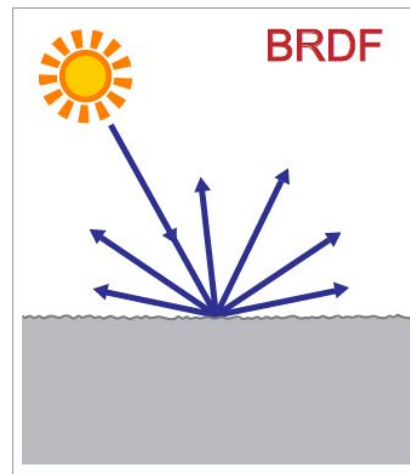
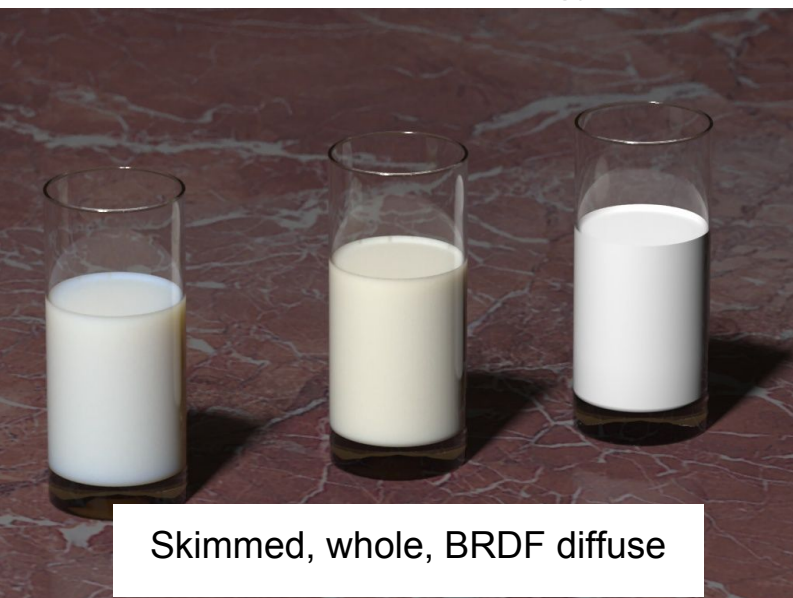
Models: B^TDF, B^SDF

- B^TDF: Transmission
- B^SDF: B^RDF + B^TDF



Models: BSSRDF

- BSSRDF (Bidirectional reflectance distribution function)
 - General case of BRDF
 - Entry and exit point do not have to be the same
 - Same laws (energy conservation, reciprocity)



Subsurface Scattering

- Not obvious to take into account
- Obvious when the effect is missing



Subsurface Scattering

- Translucent materials
 - Wax, milk, marble
- Different shapes and colors inside
 - Leaves, skin
- Light enters, scatters within, and exits
- Some light may be absorbed

Subsurface Scattering

- Single scattering approximation
 - A single bounce
 - Estimate number of photons reflected toward camera
- Depth map approximation
- Texture space diffusion
 - “General blurring of the diffuse lighting”

Subsurface Scattering - Multiple Layers

- Light Diffusion in Multi-Layered Translucent Materials ([2005](#))
 - The skin is composed of **three layers**: epidermis, dermis, and the bloody dermis.
 - Scattering parameters for the layers are from **measured data** in medical literature.
 - The multilayered model gives the skin a **less waxy look** compared to the standard BSSRDF
- Reflectance and transmittance over radial distance
- Unique functions per layer



Jade

Jade + paint

Figure 5: A buddha statuette sprayed with a thin layer of white paint. The first and third images are front-lit, the second and fourth back-lit.

Models: BRDF

- Many models
 - Difference in highlights
 - Size, fall-off
- Physically plausible
 - Cook-Torrance (1982)
 - GGX (2007)
 - Schlick (1994)
 - Oren-Nayar (non-simplified; 1994)



Chrome, GGX, Beckmann

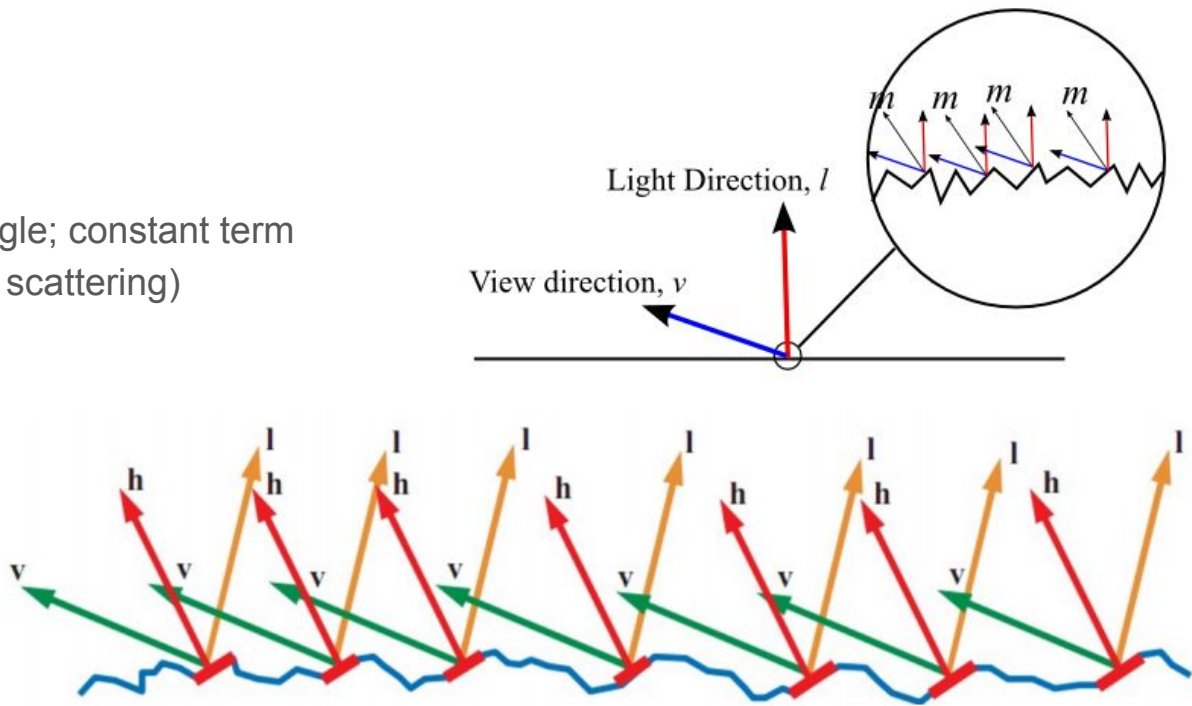
Source: *Physically-Based Shading at Disney* (2012)

Cook-Torrance

Paper:

*A Reflectance Graphics Model for
Computer Graphics (1982)*

- Two components
 - $\mathbf{f} = d\mathbf{f}_{\text{diff}} + s\mathbf{f}_{\text{spec}}$
 - Weights: $d + s = 1$
- Diffuse
 - “Body reflectance”
 - Independent of viewing angle; constant term
 - (Approximates subsurface scattering)
- Specular
 - “Surface reflectance”
 - Models **microfacets**
 - $\mathbf{h} = \text{normalize}(\mathbf{l} + \mathbf{v})$
 - Contributes if $\mathbf{h} \cdot \mathbf{n} > 0$



Cook-Torrance: Microfacet phenomena

- Shadowing
 - Light-occlusion by microgeometry
 - “Self-shadowing”
- Masking
 - Visibility-occlusion by microgeometry
 - “Self-occlusion”
- Interreflections
 - When facets reflect onto other facets
 - Not taken into account

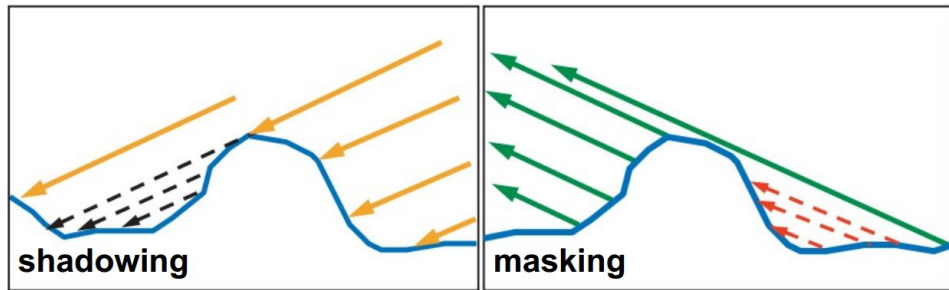


Figure 2: On the left, occlusion of light source by microgeometry (shadowing). On the right, visibility occlusion of microgeometry (masking). Source: [1]

Cook-Torrance:
$$f_{\text{spec}}(\omega_i, \omega_o) = \frac{F}{\pi} \frac{GD}{(\mathbf{n} \cdot \omega_i)(\mathbf{n} \cdot \omega_o)}$$

- Reflectance: $\mathbf{f} = d\mathbf{f}_{\text{diff}} + s\mathbf{f}_{\text{spec}}$
 - $d + s = 1$
 - $\mathbf{f}_{\text{diff}}$ is constant (e.g. Lambertian)
- $\mathbf{f}_{\text{spec}}$
 - F: Fresnel term
 - G: Geometric attenuation (shadowing, masking)
 - D: Normal distribution of facets oriented along $\mathbf{h}$

Cook-Torrance:

$$f_{\text{spec}}(\omega_i, \omega_o) = \frac{F}{\pi} \frac{GD}{(\mathbf{n} \cdot \omega_i)(\mathbf{n} \cdot \omega_o)}$$

Fresnel term F

$$F(\theta) = \frac{1}{2} \frac{(g - c)^2}{(g + c)^2} \left(1 + \frac{(c(g + c) - 1)^2}{(c(g - c) + 1)^2} \right) \quad \begin{aligned} c &= \cos \theta = \mathbf{v} \cdot \mathbf{h} \\ g &= \sqrt{\eta^2 + c^2 - 1} \end{aligned}$$



Geometric attenuation G

$$G(\omega_i, \omega_o) = \min \left\{ 1, \frac{2(\mathbf{n} \cdot \mathbf{h})(\mathbf{n} \cdot \omega_o)}{(\omega_o \cdot \mathbf{h})}, \frac{2(\mathbf{n} \cdot \mathbf{h})(\mathbf{n} \cdot \omega_i)}{(\omega_i \cdot \mathbf{h})} \right\}$$

Normal distribution D - (fraction of facets with normal = $\mathbf{h}$) : (Phong, Heidrich-Seidel, GGX...)

Beckmann (rough surfaces):

$$D_{\text{Beckmann}} = \frac{1}{m^2 \cos^4 \alpha} e^{-[(\tan \alpha / m)^2]}$$

Gaussian:

$$D_{\text{Gaussian}} = c e^{-\left(\frac{\alpha}{m^2}\right)^2}$$

GGX

- Microfacet distribution model **D**
- Improvement over Beckmann distribution
 - Better fit to measured data (for some surfaces)
 - Derived from geometry term **G**
- **B**SDF
 - Handles transmittance

Paper:

Microfacet Models for Refraction through Rough Surfaces (2007)



GGX

Cook-Torrance specular BRDF:

$$f_{\text{spec}}(\omega_i, \omega_o) = \frac{F}{\pi} \frac{GD}{(\mathbf{n} \cdot \omega_i)(\mathbf{n} \cdot \omega_o)}$$

GGX BRDF:

$$f(\omega_i, \omega_o) = \frac{FGD}{4(\mathbf{n} \cdot \omega_i)(\mathbf{n} \cdot \omega_o)}$$

GGX

Beckmann D (used in Cook-Torrance):

$$D_{Beckmann} = \frac{1}{m^2 \cos^4 \alpha} e^{-[(\tan \alpha / m)^2]}$$

GGX D:

$$D = \frac{\alpha_g^2 \chi^+(\mathbf{h} \cdot \mathbf{n})}{\pi \cos^4 \theta_h (\alpha_g^2 + \tan^2 \theta_h)^2}$$

GGX

Cook-Torrance G:

$$G(\omega_i, \omega_o) = \min \left\{ 1, \frac{2(\mathbf{n} \cdot \mathbf{h})(\mathbf{n} \cdot \omega_o)}{(\omega_o \cdot \mathbf{h})}, \frac{2(\mathbf{n} \cdot \mathbf{h})(\mathbf{n} \cdot \omega_i)}{(\omega_o \cdot \mathbf{h})} \right\}$$

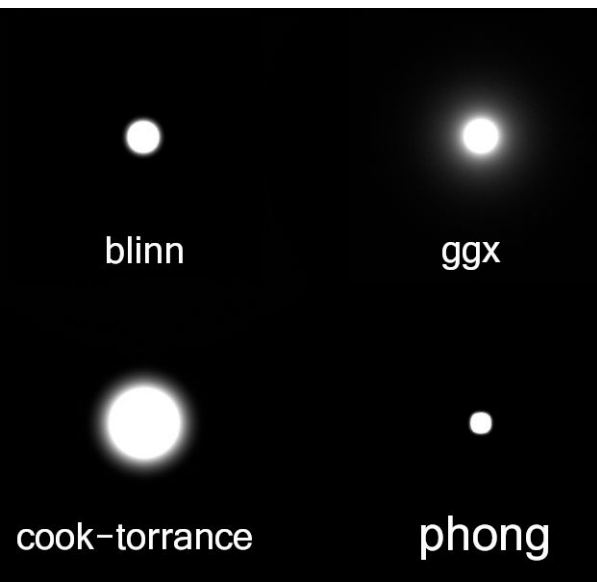
GGX G (Smith):

$$G(\omega_i, \omega_o) \approx G_1(\omega_i)G_1(\omega_o)$$

$$G_1(\mathbf{v}) = \chi^+ \left(\frac{\mathbf{v} \cdot \mathbf{h}}{\mathbf{v} \cdot \mathbf{n}} \right) \frac{2}{1 + \sqrt{1 + \alpha_g^2 \tan^2 \theta_v}}$$

GGX: Result

- Bigger tail
- Closer to real surfaces



(Measured chrome), GGX, Beckmann



Schlick

Paper by Christophe Schlick:
An Inexpensive BRDF Model for Physically-based Rendering (1994)

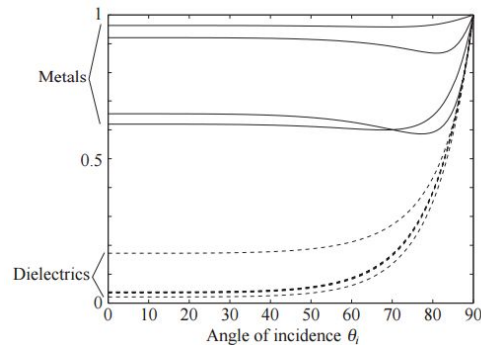
Problems with BRDF models:

- Linear combination of specular, diffuse
 - Constant weights (Cook-Torrance: $\mathbf{f} = d\mathbf{f}_{\text{diff}} + s\mathbf{f}_{\text{spec}}$)
 - Instead, $\mathbf{f}$ should be a function of incident angle
- **G** only models reflection toward light
 - **G**: the fraction of light **not obstructed** by microgeometry
 - Problem: the (unabsorbed) obstructed light ($1 - \mathbf{G}$) is reflected elsewhere in reality
 - Existing models do not account for this “re-emission” of light
- Physically plausible models are expensive
 - Schlick’s approximation

Schlick: Approximations

Fresnel term F (Cook-Torrance):

$$F(\theta) = f_0 + (1 - f_0)(1 - \cos \theta)^5 \quad f_0 = \left(\frac{\eta_1 - \eta_2}{\eta_1 + \eta_2} \right)^2$$



Geometrical attenuation G (Smith):

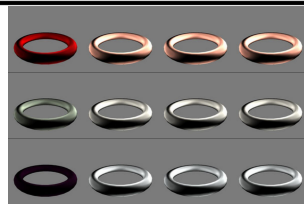
$$G(v) = \frac{v}{v - kv + k} \quad \text{with} \quad k = \sqrt{\frac{2m^2}{\pi}}$$

* Paper:
Fresnel term approximations for Metals (2005)

$$F^*(n, k, \cos \theta) := \frac{(n-1)^2 + 4n(1 - \cos \theta)^5 + k^2}{(n+1)^2 + k^2}$$

Distribution D (Beckmann):

$$\forall t \in [1-m, 1] \quad D(t) = \frac{m^3 x}{t (mx^2 - x^2 + m^2)^2} \quad \text{with} \quad x = t + m - 1$$



Schlick

- Approximations → faster Cook-Torrance
- Two new BRDF models:
 - Homogeneous
 - metal, glass, paper, cotton
 - Heterogeneous (two layers)
 - opaque layer + translucent layer
 - varnished wood, lacquered glass
- Layer properties
 - All values in $[0, 1]$:
 - C_λ : Reflection factor at wavelength λ
 - r : Roughness factor (0: perfectly specular; 1: perfectly diffuse)
 - p : Isotropy factor (0: perfectly anisotropic; 1: perfectly isotropic)

Summary: Cook-Torrance, GGX, Schlick

- Physically plausible?
 - Reciprocal: **All**
 - Energy-conserving: **GGX, Schlick**
 - **Cook-Torrance**: not energy-conserving under all angles

Summary: Cook-Torrance, GGX, Schlick

- **Cook-Torrance**

- **Suitable for:** plastics, metals.
- “Not as intuitive parameters. Experimentation required”
- **F, D, G** are independent and can be replaced.

- **GGX**

- **Suitable for:** developed for transmittance through rough surfaces (etched glass)
- In general, “improved Cook-Torrance”
- Many different versions of **D, G**

- **Schlick**

- **Suitable for:** heterogeneous materials (translucent + opaque)
- Continuums for isotropy, specular/diffuse
- “Intuitive parameters”

Overview

Models	Physical	Plausible	Fresnel Eq.	Anisotropic	Sampling	Rel.Cost (cycles)	Material Type
Ideal Specular	★	★	▼	▼	★	x	perfect specular
Ideal Diffuse	★	★	▼	▼	★	x	perfect diffuse
Minnaert	▼	...	▼	▼	▼	$5.35x$	Moon surf.
Torrance-Sparrow	★	▼	★	★	▼	...	rough surf.
Beard-Maxwell	★	▼	★	▼	▼	$397x$	painted surf.
Blinn-Phong	▼	▼	▼	▼	★	$9.18x$	rough surf.
Cook-Torrance	★	★	★	▼	▼	$16.9x$	metal,plastic
Kajiya	★	▼	★	★	▼	...	metal,plastic
Poulin-Fournier	★	▼	▼	★	▼	$67x$	clothes
Strauss	▼	...	★	▼	▼	$14.88x$	metal,plastic
He et al.	★	★	★	▼	▼	$120x$	metal
Ward	▼	▼	▼	★	★	$7.9x$	wood
Westin	★	...	★	★	▼	...	metal
Lewis	▼	★	▼	▼	★	$10.73x$	mats
Schlick	▼	★	★	★	▼	$26.95x$	heterogeneous
Hanrahan	★	...	★	▼	▼	...	human skin
Oren-Nayar	★	★	▼	▼	★	$10.98x$	matte, dirty.
Neumann	▼	★	▼	★	★	...	metal,plastic
Lafortune	▼	★	▼	★	★	$5.43x$	rough surf.
Coupled	★	★	★	▼	★	$17.65x$	polished surf.
Ashikhmin-Shirley	★	▼	★	★	★	$79.6x$	polished surf.
Granier-Heidrich	★	...	★	▼	▼	...	old-dirty metal

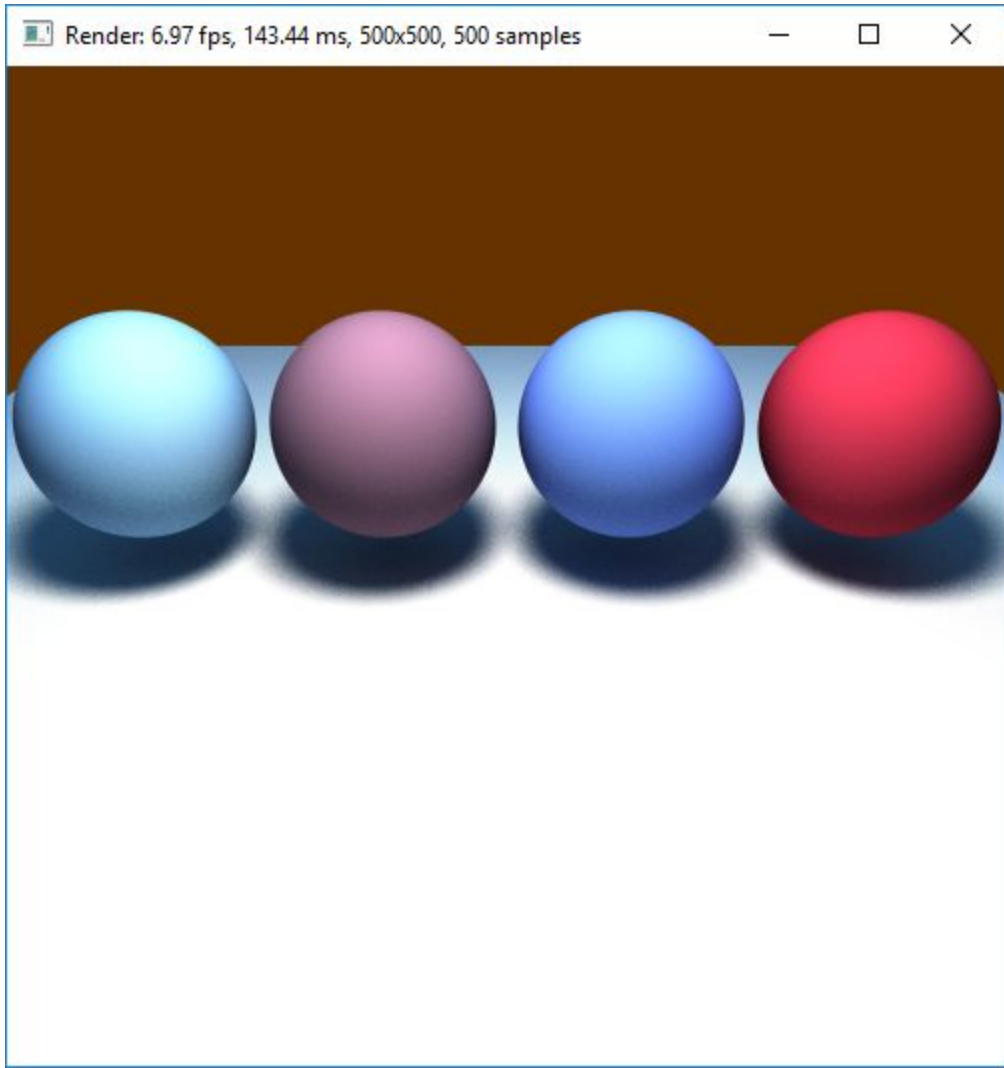
Table 1: Brief summary of the properties exhibited by the reviewed BRDFs. Legend: (★) if the BRDF has this property; (▼) if the BRDF does not; (...) unknown value.

Demo

Lambertian, Oren-Nayar

Roughness:

0 → 0.1 → 0.5 → 0.9

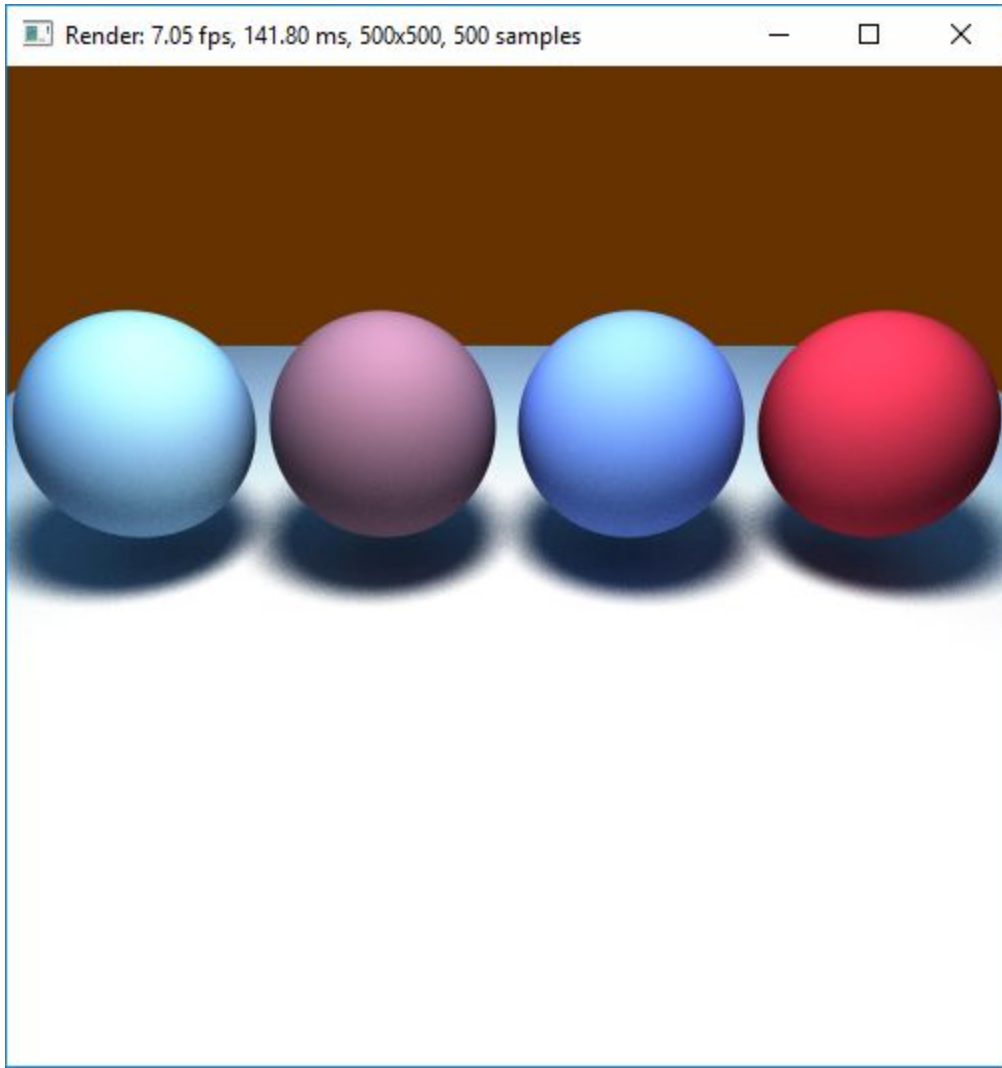


Demo

Lambertian, **Oren-Nayar**

Roughness:

0 → **0.1** → 0.5 → 0.9

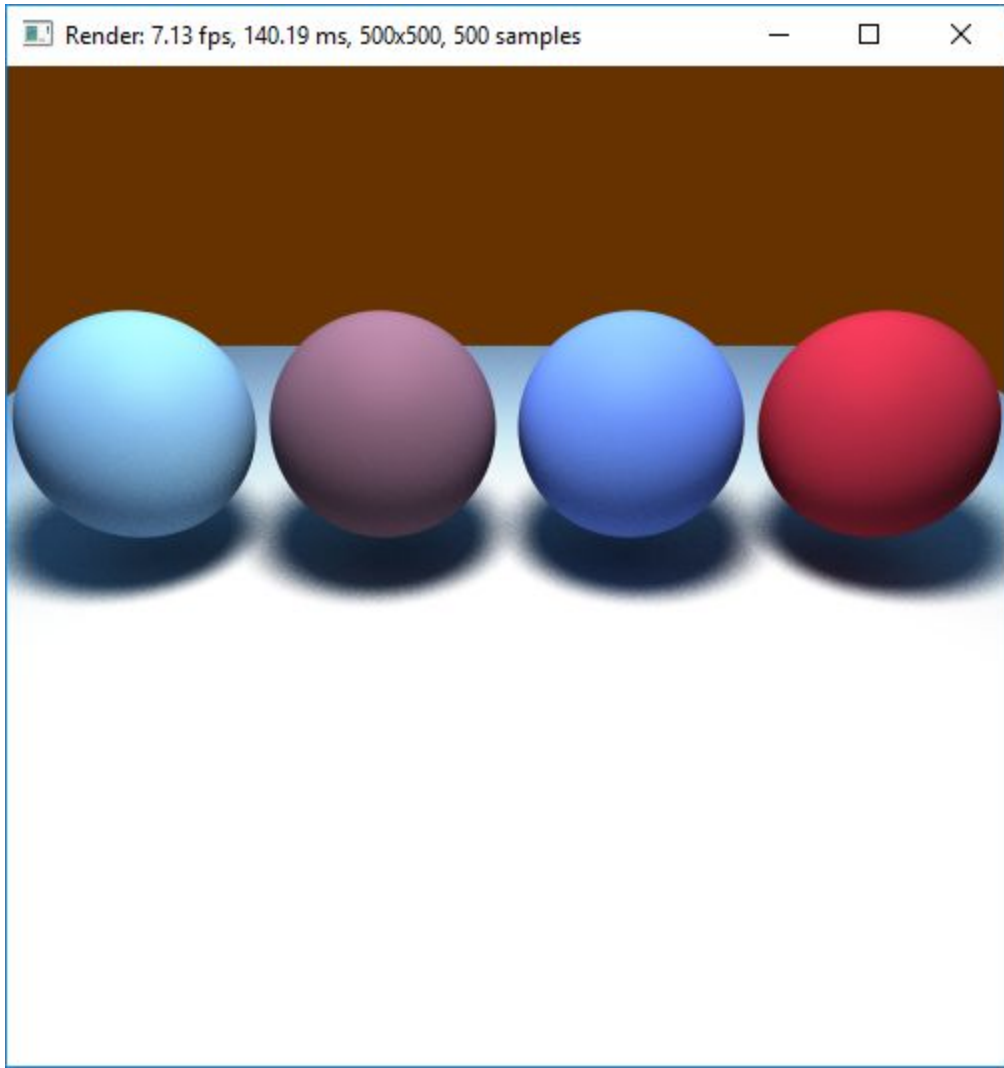


Demo

Lambertian, **Oren-Nayar**

Roughness:

0 → 0.1 → **0.5** → 0.9

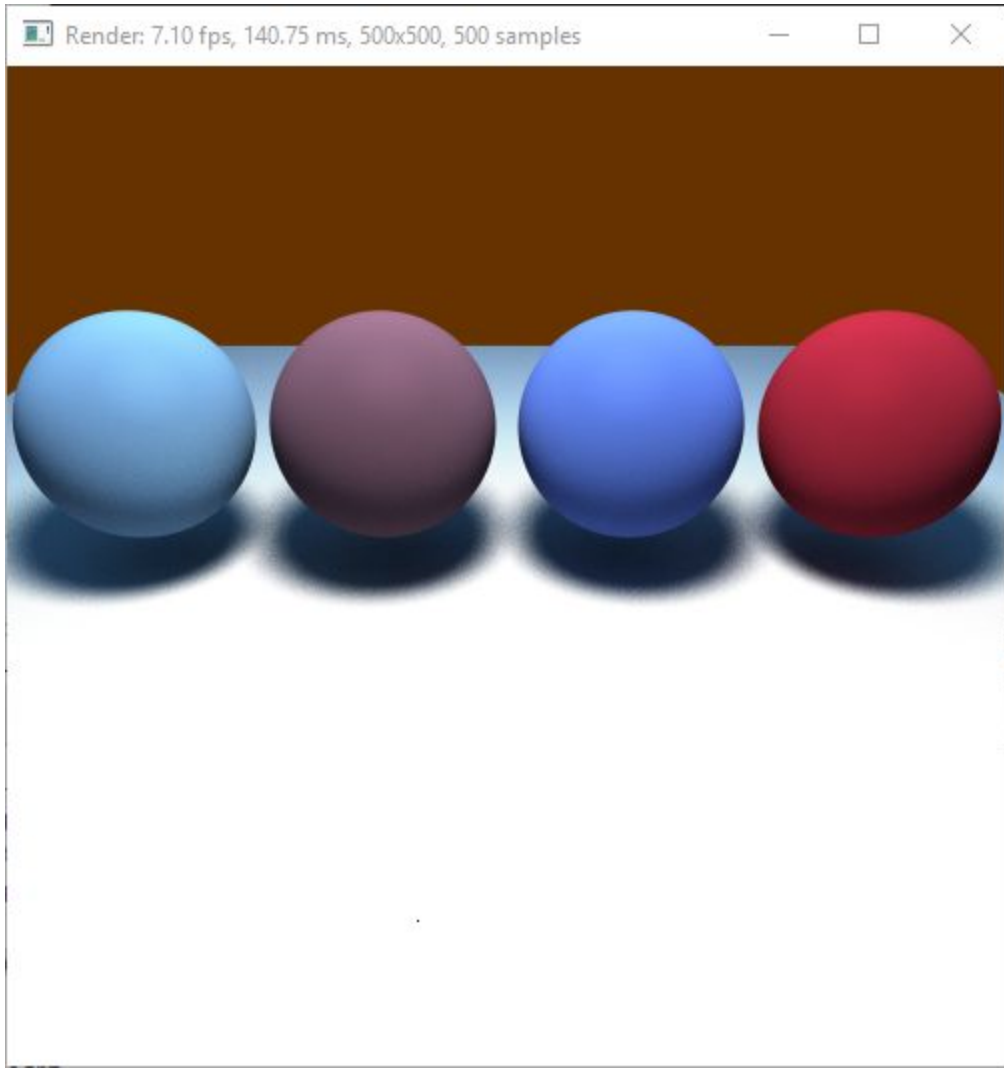


Demo

Lambertian, **Oren-Nayar**

Roughness:

0 → 0.1 → 0.5 → **0.9**



Demo

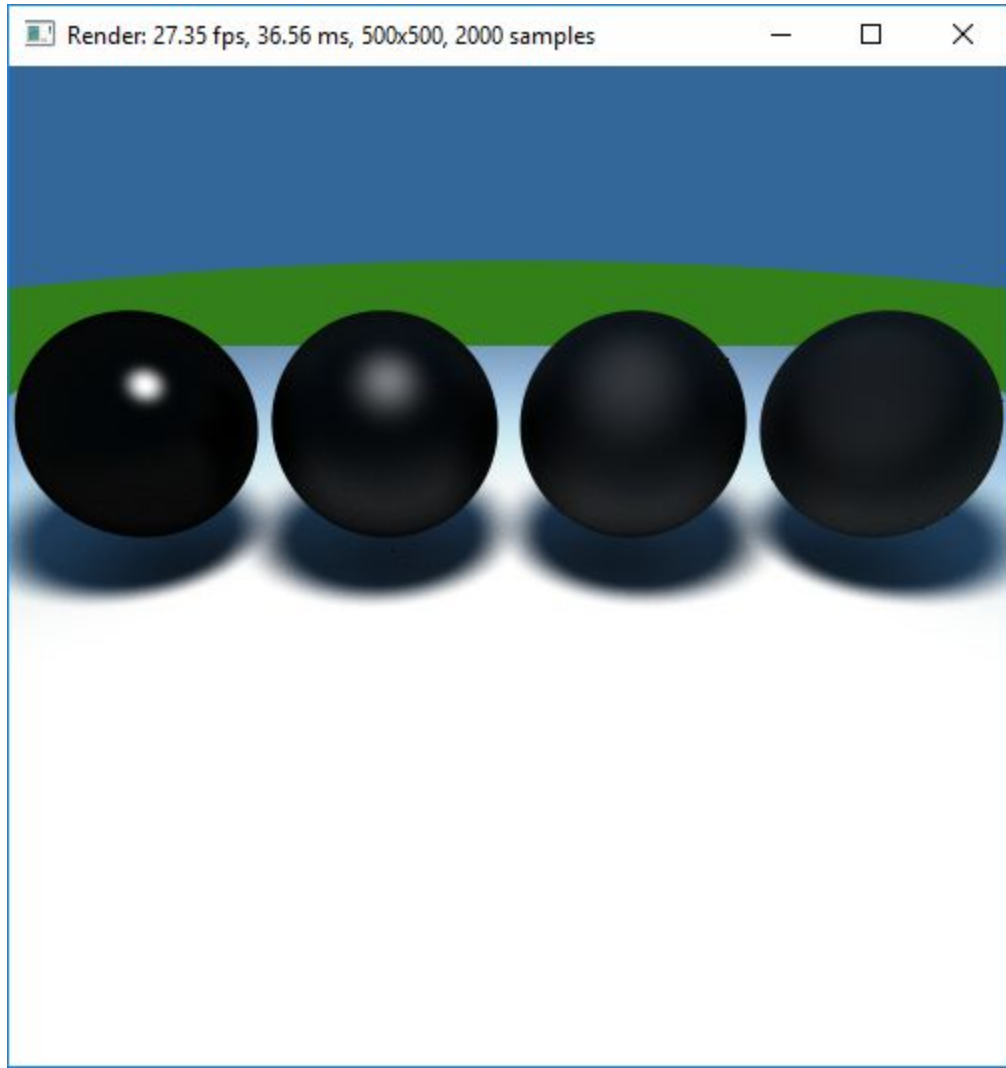
Cook-Torrance (specular only)

ior = 1.5 (typical glass)

($\Rightarrow f_0 = 0.04$)

Roughness:

0.10 $\rightarrow$ 0.25 $\rightarrow$ 0.40 $\rightarrow$ 0.55



Demo

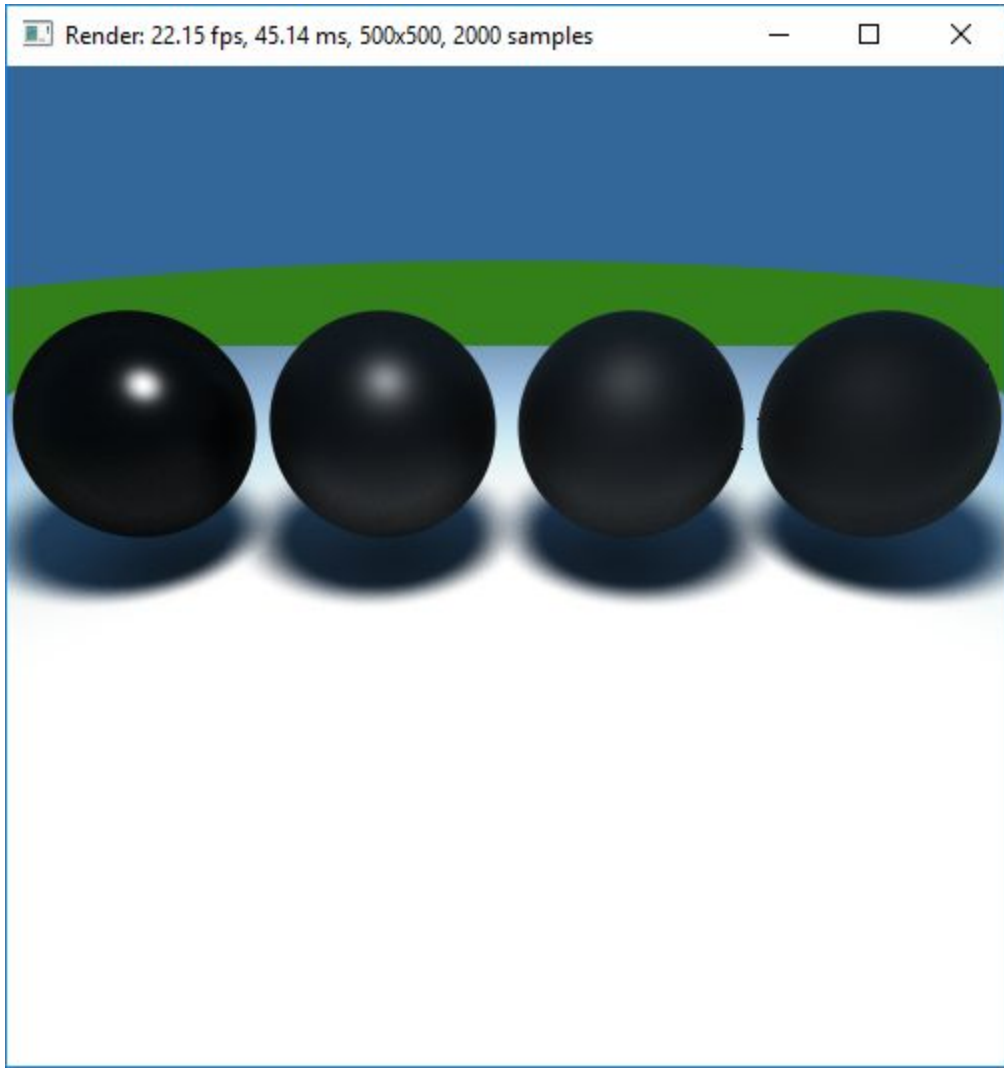
GGX (specular only)

ior = 1.5 (typical glass)

($\Rightarrow f_0 = 0.04$)

Roughness:

0.10 → 0.25 → 0.40 → 0.55



Demo

Cook-Torrance (specular only)

Random parameters:

f_0 in $[0.02, 0.05]$

($\Rightarrow$ ior in $\sim[1.33, 1.58]$)

α in $[0, 1]$

white specular color



Demo

GGX (specular only)

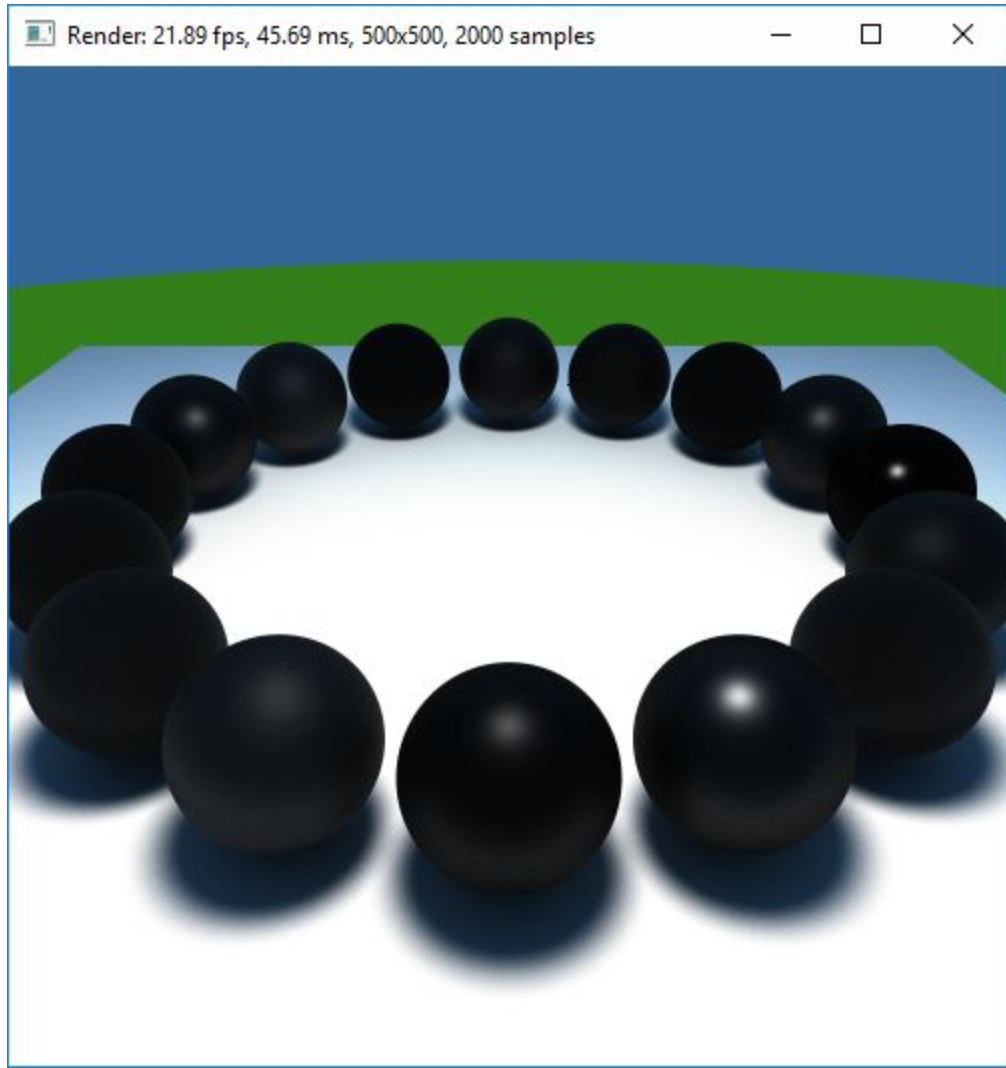
Random parameters:

f_0 in $[0.02, 0.05]$

($\Rightarrow$ ior in $\sim[1.33, 1.58]$)

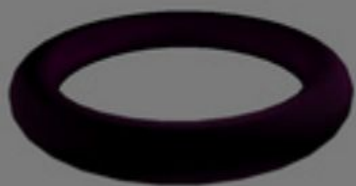
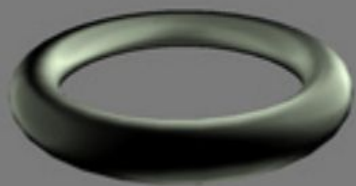
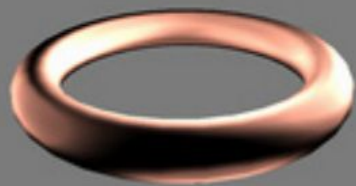
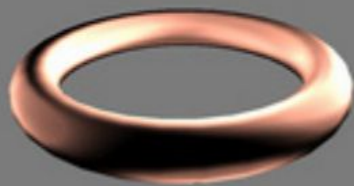
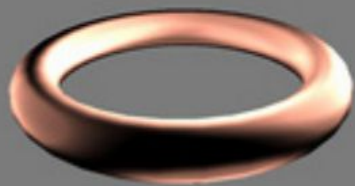
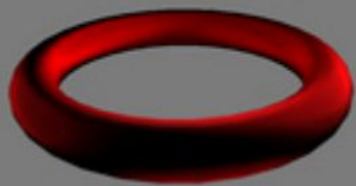
α in $[0, 1]$

white specular color



The End

Extra



Microfacet distributions visualised

- Experimental Analysis of BRDF Models
 - http://people.csail.mit.edu/addy/research/ngan05_brdf_eval.pdf

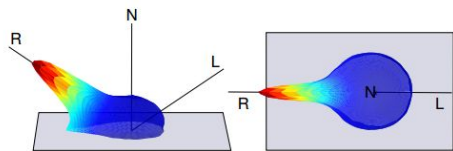


Figure 8: Side and top-down view of the measured "PVC" BRDF, at 55° incidence. (Cubic root is applied to the BRDF for visualization.) Its specular lobe exhibits a similar asymmetry to the $H \cdot N$ lobe.

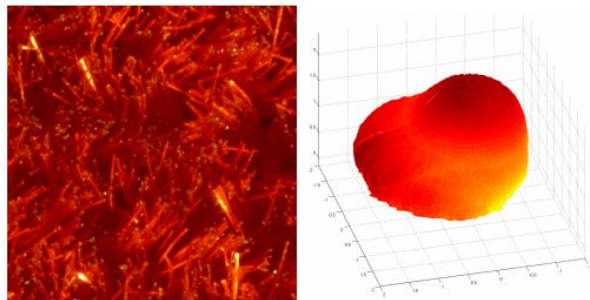


Figure 13: Left: Red velvet macro photograph. Right: deduced microfacet distribution (log plot).

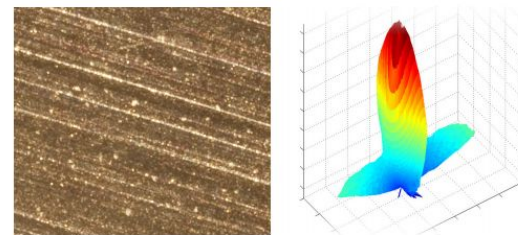


Figure 11: Left: Brushed aluminium macro photograph. Right: deduced microfacet distribution (log plot).



Figure 12: Left: Purple satin macro photograph with sketched double cones. Right: deduced microfacet distribution (log plot).