

# Formal Methods for Software Development

## Verification with SPIN

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# SPIN: Previous Lecture vs. This Lecture

## Previous lecture

SPIN appeared as a PROMELA **simulator**

## This lecture

Intro to SPIN as a **model checker**

# What Does A Model Checker Do?

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⇒ **Finding no counter example proves stated correctness properties.**

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- ▶ explicit, local:

if/do statements

:: guardX -> ...

:: guardY -> ...

- ▶ implicit, global:

scheduling of concurrent processes  
(see next lecture)

# Model Checker for This Course: SPIN

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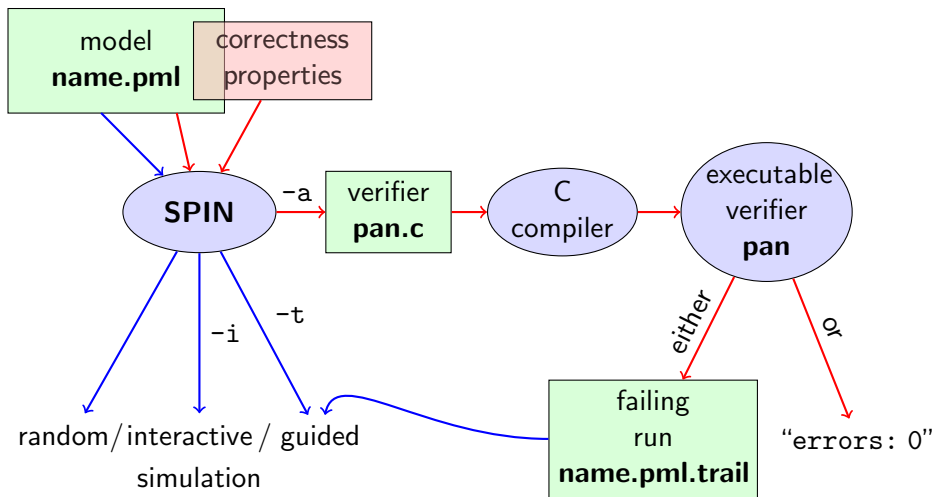
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- ▶ generating a verifier

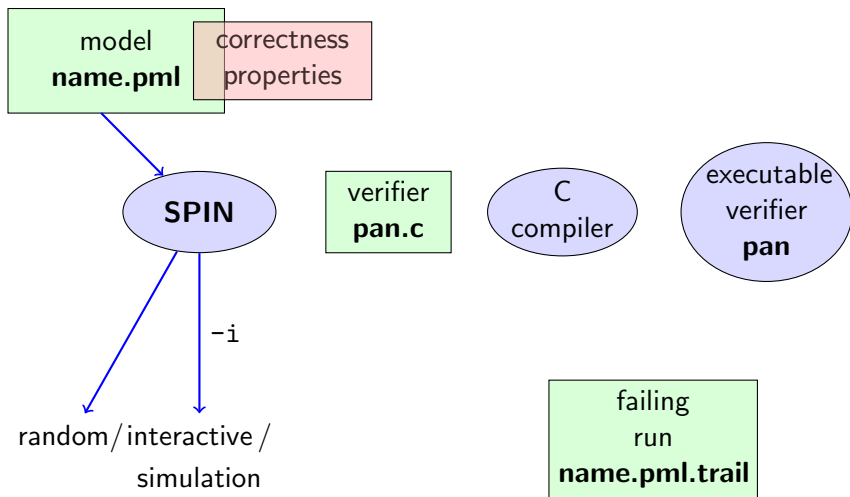
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model checking:

- ▶ exhaustively checks PROMELA model against correctness properties
- ▶ in case the check is negative:  
generates a failing run of the model, to be simulated by SPIN

# SPIN Workflow: Overview



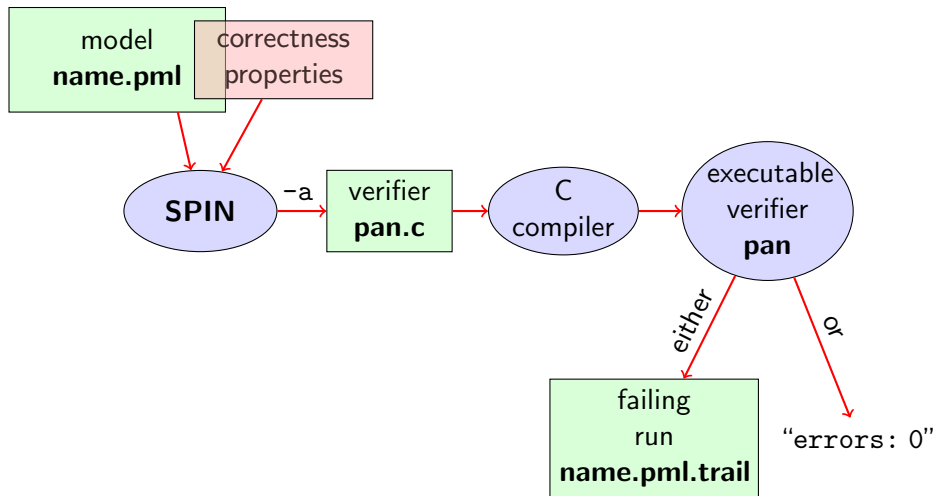
# Plain Simulation with SPIN



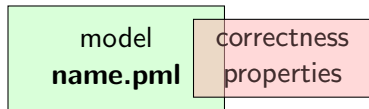
# Rehearsal: Simulation Demo

- ▶ run example, random and interactive  
`zero.pml`

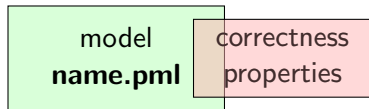
# Model Checking with SPIN



# Stating Correctness Properties



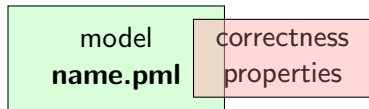
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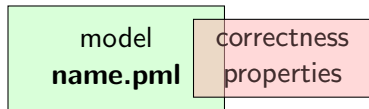


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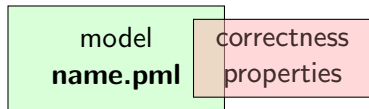


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  - ▶ end labels
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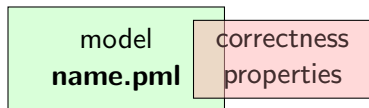
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**stating properties within model**, using

- ▶ **assertion statements** (today)
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Assertion statements in PROMELA are statements of the form

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...  
stmt1;  
assert(max == a);  
stmt2;  
...
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Typically, *expr* is of type `bool`.

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```
...                               ...
stmt1;                             if
assert(max == a);                   :: b1 -> stmt3;
stmt2;                               assert(x < y)
...                                   :: b2 -> stmt4
...                                   ...
```

# Meaning of **Boolean** Assertion Statements

`assert(expr)`

- ▶ has **no effect** if *expr* evaluates to **true**
- ▶ triggers an **error message** if *expr* evaluates to **false**

This holds in both, simulation and model checking mode.

# Meaning of **General** Assertion Statements

`assert(expr)`

- ▶ has no effect if *expr* evaluates to **non-zero value**
- ▶ triggers an error message if *expr* evaluates to **0**

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This holds in both, simulation and model checking mode.

Recall:

`bool true false` is syntactic sugar for

`bit 1 0`

⇒ general case covers Boolean case

## Instead of using 'printf's for Debugging ...

```
/* after choosing a,b from {1,2,3} */  
if  
  :: a >= b -> max = a  
  :: a <= b -> max = b  
fi;  
printf("the maximum of %d and %d is %d\n",  
       a, b, max)
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### Command Line Execution

*(simulate, inject fault, simulate again)*

```
> spin [-i] max.pml
```



## ... we can employ **Assertions**

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/* after choosing a,b from {1,2,3} */  
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## ... we can employ **Assertions**

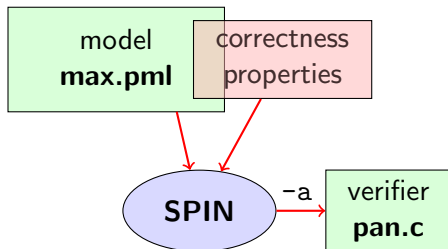
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(Historic moment in the course.)

# Generate Verifier in C



## Command Line Execution

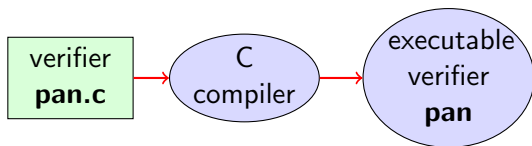
*Generate Verifier in C*

```
> spin -a max2.pml
```

SPIN generates **Verifier** in C, called **pan.c**

(plus helper files)

# Compile To Executable Verifier

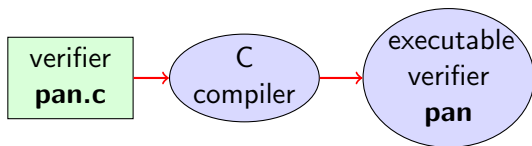


## Command Line Execution

*compile to executable verifier*

```
> gcc -o pan pan.c
```

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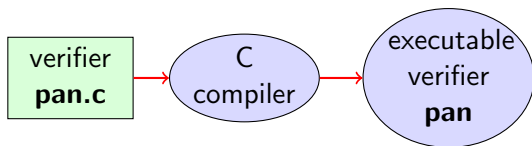
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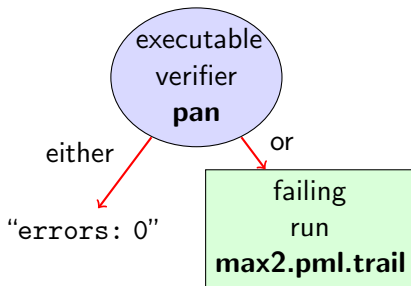
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C compiler generates **executable verifier pan**

**pan**: historically “**protocol analyzer**”, now “**process analyzer**”



# Run Verifier (= Model Check)

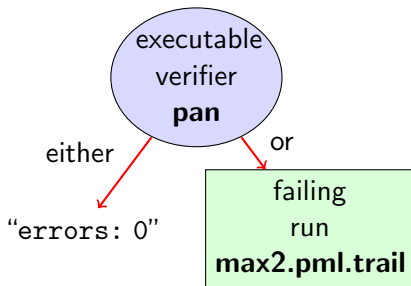


## Command Line Execution

```
run verifier pan
```

```
> ./pan or > pan
```

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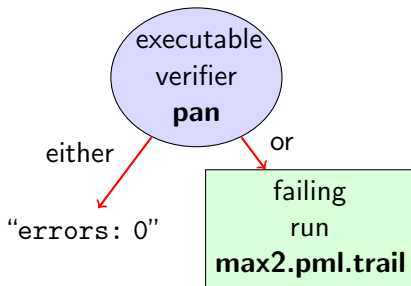
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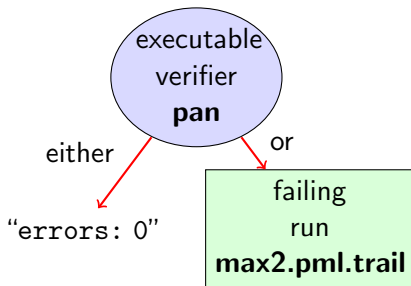
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- ▶ prints "errors: 0" ⇒ Correctness Property verified!

# Run Verifier (= Model Check)



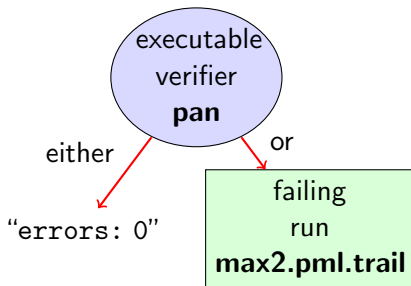
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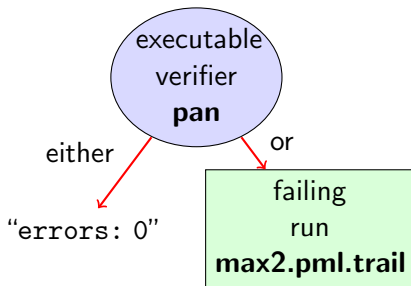
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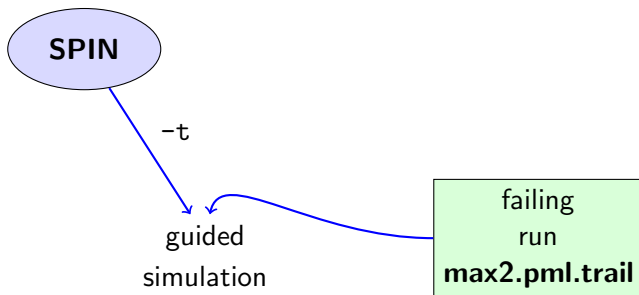
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records failing run in **max2.pml.trail**

# Guided Simulation

To **examine failing run**: employ **simulation mode**, “guided” by trail file.



## Command Line Execution

*inject a fault, re-run verification, and then:*

```
> spin -t -p -l max2.pml
```

# Output of Guided Simulation

can look like:

Starting P with pid 0

```
1: proc 0 (P) line 8 "max2.pml" (state 1) [a = 1 ]
      P(0):a = 1
2: proc 0 (P) line 14 "max2.pml" (state 7) [b = 2 ]
      P(0):b = 2
3: proc 0 (P) line 23 "max2.pml" (state 13) [((a<=b))]
3: proc 0 (P) line 23 "max2.pml" (state 14) [max = a ]
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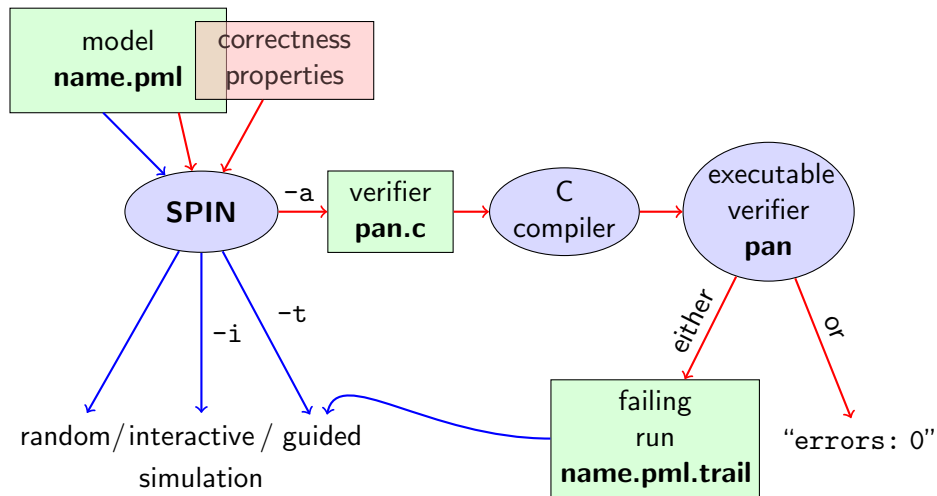
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(If output doesn't mention max variable, re-verify with ./pan -E)

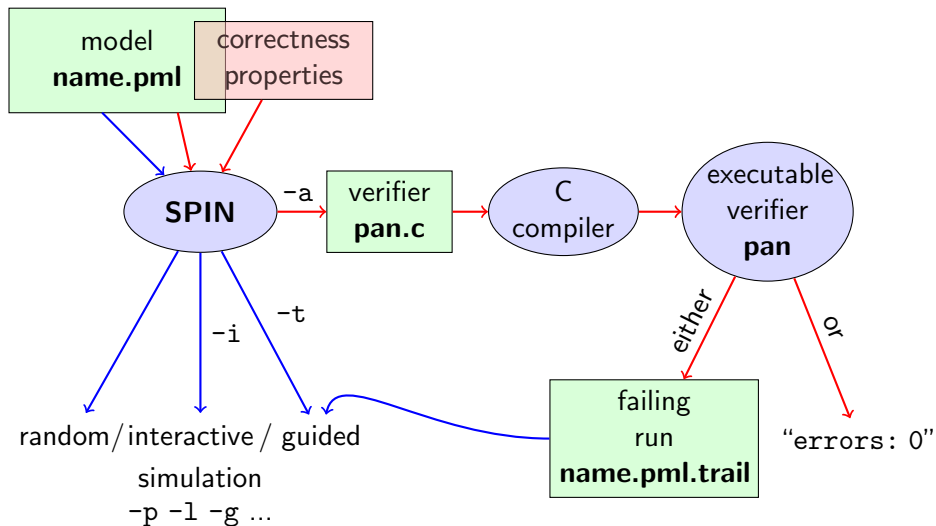
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following whole cycle (most primitive example, assertions only)



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## Further Examples: Integer Division

```
int dividend = 15;
int divisor  = 4;
int quotient, remainder;

quotient = 0;
remainder = dividend;
do
    :: remainder > divisor ->
        quotient++;
        remainder = remainder - divisor
    :: else ->
        break
od;
printf("%d divided by %d = %d, remainder = %d\n",
       dividend, divisor, quotient, remainder)
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```

simulate, put assertions, verify, change values, ...

## Further Examples: Greatest Common Divisor

greatest common divisor of x and y

```
int a, b;
a = x; b = y;
do
  :: a > b -> a = a - b
  :: b > a -> b = b - a
  :: a == b -> break
od;
printf("The GCD of %d and %d = %d\n", x, y, a)
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⇒ **typical for model checking**

# Typical Command Lines

typical command line sequences:

## random simulation

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## model checking

```
spin -a name.pml  
gcc -o pan pan.c  
./pan
```

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## random simulation

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## interactive simulation

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spin -i name.pml
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## model checking

```
spin -a name.pml
```

```
gcc -o pan pan.c
```

```
./pan
```

and in case of error

```
spin -t -p -l -g name.pml
```

Ben-Ari produced [Spin Reference Card](#), summarizing

- ▶ typical command line sequences
- ▶ options for
  - ▶ SPIN
  - ▶ gcc
  - ▶ pan
- ▶ PROMELA
  - ▶ datatypes
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  - ▶ statements
  - ▶ guarded commands
  - ▶ processes
  - ▶ channels
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⇒ [available from course page](#) (see 'Links, Papers, and Software')

# Why SPIN?

- ▶ SPIN targets software, instead of hardware verification (“Formal Methods for *Software* Development”)
- ▶ 2001 ACM Software Systems Award (other winning systems include: Unix, TCP/IP, WWW, Tcl/Tk, Java, GCC, T<sub>E</sub>X, Coq)
- ▶ used for safety critical applications
- ▶ distributed freely as research tool, well-documented, actively maintained, large user-base in academia and in industry
- ▶ annual SPIN user workshops series held since 1995
- ▶ based on standard theory of ( $\omega$ -)automata and linear temporal logic

## Why SPIN? (Cont'd)

- ▶ PROMELA and SPIN are rather simple to use
- ▶ good to understand a few systems really well, rather than many systems poorly
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- ▶ availability of front end JSPIN (also Ben-Ari)
- ▶ and: availability of our own web interface

# What is JSPIN?

- ▶ graphical user interface for SPIN
- ▶ developed for pedagogical purposes
- ▶ written in JAVA
- ▶ simple user interface
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- ▶ makes back-end calls transparent

## Command Line Execution

*calling JSPIN*

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> java -jar /usr/local/jSpin/jSpin.jar
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*(with path adjusted to your setting)*

*or use shell script:*

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play around with similar examples ...



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But how to write Correctness Properties?

## Catching A Different Type of Error

quoting from file **max3.pml**:

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Note: no assert in **max3.pml**.

# Catching A Different Type of Error

Further inspection of **pan** output:

```
...  
pan: invalid end state (at depth 1)  
pan: wrote max3.pml.trail  
...
```

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(Fix error)

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Can get SPIN to ignore 'invalid end state' error: `./pan -E`

# Literature for this Lecture

**Ben-Ari** Chapter 2, Sections 4.7.1, 4.7.2