# TRIAL-EXAM <br> Software Engineering using Formal Methods <br> TDA293 (TDA292) / DIT270 

Extra aid: Only dictionaries may be used. Other aids are not allowed!

Please observe the following:

- This exam has 10 numbered pages, plus two pages of the Spin Reference Card. Please check immediately that your copy is complete
- Answers must be given in English
- Use page numbering on your pages
- Start every assignment on a fresh page
- Write clearly; unreadable = wrong!
- Fewer points are given for unnecessarily complicated solutions
- Indicate clearly when you make assumptions that are not given in the assignment


## Good luck!

## Assignment 1 PROMELA

The task is to model a simplified version of the TicTacToe game in PROMELA. TicTacToe is a two player game which is played on a $3 \times 3$ board as shown below:

| 0 | 1 | 2 |
| :--- | :--- | :--- |
| 3 | 4 | 5 |
| 6 | 7 | 8 |

(The numbers suggest how to represent the board by a simple array of size 9.)
The game is played turn-by-turn. The player whose turn it is, selects an empty field and marks it with her unique id.
We use here a simplified winning condition: the player who manages to mark one of the two diagonals completely (i.e., all fields belonging to that diagonal) with her unique id wins the game.

The game is over if either one of the players has won or if there is no empty field left which belongs to one of the diagonals and none of the diagonals is owned by one of the two players. In the latter case, we call the game to be a draw.
(a) Modeling TicTacToe in PROMELA.

Below you find a skeleton model of a TicTacToe game modelled in PROMELA:

```
/* message type */
mtype = {move, done}
/* board */
byte board[9];
/* channel to communicate with referee. The second parameter holds the
    player's process id */
chan ch = [0] of {mtype, byte};
/* variable that is 0 if game is ongoing, _pid if player _pid has won,
    255 if game is a draw */
byte over = 0;
proctype player() { /* to be filled in */ }
proctype referee() { /* to be filled in */ }
/* Initialises and starts the players and referee. Ensures that the
    * first player has _pid 1 and the second player has _pid 2 */
init {
    run player();
    run player();
    run referee()
}
```

The PROMELA model realizes the playfield as a global variable called board, a byte array of size 9 . Initially all components of the board have the value 0 .

The message type mtype is defined to consist of the two values move and done. Further, there are two global variables called (i) ch of type chan which is used for the communication between the referee and the players; (ii) over of type byte which indicates whether the game is still ongoing (over is 0 ), or one player has won (over carries that player's process id), or the game is a draw (over has is 255 ).

The process init initializes the game with two players and one referee.
Your task is now to provide an implementation for the player and referee process according to the following description:

Player: For as long as over is 0 , the player does the following over and over again:

1. Wait for the referee to inform her that it is her move (by sending a message containing move and this player's process id).
2. Select non-deterministically a free field (a field is free if its value is 0 ).
3. Store her process id in that field.
4. Informs the referee that this turn is completed, by sending the message done together with her process id.

Afterwards, the player prints "Game Over!" and terminates.

## Referee:

1. Initially the referee starts the game by giving the turn to the first player. A turn is assigned to a player by sending the message move followed by the player's process id via the channel ch.
2. The referee then waits for the player to finish her turn.
3. Upon receiving that the player has finished the turn, the referee checks if this player has won the game (i.e., if the player has marked one of the two diagonals completely with her process id). If that is the case, the referee sets the global variable over to the player's id and the referee process terminates. Otherwise the referee continues with step 4.
4. The referee checks now if it is a draw, if that is not the case, it hands the turn over to the other player by sending the move message followed by the corresponding process id of the player. The referee continues then with step 2.
5. Otherwise, it is a draw. The variable over is set to 255 and the referee process terminates.

## Assignment 2 Linear Temporal Logic (LTL)

Tell for each formula whether it is valid or not.
(Each question is worth 1 point, except question 7., which is worth 2 points. Missing answers get no points, wrong answers get -1 point. Still, you will never get a negative total for this assignment.)

1. $\square p \rightarrow \diamond p$
2. $\Delta p \rightarrow \square p$
3. $\square \diamond p \rightarrow \diamond \square p$
4. $\Delta \square p \rightarrow \square \diamond p$
5. $\diamond(p \vee q) \rightarrow \neg \square(\neg p \vee \neg q)$
6. $\square \neg \diamond p \rightarrow \neg p$
7. $(\square p \vee \diamond q) \rightarrow(\square \neg q \rightarrow \diamond p)$

## Assignment 3 (Büchi Automata and Model Checking)

(a) $[3 p]$

Consider the following Büchi automaton.


Give the $\omega$-expression describing the language accepted by this automaton.
(b) $[2 \mathrm{p}]$

The following Büchi automaton does not exactly accept the runs that satisfy the LTL formula $\diamond \square p$ :


Demonstrate this mismatch, by giving a run which is accepted by the automaton and not by the LTL formula, or vice-versa.
(c) $[2 \mathrm{p}]$

Give an LTL formula that is satisfied exactly by accepted runs of the automaton from (b).
(d) $[2 \mathrm{p}]$

The Büchi automaton from (b) requires just a small modification to accept exactly those runs satisfying $\diamond \square p$. Give this modified automaton.

## Assignment 4 (First-Order Sequent Calculus)

We work here in untyped first-order logic with the trivial type $T$, which is omitted in the formulas below.
Let $p$ denote a predicate of arity 2 and $c, d$ be constant symbols. Prove that the following first-order logic formula is valid using the first-order sequent calculus. For each step name the rule you have applied and for the quantification rules also the side-conditions like substitution or introduction.

You are only allowed to use the calculus rules presented in the lectures.
Your task is to build a proof for the following sequent:

$$
\begin{aligned}
& \forall x ; \forall y ;(p(x, y) \rightarrow \neg p(y, x)), \\
& \forall x ; \forall y ; \forall z ;((p(x, y) \wedge p(y, z)) \rightarrow p(x, z)), \\
& p(c, d) \Rightarrow \\
& \forall z ;(p(d, z) \rightarrow \neg p(z, c))
\end{aligned}
$$

Hint: You may abbreviate formulas, but only if you clearly describe your abbreviations.

Consider the class Hashtable:
public class Hashtable \{

```
    private Object[] h;
    private int capacity;
    private int size = 0;
    Hashtable (int capacity) {
        h = new Object[capacity];
        this.capacity = capacity;
    }
    /*@ public normal_behavior
        0 requires val > 0;
        @ ensures \result >= 0 && \result =< capacity;
        @*/
        private int hash_function (int val) { ..... }
    public void add (Object obj, int key) {
        if (size < capacity) {
                int i = hash_function(key);
                if (h[i] == null) {
                    h[i] = obj;
                        size++;
                }
                else {
                    while (h[i] != null){
                        if (i == capacity-1) {i = 0;} else {i++;}
                    }
                    h[i] = obj;
                    size++;
                }
                return;
        } else
                throw new FullHashtableException();
    }
```

\}

This class represents an open addressing hash table with linear probing as collision resolution. Within a hash table, objects are stored into a fixed array h. Besides, in order to have an easy way of checking whether or not the capacity of $h$ is reached (i.e. the array $h$ is full), a field size keeps track of the number of stored objects and a field capacity represents the total amount of objects that can be added to the hash table.

The method add, which is used to add objects to the hash table, first tries to put the corresponding object at the position of the computed hash code. However, if that index is occupied, then add searches upwards (modulo the array length) for the nearest following index which is free. A position is considered free if and only if it contains a null object.

Augment class Hashtable with JML specification stating the following:

- The size field is never negative, and always $\leq$ capacity.
- The capacity should be the same value as h.length.
- The array h cannot be null.
- There should be space for at least one element in the hash table.
- The number of elements stored in array h (i.e., the number of array cells whose content is not null) is size.
- If the size is strictly smaller than capacity, then all of the following must hold:
- add terminates normally
- add increases size by one
- After add (obj, key), the object obj is stored in h at some index i .
- If the size has reached capacity, add will throw an FullHashtableException, and the state does not change.

In addition:

- Write assignable clauses where appropriate.
- Add JML modifiers where necessary.


## Assignment 6 (Loop-Invariant)

Consider the following Arrays class with utility methods for copying portions of int arrays from some source array src to some destination array dest. The top level method arrayCopy is capable of copying data even within the same array (when src == dest) in which case the data is first copied from the source region to a temporary array and then from the temporary array to the destination region. This way data corruption is avoided when the two regions overlap. The private helper method arrayCopyHelper works under the assumption that the provided arrays are non-null and different by reference, and that all other data (offsets and number of elements to be copied) is welldefined. This is reflected in the method's precondition. Note that the postcondition specification for arrayCopyHelper does not use the \old operator, because the source array will never be overwritten by this method. This is not the case for the top-level method arrayCopy, where the src array may change after the method is finished (when src == dest).
public class Arrays \{

```
private static /*@ spec_public @*/ IllegalArgumentException iae =
    new IllegalArgumentException();
/*@ public normal_behavior
        requires numElems >= 0;
        requires src != null && dest != null;
        requires srcOffset >= 0 && destOffset >= 0;
        requires srcOffset + numElems <= src.length;
        requires destOffset + numElems <= dest.length;
        ensures (\forall int i; i >= 0 && i < numElems;
            dest[destOffset + i] == \old(src[srcOffset + i]));
        assignable dest[*];
    also
    public exceptional_behavior
        requires src == null || dest == null || numElems < 0 ||
            srcOffset < 0 || destOffset < 0 ||
            srcOffset + numElems > src.length ||
            destOffset + numElems > dest.length;
        signals_only IllegalArgumentException;
        assignable \nothing;
    @*/
public void arrayCopy(/*@ nullable @*/ int[] src, int srcOffset,
                                    /*@ nullable @*/ int[] dest, int destOffset,
                                    int numElems) throws IllegalArgumentException {
    if(src == null || dest == null || numElems < 0 ||
        srcOffset < 0 || destOffset < 0 ||
        srcOffset + numElems > src.length ||
        destOffset + numElems > dest.length) {
        throw iae;
    }
```

```
    if(src == dest) {
        int[] temp = new int[numElems];
        arrayCopyHelper(src, srcOffset, temp, 0, numElems);
        arrayCopyHelper(temp, 0, dest, destOffset, numElems);
    } else {
        arrayCopyHelper(src, srcOffset, dest, destOffset, numElems);
    }
}
/*@
    @ public normal_behavior
        requires numElems >= 0;
        requires src != dest;
        requires srcOffset >= 0 && destOffset >= 0;
        requires srcOffset + numElems <= src.length;
        requires destOffset + numElems <= dest.length;
        ensures (\forall int i; i >= 0 && i < numElems;
            dest[destOffset + i] == src[srcOffset + i]);
        assignable dest[*];
    @*/
    private void arrayCopyHelper(int[] src, int srcOffset,
                                    int[] dest, int destOffset,
                                    int numElems) {
    int i = 0;
    while(i < numElems) {
        dest[destOffset + i] = src[srcOffset + i];
        i++;
    }
    }
}
```

Assignments:

- Provide a strong enough loop invariant, variant (decreases clause), and assignable clause for the loop in the arrayCopyHelper method, so that the postcondition of this method is provable.


## Spin Reference Card Mordechai (Moti) Ben-Ari


Datatypes
bit (1-bit)
bool (1 bit)
byte ( 8 bits unsigned)
short $\left(16^{*}\right.$ bits signed)
int (32* bits signed)
unsigned $\left(\leq 32^{*}\right.$ bits unsigned)

*     - for a 32-bit machine.

mtype $=\{$ name, name,...$\}(8$ bits $)$
typedef typename $\{$ sequence of declarations $\}$
Array declaration - type var[N] [=initial value]
Array initial value assigned to all elements.



$\begin{array}{ll}-f & \text { translate an LTL formula into a never claim } \\ -\mathrm{F} & \text { translate an LTL formula in a file into a never claim } \\ -\mathrm{N} & \begin{array}{ll}\text { include never claim from a file }\end{array} \\ -\mathrm{l} & \text { display local variables } \\ -\mathrm{g} & \text { display global variables } \\ -\mathrm{p} & \text { display statements } \\ -\mathrm{r} & \begin{array}{l}\text { display receive events } \\ -\mathrm{s}\end{array} \\ \end{array}$
Compile arguments
$\begin{array}{ll}\text {-DBFS } & \text { breadth-first search } \\ \text {-DNP } & \text { enable detection of non-progress cycles }\end{array}$
optimize for safety
$\begin{array}{cc}\text { Spin arguments } \\ \text {-a } & \text { generate }\end{array}$
generate verifier and syntax check

display Promela program after preprocessing seed for random simulation

maximum number of steps is N
-- 1
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-DBITSTATE bitstate hashing -DCOLLAPSE collapse compression
$-D M A=n \quad$ minimized DFA with maximum $n$ bytes -DMEMLIM=N use up to N megabytes of memory

[^0]
 accept - accept cycle
end - valid end state

Label prefixes with a special meaning break - exit from innermost do loop
goto - jump to label skip - no operation
break - exit from inn

әрош ио!̣e[nu!̣s u! andu! prepuełs wory pear - ғueวs \%c (character), \%d (decimal), \%e (mtype),
$\%$ (octal), \%u (unsigned), \%x (hex)
printf, printm - print to standard output assert(expression) Assignment - var = expression, var++, var-Statements
inline name (arguments) $\{\ldots\}$ \#undef, \#if, \#ifdef, \#ifndef, \#else, \#endif \#define name (arguments) string Preprocessor
timeout - no executable statements in the system? nr_pr - number of processes
pid - instantiation number of

-     - write-only hidden scratch variable
nr_pr - number of processes

Constants - true,
Variables (read-only except _):

 -> .. : ... ) conditional expression
len(ch) - number of messages in a channel
empty(ch) / nempty(ch) - is channel empty / not empty?
full(ch) / nfull(ch) - is channel full / not full?
Channel use assertions:
$\quad$ xr ch - channel ch is receive-only in this process
xs ch - channel ch is send-only in this process current value of the expression. the message; eval(expression) forces a match with the symbols must match; variables are assigned the values in Matching in a receive statement: constants and mtype ch ?? [args] poll any message (side-effect free)



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## риәs рәıоя

ch ! args
ch ! ! args
chan ch $=[$ capacity $]$ of $\{$ type, type,...$\}$ Channels
provided (e) - executable only if expression e is true Declaration suffixes: Initial process - init $\{\ldots\}$ Explicit process activation - run procname (arguments) Processes
Declaration - proctype procname (parameters) $\{\ldots\}$
Activate with prefixes - active or active[N] else guard - executed if all others are false. if :: guard -> statements :: ... fi Guarded commands


[^0]:    Pan arguments
    -a find accep

    ## $\begin{array}{ll}\text {-a } & \text { find acceptance cycles } \\ -f & \text { weak fairness } \\ -1 & \text { find non-progress cycle }\end{array}$

