

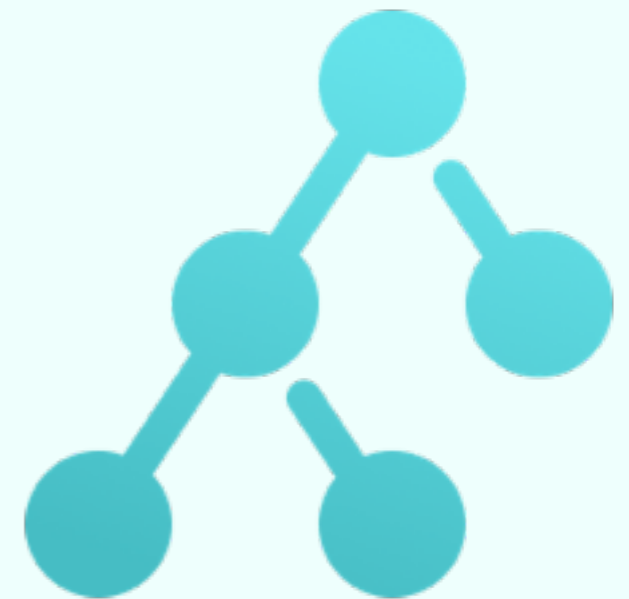


# Data Structures

## Exercise Session



Marco Vassena

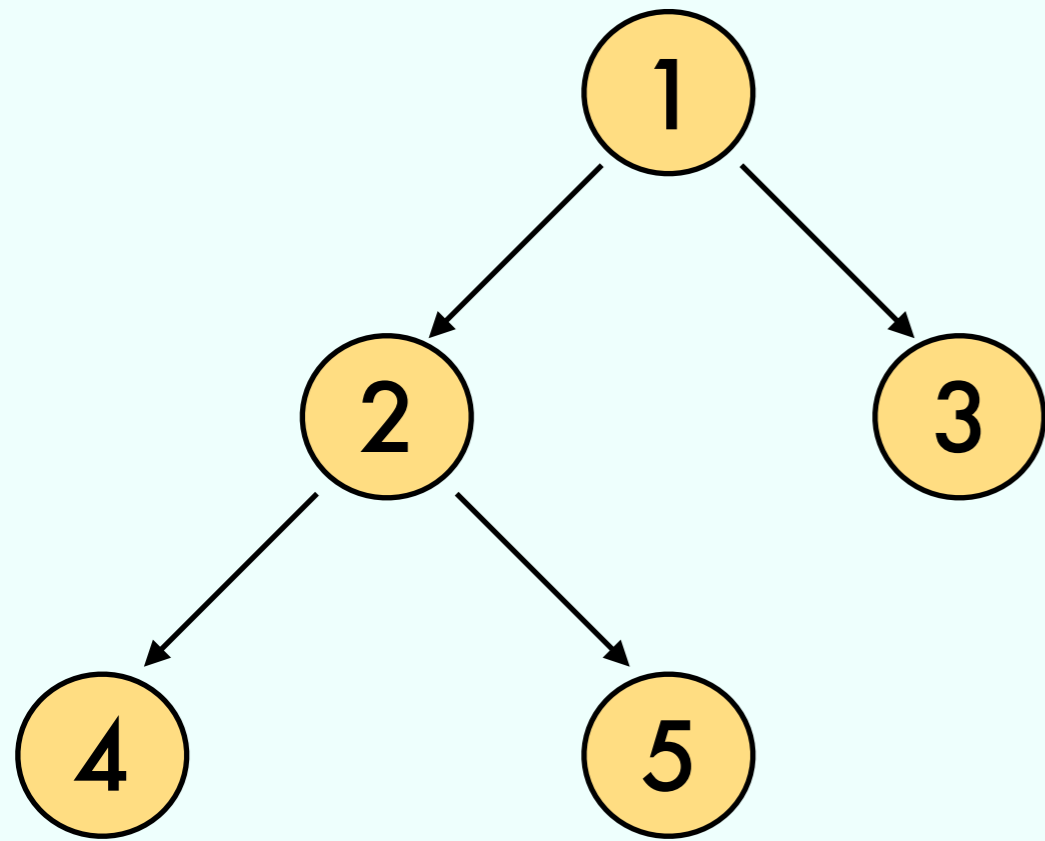


# Exercise 2 from 12/11

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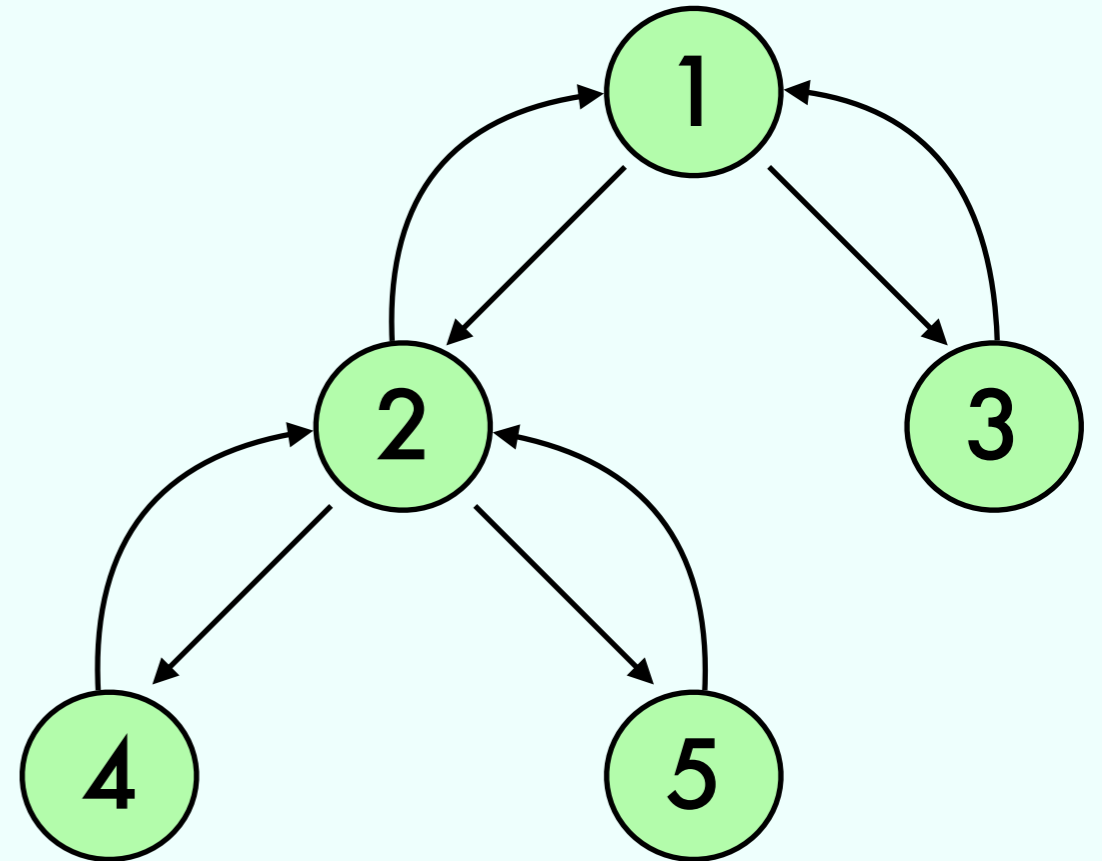
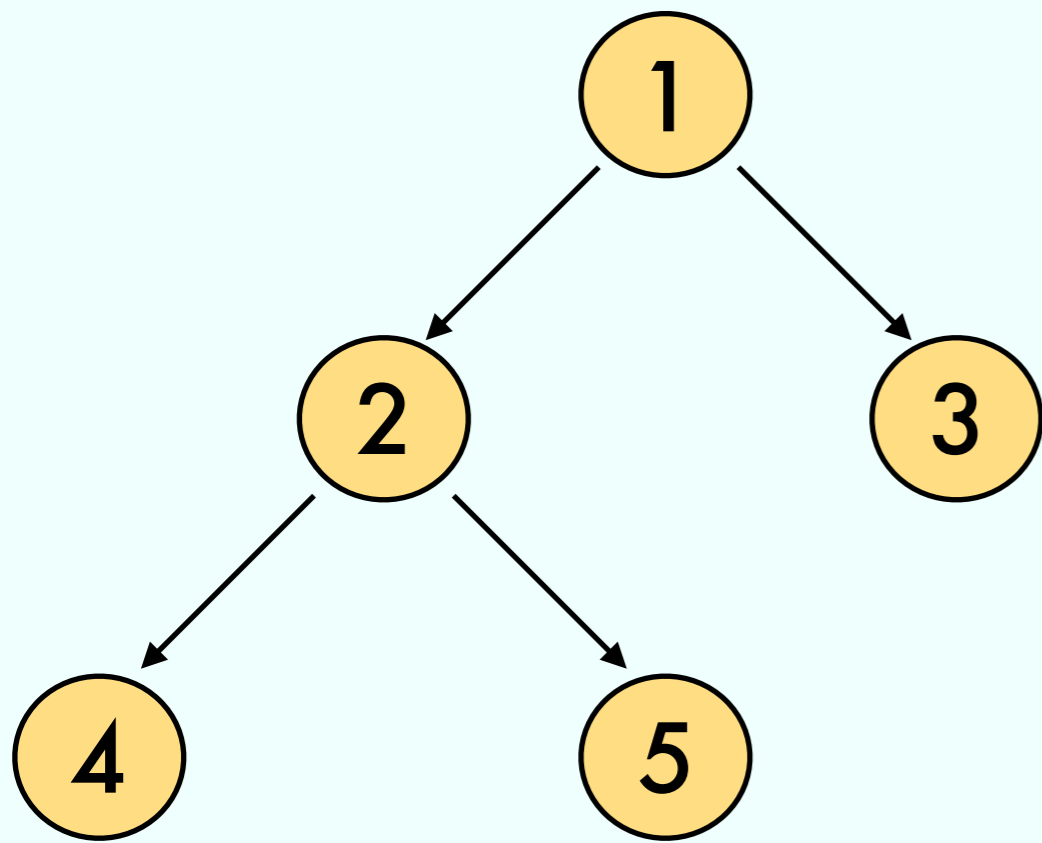
# Exercise 2 from 12/11

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# Exercise 2 from 12/11

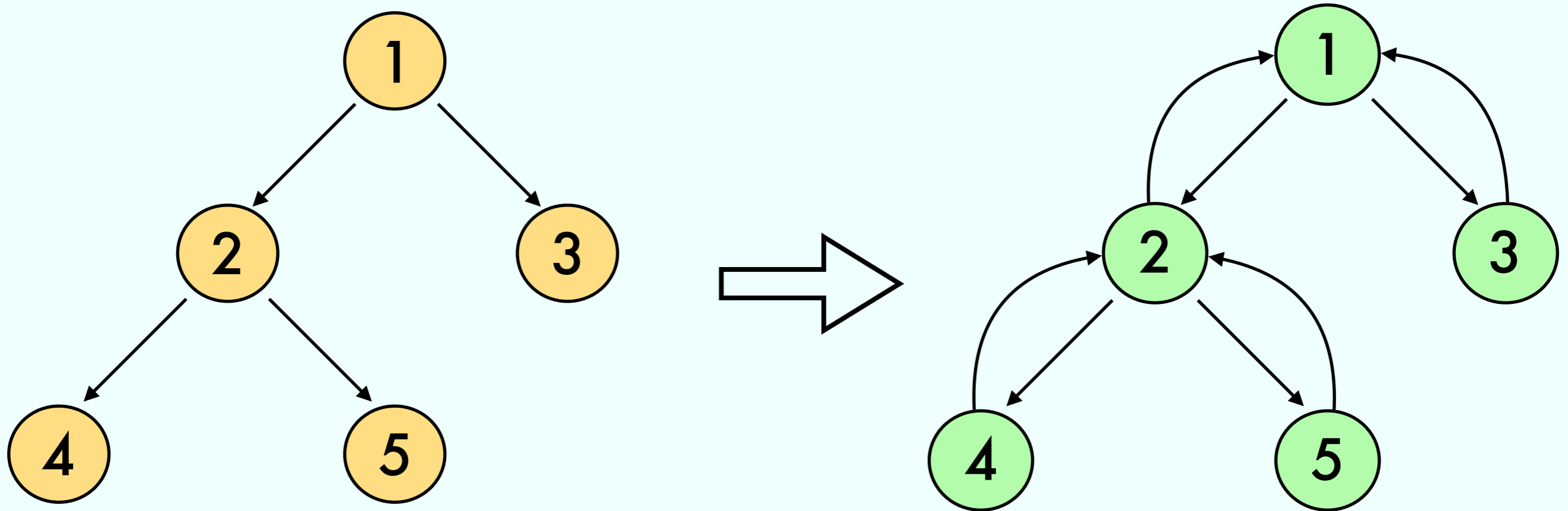
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Add to each node a reference to the parent

# Exercise 2 from 12/11

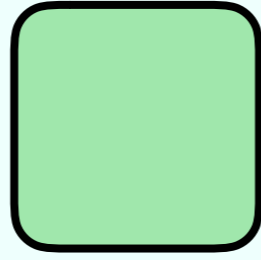
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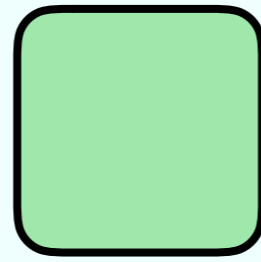
Add to each node a reference to the parent

# Tree

# Tree

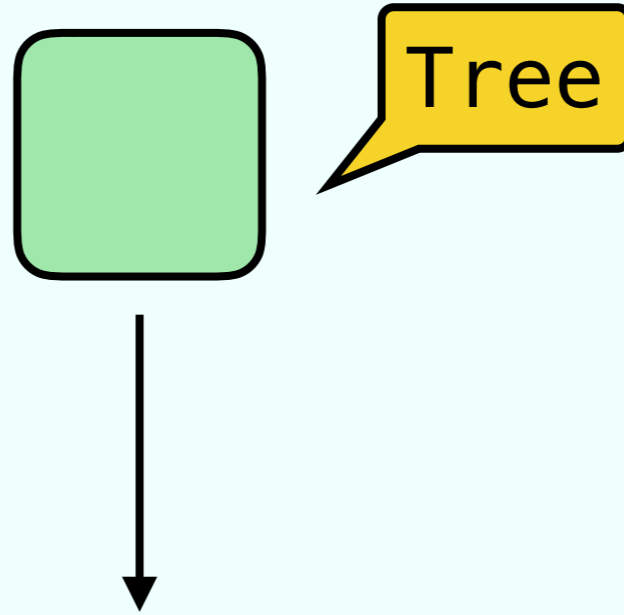


# Tree

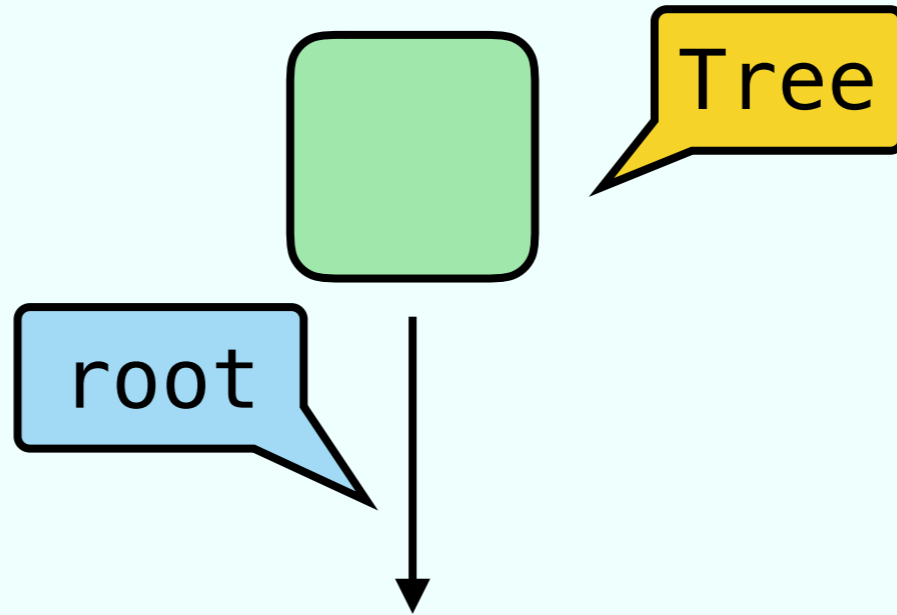




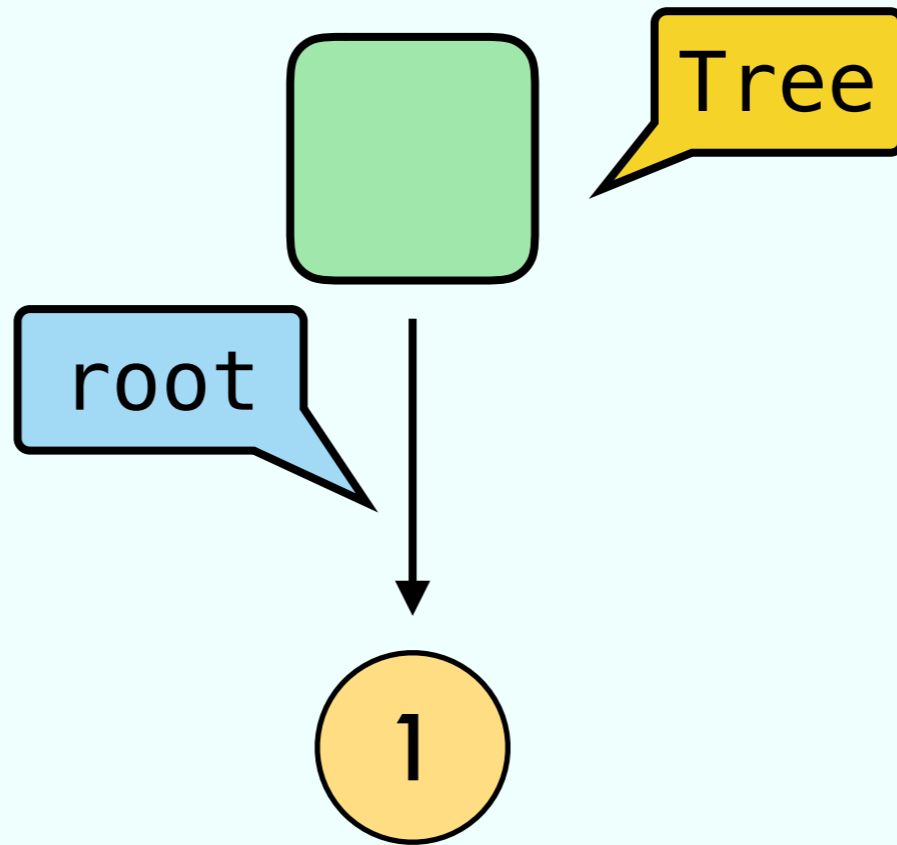
# Tree



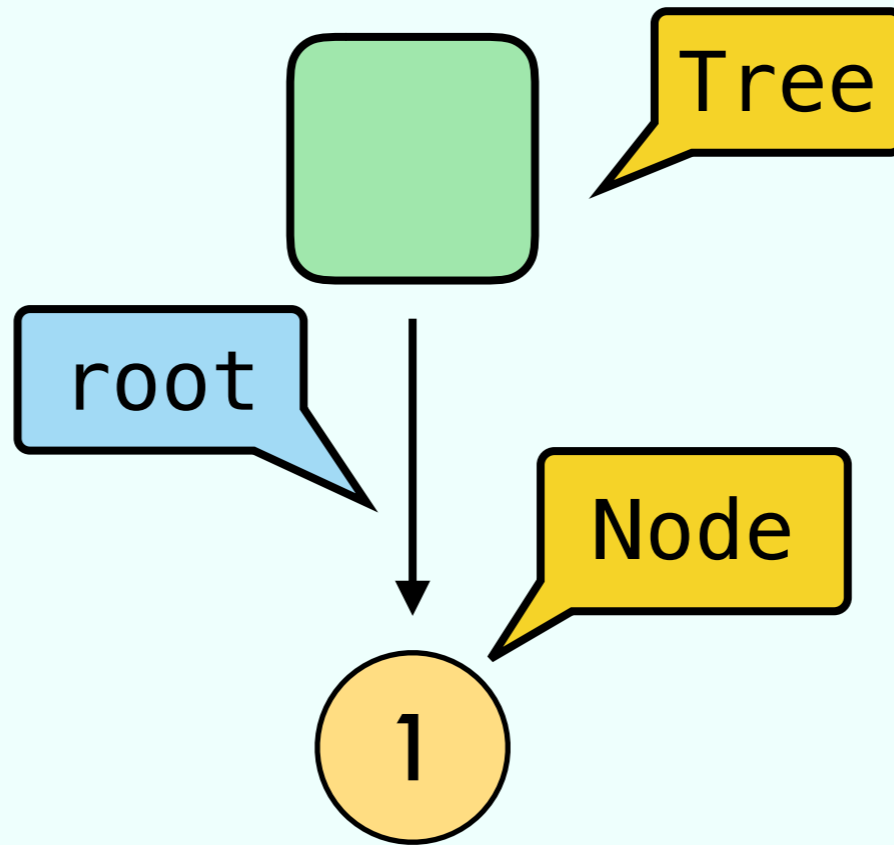
# Tree



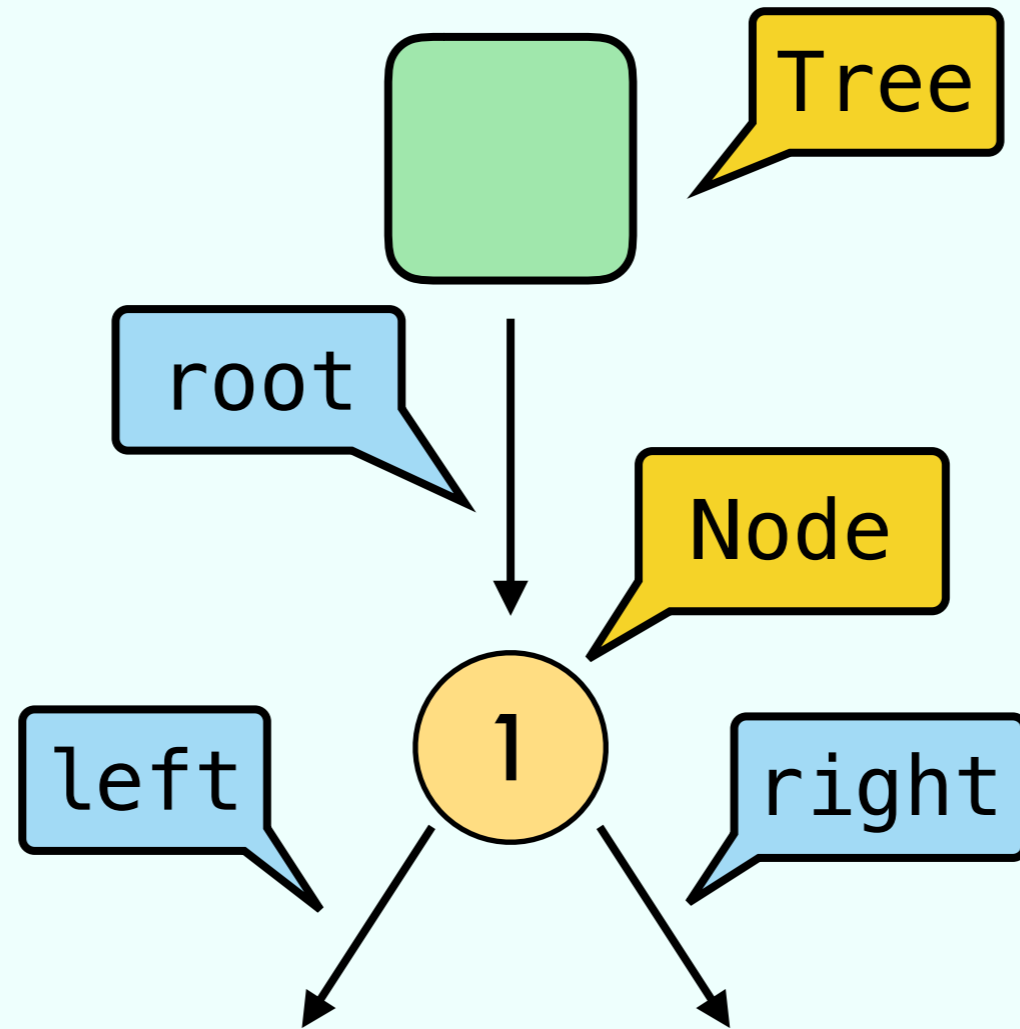
# Tree



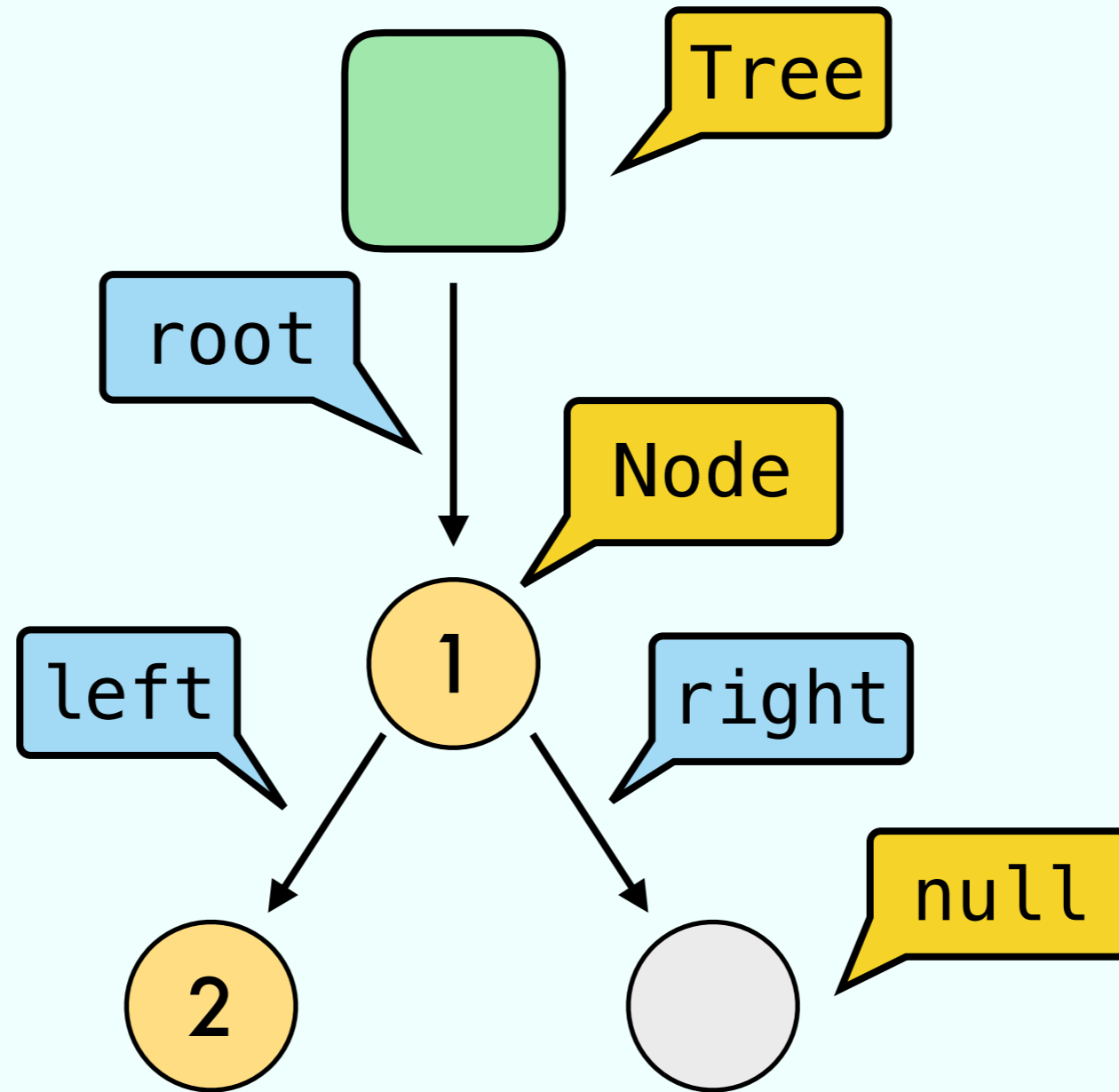
# Tree



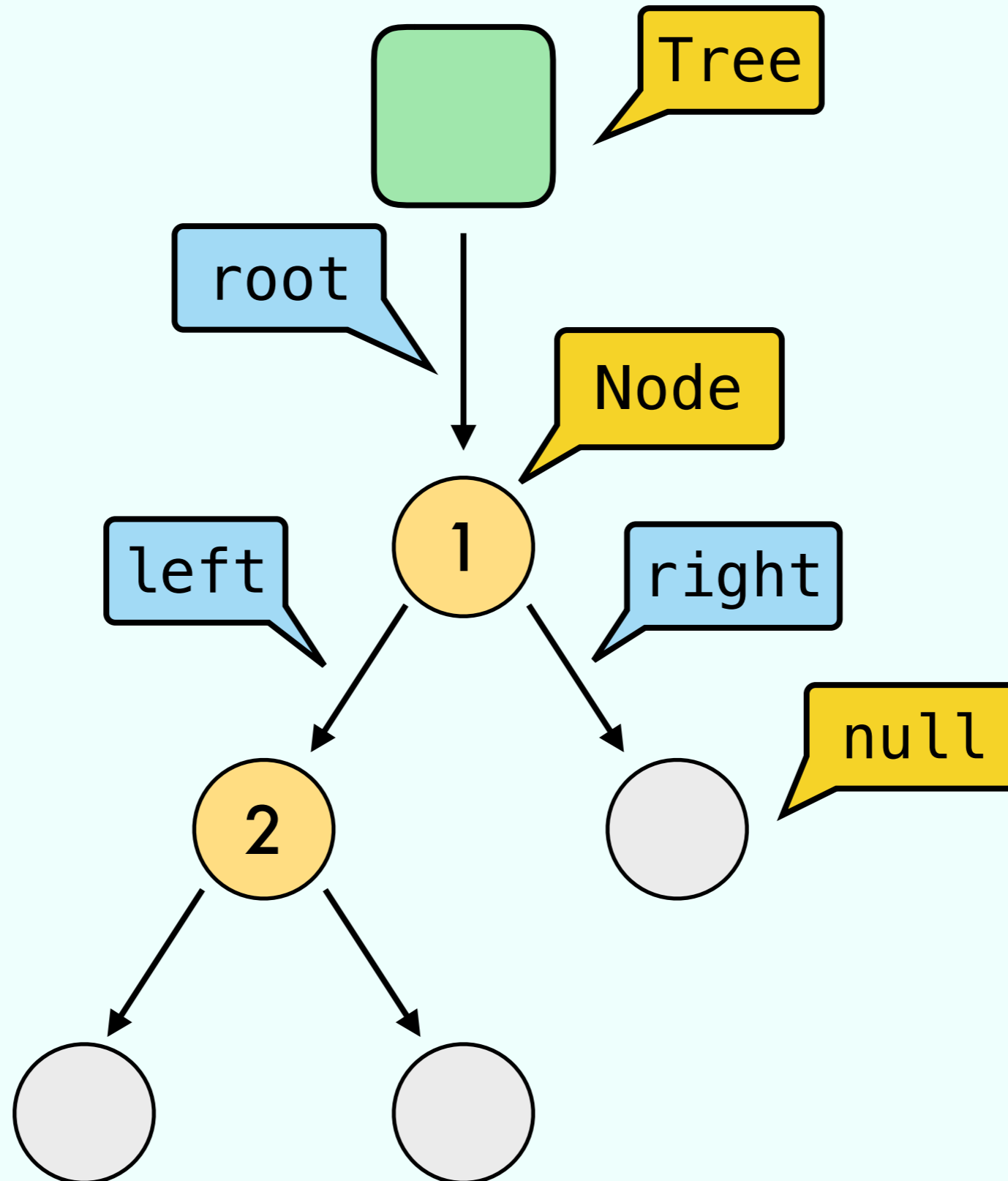
# Tree



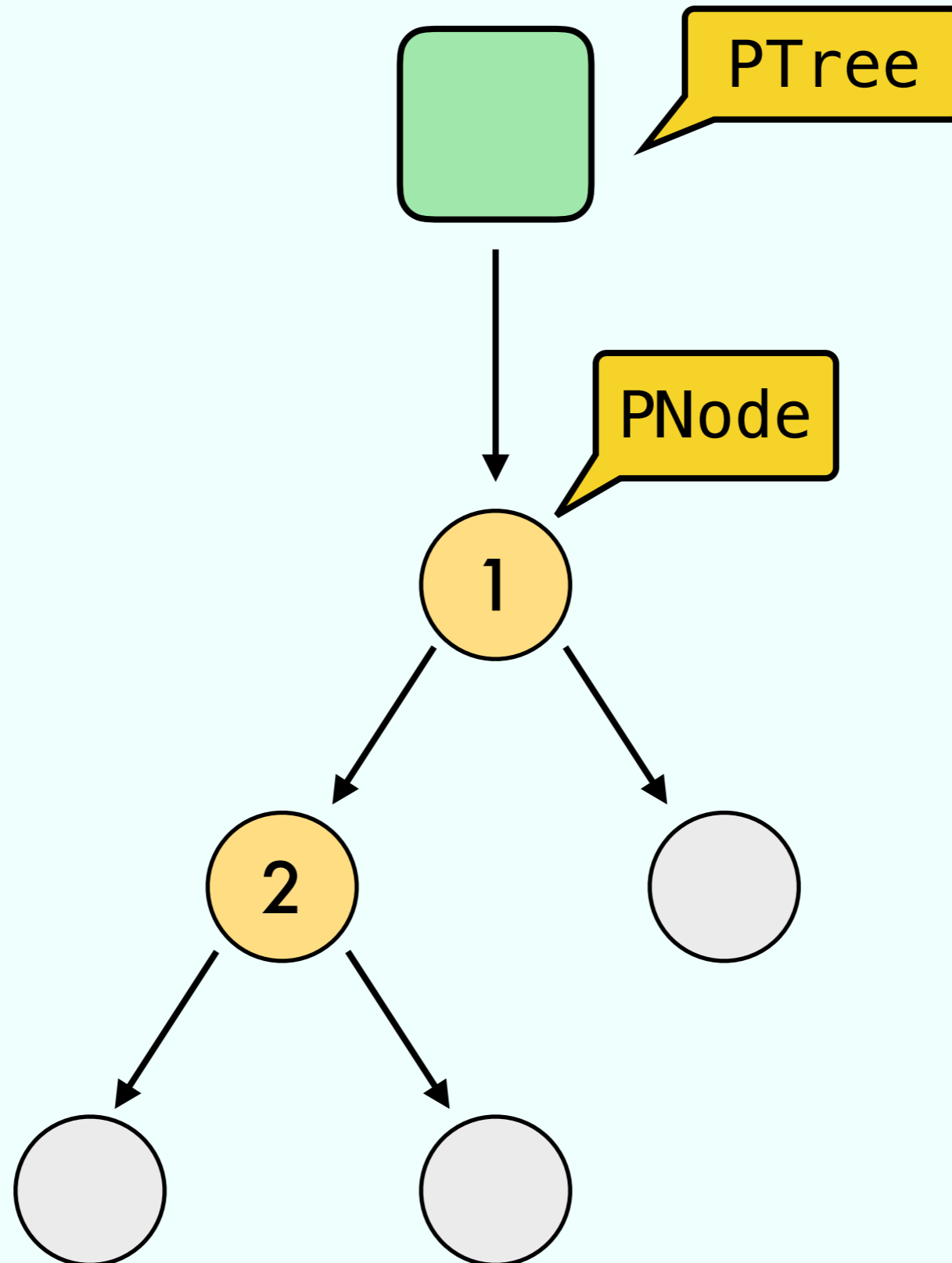
# Tree



# Tree

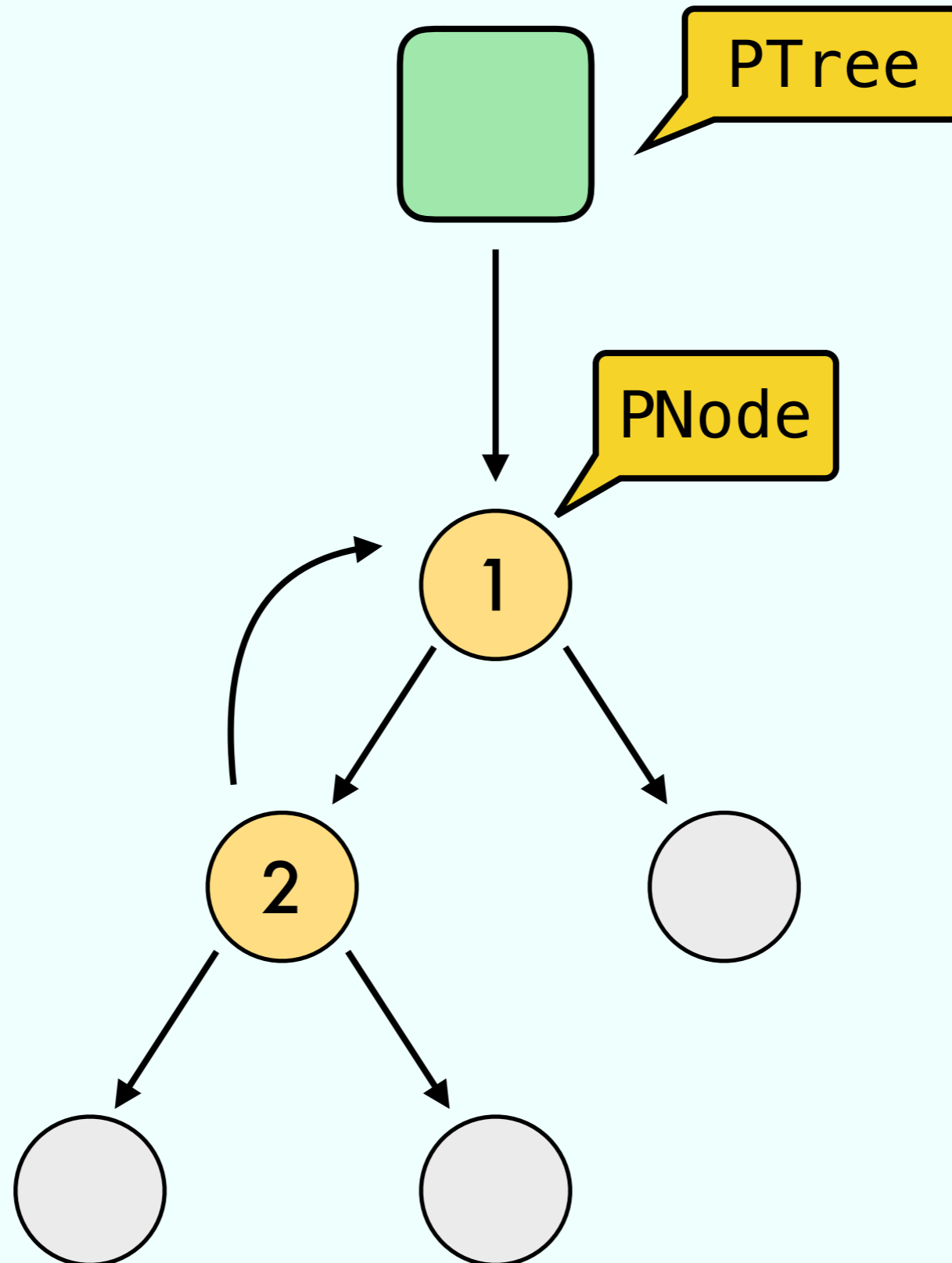


# Parent Tree

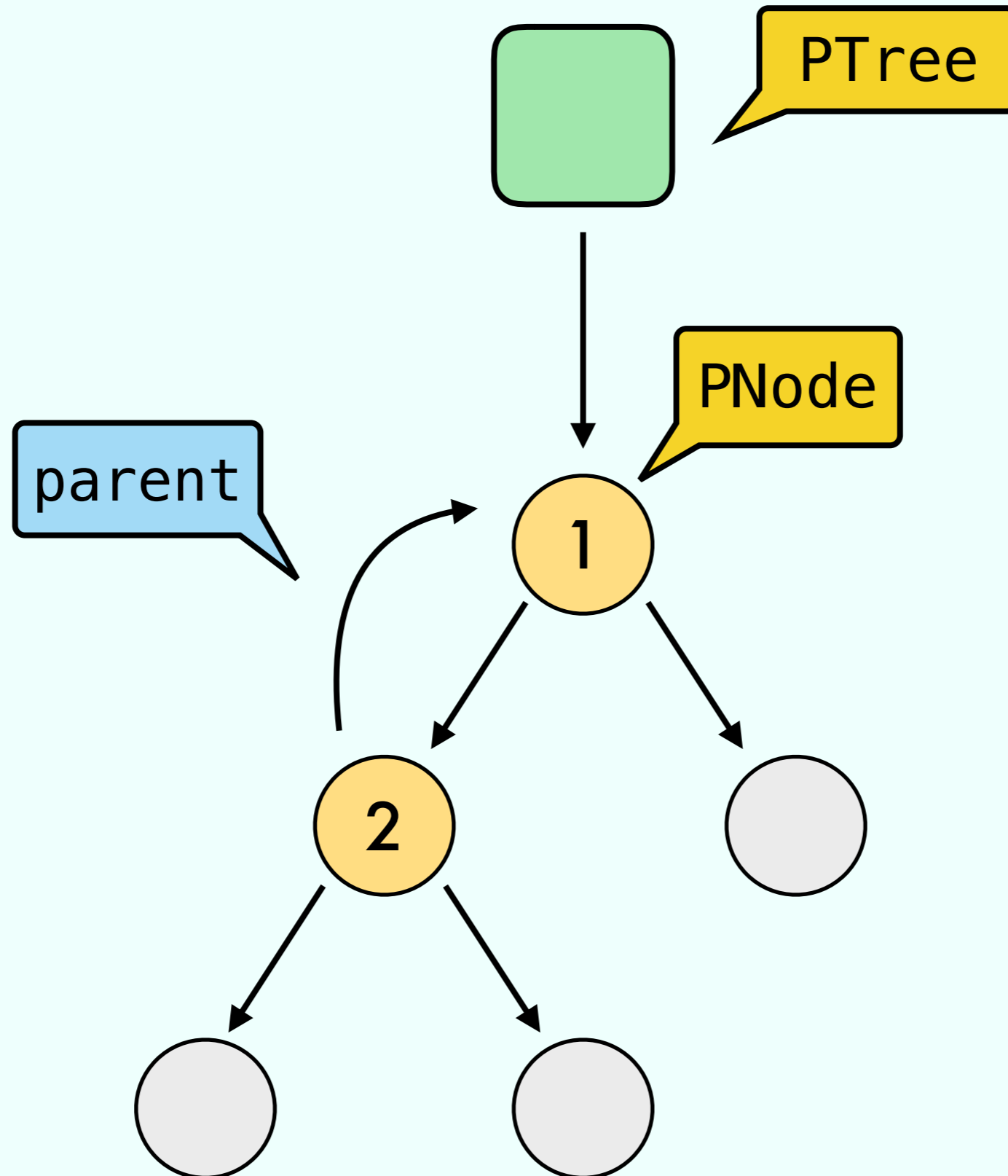




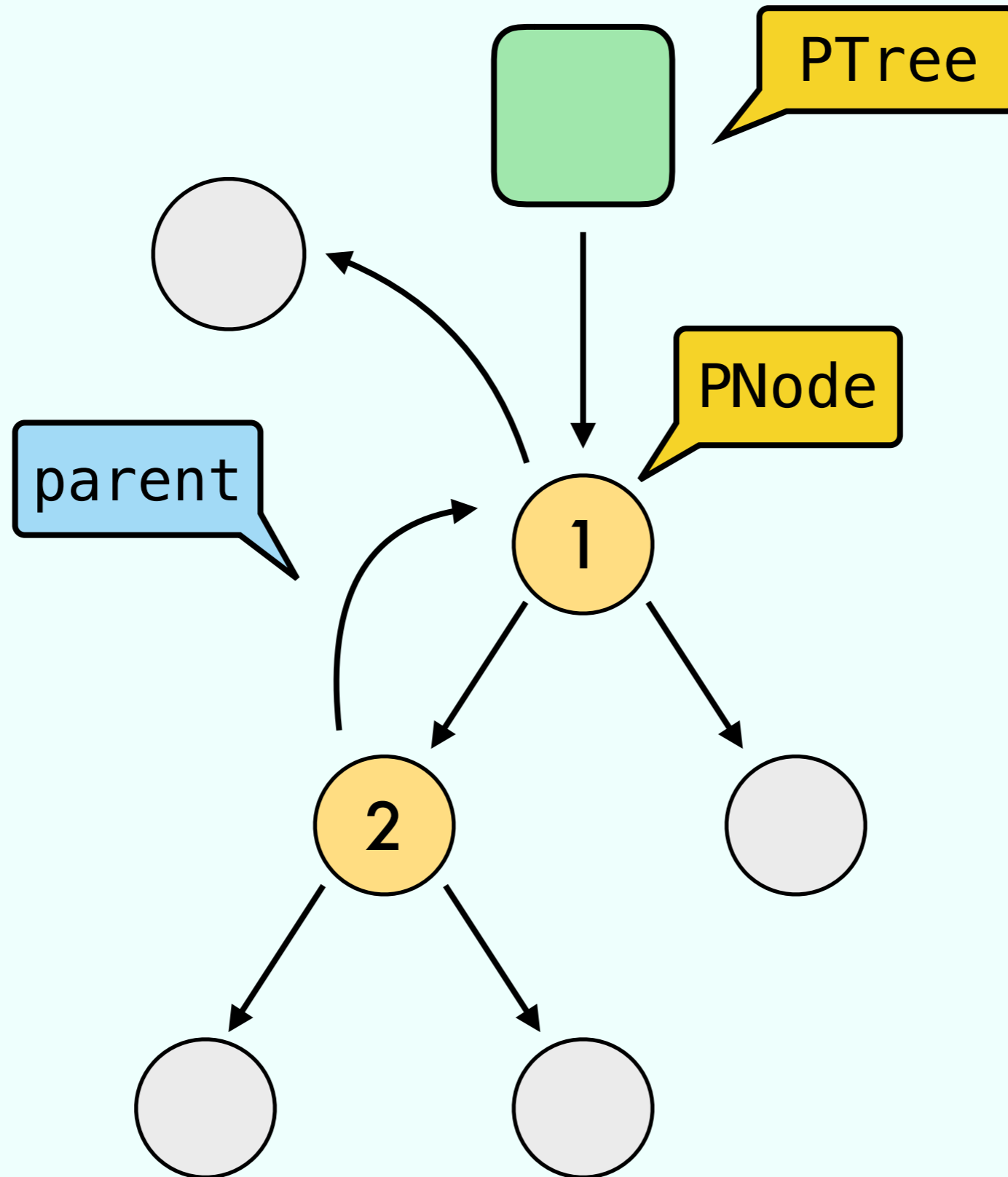
# Parent Tree



# Parent Tree



# Parent Tree



# Exercise 1 from 12/08

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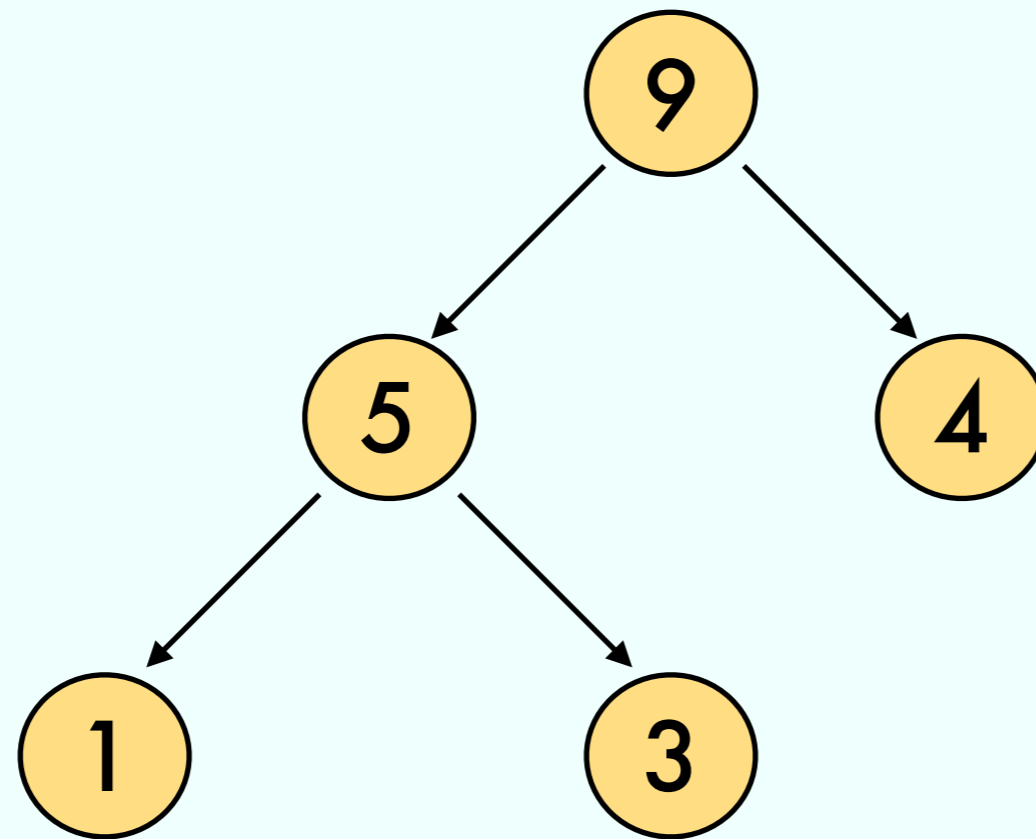
Analyze the time complexity

```
// A : Dynamic Array
// PQ : Priority Queue, |PQ| = N3
for(int i = 0; i < N; i++)
    A.add(0 , PQ.deleteMin())
```

in terms of N

# Heap Recap

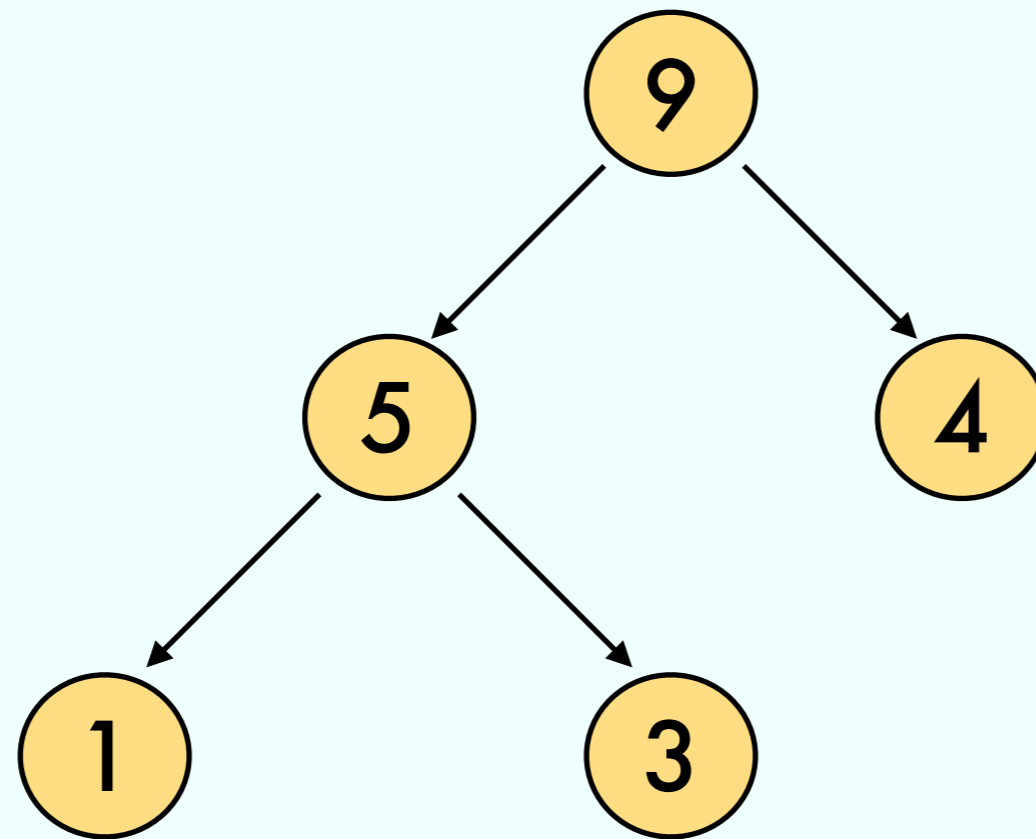
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# Heap Recap

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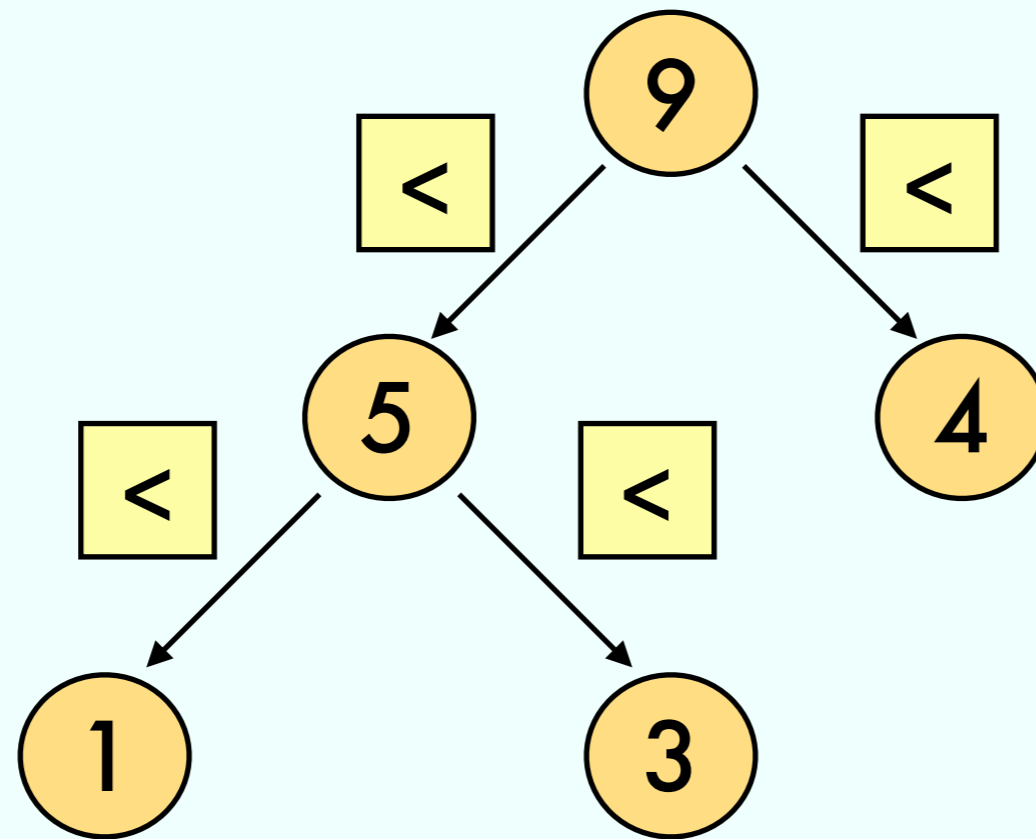
Order Property



# Heap Recap

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Order Property

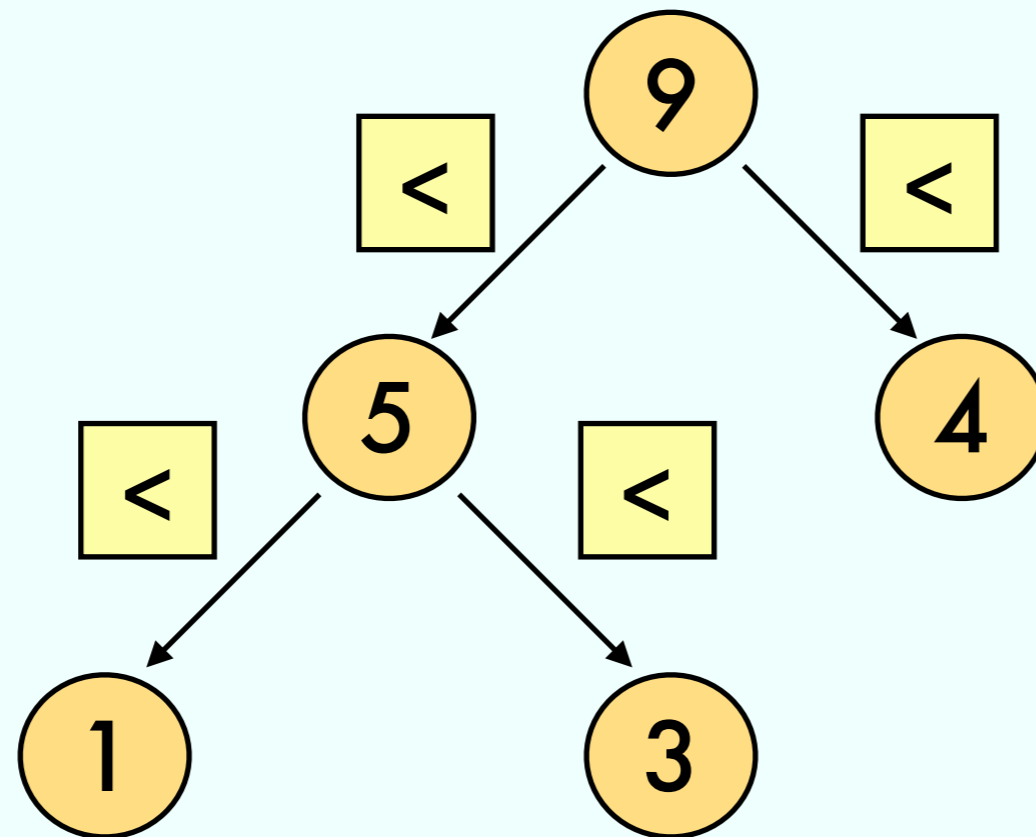


# Heap Recap

---

Order Property

Structure Property



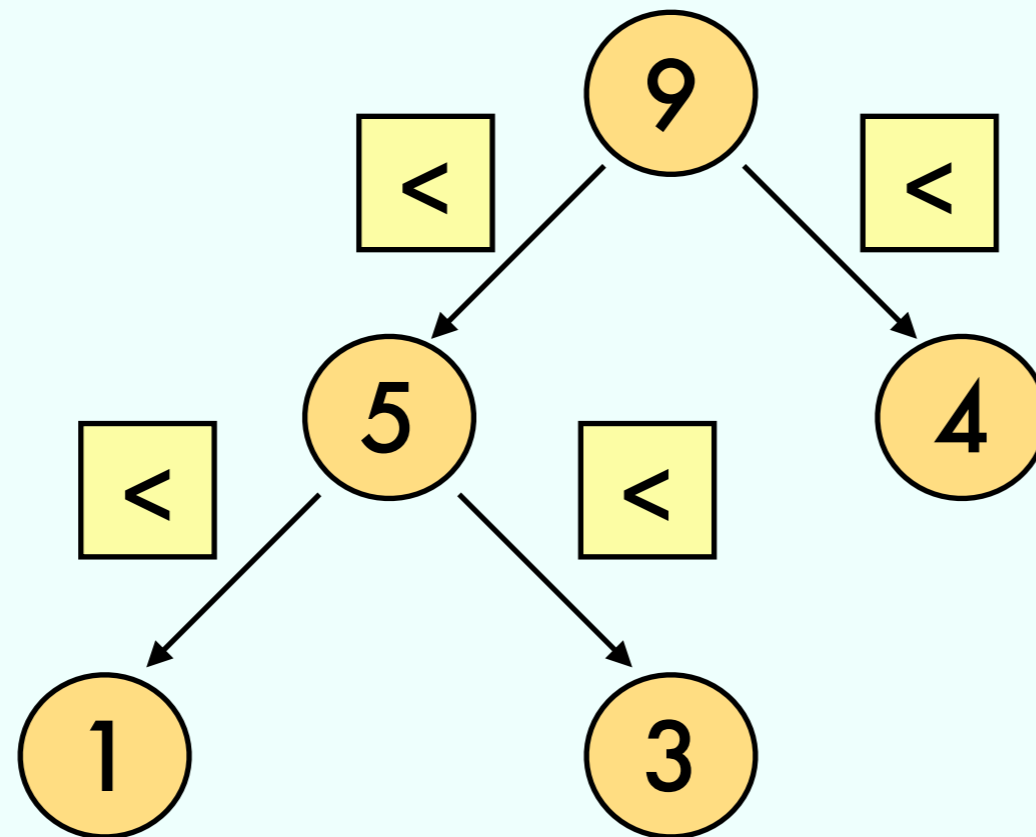


# Heap Recap

---

Order Property

Structure Property



Complete Binary Tree

Except Last Level

# Exercise 6.2, 6.3

---

**Draw the heap after each operation**

# Exercise 6.2, 6.3

---

Draw the heap after each operation

1. `for i in [10, 12, 1, 14, 6, 5, ...]  
PQ.insert(i)`

# Exercise 6.2, 6.3

---

Draw the heap after each operation

1. `for i in [10, 12, 1, 14, 6, 5, ...]  
 PQ.insert(i)`

2. `PQ = buildHeap([10, 12, 1, 14, 6, ...])`

# Exercise 6.2, 6.3

---

Draw the heap after each operation

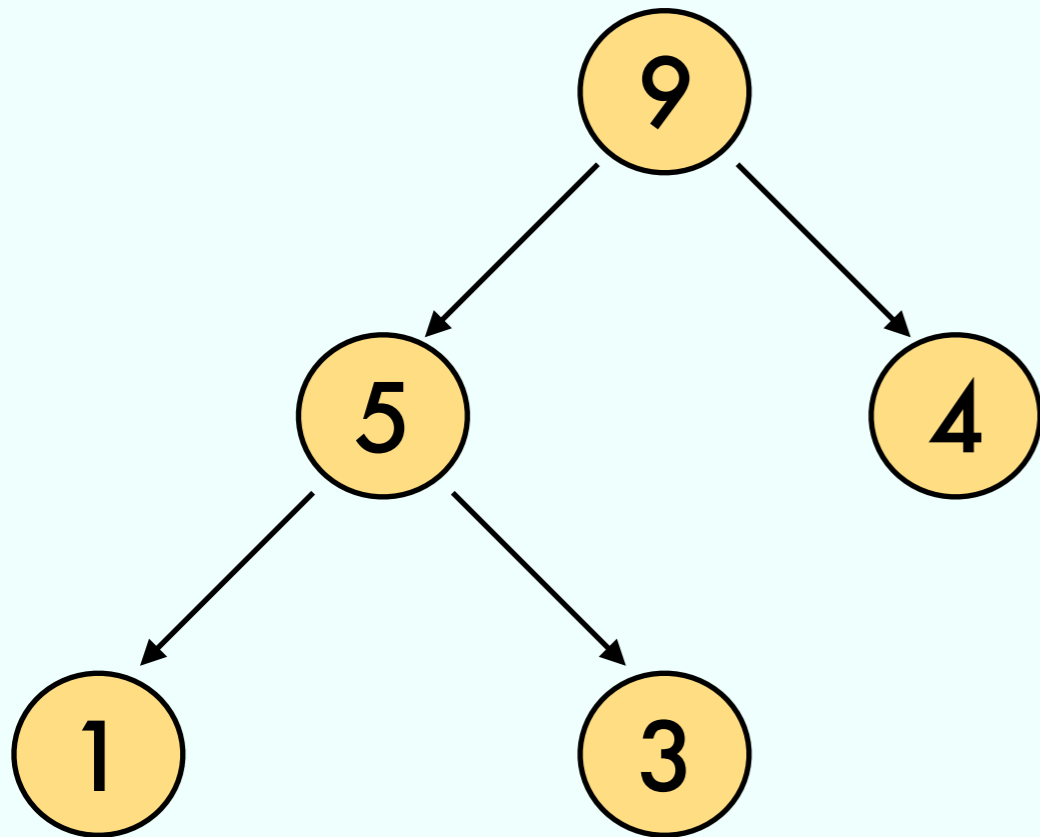
1. `for i in [10, 12, 1, 14, 6, 5, ...]  
PQ.insert(i)`

2. `PQ = buildHeap([10, 12, 1, 14, 6, ...])`

3. `PQ.deleteMin()`

# Heap Recap

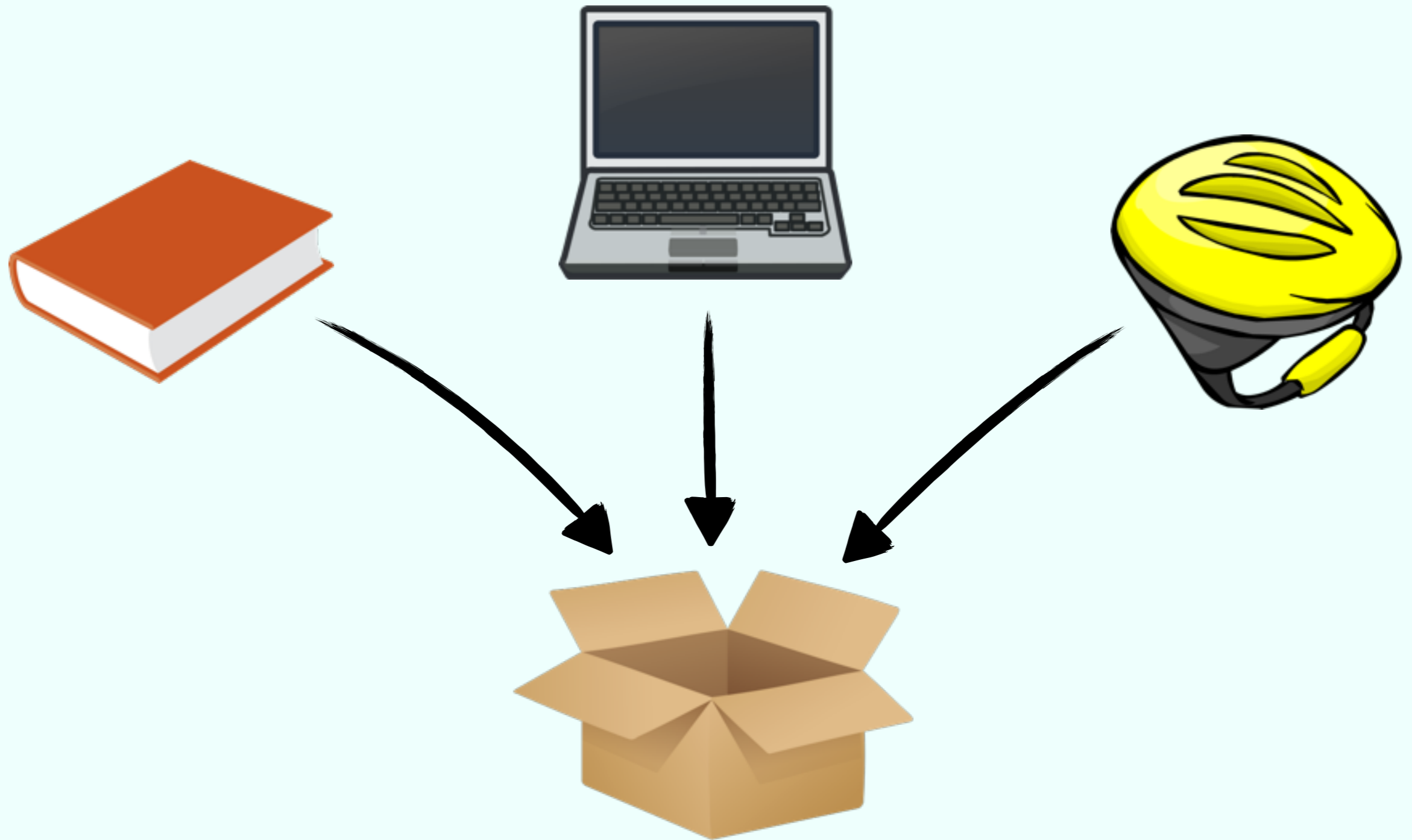
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Operation	Time Complexity
<code>findMin()</code>	$O(1)$
<code>deleteMin()</code>	$O(\log N)$
<code>insert(x)</code>	$O(\log N)$

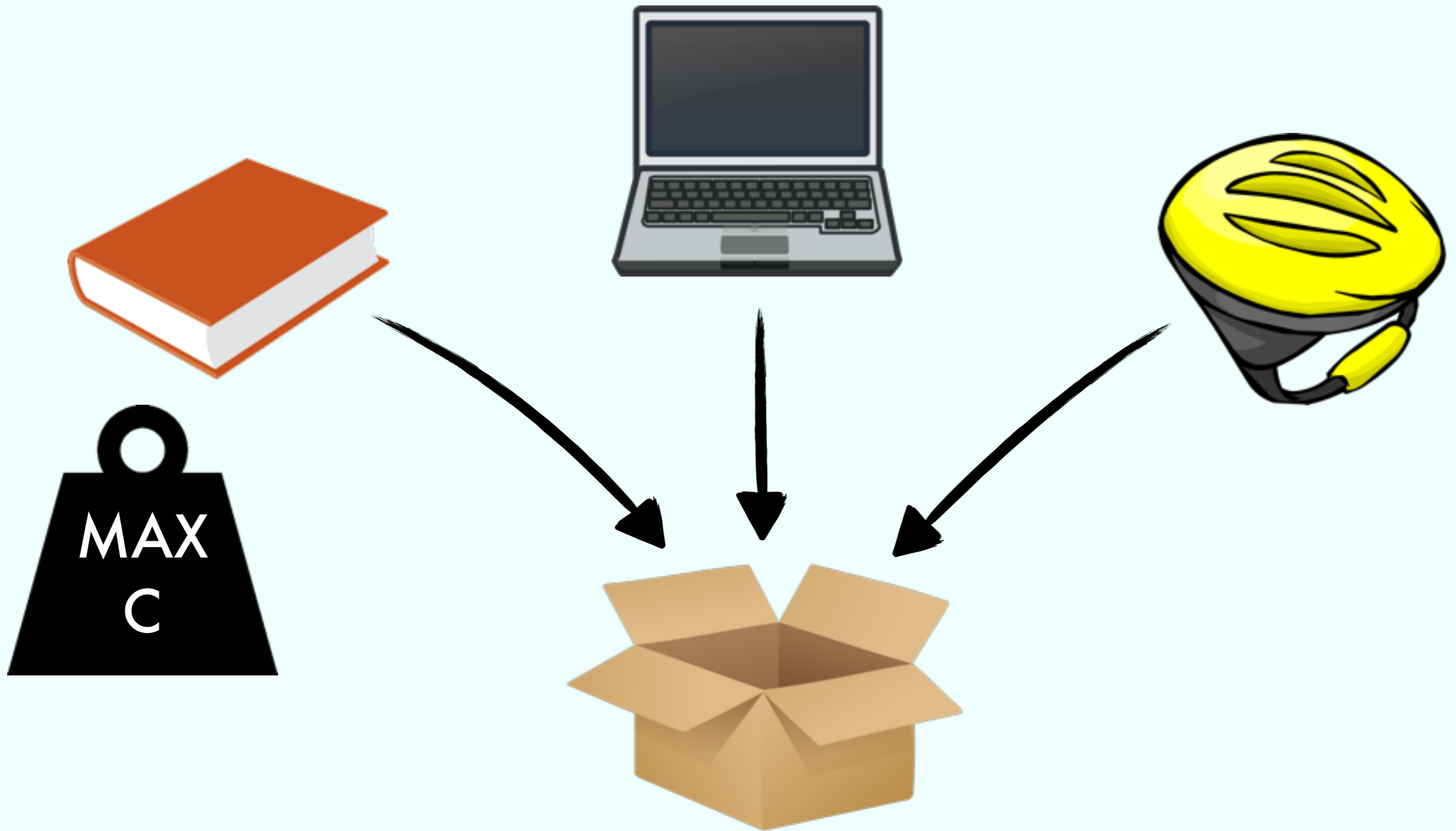
# Exercise 6.2, 6.3

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# Exercise 6.2, 6.3

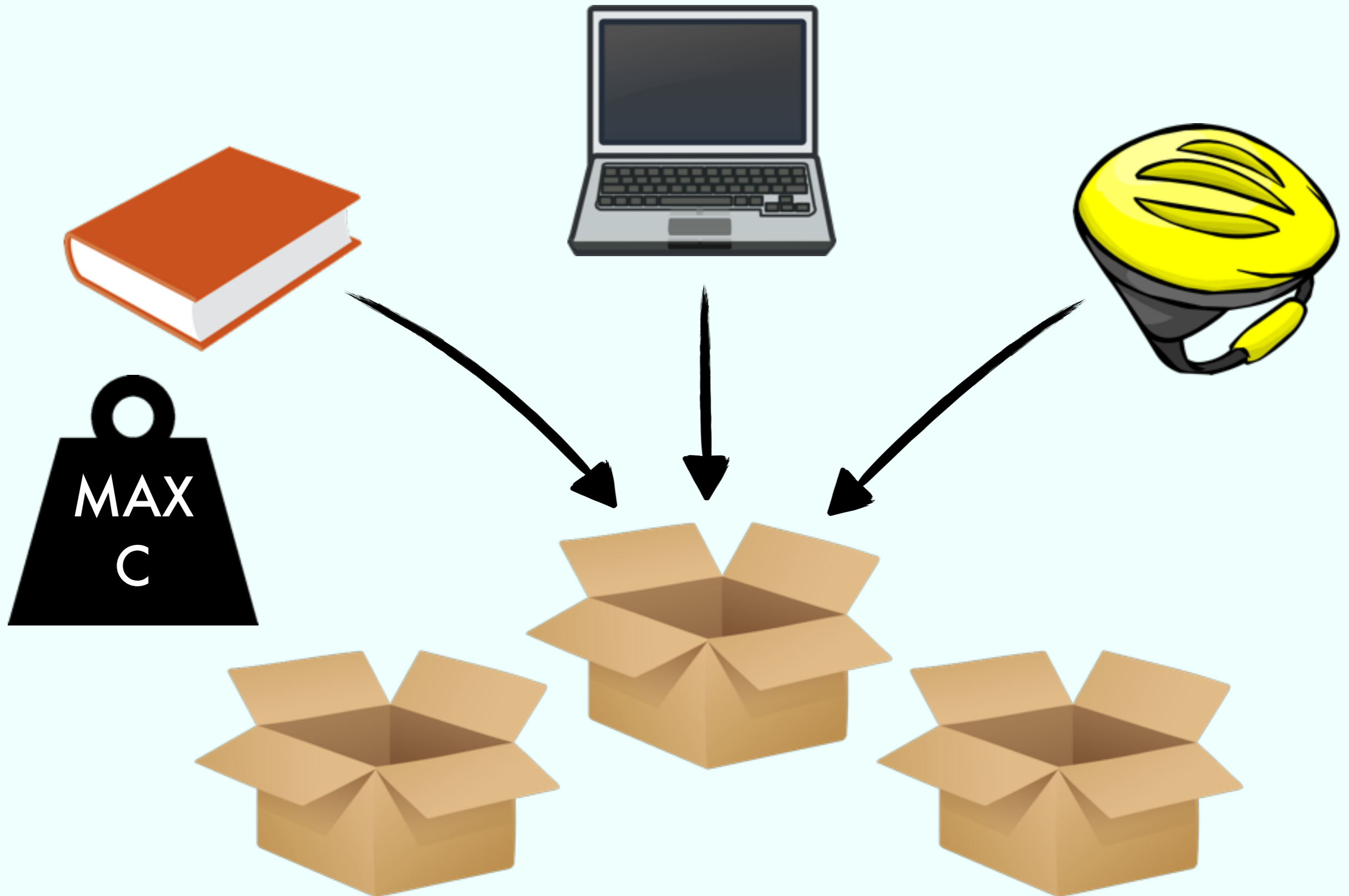
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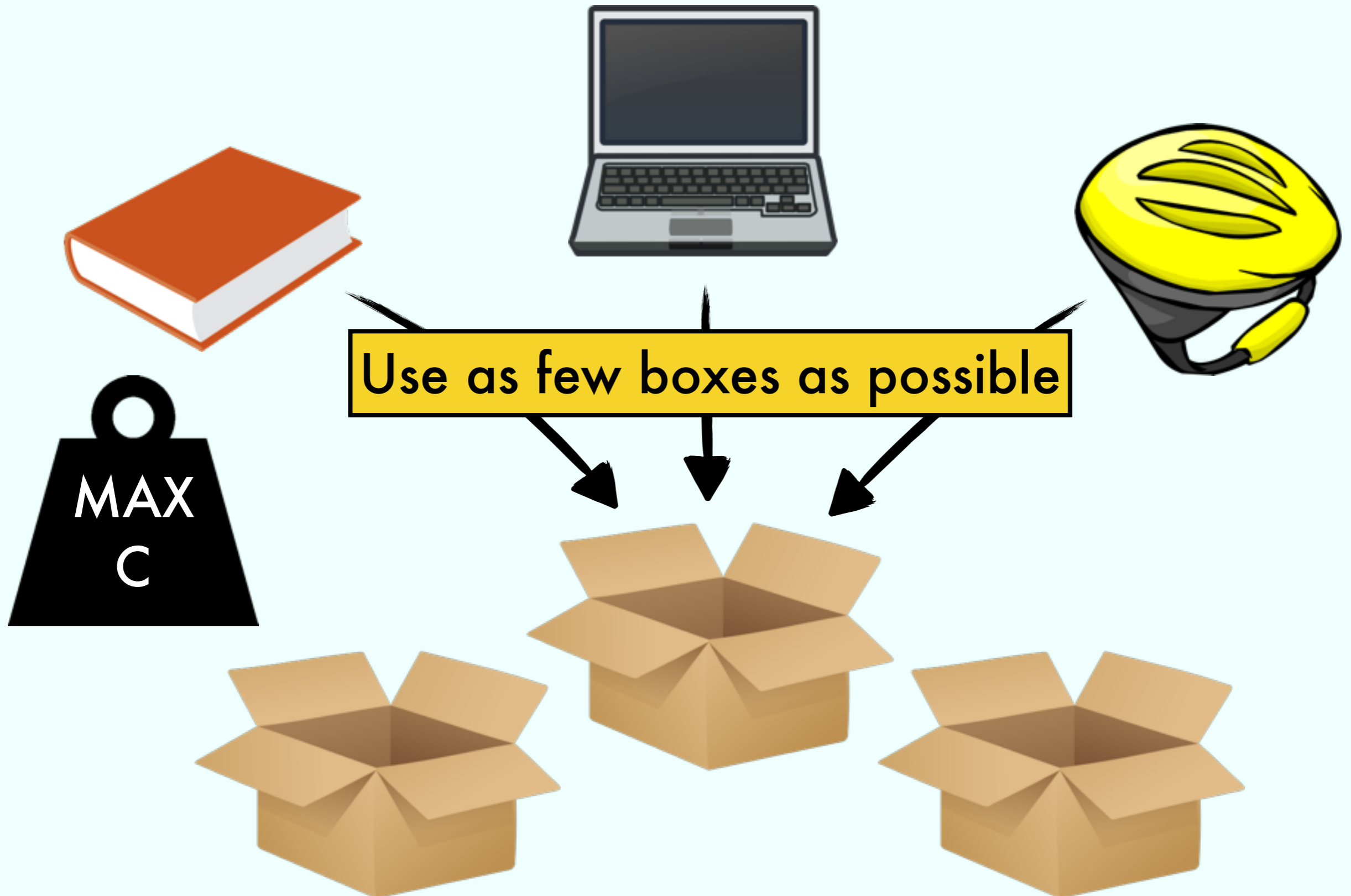
# Exercise 6.2, 6.3

---



# Exercise 6.2, 6.3

---



```
int pack (double C, double[] W)
```

- Use as few boxes as possible
- Put each weight in the box with most room for it

Capacity of boxes

```
int pack (double C, double[] W)
```

- Use as few boxes as possible
- Put each weight in the box with most room for it

Capacity of boxes

Weights of objects

```
int pack (double C, double[] W)
```

- Use as few boxes as possible
- Put each weight in the box with most room for it