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# Schedulability analysis

Complexity of feasibility testing:

(Leung, 1989; Baruah et al 1990)

The problem of deciding the feasibility of a schedule produced on m ≥ 1 processors by a <u>particular</u> static or dynamic priority assignment is NP-hard in the strong sense.

### Observation:

 If an optimal priority assignment can be found in polynomial time, the complexity of the priority assignment problem reduces to that of the feasibility testing problem.

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### **Priority assignment**

Relaxing the zero offset assumption:

 In order for the RM, DM and EDF priority-assignment policies to be optimal for the single-processor case we assume synchronous task sets where the offsets of tasks are identical, that is:

$$\forall i, j : O_i = O_i$$

In asynchronous task sets the offsets of at least one pair of tasks are not identical, that is:

$$\exists i, j : i \neq j, O_i \neq O_j$$

Asynchronous task sets are typically used to reduce jitter or to remove the need for resource access protocols (e.g. PCP).

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# **Priority assignment**

A priority assignment policy P is said to be <u>optimal</u> with respect to <u>a feasibility test</u> S and a given task model, if and only if the following holds: P is optimal if there are no task sets that are compliant with the task model that are deemed schedulable by test S using another priority assignment policy, that are not also deemed schedulable by test S using policy P.

#### Observations:

 The definition is applicable to both sufficient feasibility tests and exact feasibility tests; optimal performance is still provided with respect to the limitations of the test itself.

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# **Priority assignment**

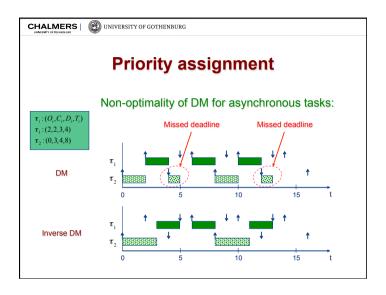
Relaxing the zero offset assumption (cont'd):

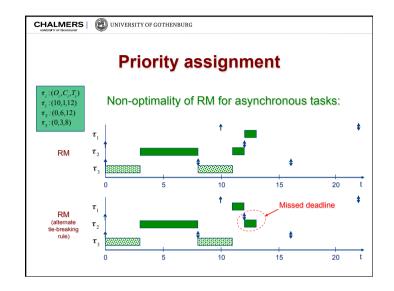
 In an asynchronous task set two tasks with identical periods but different offsets could never be released simultaneously during the lifetime of the system.

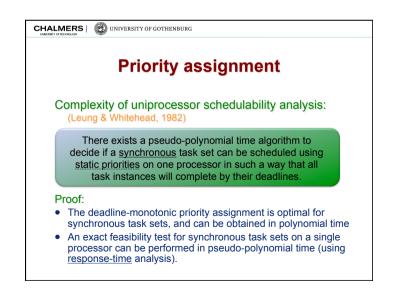
This means that the worst-case response times of the tasks will be lower than if the offsets of the task were equal.

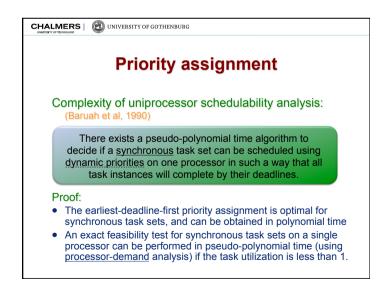
 A priority-assignment policy that is shown to be optimal for a synchronous system is not necessarily optimal for an asynchronous system.

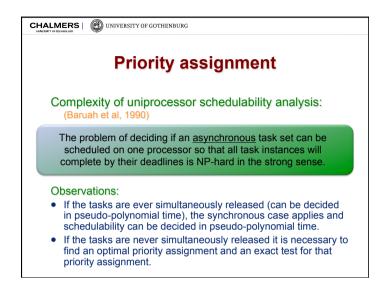
For example, it is known that RM and DM are not optimal for asynchronous task systems. (Leung & Whitehead, 1982)

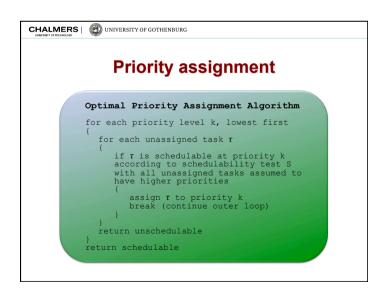


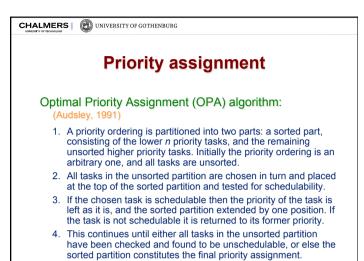


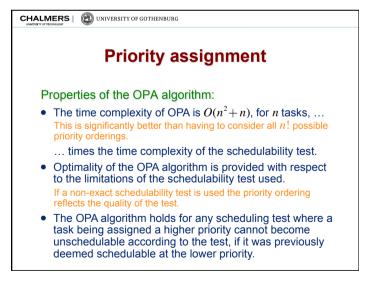


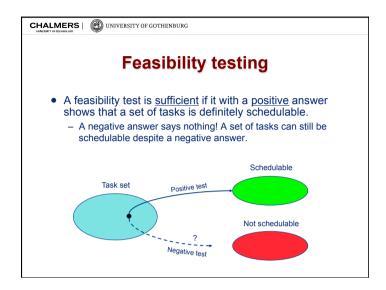


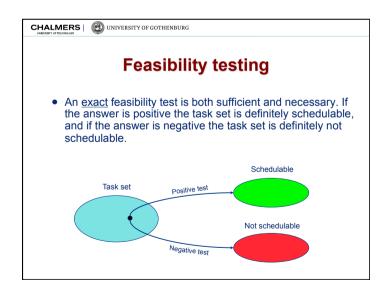


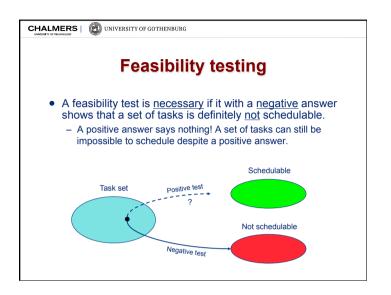


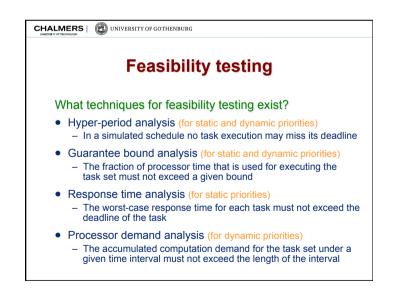








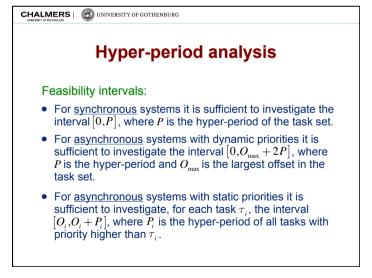


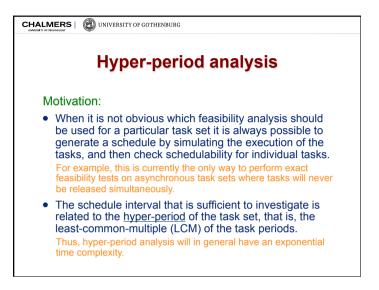


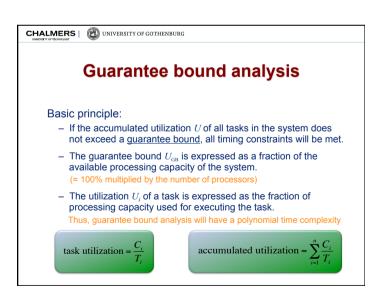


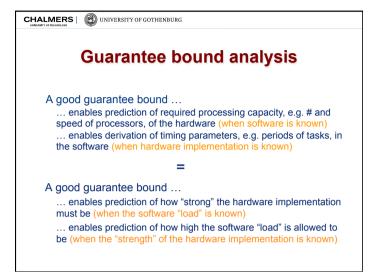
- The accumulated computation demand for the task set under a

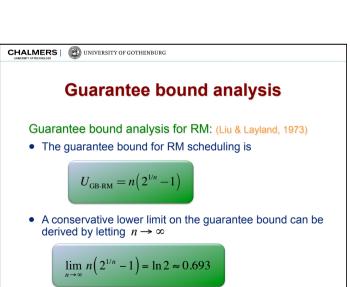
given time interval must not exceed the length of the interval

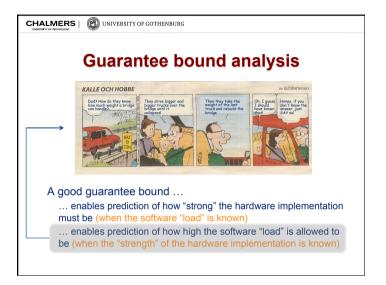












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Guarantee bound analysis for RM: (Liu & Layland, 1973)

• A sufficient condition for RM scheduling is  $U = \sum_{i=1}^{n} \frac{C_i}{T_i} \le n \Big( 2^{1/n} - 1 \Big)$ • The test is only valid if all of the following conditions apply:

1. Single-processor system
2. Synchronous task sets
3. Independent tasks
4. Periodic or sporadic tasks
5. Tasks have deadlines equal to period  $(D_i = T_i)$ 

