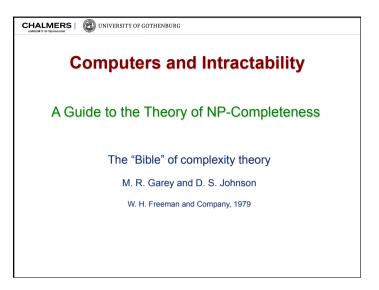
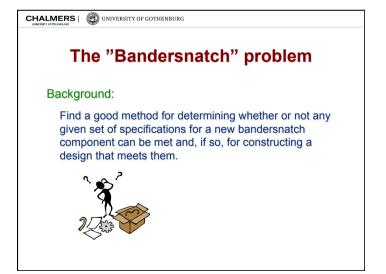


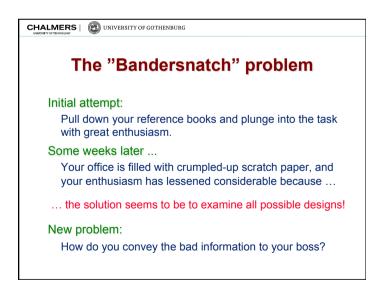
Lecture #3

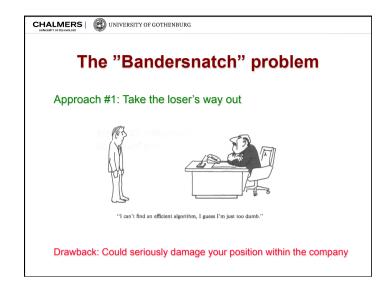
Professor Jan Jonsson

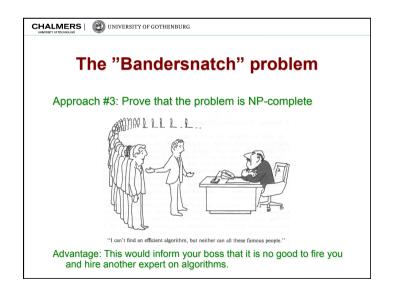
Department of Computer Science and Engineering Chalmers University of Technology

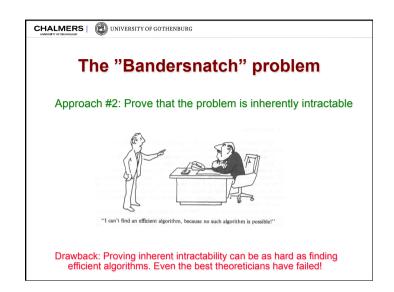


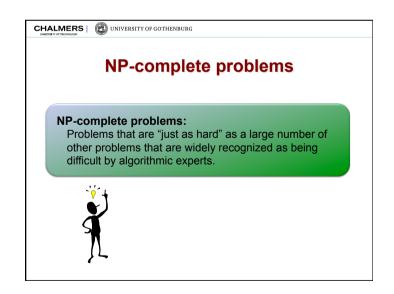


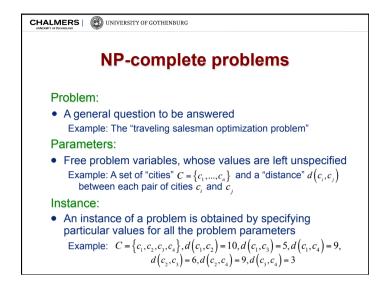


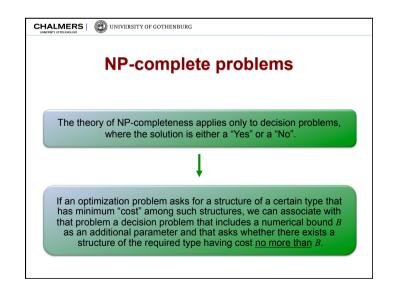


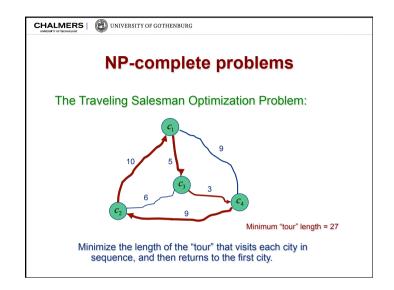


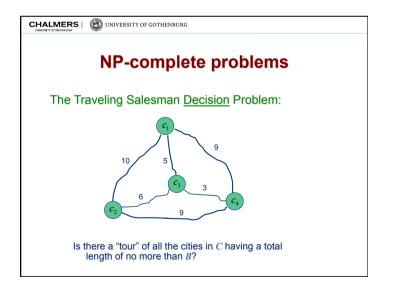












## Intractability

Reasonable encoding scheme:

- Conciseness:
  - The encoding of an instance I should be concise and not "padded" with unnecessary information or symbols
  - Numbers occurring in I should be represented in binary (or decimal, or octal, or in any fixed base other than 1)
- Decodability:
  - It should be possible to specify a polynomial-time algorithm that can extract a description of any component of I.

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## Intractability

Polynomial-time algorithm:

 An algorithm whose time-complexity function is O(p(Len)) for some polynomial function p, where Len is the input length.

Exponential-time algorithm:

 Any algorithm whose time-complexity function cannot be so bounded.

A problem is said to be <u>intractable</u> if it is so hard that no polynomial-time algorithm can possibly solve it.

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## Intractability

Input length:

The number of information symbols needed for describing a problem instance using a reasonable encoding scheme
Example: Len = n + [log, B] + max {[log, d(c,c,)]: c,c,c ∈ C}

Largest number:

• The magnitude of the largest number in a problem instance Example:  $Max = \max \left\{ d(c_i, c_j) : c_i, c_j \in C \right\}$ 

Time-complexity function:

 Expresses an algorithm's time requirements giving, for each possible input length, the largest amount of time needed by the algorithm to solve a problem instance of that size

## Class P

Deterministic algorithm: (Deterministic Turing Machine)

- Finite-state control:
  - The algorithm can pursue only one computation at a time
  - Given a problem instance I, some structure (= solution) S is derived by the algorithm
  - The correctness of S is inherent in the algorithm

The <u>class P</u> is the class of all decision problems  $\Pi$  that, under reasonable encoding schemes, can be solved by polynomial-time deterministic algorithms.

