Software Engineering using Formal Methods Proof Obligations

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making the connection between

JML

and

Dynamic Logic / KeY

making the connection between

JML

and

Dynamic Logic / KeY

generating,

making the connection between

JML

and

Dynamic Logic / KeY

- generating,
- understanding,

making the connection between

JML

and

Dynamic Logic / KeY

- generating,
- understanding,
- and proving

DL proof obligations from JML specifications

Tutorial Example

```
we follow 'KeY Quicktour' (for KeY 1.6) (cited below as [KQ])

paper + sources:
see 'KeY Quicktour' on course page, under 'Links, Papers, and Software'

scenario: simple PayCard
```

Inspecting JML Specification

inspect quicktour/jml/paycard/PayCard.java

follow [KQ, 2.2]

New JML Feature I: Nested Specification Cases

```
method charge() has nested specification case:
@ public normal behavior
@ requires amount > 0;
0 { |
0
    requires amount + balance < limit && isValid()==true;</pre>
    ensures \result == true;
0
    ensures balance == amount + \old(balance);
@
0
    assignable balance;
0
0
    also
@
0
    requires amount + balance >= limit;
@
    ensures \result == false;
@
    ensures unsuccessfulOperations
@
             == \old(unsuccessfulOperations) + 1;
@
    assignable unsuccessfulOperations;
```

nested specification cases allow to factor out common preconditions

```
@ public normal_behavior
@ requires R;
0 { |
@
    requires R1;
0
    ensures E1;
@
    assignable A1;
@
0
    also
0
    requires R2;
0
    ensures E2;
0
    assignable A2;
  1}
expands to ... (next page)
```

```
(previous page) ... expands to
@ public normal_behavior
0 requires R;
@ requires R1;
@ ensures E1:
@ assignable A1;
0
 also
0
@ public normal_behavior
@ requires R;
@ requires R2;
@ ensures E2;
@ assignable A2;
```

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@
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0
0
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    requires amount + balance >= limit;
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    ensures \result == false;
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    ensures unsuccessfulOperations
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```

method charge() has exceptional behavior case:

- @ public exceptional_behavior
- @ requires amount <= 0;</pre>
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- assignable clause is local to specification case

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difference to pure:

- ▶ pure is method-global, also prohibits non-termination & exceptions
- assignable clause is local to specification case
- pure not usable in this particular context

generate EnsuresPost PO for normal behavior of charge()

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follow [KQ, 3.1+3.2]

summary:

- start KeY prover
- ▶ in quicktour/jml, open paycard
- select paycard > PayCard > charge and EnsuresPost
- ► inspect Assumed Invariants

generate EnsuresPost PO for normal behavior of charge()

follow [KQ, 3.1+3.2]

summary:

- start KeY prover
- ▶ in quicktour/jml, open paycard
- select paycard > PayCard > charge and EnsuresPost
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 - ▶ is fully sound
 - can compromise provability

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- select contract which modifies balance (in JML: modifies synonymous for assignable)
- Current Goal pane displays proof obligation as DL sequent

for loading more proof obligations: re-open **Proof Obligation Browser** under **Tools** menu (or **Ctrl-B**)

generate EnsuresPost PO for normal behavior of isValid()

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generate EnsuresPost PO for normal behavior of isValid()

generate EnsuresPost PO for exceptional behavior of charge()

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generate EnsuresPost PO for normal behavior of isValid()

generate EnsuresPost PO for exceptional behavior of charge()

generate PreservesOwnInv PO for charge()

expressing that charge() preserves all invariants (of its own class)

for loading more proof obligations: re-open **Proof Obligation Browser** under **Tools** menu (or **Ctrl-B**)

generate EnsuresPost PO for normal behavior of isValid()

generate EnsuresPost PO for exceptional behavior of charge()

generate **PreservesOwnInv** PO for charge()

expressing that charge() preserves all invariants (of its own class)

follow [KQ, 4.3.1+4.3.2]

in the following:

principles of translating JML to proof obligations in DL

- issues in translating arithmetic expressions
- translating this
- identifying the method's implementation
- ▶ translating boolean JML expressions to first-order logic formulas
- translating preconditions
- translating class invariants
- translating postconditions
- storing \old fields prior to method invocation
- storing actual parameters prior to method invocation
- expressing that 'exceptions are (not) thrown'
- putting everything together

WARNING:

following presentation is

- incomplete
- not fully precise
- simplifying
- omitting details/complications
- deviating from exact implementation in KeY

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enable you to read/understand proof obligations

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(notational remark: stick to ASCII syntax of KeY logic in this lecture)

Issues on Translating Arithmetic Expressions

often:

► KeY replaces arithmetic Java operators by generalized operators, generic towards various integer semantics (Java, Math). example: "+" becomes "javaAddInt"

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- KeY inserts casts like (jint), needed for type hierarchy among primitive types. example: "0" becomes "(jint)(0)"

(no need to memorize this)

Translating this

both

- explicit
- ► implicit

this reference translated to self

Translating this

```
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```

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- ▶ implicit

```
this reference translated to self
e.g., given class
public class MyClass {
    ...
    private int f;
    ...
```

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  implicit
this reference translated to self
e.g., given class
public class MyClass {
  . . .
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```

- ▶ f translated to self.f
- this.f translated to self.f

Identifying the Method's Implementation

JAVA's dynamic dispatch selects a method's implementation at runtime

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for a method call m(args), KeY models selection of implementation from package.Class by m(args)@package.Class

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Identifying the Method's Implementation

JAVA's dynamic dispatch selects a method's implementation at runtime

for a method call m(args), KeY models selection of implementation from package.Class by m(args)@package.Class

example:

Translating Boolean JML Expressions

first-order logic treated fundamentally different in JML and KeY logic

JML

- formulas no separate syntactic category
- instead:JAVA's boolean expressions extended with first-order concepts (i.p. quantifiers)

KeY logic

- ▶ formulas and expressions completely separate
- truth constants true, false are formulas, boolean constants TRUE, FALSE are expressions
- atomic formulas take expressions as arguments; e.g.:
 - x y < 5</p>
 - \triangleright b = TRUE

\mathcal{F} Translates boolean JML Expressions to Formulas

```
v/f/m() boolean variables/fields/pure methods b_0, b_1 boolean JML expressions e_0, e_1 JAVA expressions
```

 \mathcal{T} may add 'self.' or '@ClassName' (see pp. 16, 17) \mathcal{E} may add casts, transform operators (see p. 15)

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$\mathcal F$ Translates boolean JML Expressions to Formulas

```
\mathcal{F}((\mathbf{T} \mathbf{n}))
                                             = \forall T x;
                                                        !x = null \rightarrow \mathcal{F}(e_0)
\mathcal{F}((\text{exists T x; e_0}))
                                             = \exists T x;
                                                        !x = null & \mathcal{F}(e_0)
\mathcal{F}((\int \mathbf{forall} \ T \ x; \ e_0; \ e_1)) = \int \mathbf{forall} \ T \ x;
                                                            !x = null & \mathcal{F}(e_0)
                                                       \rightarrow \mathcal{F}(e_{-}1)
\mathcal{F}((\text{exists T x; e_0; e_1})) = \text{exists T x;}
                                                            !x = null
```

& $\mathcal{F}(e_{-}0)$ & $\mathcal{F}(e_{-}1)$

Translating Preconditions

```
if selected contract Contr has preconditions
@ requires b_1;
@ ...
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$$\mathcal{PRE}(Contr) = \\ \mathcal{F}(b_1) \& \dots \& \mathcal{F}(b_n)$$

Translating Class Invariants

```
the invariant
class C {
    ...
    //@ invariant inv_i;
    ...
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the invariant
class C {
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   . . .
is translated to
                             \mathcal{INV}(inv_i)
\forall C o: ((o.<created> = TRUE & !o = null) ->
                                                   \{self:=o\}\mathcal{F}(inv_i)
```

Translating Postconditions

```
if selected contract Contr has postconditions
@ ensures b_1;
@ ...
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special treatment of expressions in post-condition: see next slide

below, we assume the following assignable clause

@ assignable <assignable_fields>;

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translating expressions in postconditions (interesting cases only):

$$\mathcal{E}(\text{result}) = \text{result}$$
 $\mathcal{E}(\text{old}(e)) = \mathcal{E}_{old}(e)$

 \mathcal{E}_{old} defined like \mathcal{E} , with the exception of:

$$\mathcal{E}_{old}(e.f) = fAtPre(\mathcal{E}_{old}(e))$$

 $\mathcal{E}_{old}(f) = fAtPre(self)$

 $\text{for } \mathsf{f} \in \textit{<} assignable_fields \textit{>}$

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for $\mathbf{f} \in \langle assignable_fields \rangle$

'fAtPre' intuitively refers to field 'f' in the pre-state

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for $\mathbf{f} \in \langle assignable_fields \rangle$

'fAtPre' intuitively refers to field 'f' in the pre-state

But the logic does not know. Must be expressed in formula (next slide).

```
given an assignable field f of class C
class C {
    ...
    private T f;
    ...
}
translation of postcondition replaces f in \old(...) by fAtPre (p. 24)
left to do: store pre-state values of f in fAtPre
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$$\mathcal{STORE}(f)$$

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```

```
STORE(f)
=
\for C o; fAtPre(o) := o.f
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note: not a formula, but

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STORE(f)
=
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```

note: not a formula, but a quantified update (more proper explanation next lecture)

Storing Pre-State of All Assignable Fields

if selected contract Contr has assignable clause:

```
@ assignable f_1, ..., f_n;
```

then pre-state of all assignable fields can be stored by

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Storing Pre-State of All Assignable Fields

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how can you express in DL: method call m() will not throw an exception

how can you express in DL: method call m() will not throw an exception (if method body from class C in package p is executed)

```
how can you express in DL:
method call m() will not throw an exception
(if method body from class C in package p is executed)
\<{ exc = null;
    try {
      m()@p.C;
    } catch (Throwable e) {
      exc = e;
  } exc = null
```

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}\> exc = null
```

note difference:

- ► JAVA assignments
- ▶ equation, i.e., formula

how can you express in DL: method call m() will throw an exception

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method call m() will throw an exception
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\<{ exc = null;
    try {
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      exc = e;
  }\> !exc = null & <exc has right type>
```

PO for Normal Behavior Contract

PO for a normal behavior contract *Contr* for void method m(), with chosen assumed invariants inv_1, ..., inv_n ==>

```
\mathcal{INV}(inv_1)
   & . . .
   & \( \mathcal{INV}(inv_n) \)
   & PRE(Contr)
-> STORE(Contr)
      \<{ exc = null;
           try {
             m()@p.C;
           } catch (Throwable e) {
             exc = e;
        \rightarrow exc = null & POST(Contr)
```

PO for Normal Behavior Allowing Non-Termination

```
PO for a normal behavior contract Contr for method m().
where Contr has clause diverges true;
==>
      \mathcal{INV}(inv_1)
    & . . .
    & INV(inv_n)
    & PRE(Contr)
 -> STORE(Contr)
      \{ exc = null; \}
           try {
             m()@p.C;
           } catch (Throwable e) {
             exc = e;
        \ exc = null & POST(Contr)
```

PO for Normal Behavior of Non-Void Method

PO for a normal behavior contract *Contr* for non-void method m(), ==> $\mathcal{INV}(inv_1)$ & ... & $INV(inv_n)$ & PRE(Contr) -> STORE(Contr) try { result = m()@p.C; } catch (Throwable e) { exc = e; $\rightarrow \infty = \text{null & } POST(Contr)$

PO for Normal Behavior of Non-Void Method

PO for a normal behavior contract *Contr* for non-void method m(), ==> $\mathcal{INV}(inv_1)$ & ... & $INV(inv_n)$ & PRE(Contr) -> STORE(Contr) try { result = m()@p.C; } catch (Throwable e) { exc = e; $\rightarrow \$ exc = null & POST(Contr)

recall: POST(Contr) translates \result to result (p. 24)

PO for Preserving Invariants

```
assume method m() has contracts Contr_1, \ldots, Contr_i
PO stating that:
              Invariants inv_1, ..., inv_n are preserved
                  in all cases covered by a contracts.
==>
       \mathcal{INV}(inv_1) \& \dots \& \mathcal{INV}(inv_n)
    & ( \mathcal{PRE}(Contr_1) \mid \ldots \mid \mathcal{PRE}(Contr_1) )
 \rightarrow \[{ exc = null:
         try {
            m()@p.C;
         } catch (Throwable e) {
            exc = e;
```

Examples

don't fit on slide: execute quicktour with KeY instead

Literature for this Lecture

Essential

KeY Quicktour see course page, under 'Links, Papers, and Software'

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