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Parallel & Distributed Real-Time Systems

Lecture #8

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Multiprocessor scheduling

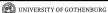
How are tasks assigned to processors?

Static assignment

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- The processor(s) used for executing a task are determined before system is put in mission ("off-line")
- Approaches: partitioned scheduling, guided search, non-guided search, ...
- Dynamic assignment
 - The processor(s) used for executing a task are determined during system operation "on-line"
 - Approach: global scheduling

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Multiprocessor scheduling

How are tasks allowed to migrate?

- Partitioned scheduling (no migration!)
 - Each instance of a task must execute on the same processor
 - Equivalent to multiple uniprocessor systems!
- Guided search & non-guided techniques
 - Depending on migration constraints, a task may or may not execute on more than one processor
- Global scheduling (full migration!)
 - A task is allowed to execute on an arbitrary processor (sometimes even after being preempted)

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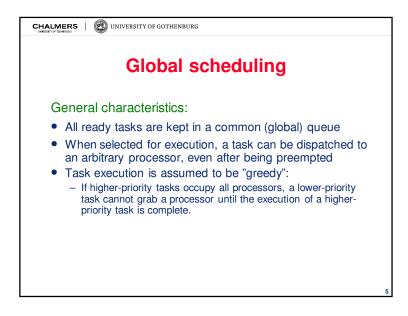
Multiprocessor scheduling

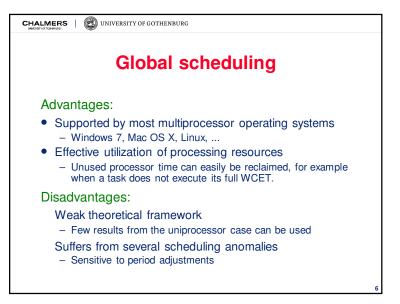
A fundamental limit: (Andersson, Baruah & Jonsson, 2001)

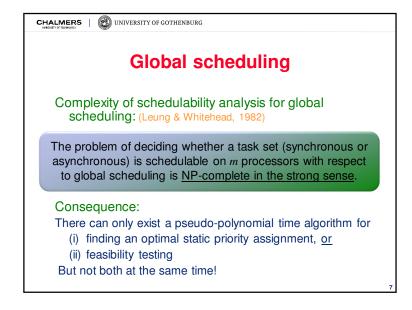
The utilization guarantee bound for multiprocessor scheduling (strictly partitioned or strictly global) using static task priorities cannot be higher than 50% of the processing capacity.

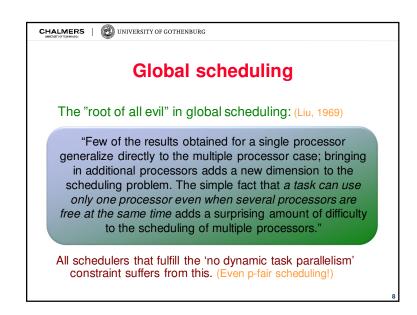
One (older) approach to circumvent this limit is to use p-fair (priorities + time quanta) scheduling and dynamic task priorities.

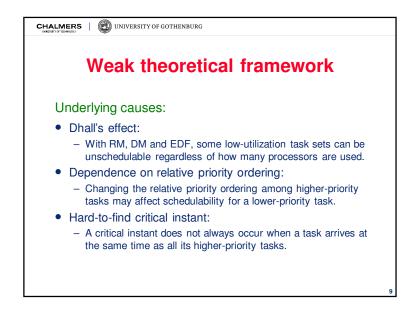
Another (newer) approach to circumvent this limit is to split a certain number of tasks into two or more parts, and then run each part on a separate processor. The remaining tasks use partitioned scheduling.

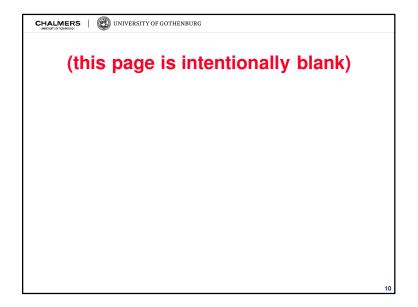


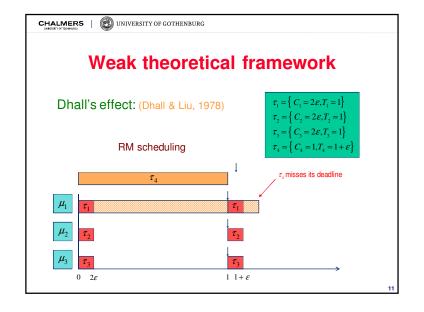


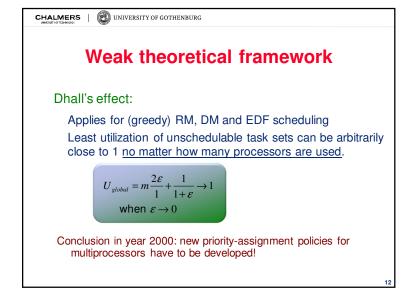


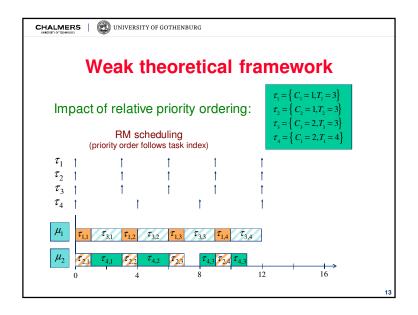


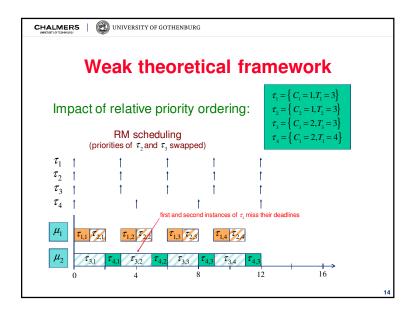


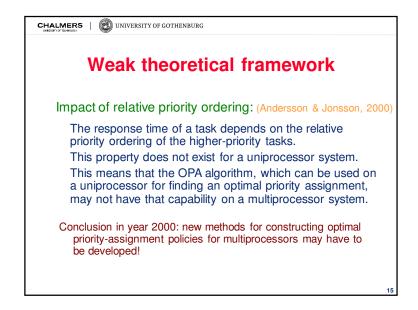


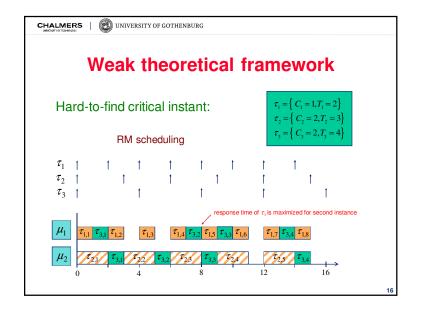


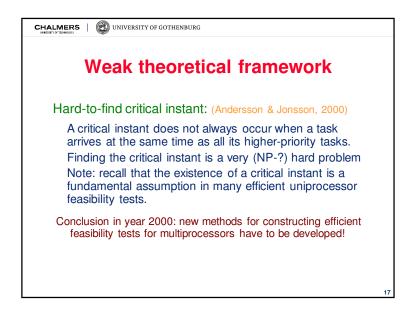


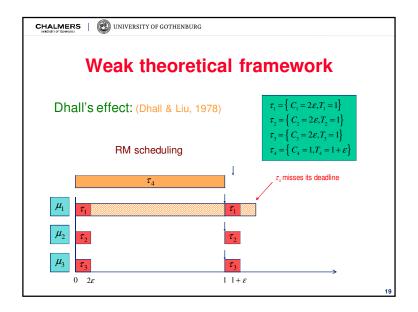


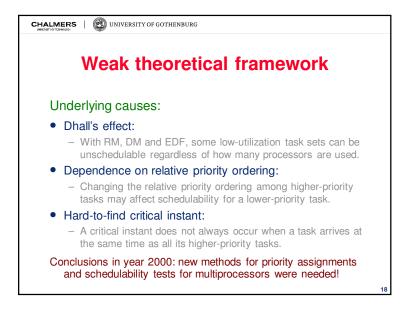


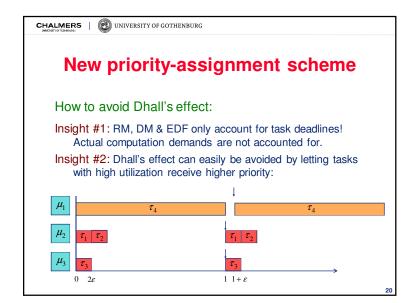












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New priority-assignment scheme

Scientific breakthrough: (Andersson, Baruah & Jonsson, 2001)

$RM-US\{m/(3m-2)\}$

 RM-US{m/(3m-2)} assigns (static) priorities to tasks according to the following rule:

If $U_i > m/(3m-2)$ then τ_i has the highest priority (ties broken arbitrarily)

If $U_i \le m/(3m-2)$ then τ_i has RM priority

Clearly, tasks with higher utilization, $U_i = C_i / T_i$, get higher priority.

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New feasibility test

Scientific breakthrough:

Guarantee bound analysis for RM-US{m/(3m-2)}:

 A <u>sufficient</u> condition for RM-US{m/(3m-2)} scheduling on m identical processors is

$$U = \sum_{i=1}^{n} \frac{C_i}{T_i} \le \frac{m^2}{3m-2}$$

Question: does RM-US{m/(3m-2)} avoid Dhall's effect?

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New feasibility test

Scientific breakthrough:

Guarantee bound analysis for RM-US{m/(3m-2)}:

 We observe that, regardless of the number of processors, the task set will always meet its deadlines as long as no more than one third of the processing capacity is used:

$$U_{RM-US\{m/(3m-2)\}} = \lim_{m \to \infty} \frac{m^2}{3m-2} = \frac{m}{3}$$

RM-US{m/(3m-2)} thus avoids Dhall's effect since we can always add more processors if deadlines were missed. Note that this remedy was not possible with "pure" RM.

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New feasibility test

Scientific breakthrough: (Andersson & Jonsson, 2000)

Response-time analysis for multiprocessors:

- Uses the same principle as the uniprocessor case, where the response time for a task τ_i consists of:
 - C_i The task's uninterrupted execution time (WCET)
 - I, Interference from higher-priority tasks

$$R_i = C_i + I_i$$

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New feasibility test

Scientific breakthrough:

Response-time analysis for multiprocessors:

• The worst-case interference term is

$$I_{i} = \frac{1}{m} \sum_{\forall j \in hp(i)} \left(\left\lceil \frac{R_{i}}{T_{j}} \right\rceil \cdot C_{j} + C_{j} \right)$$

where hp(i) is the set of tasks with higher priority than τ_i .

Note: The extra execution-time term introduced in this analysis is nowadays referred to as "carry-in" work.

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New feasibility test

Scientific breakthrough:

Response-time analysis for multiprocessors:

 As before, an iterative approach can be used for finding the worst-case response time:

$$R_i^{n+1} = C_i + \frac{1}{m} \sum_{\forall j \in hp(i)} \left(\left\lceil \frac{R_i^n}{T_j} \right\rceil \cdot C_j + C_j \right)$$

We now have a <u>sufficient</u> condition for static-priority scheduling on multiprocessors:

 $\forall i: R_i \leq D_i$

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New optimality procedure

Scientific breakthrough: (Davis & Burns, 2009)

Conditions for OPA compatibility:

Condition 1: The schedulability of a task τ may, according to test S, depend on any independent properties of tasks with priorities higher than τ , but not on any properties of those tasks that depend on their relative priority ordering.

Condition 2: The schedulability of a task τ may, according to test S, depend on any independent properties of tasks with priorities lower than τ , but not on any properties of those tasks that depend on their relative priority ordering.

Condition 3: When the priorities of any two tasks of adjacent priority are swapped, the task being assigned the higher priority cannot become unschedulable according to test S, if it was previously schedulable at the lower priority. CHALMERS | UNIVERSITY OF GOTHENBURG

New optimality procedure

Scientific breakthrough:

Conditions for OPA compatibility:

Task properties are referred to as <u>independent</u> if they have no dependency on the priority assigned to the task.

(e.g. WCET, period, deadline)

Task properties are referred to as <u>dependent</u> if they have a dependency on the priority assigned to the task.

(e.g. worst-case response time)

Feasibility tests which satisfy these conditions can be used together with the OPA algorithm to derive an optimal priority assignment on a multiprocessor system.

The multiprocessor response-time analysis shown earlier satisfies these conditions.

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