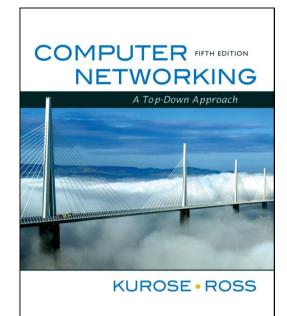
# Chapter 8 Network Security



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# Chapter 8: Network Security

### Chapter goals:

- understand principles of network security:
  - cryptography and its many uses beyond "confidentiality"
  - $\bigcirc$  authentication
  - o message integrity
- **security in practice:** 
  - o firewalls and intrusion detection systems
  - security in application, transport, network, link layers

# Chapter 8 roadmap

- 8.1 What is network security?
- 8.2 Principles of cryptography
- 8.3 Message integrity
- 8.4 Securing e-mail
- 8.5 Securing TCP connections: SSL
- 8.6 Network layer security: IPsec
- 8.7 Securing wireless LANs
- 8.8 Operational security: firewalls and IDS

# What is network security?

Confidentiality: only sender, intended receiver should "understand" message contents

• sender encrypts message

o receiver decrypts message

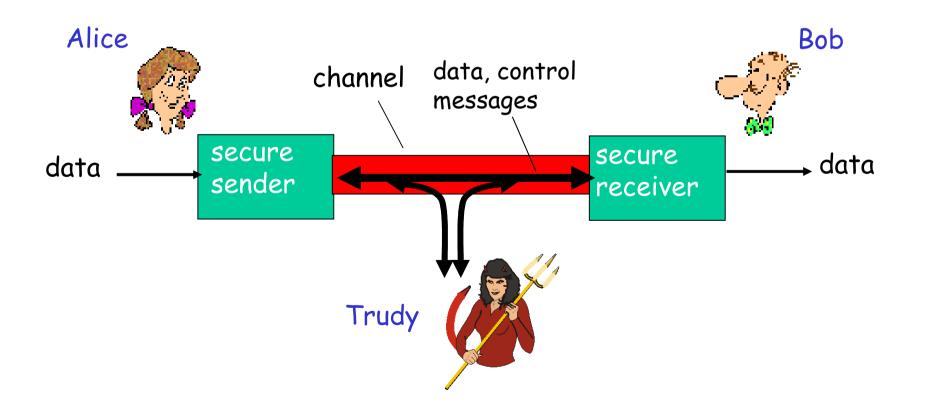
Authentication: sender, receiver want to confirm identity of each other

Message integrity: sender, receiver want to ensure message not altered (in transit, or afterwards) without detection

Access and availability: services must be accessible and available to users

### Friends and enemies: Alice, Bob, Trudy

- well-known in network security world
- Bob, Alice (lovers!) want to communicate "securely"
- Trudy (intruder) may intercept, delete, add messages



# Who might Bob, Alice be?

- ... well, real-life Bobs and Alices!
- Web browser/server for electronic transactions (e.g., on-line purchases)
- on-line banking client/server
- DNS servers
- routers exchanging routing table updates
- □ other examples?

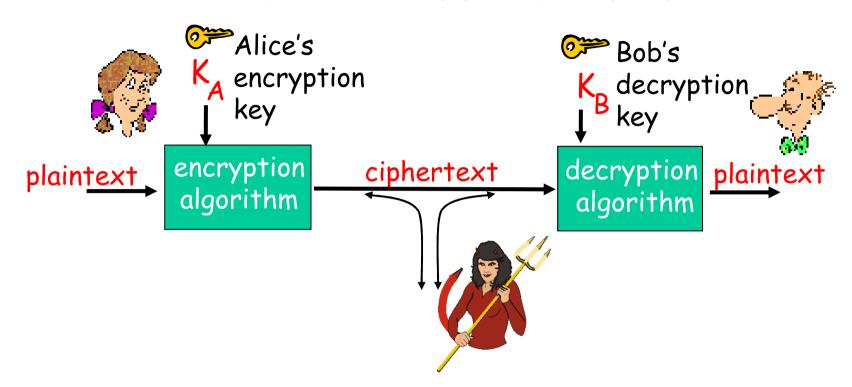
### There are bad guys (and girls) out there!

- Q: What can a "bad guy" do?
- A: A lot! See section 1.6
  - o eavesdrop: intercept messages
  - o actively *insert* messages into connection
  - *impersonation:* can fake (spoof) source address in packet (or any field in packet)
  - *hijacking:* "take over" ongoing connection by removing sender or receiver, inserting himself in place
  - *denial of service*: prevent service from being used by others (e.g., by overloading resources)

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### The language of cryptography



m plaintext message  $K_A(m)$  ciphertext, encrypted with key  $K_A$  $m = K_B(K_A(m))$ 

# Simple encryption scheme

substitution cipher: substituting one thing for another
 monoalphabetic cipher: substitute one letter for another

E.g.: Plaintext: bob. i love you. alice ciphertext: nkn. s gktc wky. mgsbc

<u>Key:</u> the mapping from the set of 26 letters to the set of 26 letters

# Polyalphabetic encryption

- □ n monoalphabetic cyphers, M<sub>1</sub>,M<sub>2</sub>,...,M<sub>n</sub>
- **Cycling pattern:** 
  - $\bigcirc$  e.g., n=4, M<sub>1</sub>, M<sub>3</sub>, M<sub>4</sub>, M<sub>3</sub>, M<sub>2</sub>; M<sub>1</sub>, M<sub>3</sub>, M<sub>4</sub>, M<sub>3</sub>, M<sub>2</sub>;
- For each new plaintext symbol, use subsequent monoalphabetic pattern in cyclic pattern

 $\bigcirc$  dog: d from  $M_1$ , o from  $M_3$ , g from  $M_4$ 

□ <u>Key:</u> the n ciphers and the cyclic pattern

# Breaking an encryption scheme

Cipher-text only attack: Trudy has ciphertext that she can analyze

**Two approaches:** 

- Search through all keys: must be able to differentiate resulting plaintext from gibberish
- Statistical analysis

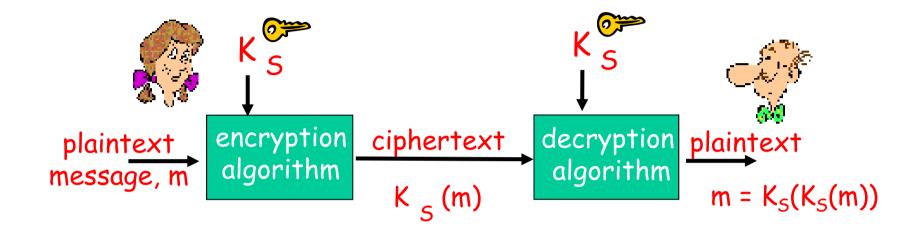
Known-plaintext attack: trudy has some plaintext corresponding to some ciphertext

- eg, in monoalphabetic cipher, trudy determines pairings for a,l,i,c,e,b,o,
- Chosen-plaintext attack: trudy can get the cyphertext for some chosen plaintext

# Types of Cryptography

Crypto often uses keys: • Algorithm is known to everyone • Only "keys" are secret Public key cryptography Involves the use of two keys Symmetric key cryptography • Involves the use one key Hash functions Involves the use of no keys • Nothing secret: How can this be useful?

## Symmetric key cryptography



symmetric key crypto: Bob and Alice share same (symmetric) key: K

- e.g., key is knowing substitution pattern in mono alphabetic substitution cipher
- Q: how do Bob and Alice agree on key value?

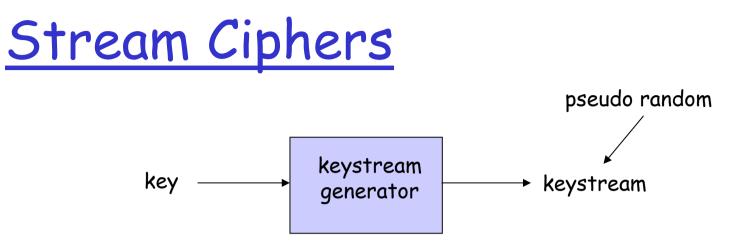
## Two types of symmetric ciphers

Stream ciphers

 encrypt one bit at time

 Block ciphers

 Break plaintext message in equal-size blocks
 Encrypt each block as a unit



Combine each bit of keystream with bit of plaintext to get bit of ciphertext

c(i) = ith bit of ciphertext

$$\Box$$
 c(i) = ks(i)  $\oplus$  m(i) ( $\oplus$  = exclusive or)

 $\Box$  m(i) = ks(i)  $\oplus$  c(i)

# RC4 Stream Cipher

RC4 is a popular stream cipher
 Extensively analyzed and considered good
 Key can be from 1 to 256 bytes
 Used in WEP for 802.11
 Can be used in SSL

## Public Key Cryptography

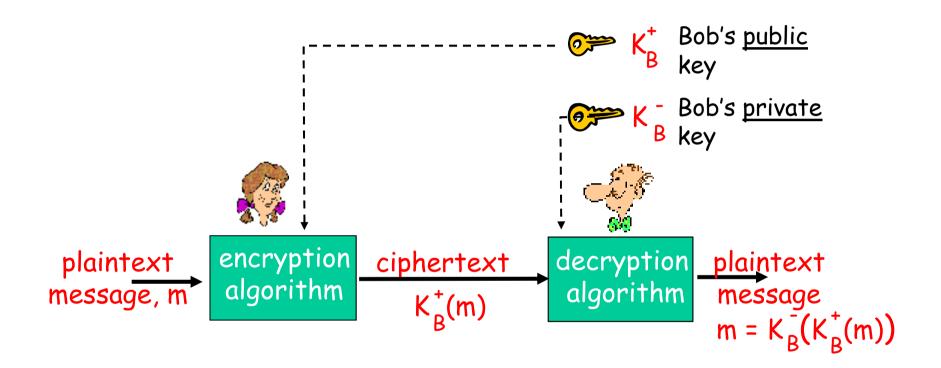
#### symmetric key crypto

- requires sender, receiver know shared secret key
- Q: how to agree on key in first place (particularly if never "met")?

#### *public* key cryptography

- radically different approach [Diffie-Hellman76, RSA78]
- sender, receiver do not share secret key
- public encryption key known to all
- private decryption key known only to receiver

## Public key cryptography



## Public key encryption algorithms

Requirements:

1 need 
$$K_B^+(\cdot)$$
 and  $K_B^-(\cdot)$  such that  
 $K_B^-(K_B^+(m)) = m$ 

RSA: Rivest, Shamir, Adelson algorithm

### Prerequisite: modular arithmetic

- $\Box$  x mod n = remainder of x when divide by n
- □ Facts:
  - $[(a \mod n) + (b \mod n)] \mod n = (a+b) \mod n$  $[(a \mod n) - (b \mod n)] \mod n = (a-b) \mod n$  $[(a \mod n) * (b \mod n)] \mod n = (a*b) \mod n$
- J Thus

 $(a \mod n)^d \mod n = a^d \mod n$ 

Example: x=14, n=10, d=2: (x mod n)<sup>d</sup> mod n = 4<sup>2</sup> mod 10 = 6 x<sup>d</sup> = 14<sup>2</sup> = 196 x<sup>d</sup> mod 10 = 6

# RSA: getting ready

- ☐ A message is a bit pattern.
- A bit pattern can be uniquely represented by an integer number.
- Thus encrypting a message is equivalent to encrypting a number.

<u>Example</u>

- m= 10010001. This message is uniquely represented by the decimal number 145.
- To encrypt m, we encrypt the corresponding number, which gives a new number (the cyphertext).

## <u>RSA: Creating public/private key</u> <u>pair</u>

- Choose two large prime numbers p, q. (e.g., 1024 bits each)
- 2. Compute n = pq, z = (p-1)(q-1)
- 3. Choose *e* (with *e<n*) that has no common factors with z. (*e*, *z* are "relatively prime").
- 4. Choose *d* such that *ed-1* is exactly divisible by *z*. (in other words: *ed* mod z = 1).

5. Public key is (n,e). Private key is (n,d).  $K_{B}^{+}$ 

# **RSA:** Encryption, decryption

- **O**. Given (n,e) and (n,d) as computed above
- 1. To encrypt message m (<n), compute  $c = m^{e} \mod n$
- 2. To decrypt received bit pattern, *c*, compute  $m = c^{d} \mod n$

RSA example:

Bob chooses *p=5, q=7*. Then *n=35, z=24*. *e=5* (so *e, z* relatively prime). *d=29* (so *ed-1* exactly divisible by z).

Encrypting 8-bit messages.

encrypt:  $\frac{bit pattern}{00001000} \frac{m}{12} \frac{m^{e}}{24832} \frac{c = m^{e} \mod n}{17}$  $\frac{c}{17} \frac{c}{481968572106750915091411825223071697} \frac{m = c^{d} \mod n}{12}$ 

# Why does RSA work?

- Must show that c<sup>d</sup> mod n = m where c = m<sup>e</sup> mod n
- □ Fact: for any x and y:  $x^{y} \mod n = x^{(y \mod z)} \mod n$ ○ where n= pq and z = (p-1)(q-1)
- 🗖 Thus,
  - $c^d \mod n = (m^e \mod n)^d \mod n$ 
    - = m<sup>ed</sup> mod n
    - = m<sup>(ed mod z)</sup> mod n
    - $= m^1 \mod n$
    - = m

### RSA: another important property

The following property will be *very* useful later:

$$K_{B}(K_{B}^{+}(m)) = m = K_{B}^{+}(K_{B}(m))$$

use public key first, followed by private key use private key first, followed by public key

Result is the same!

Why 
$$K_{B}(K_{B}^{+}(m)) = m = K_{B}^{+}(K_{B}(m))$$
 ?

Follows directly from modular arithmetic:

# Why is RSA Secure?

- Suppose you know Bob's public key (n,e). How hard is it to determine d?
- Essentially need to find factors of n without knowing the two factors p and q.
- □ Fact: factoring a big number is hard.

# Generating RSA keys

Have to find big primes p and q

Approach: make good guess then apply testing rules (see Kaufman)



Exponentiation is computationally intensive
 DES is at least 100 times faster than RSA
 <u>Session key, K<sub>S</sub></u>

- Bob and Alice use RSA to exchange a symmetric key K<sub>S</sub>
- Once both have K<sub>S</sub>, they use symmetric key cryptography

# Chapter 8 roadmap

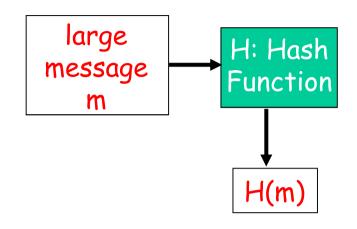
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# <u>Message Integrity</u>

Allows communicating parties to verify that received messages are authentic.
 Content of message has not been altered
 Source of message is who/what you think it is
 Message has not been replayed
 Sequence of messages is maintained
 Let's first talk about message digests

### <u>Message Digests</u>

- Function H() that takes as input an arbitrary length message and outputs a fixed-length string: "message signature"
- Note that H() is a manyto-1 function
- H() is often called a "hash function"



- Desirable properties:
  - Easy to calculate
  - Irreversibility: Can't determine m from H(m)
  - Collision resistance: Computationally difficult to produce m and m' such that H(m) = H(m')
  - Seemingly random output

### Internet checksum: poor message digest

Internet checksum has some properties of hash function:

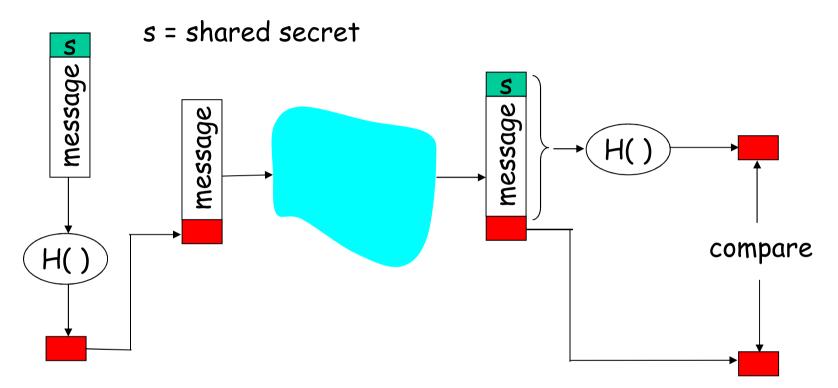
- ➡ produces fixed length digest (16-bit sum) of input
- ➡ is many-to-one
- But given message with given hash value, it is easy to find another message with same hash value.
- **D** Example: Simplified checksum: add 4-byte chunks at a time:

| <u>message</u> | <u>ASCII format</u>                      | message | <u>ASCII format</u> |
|----------------|--|---------|---------------------|
| I O U 1        | 49 4F 55 31                              | IOU1    | 49 4F 55 31         |
| 00.9           | 30 30 2E 39                              | 00.9    | 30 30 2E 39         |
| 9 B O B        | 39 42 D2 42                              | 9 B O B | 39 42 D2 42         |
|                | B2 C1 D2 AC different r<br>but identical |         | B2 C1 D2 AC         |
|                | 34                                       |         |                     |

## Hash Function Algorithms

- MD5 hash function widely used (RFC 1321)
   computes 128-bit message digest in 4-step process.
- □ SHA-1 is also used.
  - O US standard [NIST, FIPS PUB 180-1]
  - O 160-bit message digest

## Message Authentication Code (MAC)



- Authenticates sender
- Verifies message integrity
- No encryption !
- Also called "keyed hash"
- □ Notation:  $MD_m = H(s||m)$ ; send  $m||MD_m|$

# HMAC

- Popular MAC standard
- Addresses some subtle security flaws
- 1. Concatenates secret to front of message.
- 2. Hashes concatenated message
- 3. Concatenates the secret to front of digest
- 4. Hashes the combination again.

# Example: OSPF

- Recall that OSPF is an intra-AS routing protocol
- Each router creates map of entire AS (or area) and runs shortest path algorithm over map.
- Router receives linkstate advertisements (LSAs) from all other routers in AS.

#### Attacks:

- Message insertion
- Message deletion
- Message modification
- How do we know if an OSPF message is authentic?

# **OSPF** Authentication

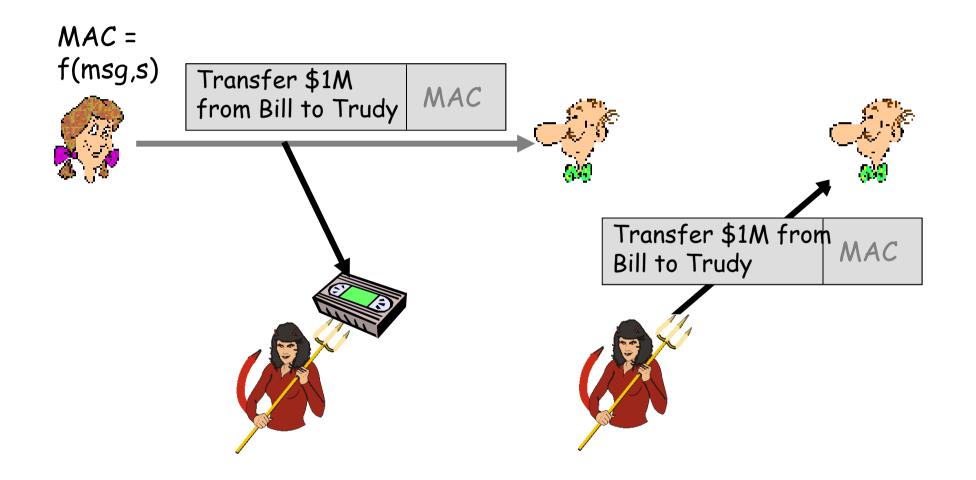
- Within an Autonomous System, routers send OSPF messages to each other.
- OSPF provides authentication choices
  - No authentication
  - Shared password: inserted in clear in 64bit authentication field in OSPF packet
  - Cryptographic hash

- Cryptographic hash with MD5
  - 64-bit authentication field includes 32-bit sequence number
  - MD5 is run over a concatenation of the OSPF packet and shared secret key
  - MD5 hash then appended to OSPF packet; encapsulated in IP datagram

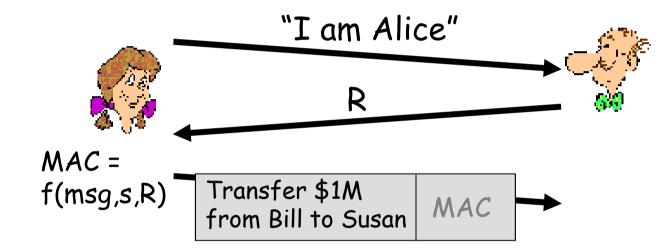
# End-point authentication

- Want to be sure of the originator of the message end-point authentication.
- Assuming Alice and Bob have a shared secret, will MAC provide end-point authentication.
  - We do know that Alice created the message.
  - But did she send it?

# Playback attack



# <u>Defending against playback</u> <u>attack: nonce</u>



## Digital Signatures

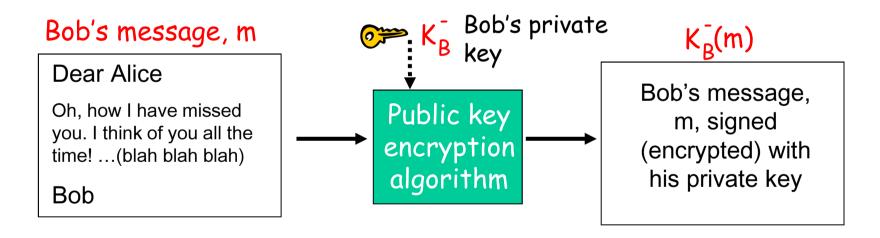
Cryptographic technique analogous to handwritten signatures.

- sender (Bob) digitally signs document, establishing he is document owner/creator.
- Goal is similar to that of a MAC, except now use public-key cryptography
- verifiable, nonforgeable: recipient (Alice) can prove to someone that Bob, and no one else (including Alice), must have signed document

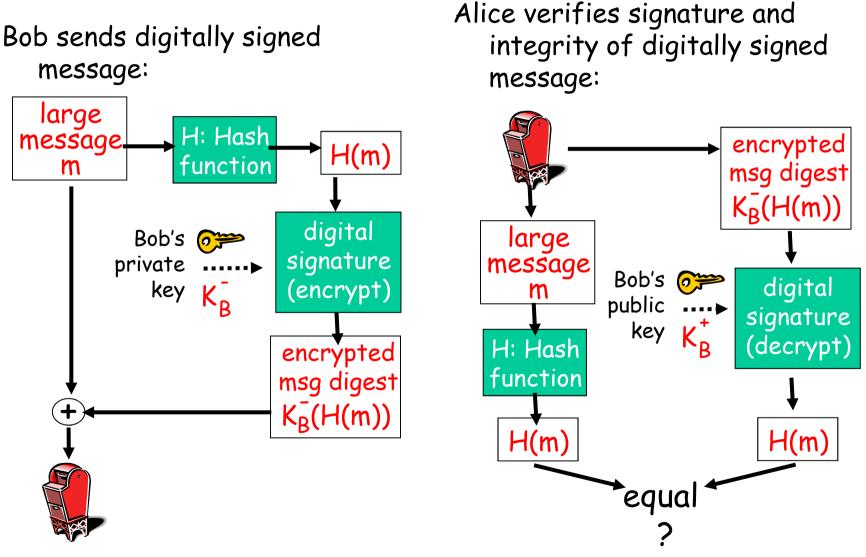
## Digital Signatures

#### Simple digital signature for message m:

Bob signs m by encrypting with his private key K<sub>B</sub>, creating "signed" message, K<sub>B</sub>(m)



#### <u>Digital signature = signed message digest</u>



# Digital Signatures (more)

- □ Suppose Alice receives msg m, digital signature  $K_B(m)$
- □ Alice verifies m signed by Bob by applying Bob's public key  $K_B^+$  to  $K_B^-$ (m) then checks  $K_B^+$ ( $K_B^-$ (m)) = m.
- If K<sup>+</sup><sub>B</sub>(K<sup>-</sup><sub>B</sub>(m)) = m, whoever signed m must have used Bob's private key.
  - Alice thus verifies that:
    - ➡ Bob signed m.
    - ➤ No one else signed m.
    - ➡ Bob signed m and not m'.
  - Non-repudiation (oavvislighet):
    - ✓ Alice can take m, and signature  $K_B(m)$  to court and prove that Bob signed m.

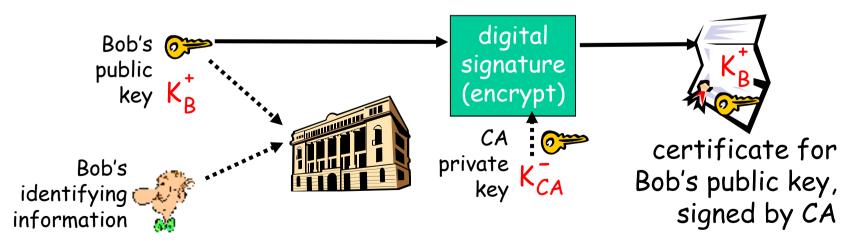
# Public-key certification

Motivation: Trudy plays pizza prank on Bob

- Trudy creates e-mail order:
   Dear Pizza Store, Please deliver to me four
  - pepperoni pizzas. Thank you, Bob
- Trudy signs order with her private key
- O Trudy sends order to Pizza Store
- Trudy sends to Pizza Store her public key, but says it's Bob's public key.
- Pizza Store verifies signature; then delivers four pizzas to Bob.
- Bob doesn't even like Pepperoni

## **Certification Authorities**

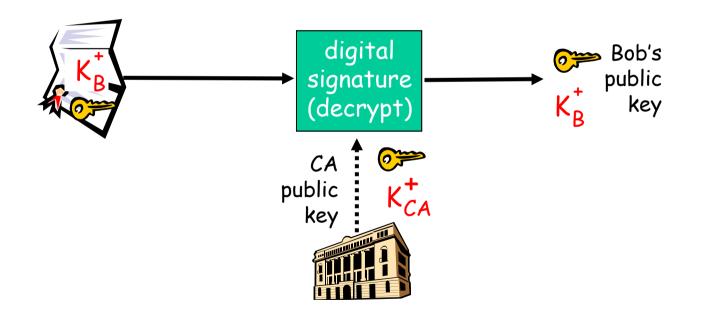
- Certification authority (CA): binds public key to particular entity, E.
- E (person, router) registers its public key with CA.
  - E provides "proof of identity" to CA.
  - CA creates certificate binding E to its public key.
  - certificate containing E's public key digitally signed by CA
    - CA says "this is E's public key"



## **Certification Authorities**

When Alice wants Bob's public key:

 gets Bob's certificate (Bob or elsewhere).
 apply CA's public key to Bob's certificate, get Bob's public key



# Certificates: summary

Primary standard X.509 (RFC 2459)

Certificate contains:

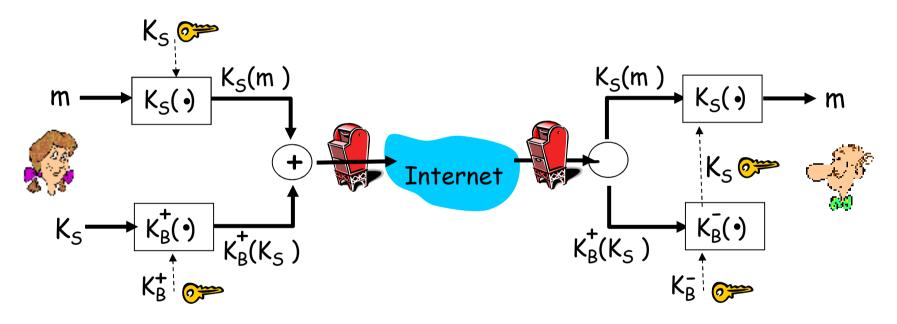
- Issuer name
- Entity name, address, domain name, etc.
- Entity's public key
- Digital signature (signed with issuer's private key)
- Public-Key Infrastructure (PKI)
  - Certificates and certification authorities
  - Often considered "heavy"

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#### Secure e-mail

□ Alice wants to send confidential e-mail, m, to Bob.

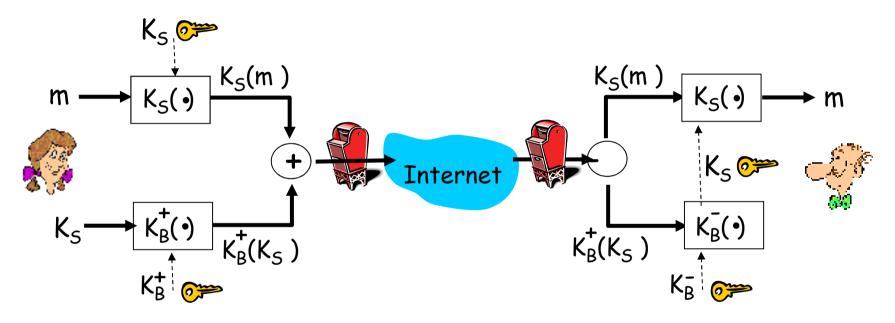


#### Alice:

- $\Box$  generates random *symmetric* private key, K<sub>S</sub>.
- $\Box$  encrypts message with  $K_S$  (for efficiency)
- $\Box$  also encrypts  $K_S$  with Bob's public key.
- □ sends both  $K_S(m)$  and  $K_B(K_S)$  to Bob.

#### Secure e-mail

□ Alice wants to send confidential e-mail, m, to Bob.

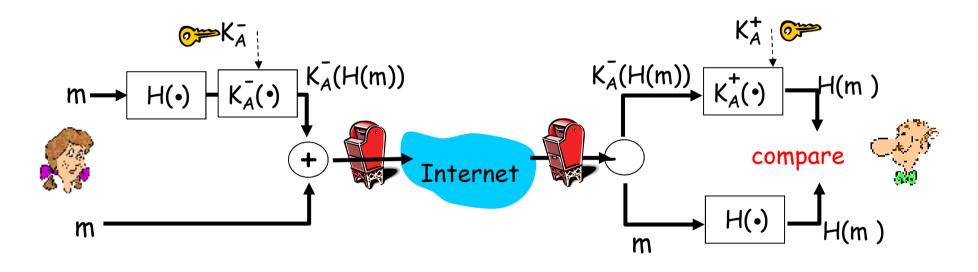


#### Bob:

- $\Box$  uses his private key to decrypt and recover  $K_s$
- $\Box$  uses  $K_S$  to decrypt  $K_S(m)$  to recover m

Secure e-mail (continued)

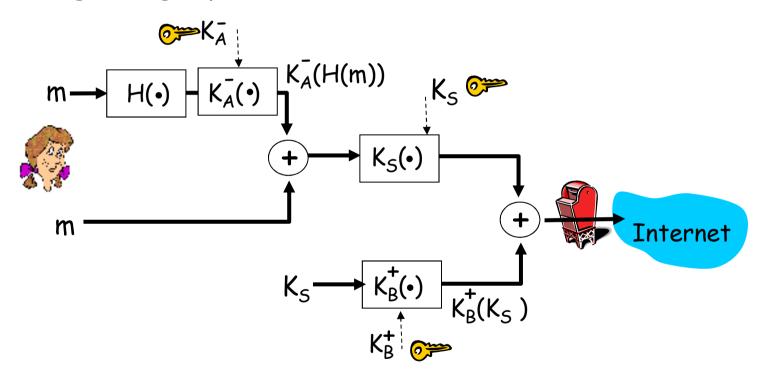
• Alice wants to provide sender authentication message integrity.



- Alice digitally signs message.
- sends both message (in the clear) and digital signature.

### Secure e-mail (continued)

• Alice wants to provide secrecy, sender authentication, message integrity.



Alice uses three keys: her private key, Bob's public key, newly created symmetric key

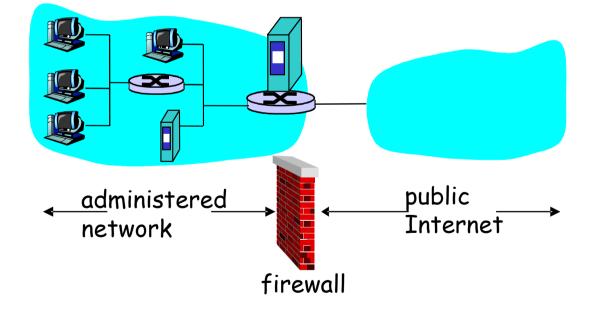
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## Firewalls

#### - firewall

isolates organization's internal net from larger Internet, allowing some packets to pass, blocking others.



## Firewalls: Why

prevent denial of service attacks:

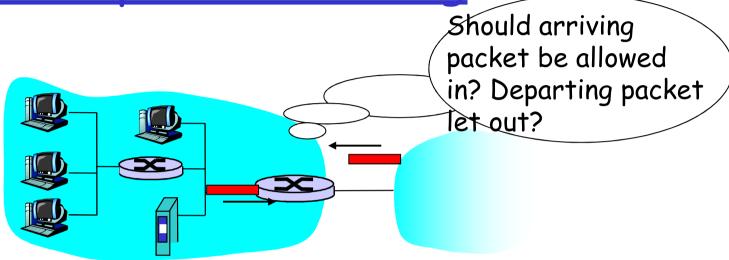
 SYN flooding: attacker establishes many bogus TCP connections, no resources left for "real" connections
 prevent illegal modification/access of internal data.

 e.g., attacker replaces CIA's homepage with something else allow only authorized access to inside network (set of authenticated users/hosts)

three types of firewalls:

- stateless packet filters
- stateful packet filters
- application gateways

## Stateless packet filtering



- internal network connected to Internet via router firewall
- router filters packet-by-packet, decision to forward/drop packet based on:
  - source IP address, destination IP address
  - TCP/UDP source and destination port numbers
  - ICMP message type
  - TCP SYN and ACK bits

#### <u>Stateless packet filtering: example</u>

- example 1: block incoming and outgoing datagrams with IP protocol field = 17 and with either source or dest port = 23.
  - all incoming, outgoing UDP flows and telnet connections are blocked.
- example 2: Block inbound TCP segments with ACK=0.
  - prevents external clients from making TCP connections with internal clients, but allows internal clients to connect to outside.

#### Stateless packet filtering: more examples

| Policy  | <u>Firewall Setting</u>   |
|---|---|
| No outside Web access.  | Drop all outgoing packets to any IP<br>address, port 80                           |
| No incoming TCP connections,<br>except those for institution's<br>public Web server only. | Drop all incoming TCP SYN packets to<br>any IP except 130.207.244.203, port<br>80 |
| Prevent Web-radios from eating<br>up the available bandwidth.                             | Drop all incoming UDP packets - except<br>DNS and router broadcasts.              |
| Prevent your network from being used for a smurf DoS attack.                              | Drop all ICMP packets going to a<br>"broadcast" address (eg<br>130.207.255.255).  |
| Prevent your network from being tracerouted   | Drop all outgoing ICMP TTL expired traffic  |

# Access Control Lists

ACL: table of rules, applied top to bottom to incoming packets: (action, condition) pairs

| action | source<br>address       | dest<br>address         | protocol | source<br>port   | dest<br>port     | flag<br>bit |
|--------|-------------------------|-------------------------|----------|------------------|------------------|-------------|
| allow  | 222.22/16               | outside of<br>222.22/16 | ТСР      | <b>&gt;</b> 1023 | 80               | any         |
| allow  | outside of<br>222.22/16 | 222.22/16               | ТСР      | 80 > 1023        |                  | ACK         |
| allow  | 222.22/16               | outside of<br>222.22/16 | UDP      | <b>&gt;</b> 1023 | 53               |             |
| allow  | outside of<br>222.22/16 | 222.22/16               | UDP      | 53               | <b>&gt;</b> 1023 |             |
| deny   | all                     | all                     | all      | all              | all              | all         |

# Stateful packet filtering

- □ stateless packet filter: heavy handed tool
  - admits packets that "make no sense," e.g., dest port = 80, ACK bit set, even though no TCP connection established:

| action | source<br>address       | dest<br>address | protocol | source dest<br>port port |                  | flag<br>bit |
|--------|-------------------------|-----------------|----------|--------------------------|------------------|-------------|
| allow  | outside of<br>222.22/16 | 222.22/16       | ТСР      | 80                       | <b>&gt;</b> 1023 | ACK         |

- stateful packet filter: track status of every TCP connection
  - track connection setup (SYN), teardown (FIN): can determine whether incoming, outgoing packets "makes sense"
  - timeout inactive connections at firewall: no longer admit packets

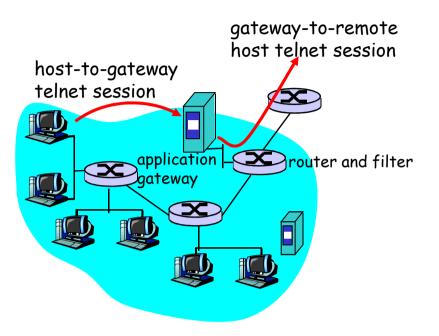
# Stateful packet filtering

 ACL augmented to indicate need to check connection state table before admitting packet

| action | source<br>address       | dest<br>address         | proto | source<br>port   | dest<br>port     | flag<br>bit | check<br>conxion |
|--------|-------------------------|-------------------------|-------|------------------|------------------|-------------|------------------|
| allow  | 222.22/16               | outside of<br>222.22/16 | ТСР   | <b>&gt;</b> 1023 | 80               | any         |                  |
| allow  | outside of<br>222.22/16 | 222.22/16               | ТСР   | 80               | <b>&gt;</b> 1023 | ACK         | ×                |
| allow  | 222.22/16               | outside of<br>222.22/16 | UDP   | > 1023           | 53               |             |                  |
| allow  | outside of<br>222.22/16 | 222.22/16               | UDP   | 53               | <b>&gt;</b> 1023 |             | ×                |
| deny   | all                     | all                     | all   | all              | all              | all         |                  |

#### Application gateways

- filters packets on application data as well as on IP/TCP/UDP fields.
- example: allow select internal users to telnet outside.



- 1. require all telnet users to telnet through gateway.
- 2. for authorized users, gateway sets up telnet connection to dest host. Gateway relays data between 2 connections
- 3. router filter blocks all telnet connections not originating from gateway.

#### Limitations of firewalls and gateways

- IP spoofing: router can't know if data "really" comes from claimed source
- if multiple app's. need special treatment, each has own app. gateway.
- client software must know how to contact gateway.
  - e.g., must set IP address of proxy in Web browser

- filters often use all or nothing policy for UDP.
- tradeoff: degree of communication with outside world, level of security
- many highly protected sites still suffer from attacks.

# Intrusion detection systems

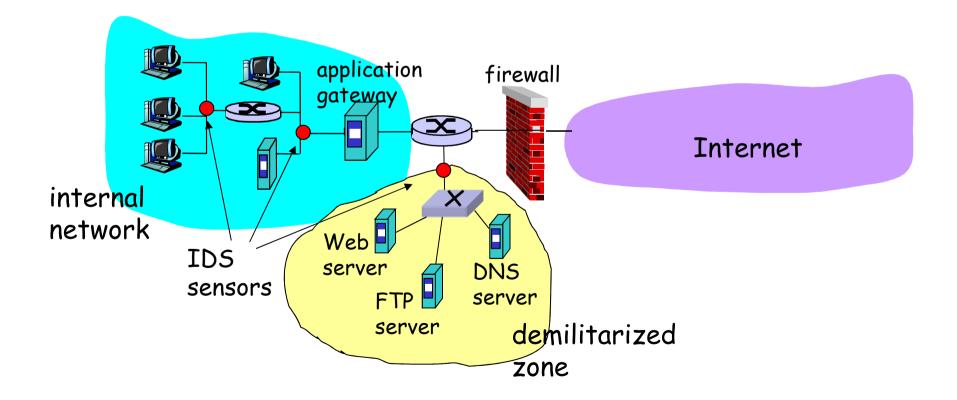
packet filtering:

o operates on TCP/IP headers only

- $\odot$  no correlation check among sessions
- **IDS:** *intrusion detection system* 
  - *deep packet inspection:* look at packet contents (e.g., check character strings in packet against database of known virus, attack strings)
  - o examine correlation among multiple packets
    - port scanning
    - network mapping
    - DoS attack

# Intrusion detection systems

multiple IDSs: different types of checking at different locations



# Network Security (summary)

Basic techniques.....

- o cryptography (symmetric and public)
- o message integrity
- o end-point authentication
- .... used in many different security scenarios
  - o secure email
  - o secure transport (SSL)
  - $\circ$  IP sec
  - 0 802.11

Operational Security: firewalls and IDS

8: Network Security

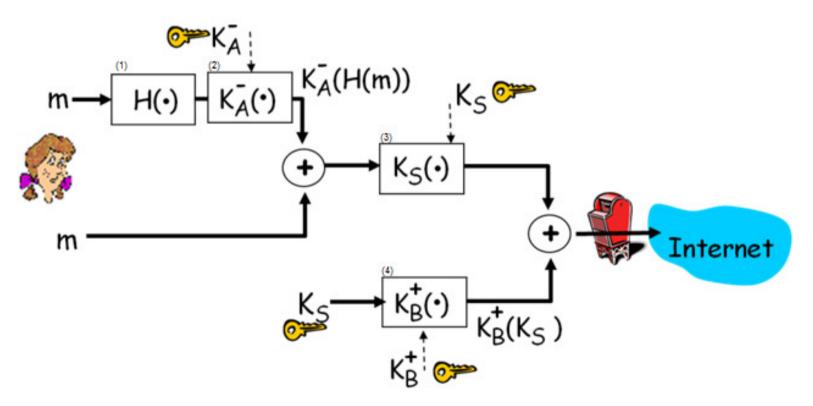
- In RSA, we create the public key (n,e) and the private key is (n,d) by:
- $\Box$  Choosing two large prime numbers p and q.
- **Computing** n = pq and z = (p-1)(q-1)
- Choosing a number e (with e<n) that has no common factors with z.</p>
- Choosing d such that ed-1 is exactly divisible by z.

- We encrypt message m by K+(m) = m<sup>e</sup> mod n and decrypt cipher text c by K<sup>-</sup> (c) = c<sup>d</sup> mod n, where x mod n is the remainder of x when divided by n.
- Useful facts:
  - [(a mod n) + (b mod n)] mod n = (a+b) mod n
     [(a mod n) (b mod n)] mod n = (a-b) mod n
     [(a mod n) \* (b mod n)] mod n = (a\*b) mod n
     (a mod n)<sup>d</sup> mod n = a<sup>d</sup> mod n
     Eon any x and x; x mod n = x(x mod z) mod n
  - For any x and y:  $x^{y} \mod n = x^{(y \mod z)} \mod n$ , where n = pq and z = (p-1)(q-1)

Please prove that:
K<sup>-</sup>(K<sup>+</sup>(m)) = m.
K<sup>+</sup>(K<sup>-</sup>(m)) = m.
Please explain that:
Why RSA is good for encryption?
Why RSA is good for authentication?



Please take a look at the figure in which Alice is preparing a message to Bob



- For each rectangle from top left to bottom right, please explain the steps that Alice takes.
- Please draw the Bob's process when processing Alice's message.
- Please explain the steps that Bob must take when processing Alice's message (for each rectangle from top left to bottom right).