

Compiling functional languages

<http://www.cse.chalmers.se/edu/year/2011/course/CompFun/>

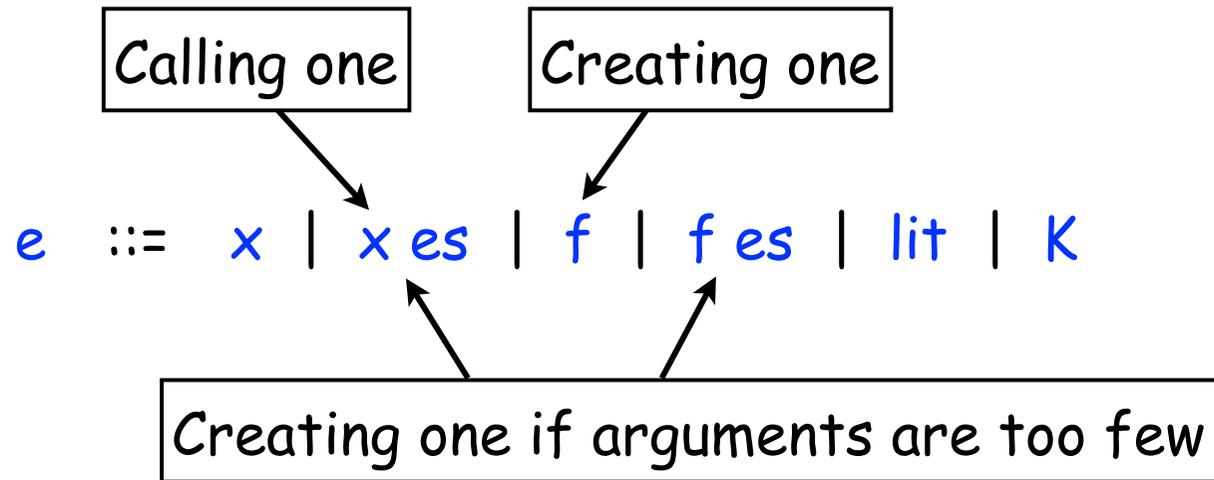
Lecture 3

Memory management

Johan Nordlander

Anonymous functions revisited

- Our latest expression grammar:



- Must be supported - not a functional language otherwise!
- Requires the concept of closures!

Closures

- The generic representation of functions: a function pointer with a list of free variables
- The limits of lambda-lifting:

$g = \lambda a \rightarrow \text{let } f = \lambda b \rightarrow a + b$
 $\quad \quad \quad \text{in } h \text{ } \underline{f}$
 $h = \lambda x \rightarrow x \ 7$

\Rightarrow

$f = \lambda a \ b \rightarrow a + b$
 $g = \lambda a \rightarrow h \ (\underline{f \ a})$
 $h = \lambda x \rightarrow x \ 7$

Too few arguments regardless!

- Closures can represent partial applications, even in the presence of free variables
- Nevertheless, lambda-lifting before closure-conversion simplifies the presentation somewhat

Closure-conversion

- Assume a lambda-lifted $f = \lambda x_1 \dots x_n \rightarrow e$

$\text{closureConvert } f = \text{CL } f_0 \ n$

$\text{closureConvert } (f \ e_1 \dots e_m) =$

$| \ m < n \quad = \ \text{CL } f_m \ (n-m) \ e_1 \dots e_m$

...

where f_m is a new top-level function

$f_m = \lambda x_{\text{this}} \ x_{m+1} \dots x_n \rightarrow \text{case } x_{\text{this}} \ \text{of}$

$\text{CL } _ _ \ y_1 \dots y_m \rightarrow f \ y_1 \dots y_m \ x_{m+1} \dots x_n$

$\text{closureConvert } (x \ e_1 \dots e_m) = \text{case } x \ \text{of } \text{CL } f_{\text{unknown}} \ n$
 $| \ m == n \rightarrow f_{\text{unknown}} \ x \ e_1 \dots e_m$

...

Closure-conversion

- Example before and after lambda-lifting:

$g = \lambda a \rightarrow \text{let } f = \lambda b \rightarrow a + b$
 $\text{in } f \ g$
 $h = \lambda x \rightarrow x \ 7$

⇒

$f = \lambda a \ b \rightarrow a + b$
 $g = \lambda a \rightarrow h \ (f \ a)$
 $h = \lambda x \rightarrow x \ 7$

- And after closure-conversion:

$f = \lambda a \ b \rightarrow a + b$
 $g = \lambda a \rightarrow \text{CL } f_1 \ 1 \ a$
 $h = \lambda x \rightarrow \text{case } x \ \text{of } \text{CL } f_{\text{unknown}} \ 1 \rightarrow f_{\text{unknown}} \ x \ 7$

$f_1 = \lambda x_{\text{this}} \ x_2 \rightarrow \text{case } x_{\text{this}} \ \text{of } \text{CL } _ _ \ y_1 \rightarrow f \ y_1 \ x_2$

- But we're still ignoring arity mismatches...

Checking arities

(eval/apply)

- Assuming $f = \lambda x_1 \dots x_n \rightarrow e$

$\text{closureConvert } f = \text{CL } f_0 \ n$

$\text{closureConvert } (f \ e_1 \dots \ e_m) =$

| $m == n$ = $f \ e_1 \dots \ e_m$

| $m < n$ = $\text{CL } f_m \ (n-m) \ e_1 \dots \ e_m$

| $m > n$ = $\text{apply}_{m-n} (f \ e_1 \dots \ e_n) \ e_{n+1} \dots \ e_m$

where each apply_k is a run-time system function TBD

- Note: checks are done at compile-time

Checking arities

(eval/apply)

- The full dynamic case (checks at run-time!):

$\text{closureConvert } (x \ e_1 \ \dots \ e_m) \quad = \quad \text{apply}_m \ x \ e_1 \ \dots \ e_m$

$\text{apply}_m = \lambda x_{\text{this}} \ x_1 \ \dots \ x_m \rightarrow \text{case } x_{\text{this}} \text{ of CL } f_{\text{unknown}} \ n$
| $m == n \rightarrow f_{\text{unknown}} \ x_{\text{this}} \ x_1 \ \dots \ x_m$
| $m < n \rightarrow \text{CL } \text{pap}_{n-m,m} \ (n-m) \ x_{\text{this}} \ x_1 \ \dots \ x_m$
| $m > n \rightarrow \text{apply}_{m-n} \ (f_{\text{unknown}} \ x_{\text{this}} \ x_1 \ \dots \ x_n) \ x_{n+1} \ \dots \ x_m$

$\text{pap}_{k,m} = \lambda x_{\text{this}} \ x_1 \ \dots \ x_k \rightarrow \text{case } x_{\text{this}} \text{ of CL } _ _ \ y_{\text{that}} \ y_1 \ \dots \ y_m \rightarrow$
 $\text{apply}_{m+k} \ y_{\text{that}} \ y_1 \ \dots \ y_m \ x_1 \ \dots \ x_k$

Recall: data layout

```
typedef int *Ptr;
```

Basic assumptions:

```
(Ptr)(int)x = x
```

```
(int)(Ptr)y = y
```

Construction:

```
x = Ki e1 ... en
```

```
Ptr x = malloc((n+1)*sizeof(int));
```

```
x[0] = i;
```

```
x[1] = (int)e1; ...; x[n] = (int)en;
```

Deconstruction:

```
case x of
```

```
....
```

```
Ki x1 ... xn -> bodyi
```

```
switch (x[0]) {
```

```
...
```

```
case i: { Ptr x1 = (Ptr)x[1]; ...
```

```
Ptr xn = (Ptr)x[n];
```

```
bodyi }
```

Nullary constructors

Could just use the generic form:

$x = K_i$

case x **of**

...

$K_i \rightarrow$ body

Ptr $x = \text{malloc}(\text{sizeof}(\text{int}));$

$x[0] = i;$

switch ($x[0]$) {

...

case i : { body }

For better memory efficiency, encode as small pointer:

K_i

case x **of**

$K_i \rightarrow$ body _{i}

...

$K_j \ x_1 \dots x_n \rightarrow$ body _{j}

(Ptr) i

switch ((int) x) {

case i : { body _{i} }

...

default: **switch** ($x[0]$) {

case j : { Ptr $x_1 = (\text{Ptr})x[1]; \dots$

Ptr $x_n = (\text{Ptr})x[n];$

body _{j} }

Single constructors

Could just use the generic form:

$x = K_0 e_1 \dots e_n$

case x of

$K_0 x_1 \dots x_n \rightarrow \text{body}_i$

```
Ptr x = malloc((n+1)*sizeof(int));
```

```
x[0] = 0;
```

```
x[1] = (int)e1; ... x->arg[n] = (int)en;
```

```
switch (x[0]) {
```

```
  case 0: { Ptr x1 = (Ptr)x[1]; ...
```

```
           Ptr xn = (Ptr)x[n];
```

```
           body0 }
```

For better efficiency, encode without a tag:

$x = K_0 e_1 \dots e_n$

case x of

$K_0 x_1 \dots x_n \rightarrow \text{body}_0$

```
Ptr x = malloc(n*sizeof(int));
```

```
x[0] = (int)e1; ...
```

```
x[n-1] = (int)en;
```

```
Ptr x1 = (Ptr)x[0]; ...
```

```
Ptr xn = (Ptr)x[n-1];
```

```
body0
```

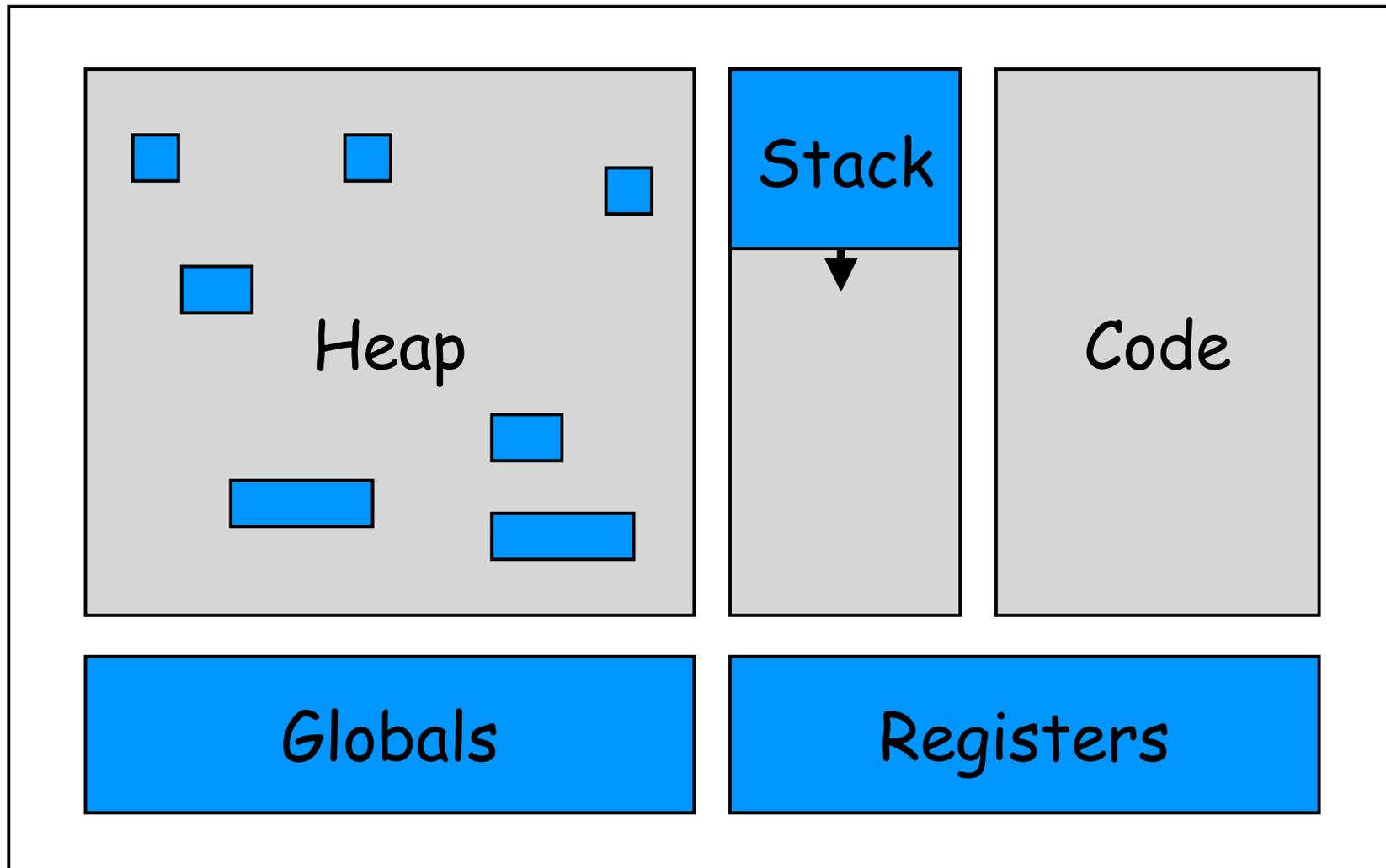

malloc

- Used as a generic name for heap allocation in C
 - no particular implementation implied
- Our demands:
 - Allocations are frequent, need to be fast
 - Active deallocations do not fit our model of execution (where would one put them?), automatic garbage collection is needed
 - Block sizes vary, compaction might be needed

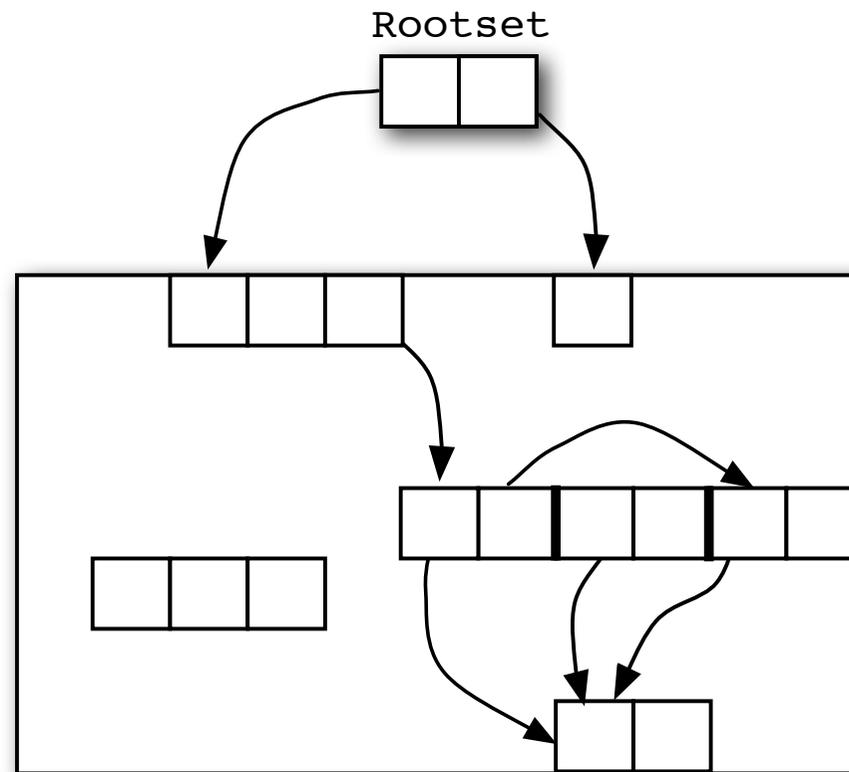
Garbage collection

- At any particular time during code execution:
 - Garbage: allocated heap blocks that are no longer live
 - Live memory: heap blocks that will be used by some subsequent machine instruction
 - Decidable approximation: blocks that are reachable from the current machine state
 - Machine state: globals, registers & stack

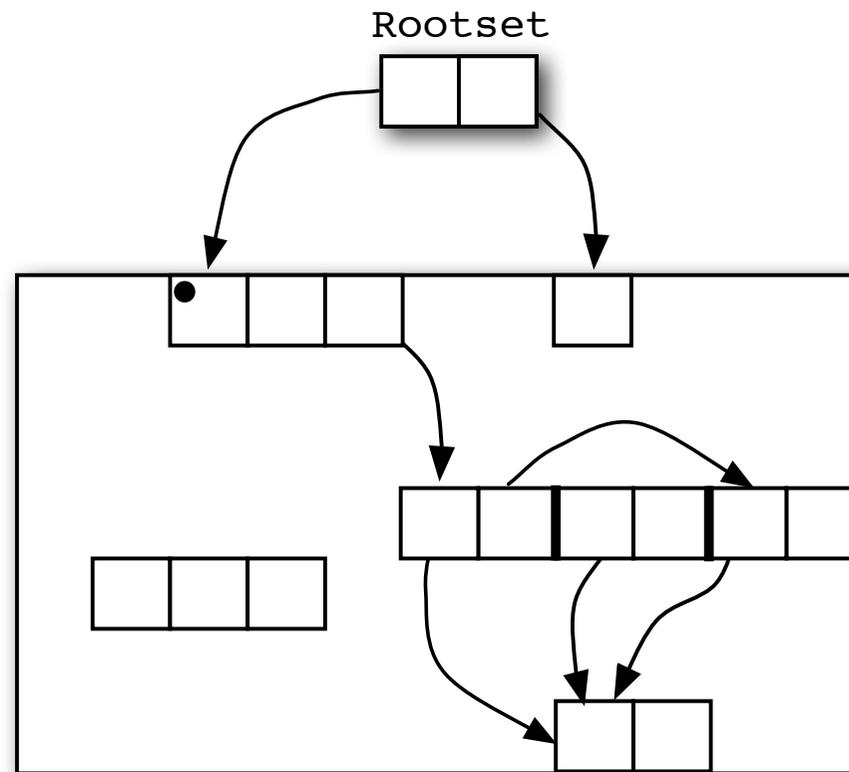
Memory layout



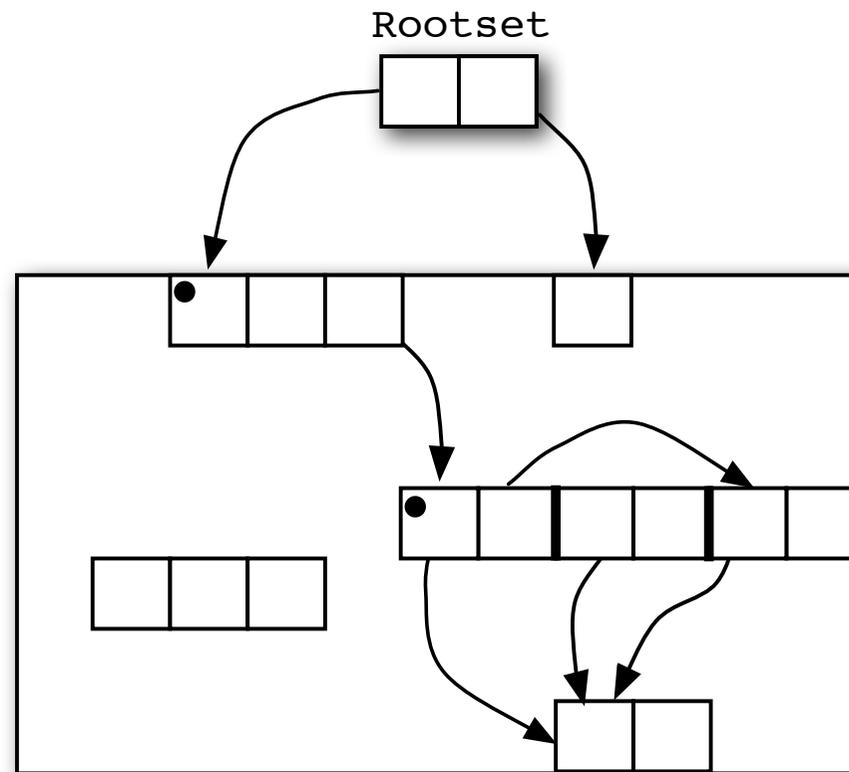
Mark-sweep collection



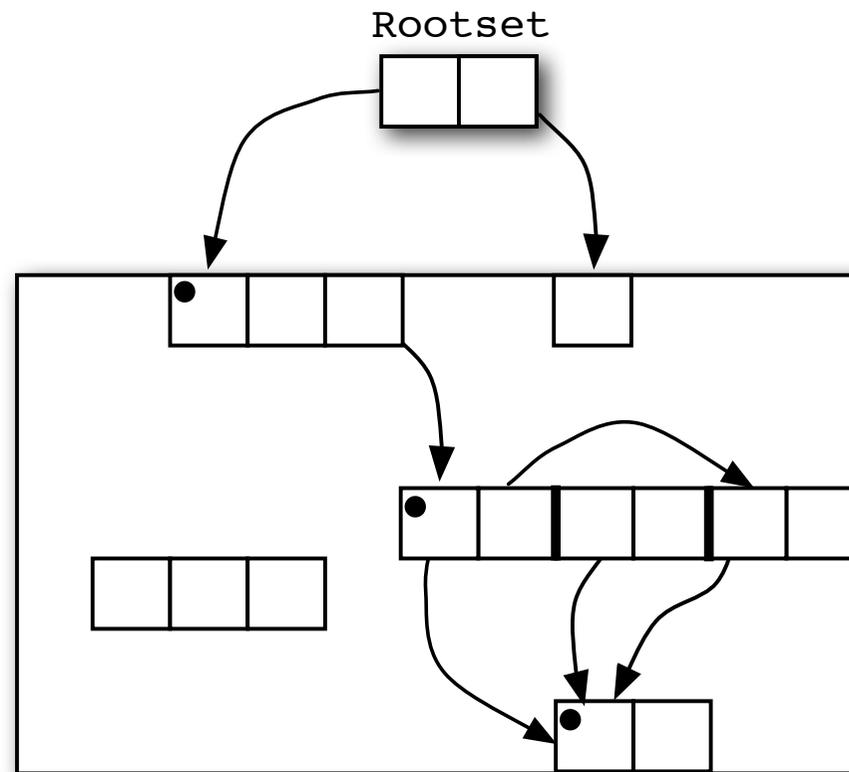
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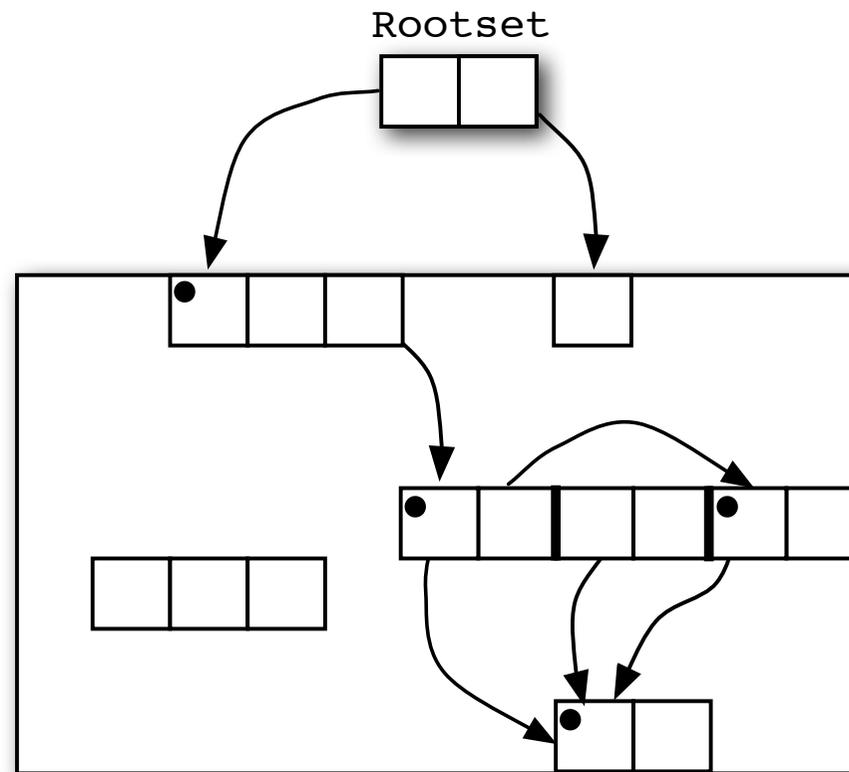
Mark-sweep collection



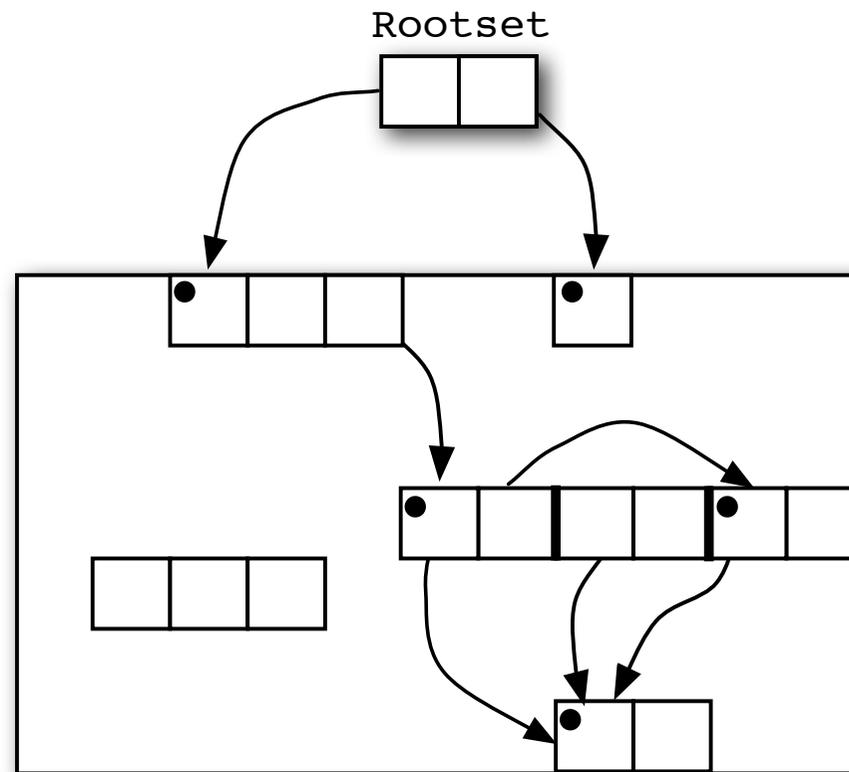
Mark-sweep collection



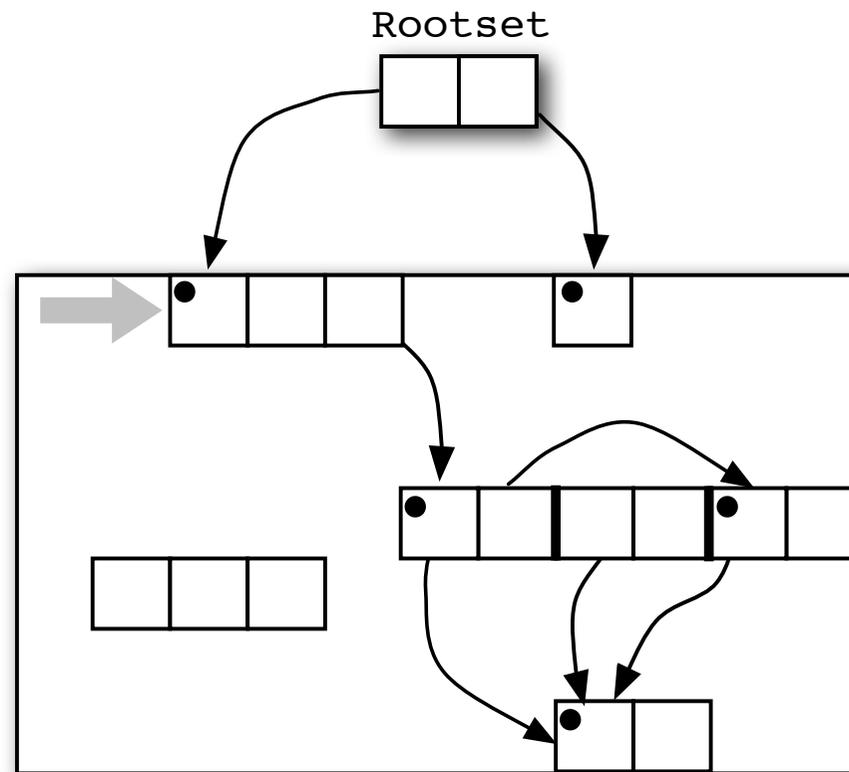
Mark-sweep collection



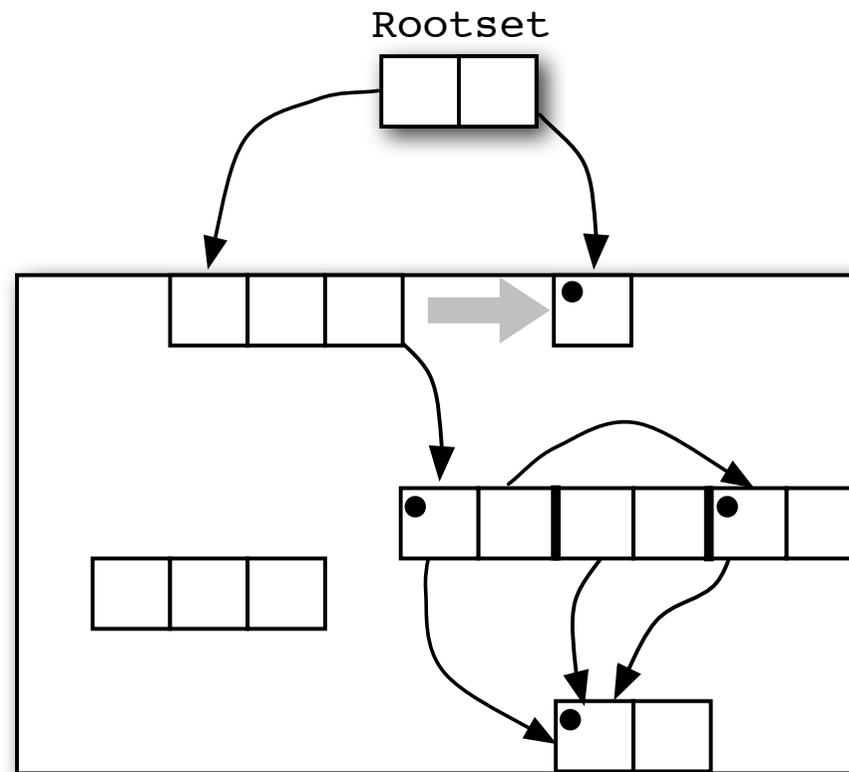
Mark-sweep collection



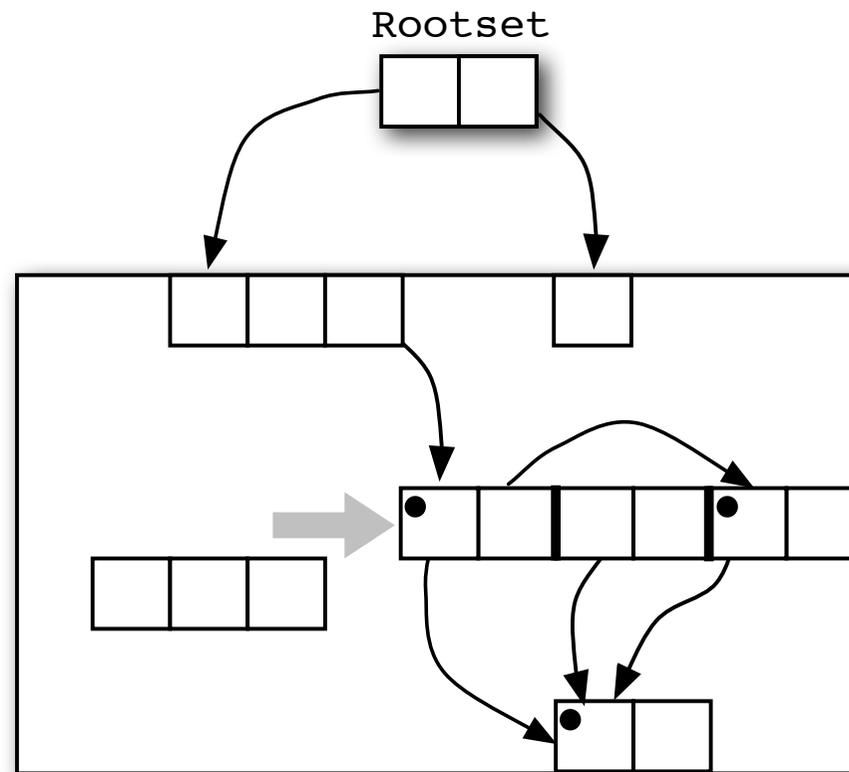
Mark-sweep collection



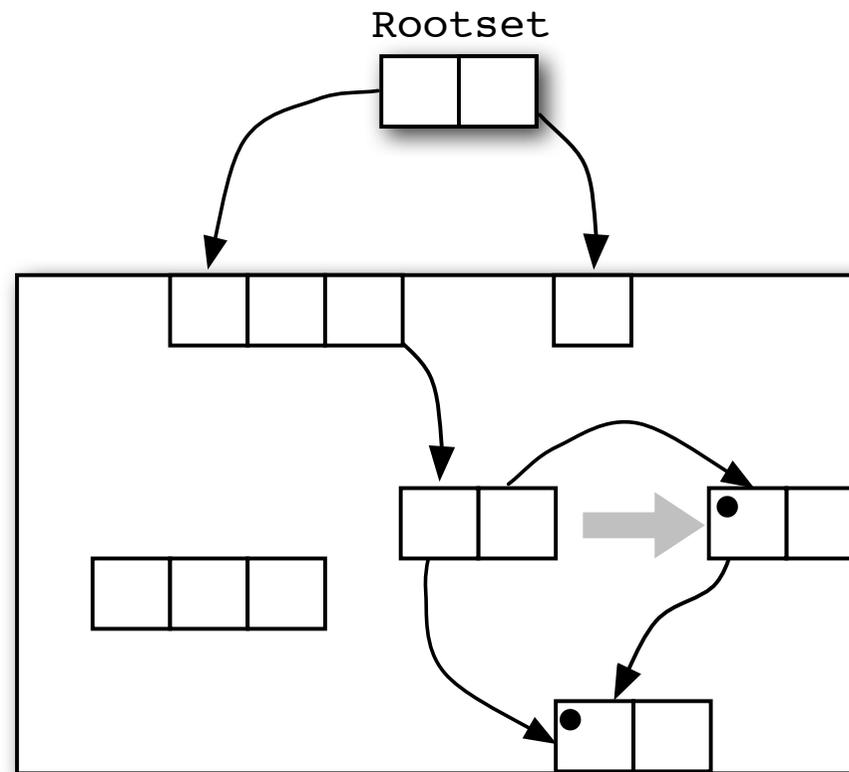
Mark-sweep collection



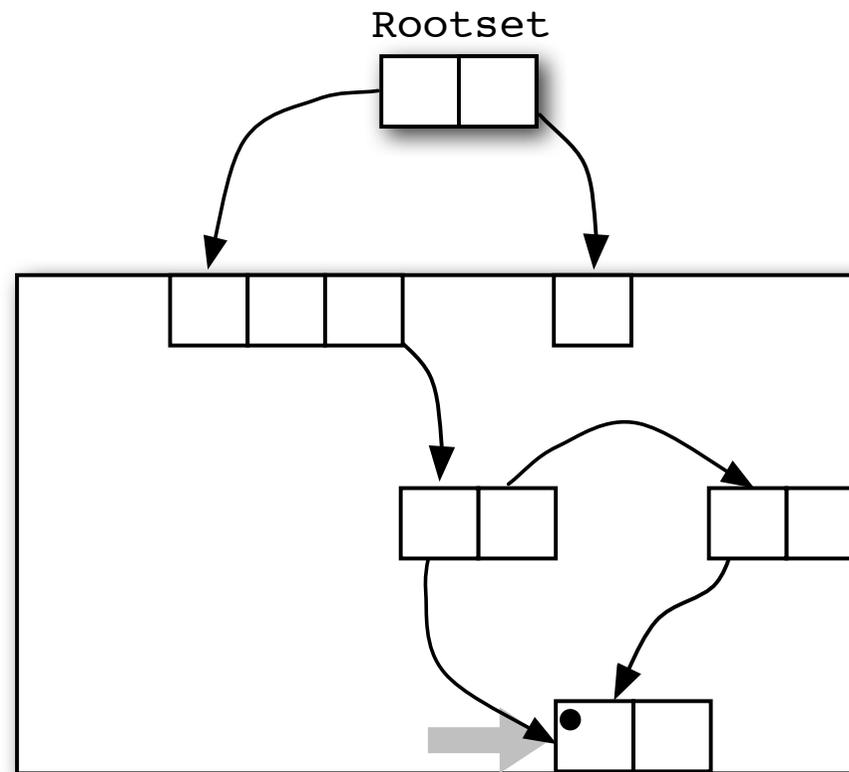
Mark-sweep collection



Mark-sweep collection



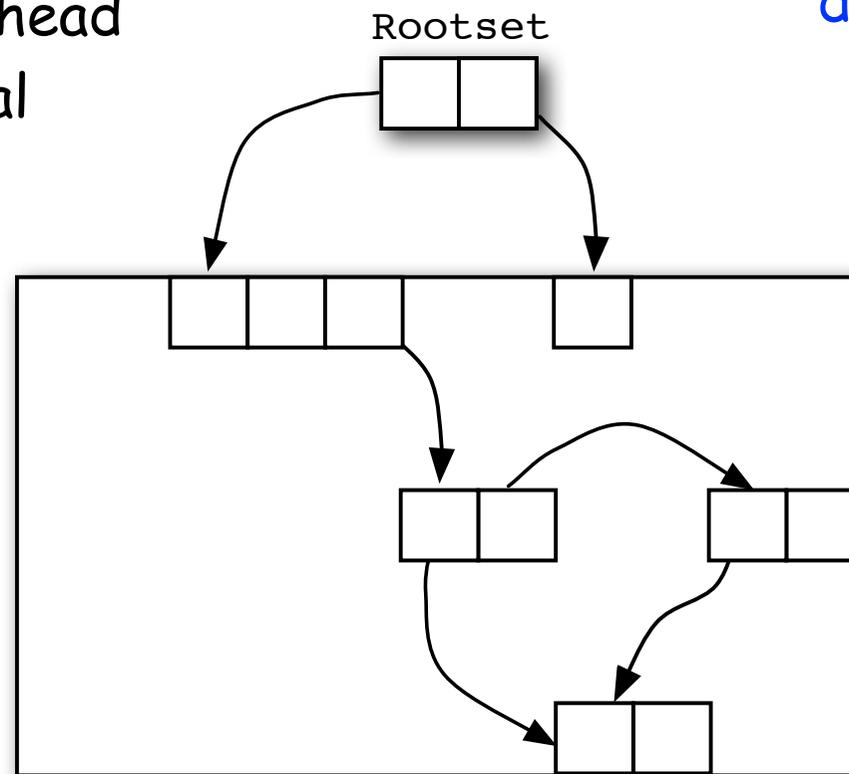
Mark-sweep collection



Mark-sweep collection

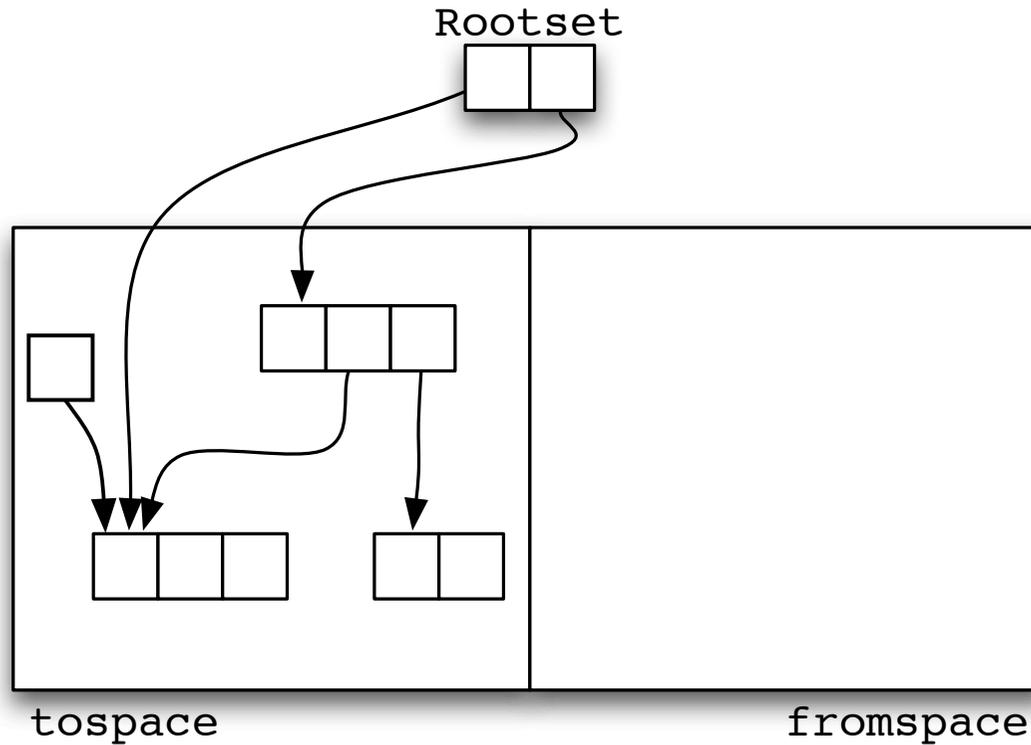
- + low memory overhead
- + easily incremental
- no compaction

depth-first GC!

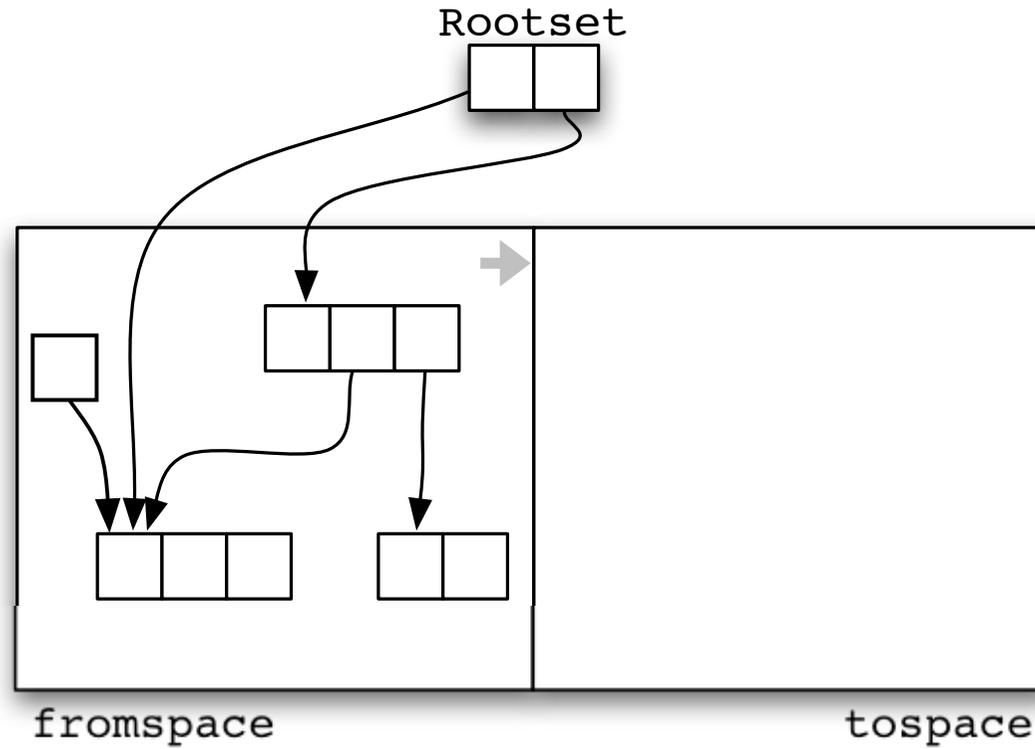


time proportional to number of allocated nodes

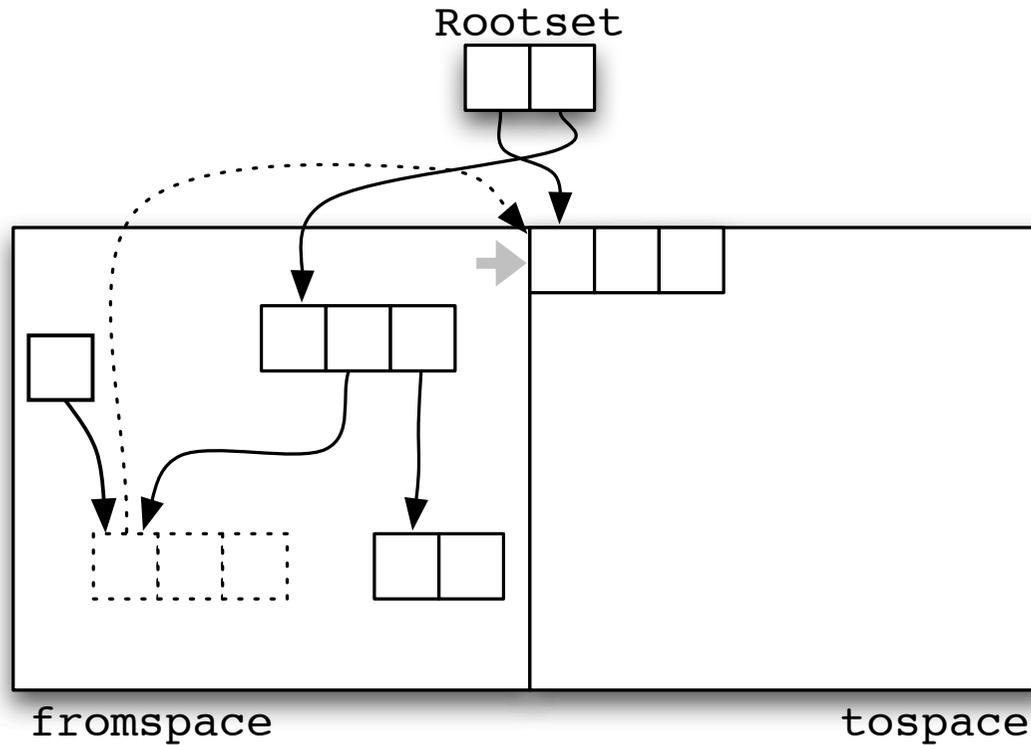
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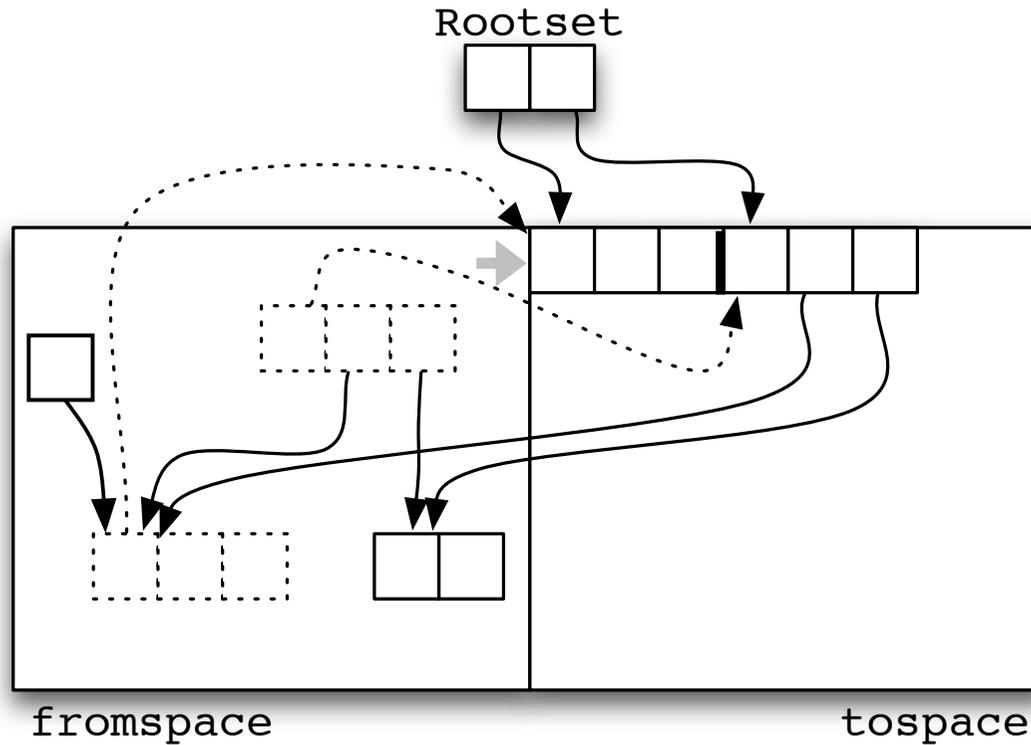
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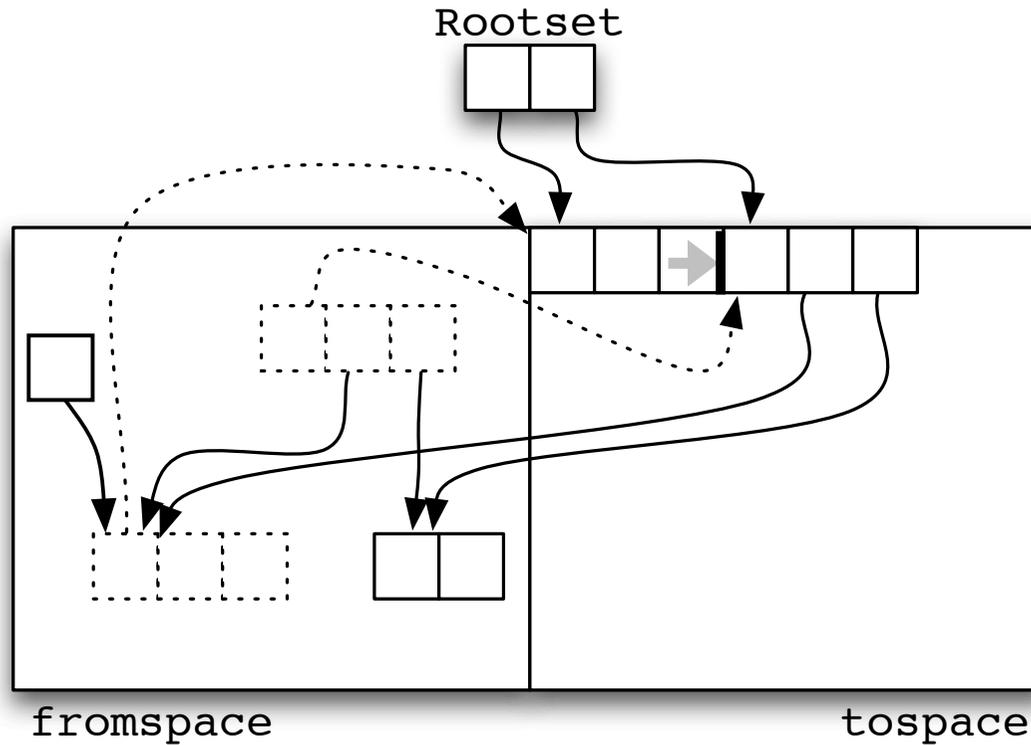
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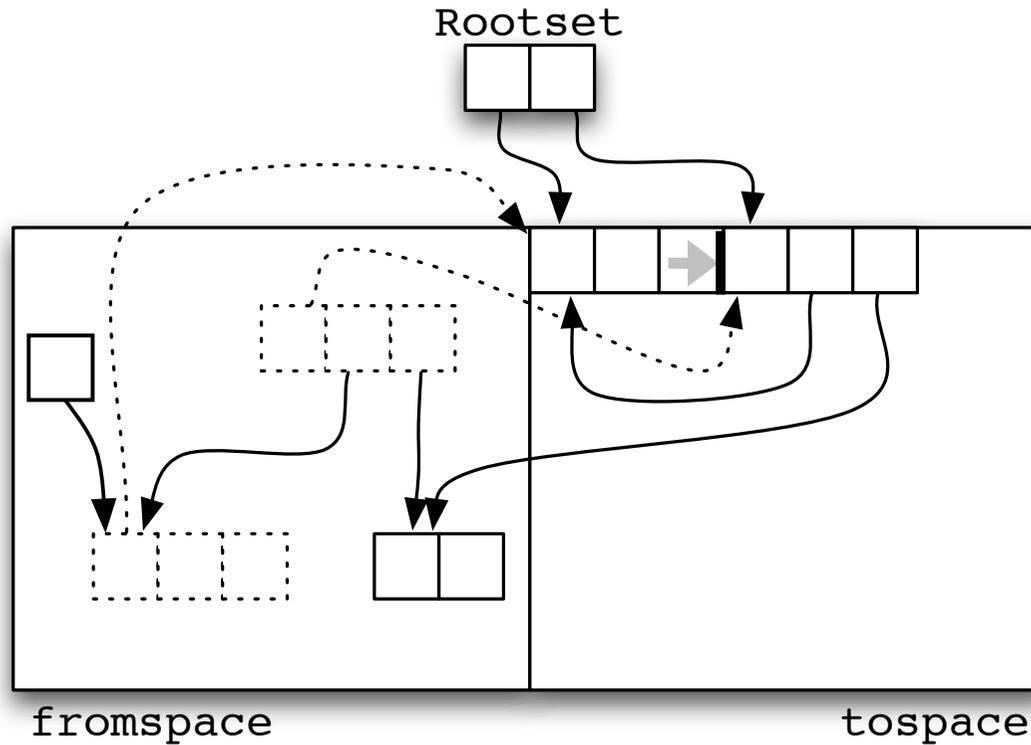
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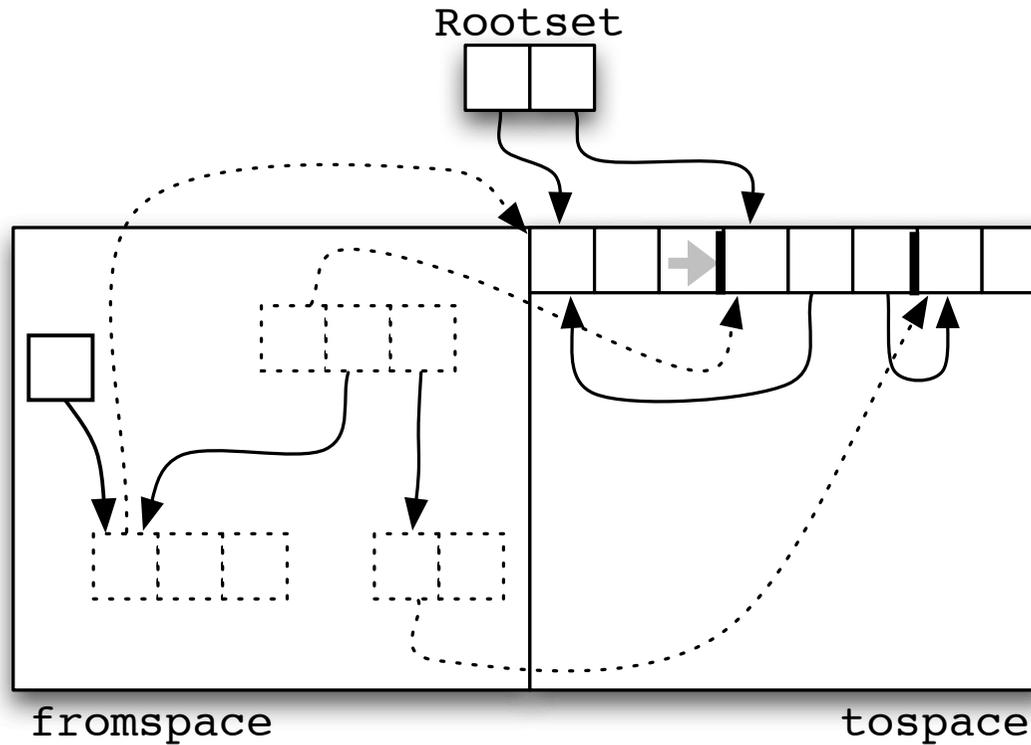
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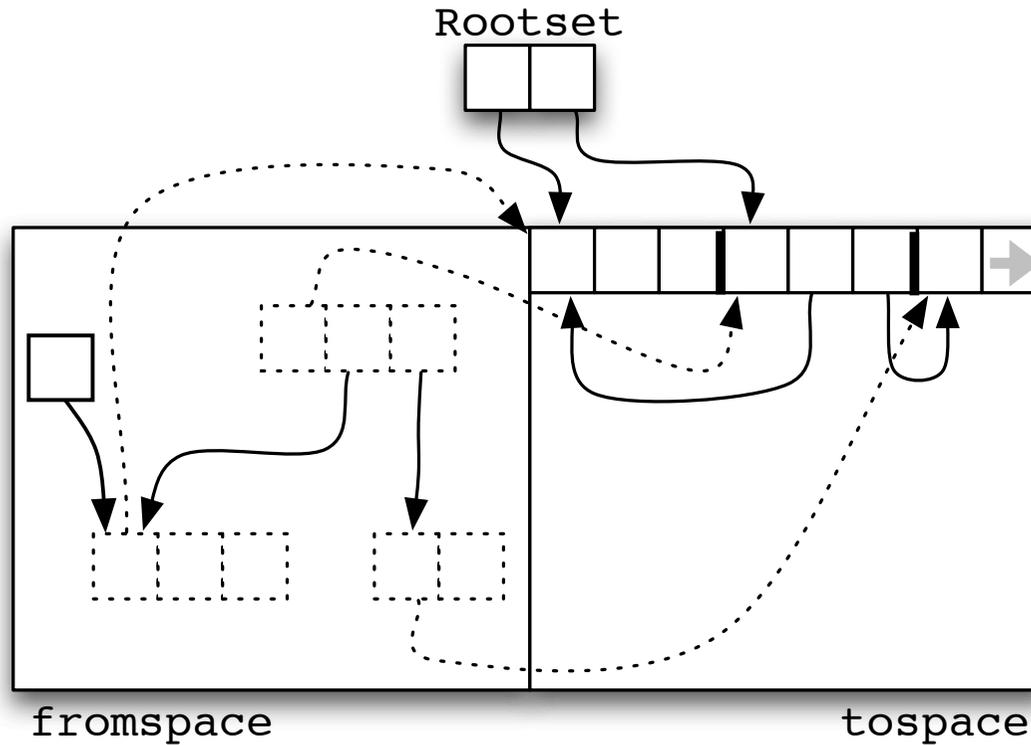
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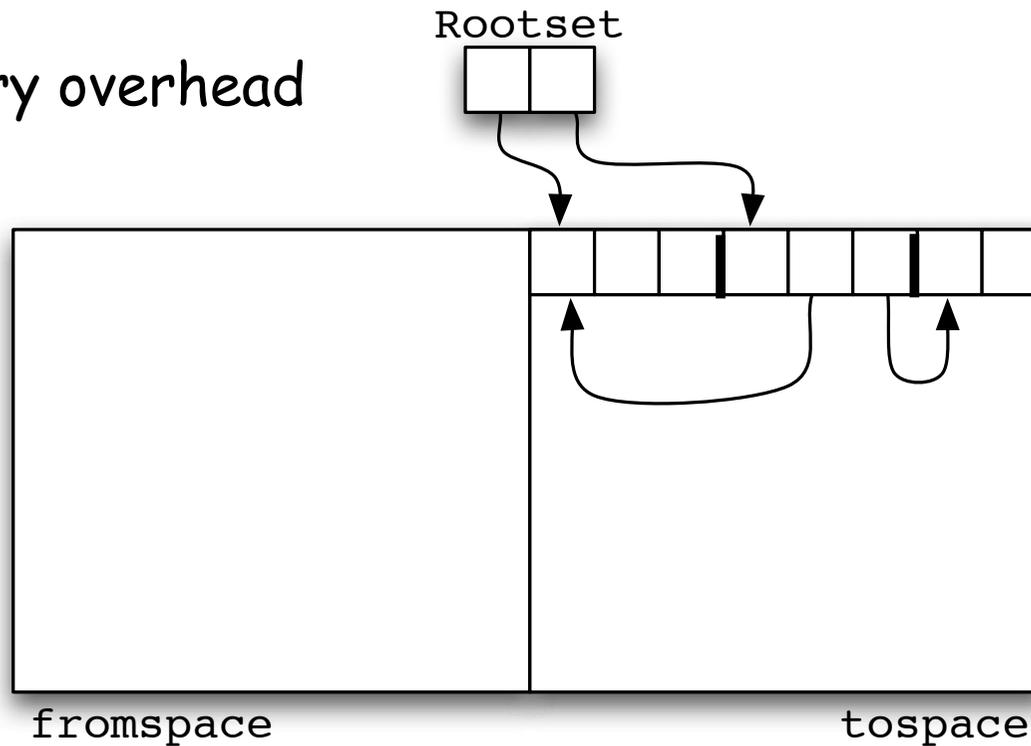
Copying collection



Copying collection

- + cheap allocation
- + compaction
- 100% memory overhead

breadth-first GC!



time proportional to size of live nodes

Finding roots

- A GC observes machine state on assembly level
- Two problems:
 - Finding actual variables among all stored bits (instructions, return addresses, cpu admin, ...)
 - Finding heap pointers among the variables (integers, floats, "small pointers", ...)

Finding heap pointers

- "Small" pointer: value way below start-of-heap
 - no real risk for confusion
- Type information can be used to distinguish integers and floats from pointer variables, but polymorphic code complicates the picture
- Polymorphism implementation strategies:
 - uniform representation (always use pointers)
 - uniform size only (all data fit a machine word)
 - code specialization for non-pointer instances

Uniform representation

- Use heap allocation for all ordinary types
- Integer n represented as heap node `Int n`
- Integer arithmetic must (1) extract values from their boxes, (2) perform operation, and (3) store result in a newly allocated `Int`
- Example: $op\ x\ (op\ y\ z) \Rightarrow$
`case x of Int x' -> case (case y of Int y' -> case z of Int z' -> Int (op' y' z')) of Int v' -> Int (op' x' v')`
where `op'` is the real operation corresponding to `op`
- Optimizations clearly desirable!

Uniform representation

- GHC uses such a boxed representation for types `Int`, `Float`, etc
- In addition, GHC makes unboxed types `Int#`, `Float#`, etc, available, which cannot be used to instantiate type variables
 - `data Int = Int Int#`
- Literal `n#` really means integer `n`, while `n = Int n#`
- To improve performance, GHC goes to great length to remove repeated boxing and unboxing, even across function calls (with help of types!)

Uniform size

- Our approach so far: just cast literals to `Ptr`
- Literals must fit the size of pointers, true for `Int` and `Float` but not `Double` on 32-bit machines
- Distinguish dynamically based on
 - (A) One bit stolen from every 32-bit value
 - (B) Separate bitvectors that describe groups of polymorphic variables

Uniform size (A)

- Stealing the least significant bit from
 - a pointer: ok if pointers are word-aligned (lowest bits are always 0) and 0 means "ptr"
 - an integer: represent n as $R(n) = 2n+1$ (halves the expressible range), and adjust primitives accordingly ($R(x+y) = 2x+2y+1 = R(x)+R(y)-1$)
 - a float: halves the precision (mask before use)
- Used by O'Cam1 to good effect

Uniform size (B)

- Adding bit-vector parameters to all polymorphic functions and constructors, which tell how they are instantiated at run-time (ptr/non-ptr flags)
 - Propagates the necessary GC information to non-local scopes
 - Note: only values of variable type need dynamic ptr/non-ptr inspection
 - Avoids the need to tag each value, but adds small overhead to function calls

Code specialization

- Create a specialized copy whenever a polymorphic function is instantiated with a non-pointer type

- Example:

`rep 0 x = []`

`rep n x = x : rep (n-1) x`

`y = (rep 7 (1,1), rep 7 1.1)`

`repF 0 x = []`

`repF n x = x : repF (n-1) x`

`y = (rep 7 (1,1), repF 7 1.1)`

- Ensures that polymorphic values are pointers, but at the price of code size increase
- Also works for types that don't fit word size

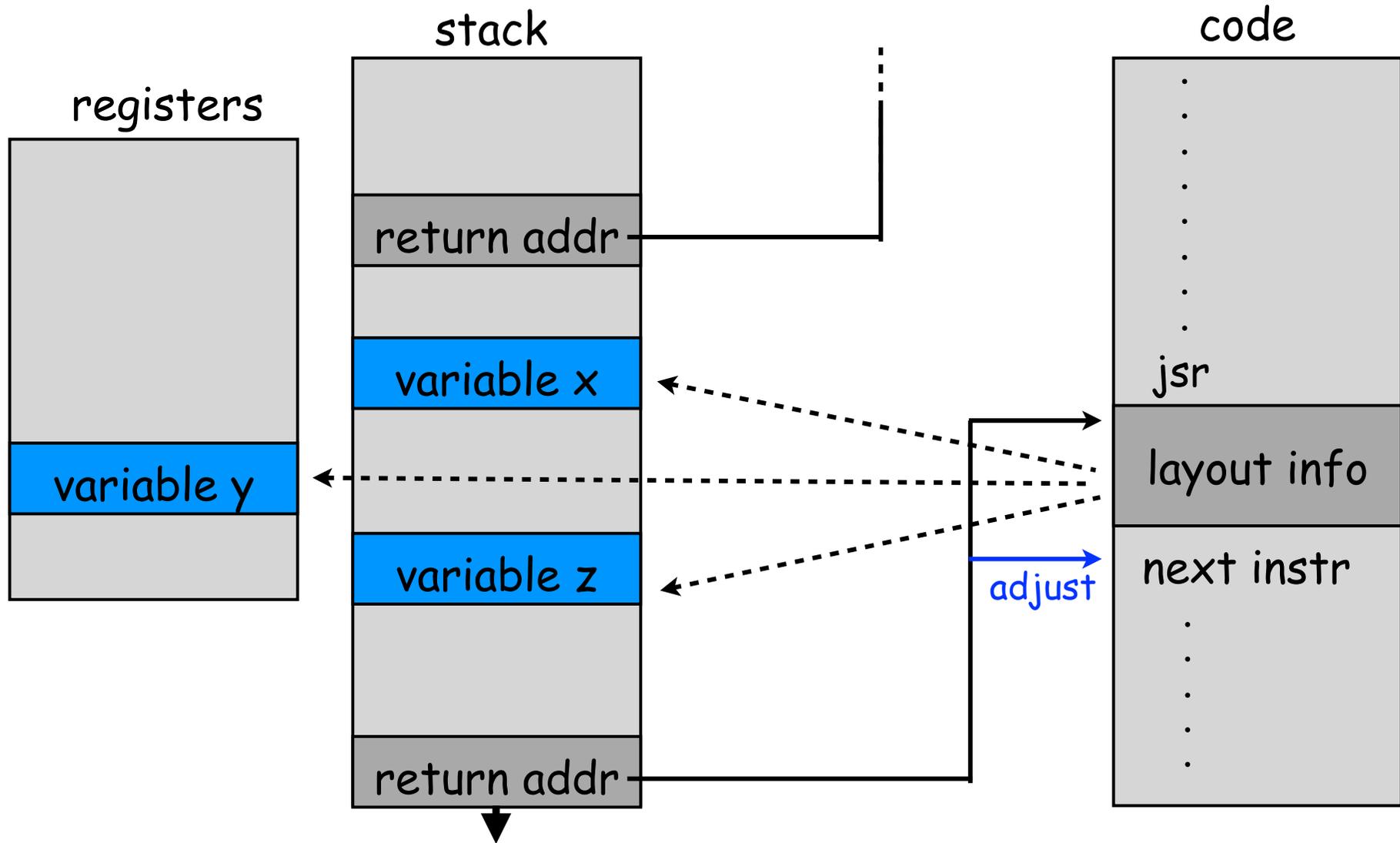
Finding all variables

- Globals are of course trivial...
- ... but layout of variables in registers and the stack is not accessible if we compile to C!
- The traditional conclusion: must generate assembly code in order to give GC full control
- But this also implies the register allocations and instruction scheduling decisions that are performance keys on modern architectures...
- A rather hefty price for the ability to just spot the data layout!

When to run the GC

- When free space drops below some threshold — a natural criterion, detected during allocations
- Memory state must thus be understandable for the GC at least at every malloc call
- Machine state at a malloc call also involves all suspended calls indirectly leading to the malloc — thus all function calls count as potential GC interruption points

Example: GHC



Example: GHC

- No cost at function call, minor cost at return
- One layout-table per function call can mean a significant size burden
- Important that static layout table is accurate no matter what path has lead to the call point
- Idea not extensible to concurrent GC (would require a layout table after every instruction!)
- (Demands of GC major motivation behind earlier work on C-- compiler target language)

Conservative GC

- Attractive alternative to writing a complete assembly-level back-end: use C with a conservative garbage collector
- Principal idea: every stack and register word is scanned, and everything that looks like a pointer is treated like one
- "Look like" = word-aligned & within heap & point at beginning of allocated block
- Precludes copying GC (can't mutate guessed root)

Conservative GC

- Leads to memory leaks if many integers, floats, etc, use bit-patterns that are also happen to be valid heap block addresses
- Has nevertheless found good use in practice
- Even eliminates the need to know the pointer-typed variables (but type info might reduce the risk for accidental misinterpretation if present)
- Ready to use in the form of a tried-and-tested implementation: the Boehm-Demers-Weiser GC library <http://www.hpl.hp.com/personal/Hans_Boehm/gc/>

Recommendation

For the lab project:

Use the Boehm-Demers-Wiser collector!

Stack management

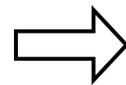
- A comparably simple issue!
- Sole concern: detect stack overflow and quit instead of continuing with corrupted data
- Handled automatically by memory-management hardware on most platforms, under most operating systems
- Should such service not exist, a simple check at the beginning of each generated C function will do the job

Optimizing tail recursion

- Main reason for excessive stack usage: deeply recursive algorithms
- Unnecessarily stack-hungry code: a tail-recursive function (ends with recursive call)
- Can easily be translated into imperative loops

sum a [] = a

sum a (x:xs) = sum (a+x) xs



```
sum (a, x) {
```

```
  while (1)
```

```
    if (x==0) return a;
```

```
    else {a += x; x = x[1];}
```

```
}
```

Summary

- Garbage collection a necessity for FP
- Collection techniques: copying vs. mark-sweep
- Relies on ability to find all program variables, and to distinguish pointers from other values
- Challenge: devise a means to locate variables without having to build a full low-level back-end
- Conservative collectors can work without knowing where the variables are, at some higher risks for space leaks