Finite Automata and Formal Languages

TMV026/DIT321-LP4 2012

Lecture 1 Ana Bove

March 12th 2012

Overview of today's lecture:

- Course Organisation
- Overview of the Course

Course Organisation

Level: This course is a *bachelor* course.

Lectures: Mondays 13.15–15, and Tuesdays 10–11:45 *Weeks 1 and 6:* Also Thursdays 10–11:45 in EA Ana Bove, bove@chalmers.se

Exercise Sessions: Thursdays 13.15–15 in EL41 VERY important!! Willard Rafnsson, willard.rafnsson@chalmers.se

Consultation Time: Thursdays 10–11.45 in 5205 *NOT* in weeks 1 and 6 Ana Bove

Exams: May 25th and August 31st. No books or written help during the exam.

Course Organisation (Cont.)

Assignments: *Individual non-obligatory* weekly assignments which generate bonus points valid *ONLY* on the exams during 20112

Each assignment will be up to 10 pts. If a student has collected n pts in assignments, this will correspond to n/10 points in the exam. (Exams are usually 60 points.)

You **MUST** write your *name*, *personal number* and *e-mail address* when you submit an assignment.

How to submit? On paper or via the Fire system.

Note: Be aware that assignments are part of the examination of the course and they **should** be done *individually*! Standard procedure will be followed if copied solutions are detected.

See the web page of the course for details on this!

Course Organisation (Cont.)

March 12th 2012, Lecture 1

Book: Introduction to Automata Theory, Languages, and Computation, by Hopcroft, Motwani and Ullman. Addison-Wesley. Both second and third edition are fine. We will cover chapters 1 to 7 and a bit of chapter 8 (if time allows).

Web Page: http://www.cse.chalmers.se/edu/course/TMV026/ Accessible from Chalmers "studieportalen". Check it regularly for news!

Wikipedia: http://en.wikipedia.org/wiki/

Course Evaluation: I need 2 GU student representatives by Thursday this week.

CTH student representatives Daniel Bergqvist, danber@student.chalmers.se Marika Hansson, hmarika@student.chalmers.se Magnus Larsson, maglars@student.chalmers.se Marcus Stigelid, stigelid@student.chalmers.se

See web page of the course for last year's evaluation.

March 12th 2012, Lecture 1

TMV026/DIT321

/21

Programming Bits in the Course

The course doesn't require much programming tasks.

Still we will present several algorithms to translate between different formalisations.

I will sometimes show a Haskell program simulating certain automaton or implementing an algorithm.

(Most of you should know Haskell, if not I really recommend you learn it: it is very elegant and nice!)

You are welcome to test your knowledge implementing things in your favourite language!

Automata

Dictionary definition:

```
Main Entry: au·tom·a·ton
Function: noun
Inflected Form(s): plural au·tom·atons or au·tom·a·ta
Etymology: Latin, from Greek, neuter of automatos
Date: 1645
```

- 1 : a mechanism that is relatively self-operating; especially : robot
- 2 : a machine or control mechanism designed to follow automatically a predetermined sequence of operations or respond to encoded instructions
- 3 : an individual who acts in a mechanical fashion

Automata: Applications

Models for ...

- Software for designing circuits
- Lexical analyser in a compiler
- Software for finding patterns in large bodies of text such as collection of web pages
- Software for verifying systems with a finite number of different states such as protocols
- Real machines like vending machines, telephones, street lights, ...
- Application in linguistic, building of large dictionary, spell programs, search
- Application in genetics, regular pattern in the language of protein





However if the man leaves the wolf and the goat unattended on either shore, the wolf surely will eat the goat.

Similarly, if the goat and the cabbage are left unattended, the goat will eat the cabbage.

Puzzle: Is it possible to cross the river without the goat or cabbage being eaten?

Solution: We write all the possible transitions, and look for possible paths between two nodes.

Solution: The Man, the Wolf, the Goat and the Cabbage



Overview of the Course

- Formal proofs
- Regular languages
- Context-free languages
- (Turing machines)

Formal Proofs

Many times you will need to prove that your program is "correct" (satisfies a certain specification).

In particular, you won't get a complex program right if you don't understand what is going on.

Different kind of formal proofs:

- Output Deductive proofs
- Proofs by contradiction
- Proofs by counterexamples
- Proofs by (structural) induction

March 12th 2012, Lecture 1

TMV026/DIT321

Example: Parity Counter

The states of an automaton can be thought of as the *memory* of the machine.



Two events: p_0 and p_1 .

The machine does nothing on the event p_1 .

The machine counts the parity of the number of p_0 's.

A finite-state automaton has *finite memory*!

We now would like to prove that the automata is on state even iff an even number of p_0 were pressed.

Functional Description: Parity Counter

Let us define 2 functions f_{even} and f_{odd} representing the 2 states of the automaton.

The input can be represented by the data type $T = 0 \mid p_0 \mid T \mid p_1 \mid T$.

The description of the automaton is: $f_{even}, f_{odd} : T \rightarrow {Even, Odd}$

$f_{\rm even} 0 = Even$	$f_{\sf odd} {\sf 0} = {\sf Odd}$
$f_{\text{even}} (p_0 \ n) = f_{\text{odd}} \ n$	$f_{ m odd} \ (p_0 \ n) = f_{ m even} \ n$
$f_{\text{even}} (p_1 \ n) = f_{\text{even}} \ n$	$f_{ m odd} \ (p_1 \ n) = f_{ m odd} \ n$

We now would like to prove that f_{even} n = Even iff n contains an even number of constructors p_0 .

March 12th 2012, Lecture 1

TMV026/DIT321

Example: on/off-switch

Recall the description of the on/off-switch.

We would like to prove that:

the automaton is in state OFF after n pushes iff n is even and

the automaton is in state ON after n pushes iff n is odd.

Alternatively, we could prove that:

 f_{OFF} n = Off iff n is even

and

 f_{ON} n = On iff n is odd.

Regular Languages

Finite automata were originally proposed in the 1940's as models of neural networks.

Turned out to have many other applications!

In the 1950s, the mathematician Stephen Kleene described these models using mathematical notation (*regular expressions*, 1956).

Ken Thompson used the notion of regular expressions introduced by Kleene in the UNIX system.

(Observe that Kleene's regular expressions are not really the same as UNIX's regular expressions.)

Both formalisms define the *regular languages*.

March 12th 2012, Lecture 1

TMV026/DIT321

Context-Free Languages

We can give a bit more power to finite automata by adding a stack that contains data.

In this way we extend finite automata into a *push down automata*.

In the mid-1950s Noam Chomsky developed the *context-free grammars*. Context-free grammars play a central role in description and design of programming languages and compilers.

Both formalisms define the *context-free languages*.

Church-Turing Thesis

In the 1930's there has been quite a lot of work about the nature of *effectively computable (calculable) functions*:

- Recursive functions by Stephen Kleene
- λ -calculus by Alonzo Church
- Turing machines by Alan Turing

The three computational processes were shown to be equivalent by Church, Kleene, (John Barkley) Rosser (1934—6) and Alan Turing (1936—7).

The *Church-Turing thesis* states that if an algorithm (a procedure that terminates) exists then, there is an equivalent Turing machine, a recursively-definable function, or a definable λ -function for that algorithm.

March 12th 2012, Lecture 1

TMV026/DIT32

Turing Machine (ca 1936–7)

Simple theoretical device that manipulates symbols contained on a strip of tape.

It is as "powerful" as the computers we know today (in term of what they can compute).

It allows the study of *decidability*: what can or cannot be done by a computer (*halting* problem).

Computability vs *complexity* theory: we should distinguish between what can or cannot be done by a computer, and the inherent difficulty of the problem (*tractable* (polynomial)/*intractable* (NP-hard) problems).

Learning Outcome of the Course

After completion of this course, the student should be able to:

- Explain and manipulate the different concepts in automata theory and formal languages;
- Have a clear understanding about the equivalence between (non-)deterministic finite automata and regular expressions;
- Acquire a good understanding of the power and the limitations of regular languages and context-free languages;
- Prove properties of languages, grammars and automata with rigorously formal mathematical methods;
- Design automata, regular expressions and context-free grammars accepting or generating a certain language;
- Describe the language accepted by an automata or generated by a regular expression or a context-free grammar;
- Simplify automata and context-free grammars;
- Determine if a certain word belongs to a language;
- Define Turing machines performing simple tasks.

March 12th 2012, Lecture 1

TMV026/DIT321

21/21