The processor(s) used for executing a task are determined during system operation "on-line"

- Approaches: partitioned scheduling, guided search,

Multiprocessor scheduling

- The processor(s) used for executing a task are determined

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- Approach: global scheduling

non-quided search, ...

Dynamic assignment

Static assignment

How are tasks assigned to processors?

before system is put in mission ("off-line")

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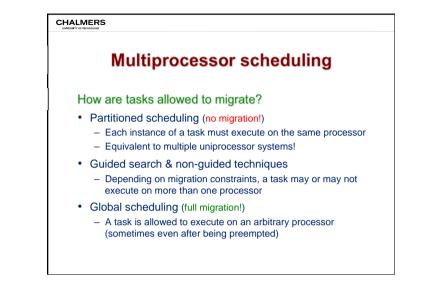
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# Partitioned scheduling

#### General characteristics:

- Each processor has its own queue for ready tasks
- Tasks are organized in groups, and each task group is assigned to a specific processor
- When selected for execution, a task can only be dispatched to its assigned processor



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## **Partitioned scheduling**

#### Advantages:

Mature scheduling framework

Lecture #9

- Most uniprocessor scheduling theory also applicable here
- Uniprocessor resource-management protocols can be used
- · Supported by automotive industry
  - AUTOSAR prescribes partitioned scheduling

#### Disadvantages:

- · Cannot exploit all unused execution time
  - Surplus capacity cannot be shared among processors
  - Will suffer from overly-pessimistic WCET derivation

2

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## 

Consequence:

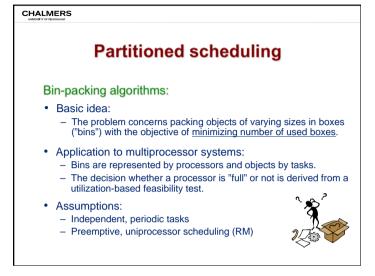
There cannot be any pseudo-polynomial time algorithm for finding an optimal partition of a set of tasks unless P = NP.

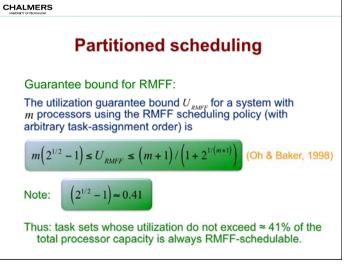
## CHALMERS Partitioned scheduling

Bin-packing algorithms:

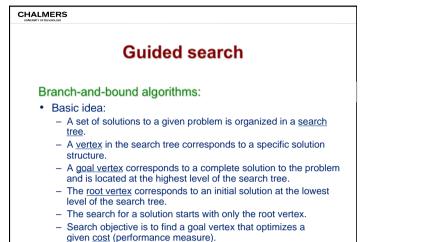
Rate-Monotonic-First-Fit (RMFF): (Dhall and Liu, 1978)

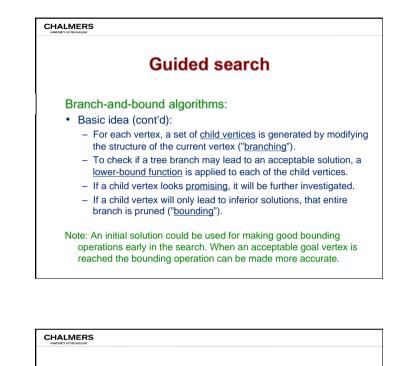
- Let the processors be indexed as  $\mu_1, \mu_2, \ldots$
- Assign the tasks in the order of increasing periods (that is, RM order).
- For each task  $\tau_i$ , choose the <u>lowest</u> previously-used *j* such that  $\tau_i$ , together with all tasks that have already been assigned to processor  $\mu_j$ , can be feasibly scheduled according to the utilization-based RM-feasibility test.
- Processors are added if needed for RM-schedulability.





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## Guided search

### Branch-and-bound for multiprocessor scheduling:

- Initial schedule is empty:
  - At each vertex in the search tree, a set of <u>ready tasks</u> (candidates for execution) are available for scheduling.
  - Generation of a child vertex corresponds to adding one of the ready tasks to the schedule in the current vertex.
- Initial schedule is complete (but possibly suboptimal):
  - At each level of the search tree, a set of <u>scheduling changes</u> (e.g., modified constraints or assignments) are available.
  - Generation of a child vertex corresponds to applying one or more of the changes to the schedule in the current vertex.

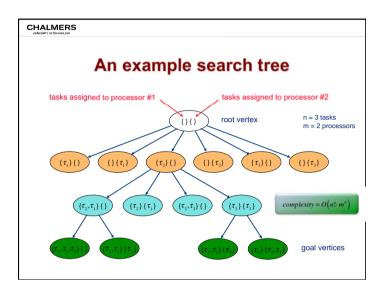
## Branch-and-bound algorithms:

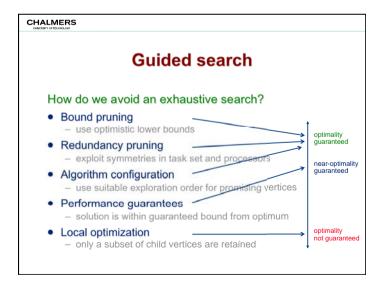
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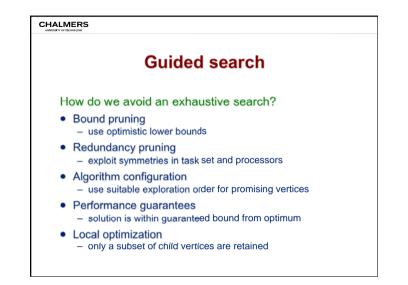
- Application to multiprocessor scheduling:
  - The search tree represents the set of all task-to-processor assignments for a given set of tasks and processors.

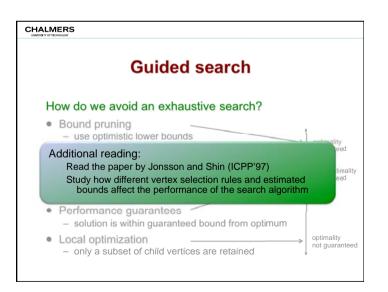
Guided search

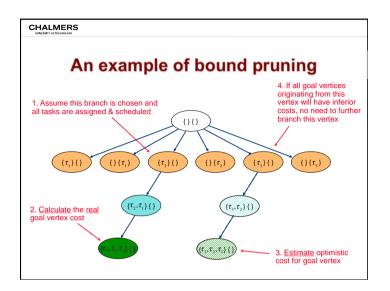
- A vertex in the search tree is a partial or complete assignment of tasks to processors.
- The root vertex corresponds to an initial (empty or complete) schedule.
- A goal vertex corresponds to a complete schedule.
- The purpose of the lower-bound function is to assess whether a child vertex is <u>feasible</u>, that is, whether the corresponding branch in the search tree contains a feasible schedule.

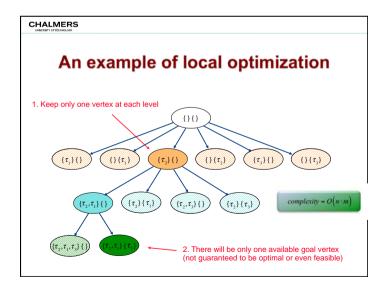


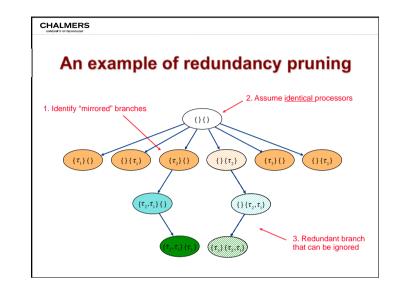


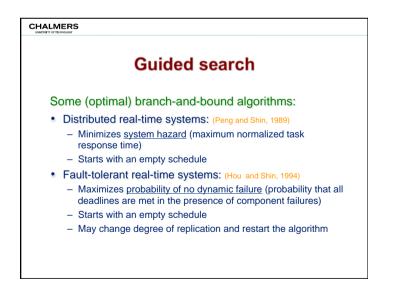












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## CHALMERS CHALMERS Guided search Some (optimal) branch-and-bound algorithms: Uniprocessor real-time systems: (Xu and Parnas, 1990) - Minimizes maximum task lateness - Starts with an initial (complete) schedule Modifies preemption, precedence and exclusion constraints Multiprocessor real-time systems: (Xu, 1993) - Minimizes maximum task lateness - Starts with an initial (complete) schedule - Modifies preemption, precedence and exclusion constraints

## CHALMERS Guided search Some good local-optimization algorithms: Pair-wise clustering: (Ramamritham, 1995) - Promising vertices are explored in the order of decreasing search-tree level; within each level, exploration is made in the order of increasing task LFT (latest finishing time). - Lower-bound function determines for the current vertex whether it is feasible using simple heuristics that keep track of latest start time and available time resources. LFT is derived from task set end-to-end deadlines. Pairs of communicating tasks are clustered based on the communication volume ratio. If the ratio between the task pair's execution times and communication volume is below a certain

bound, the two tasks are assigned to the same processor.

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## Non-guided search

### General characteristics:

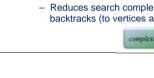
- · Each non-guided search is given an initial task-toprocessor assignment from which the search starts.
- Within each iteration step during search, different derivable alternatives of changing the current assignment are examined.
- To check whether an alternative is feasible or not, a run-time efficient feasibility test has to be used.
- In order to help the search find better assignments, the number of deadline misses is included as a penalty into the function calculating the goodness of the assignment.

Some good local-optimization algorithms: • Myopic scheduling: (Ramamritham, Stankovic and Shiah, 1990) - Promising vertices are explored in the order of decreasing search-tree level; within each level, exploration order is given by a heuristic function that calculates a weighted sum of task execution time, deadline, earliest start time and laxity.

Guided search

- Lower-bound function determines for the current vertex whether it is strongly feasible, that is, whether a feasible schedule can be obtained by expanding any of its child vertices.
- Reduces search complexity by only investigating the k child vertices with closest deadline in the check for strong feasibility.
- Reduces search complexity by limiting the number of allowed backtracks (to vertices at lower search-tree levels)

 $complexity = O(k \cdot n \cdot m)$ 



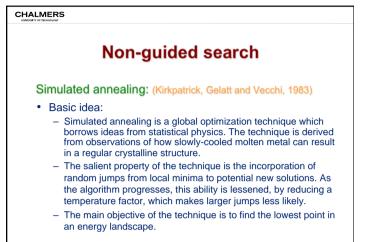
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## CHALMERS Non-quided search Examples: Simulated annealing Genetic optimization Tabu search Neighbourhood search • ... These techniques all have in common that it is sufficient to state what makes a good solution, not how to get one!

## CHALMERS Non-guided search Simulated annealing: Application to multiprocessor scheduling: - The set of all task-to-processor assignments for a given set of task and processors is called the problem space. A point in the problem space is an assignment of tasks to processors. - The neighbor space of a point is the set of points that are reachable by moving any single task to any other processor. - The energy of a point in problem space is a measure of the goodness of the task assignment represented by that point. - The energy function determines the shape of the problem space. It can be visualized as a rugged landscape, with deep valleys representing good solutions, and high peaks

representing poor or infeasible ones.



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## Non-guided search

### Simulated annealing:

- Algorithm:
  - A random starting point is chosen, and its energy  $E_s$  is evaluated. A random point in the neighbor space is then chosen, and its energy  $E_n$  is evaluated. This point becomes the new starting point if either  $E_n \leq E_s$ , or if  $E_n > E_s$  and

## $e^x \ge \operatorname{random}(0,1)$ where $x = -(E_n - E_s)/C$

The control variable C is analogous to the temperature factor in a thermodynamic system. During the annealing process, C is slowly reduced (cooling the system), making higher energy jumps less likely. Eventually, the system freezes into a low energy state.

# Non-guided search

Non-guided search

#### Genetic optimization:

Simulated annealing:

randomly-chosen processor.

characteristics of the assignment:

Total communication bus utilization

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- · Application to multiprocessor scheduling:
  - Tasks assignments and orderings are viewed as "chromosomes"
  - Tasks represent "genes"
  - Mutation means that a task is moved to another processor

