

Naív sortering

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🌐 kapitel 8, avsnitt 1–2 och 4–5

Javas sorteringsmetoder

Java.Arrays innehåller flera sorteringsmetoder för olika sorters fält

- fält med primitiva typer sorteras med QuickSort
- fält med objekt sorteras med MergeSort

Java.Collections innehåller liknande sorteringsmetoder för listor

- listor sorteras med MergeSort

Både QuickSort och MergeSort och flera andra algoritmer är $O(n \log n)$

Java's sorteringsmetoder

Method sort in Class Arrays	Behavior
<code>public static void sort(int[] items)</code>	Sorts the array <code>items</code> in ascending order.
<code>public static void sort(int[] items, int fromIndex, int toIndex)</code>	Sorts array elements <code>items[fromIndex]</code> to <code>items[toIndex]</code> in ascending order.
<code>public static void sort(Object[] items)</code>	Sorts the objects in array <code>items</code> in ascending order using their natural ordering (defined by method <code>compareTo</code>). All objects in <code>items</code> must implement the <code>Comparable</code> interface and must be mutually comparable.
<code>public static void sort(Object[] items, int fromIndex, int toIndex)</code>	Sorts array elements <code>items[fromIndex]</code> to <code>items[toIndex]</code> in ascending order using their natural ordering (defined by method <code>compareTo</code>). All objects must implement the <code>Comparable</code> interface and must be mutually comparable.
<code>public static <T> void sort(T[] items, Comparator<? super T> comp)</code>	Sorts the objects in <code>items</code> in ascending order as defined by method <code>comp.compare</code> . All objects in <code>items</code> must be mutually comparable using method <code>comp.compare</code> .
<code>public static <T> void sort(T[] items, int fromIndex, int toIndex, Comparator<? super T> comp)</code>	Sorts the objects in <code>items[fromIndex]</code> to <code>items[toIndex]</code> in ascending order as defined by method <code>comp.compare</code> . All objects in <code>items</code> must be mutually comparable using method <code>comp.compare</code> .
Method sort in Class Collections	Behavior
<code>public static <T extends Comparable<T>> void sort(List<T> list)</code>	Sorts the objects in <code>list</code> in ascending order using their natural ordering (defined by method <code>compareTo</code>). All objects in <code>list</code> must implement the <code>Comparable</code> interface and must be mutually comparable.
<code>public static <T> void sort(List<T> list, Comparator<? super T> comp)</code>	Sorts the objects in <code>list</code> in ascending order as defined by method <code>comp.compare</code> . All objects must be mutually comparable.

Generiska metoder

Allmän struktur:

```
modifiers <genericParameters>  
returnType methodName(methodParameters)
```

Två vanliga exempel:

```
public static <T>  
    void sort( T[] items,  
              Comparator<? super T> comp )
```

```
public static <T extends Comparable<T>>  
    void sort( List<T> list )
```

Comparable vs Comparator

Exempel på en komparabel klass:

```
public class Person implements Comparable<Person> {  
    ...  
    public int compareTo(Person other) {  
        return getName().compareTo(other.getName());  
    }  
    ...  
}
```

Exempel på en komparator:

```
public class CompareDate implements Comparator<Person> {  
    public int compare(Person left, Person right) {  
        return left.getBirthDay() - right.getBirthDay();  
    }  
}
```

Insättningssortering

Kursboken, avsnitt 8.4

Baseras på hur man kan sortera en korthand:

- plocka upp ett kort i taget
- stoppa in kortet på sin rätta plats i handen



Trace of Insertion Sort

[0]	30
[1]	25
[2]	15
[3]	20
[4]	28

1. for each array element from the second (`nextPos = 1`) to the last
2. Insert the element at `nextPos` where it belongs in the array, increasing the length of the sorted subarray by 1 element

To adapt the insertion algorithm to an array that is filled with data, we start with a sorted subarray consisting of only the first element

Trace of Insertion Sort (cont.)

nextPos	1
---------	---

[0]	30	
[1]	25	← nextPos
[2]	15	
[3]	20	
[4]	28	

1. for each array element from the second (`nextPos = 1`) to the last
2. Insert the element at `nextPos` where it belongs in the array, increasing the length of the sorted subarray by 1 element

Trace of Insertion Sort (cont.)

nextPos	1
---------	---

[0]	25	
[1]	30	← nextPos
[2]	15	
[3]	20	
[4]	28	

1. for each array element from the second (`nextPos = 1`) to the last
2. Insert the element at `nextPos` where it belongs in the array, increasing the length of the sorted subarray by 1 element

Trace of Insertion Sort (cont.)

nextPos	2
---------	---

1. for each array element from the second (`nextPos = 1`) to the last
2. Insert the element at `nextPos` where it belongs in the array, increasing the length of the sorted subarray by 1 element

[0]	25	
[1]	30	
[2]	15	← nextPos
[3]	20	
[4]	28	

Trace of Insertion Sort (cont.)

nextPos	2
---------	---

1. for each array element from the second (`nextPos = 1`) to the last
2. Insert the element at `nextPos` where it belongs in the array, increasing the length of the sorted subarray by 1 element

[0]	15
[1]	25
[2]	30
[3]	20
[4]	28

← nextPos

Trace of Insertion Sort (cont.)

nextPos	3
---------	---

[0]	15
[1]	25
[2]	30
[3]	20
[4]	28

← nextPos

1. for each array element from the second (`nextPos = 1`) to the last
2. Insert the element at `nextPos` where it belongs in the array, increasing the length of the sorted subarray by 1 element

Trace of Insertion Sort (cont.)

nextPos	3
---------	---

[0]	15
[1]	20
[2]	25
[3]	30
[4]	28

← nextPos

1. for each array element from the second (`nextPos = 1`) to the last
2. Insert the element at `nextPos` where it belongs in the array, increasing the length of the sorted subarray by 1 element

Trace of Insertion Sort (cont.)

nextPos	4
---------	---

[0]	15
[1]	20
[2]	25
[3]	30
[4]	28

← nextPos

1. for each array element from the second (`nextPos = 1`) to the last
2. Insert the element at `nextPos` where it belongs in the array, increasing the length of the sorted subarray by 1 element

Trace of Insertion Sort (cont.)

nextPos	4
---------	---

[0]	15
[1]	20
[2]	25
[3]	28
[4]	30

← nextPos

1. for each array element from the second (`nextPos = 1`) to the last
2. Insert the element at `nextPos` where it belongs in the array, increasing the length of the sorted subarray by 1 element

Trace of Insertion Sort (cont.)

nextPos	-
---------	---

[0]	15
[1]	20
[2]	25
[3]	28
[4]	30

1. for each array element from the second (`nextPos = 1`) to the last
2. Insert the element at `nextPos` where it belongs in the array, increasing the length of the sorted subarray by 1 element

Samma exempel, förfinad version

Den här raden:

Insert the element at nextPos where it belongs
in the array, increasing the length of the sorted
subarray by 1 element

kan förfinas till en while-loop:

nextPos is the position of the element to insert
Save the value of the element to insert in nextVal
while nextPos > 0 and the element at nextPos - 1 > nextVal:
 Shift the element at nextPos - 1 to position nextPos
 Decrement nextPos by 1
Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

[0]	30
[1]	25
[2]	15
[3]	20
[4]	28

1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

nextPos	1
nextVal	

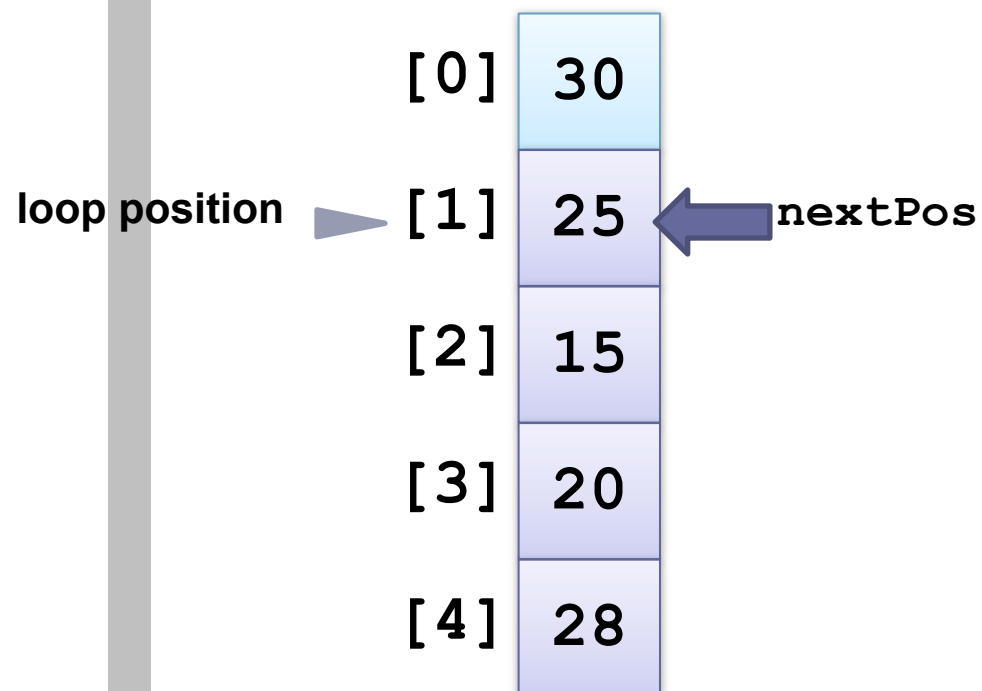
loop position

[0]	30
[1]	25
[2]	15
[3]	20
[4]	28

- ▶ 1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

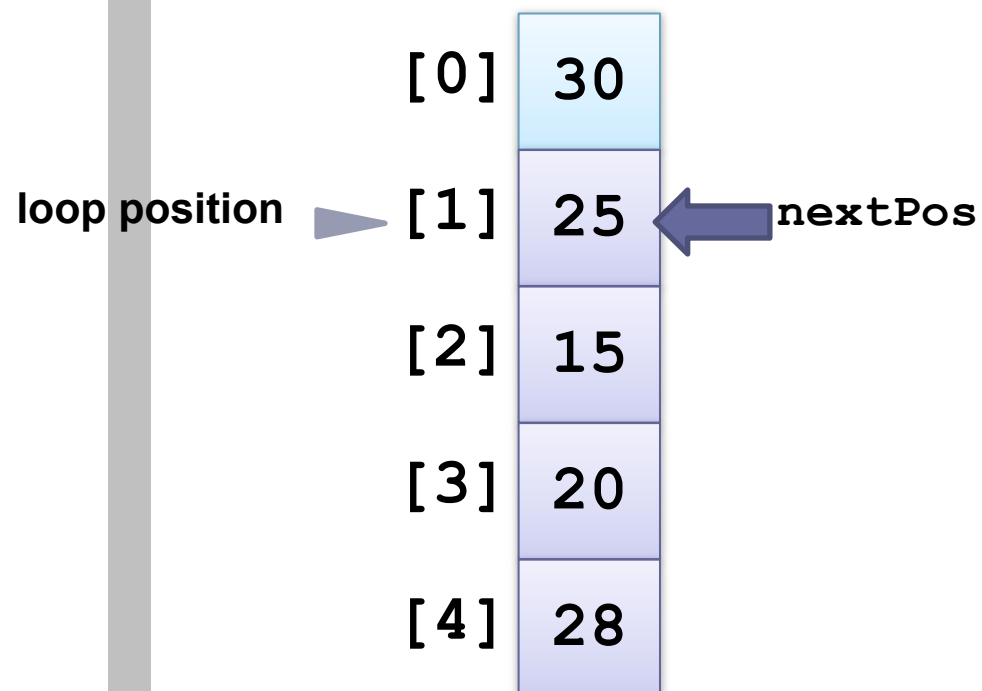
nextPos	1
nextVal	



1. for each array element from the second ($\text{nextPos} = 1$) to the last
- ▶ 2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

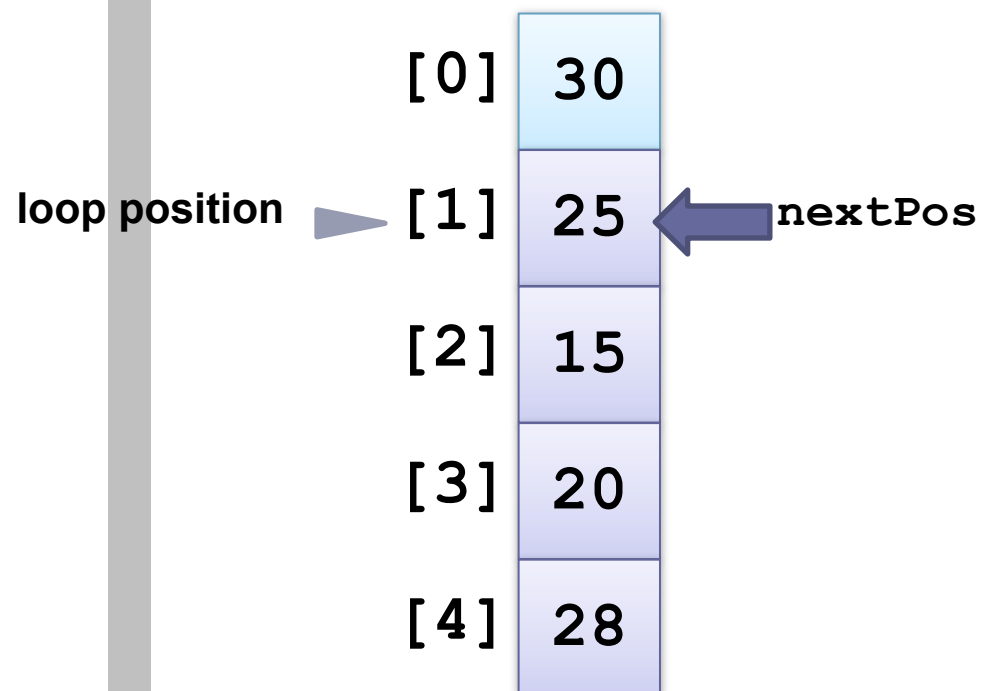
nextPos	1
nextVal	25



1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
- ▶ 3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

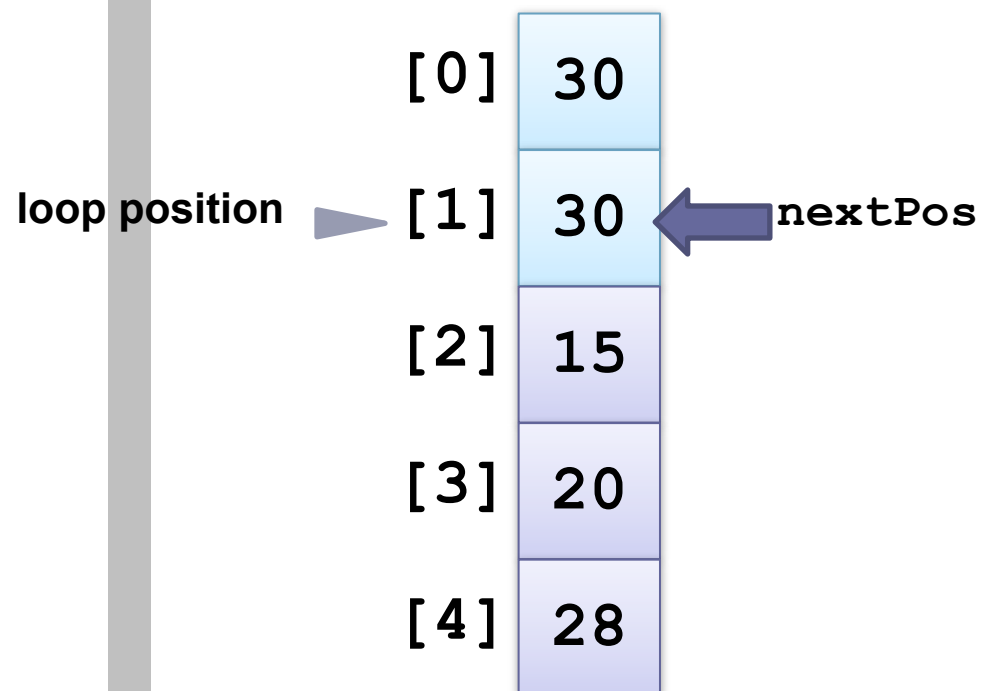
nextPos	1
nextVal	25



1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
-  4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

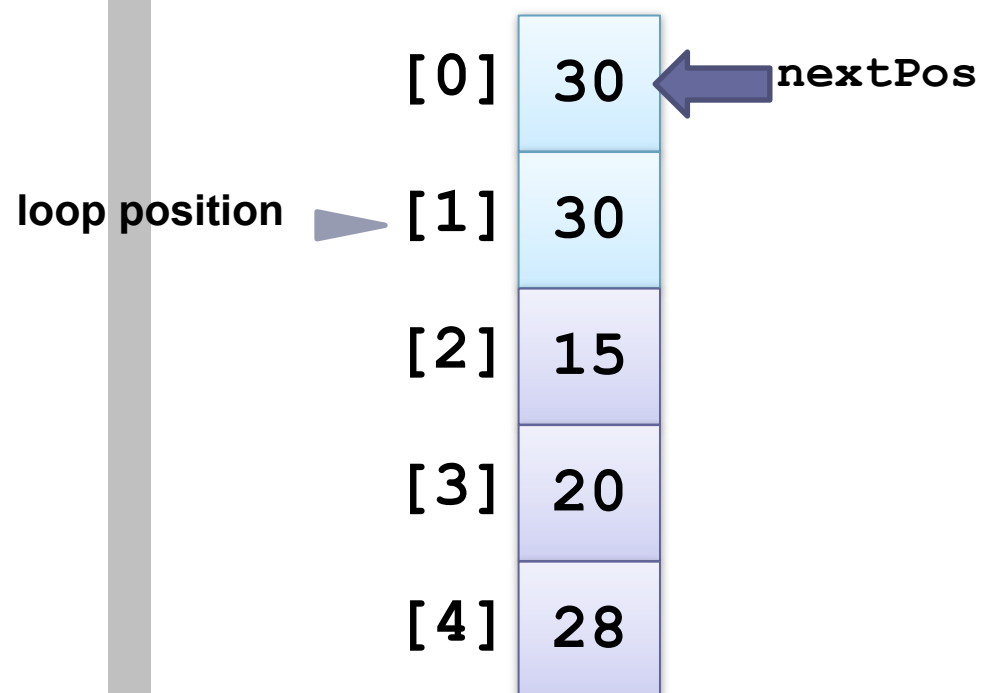
nextPos	1
nextVal	25



1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5.  Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

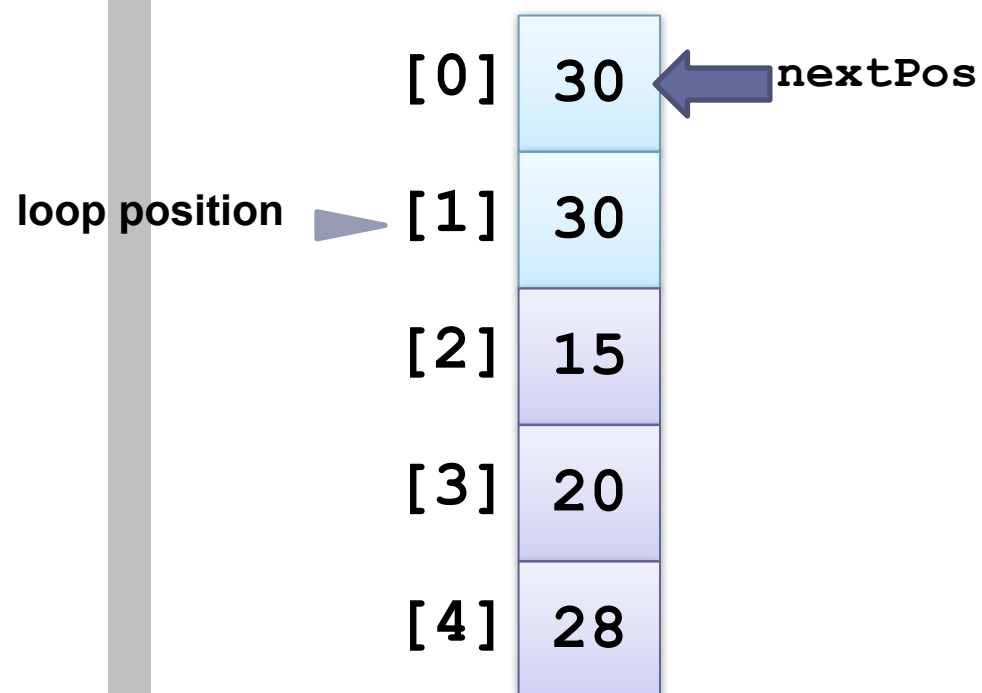
nextPos	0
nextVal	25



1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

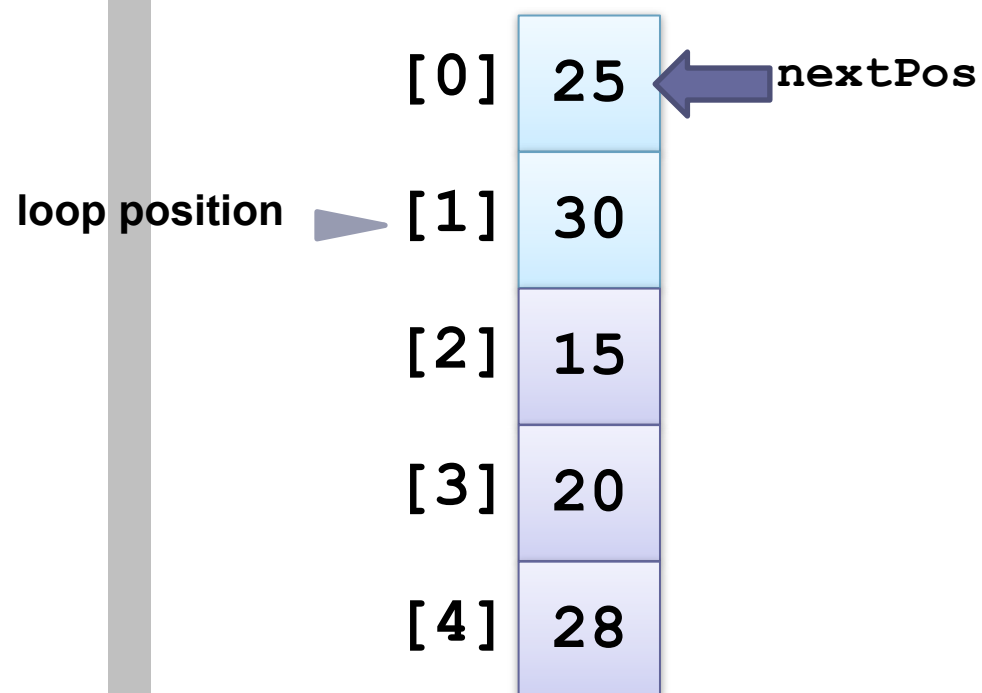
nextPos	0
nextVal	25



1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
-  4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

nextPos	0
nextVal	25



1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

nextPos	0
nextVal	25

loop position

[0]	25
[1]	30
[2]	15
[3]	20
[4]	28

- ▶ 1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

nextPos	2
nextVal	25

	[0]	25	
	[1]	30	
loop position	[2]	15	← nextPos
	[3]	20	
	[4]	28	

1. for each array element from the second ($\text{nextPos} = 1$) to the last
- ▶ 2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

nextPos	2
nextVal	15

	[0]	25	
	[1]	30	
loop position	[2]	15	← nextPos
	[3]	20	
	[4]	28	

1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
- ▶ 3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

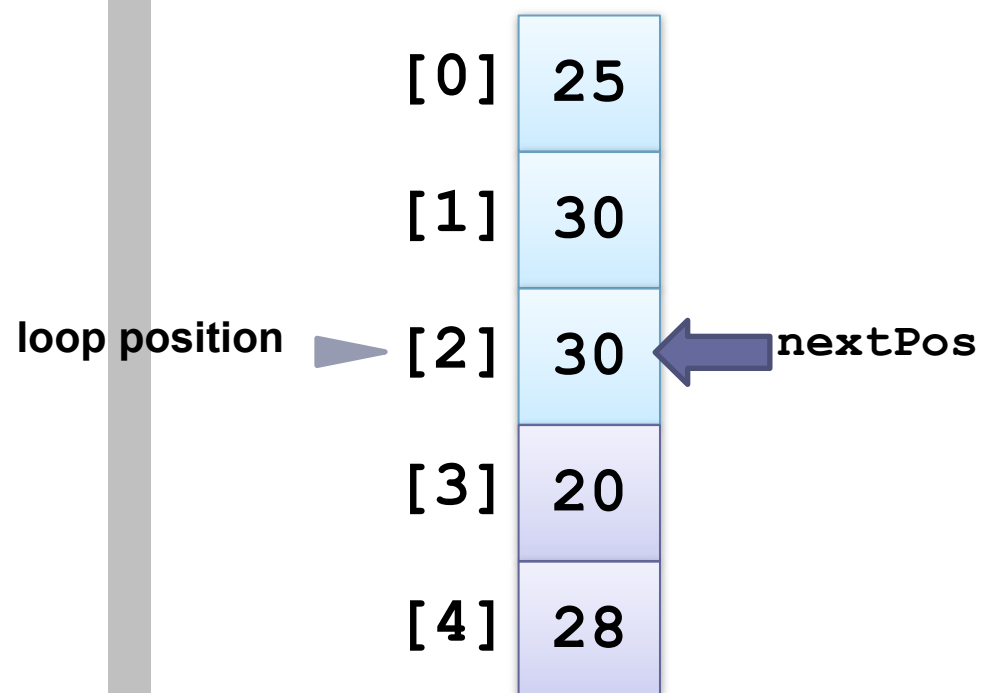
nextPos	2
nextVal	15

	[0]	25	
	[1]	30	
loop position	[2]	15	← nextPos
	[3]	20	
	[4]	28	

1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

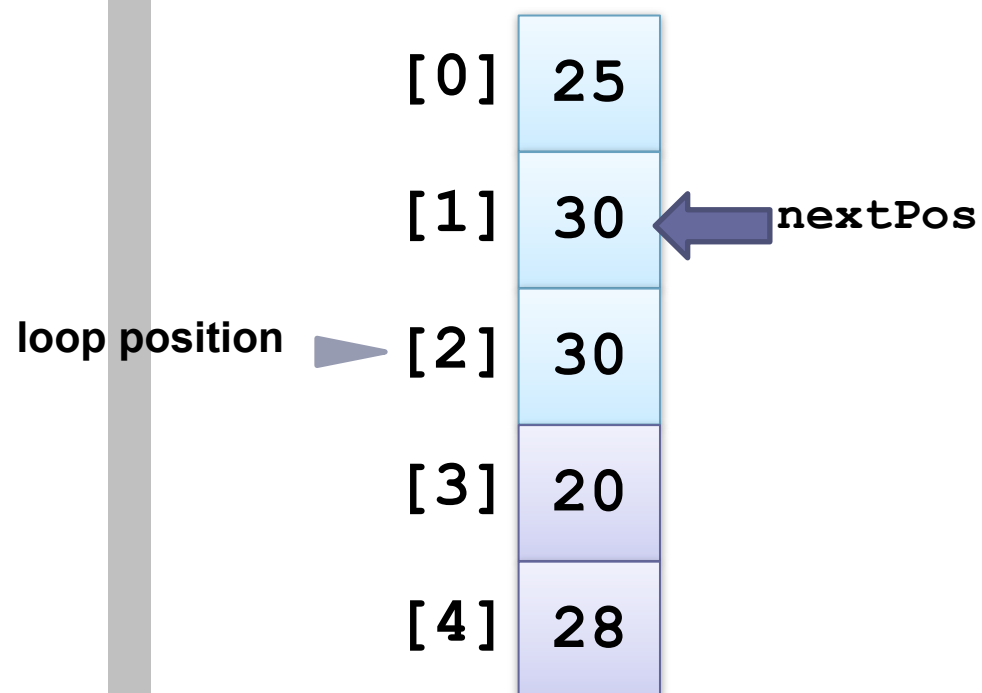
nextPos	2
nextVal	15



1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5.  Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

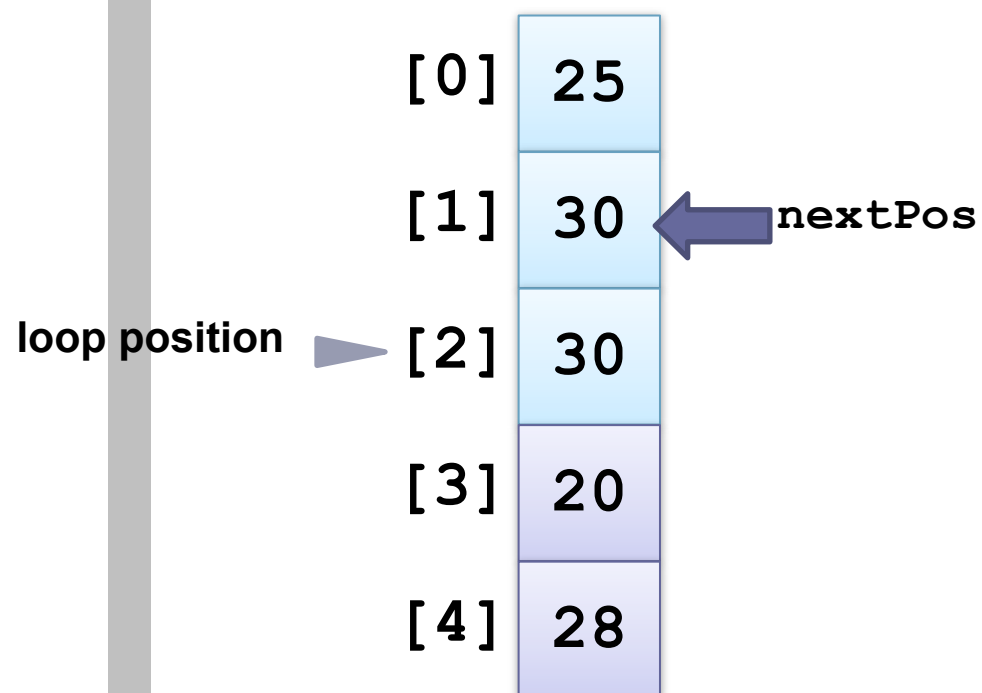
nextPos	1
nextVal	15



1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

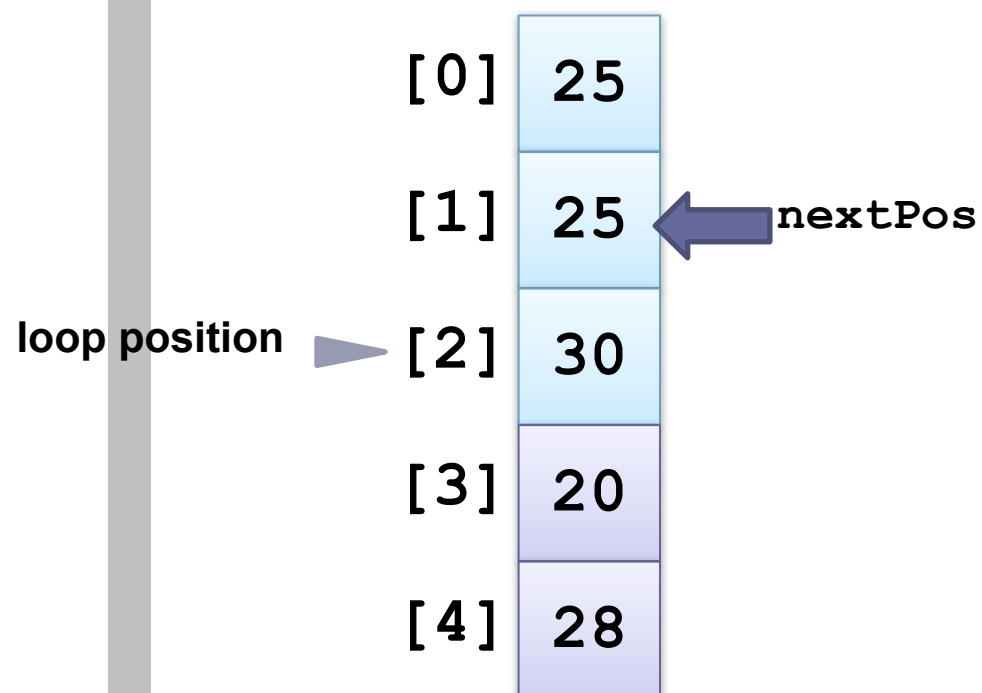
nextPos	1
nextVal	15



1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

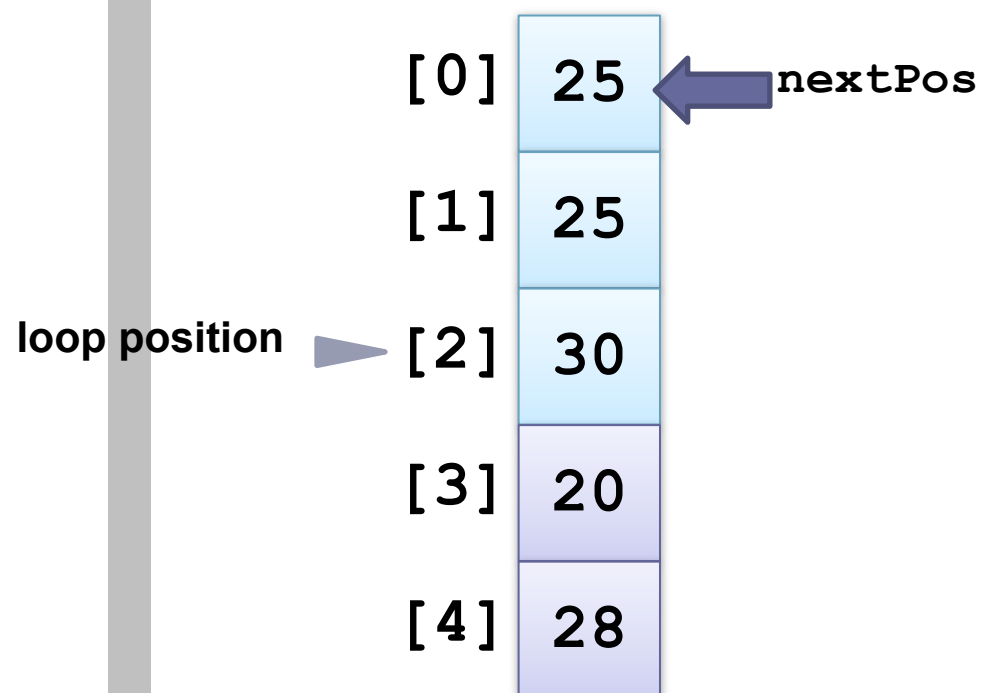
nextPos	1
nextVal	15



1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

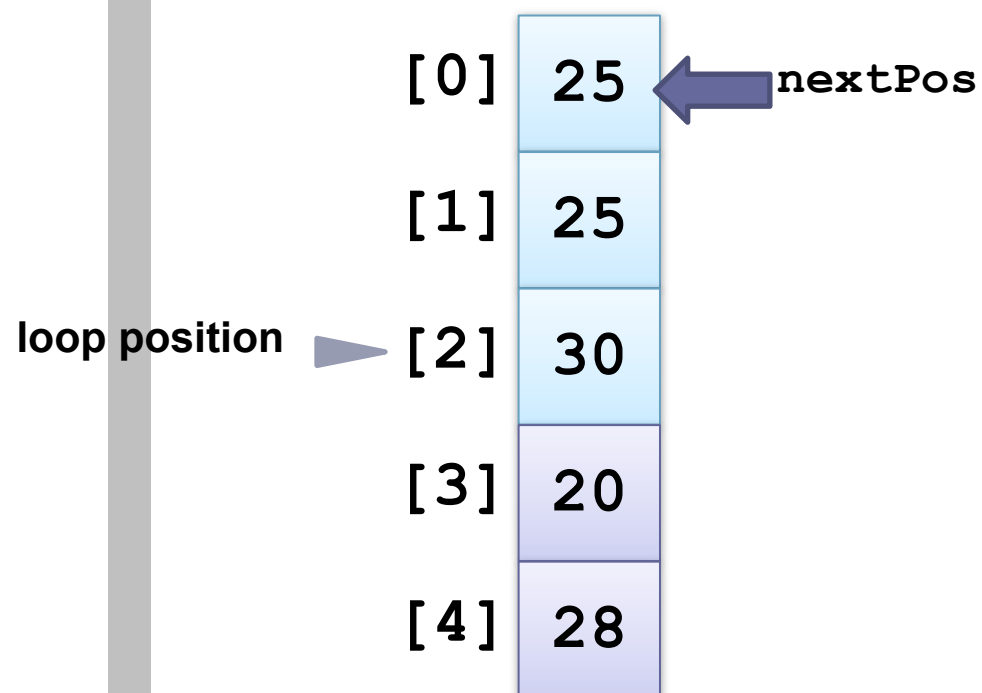
nextPos	0
nextVal	15



1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

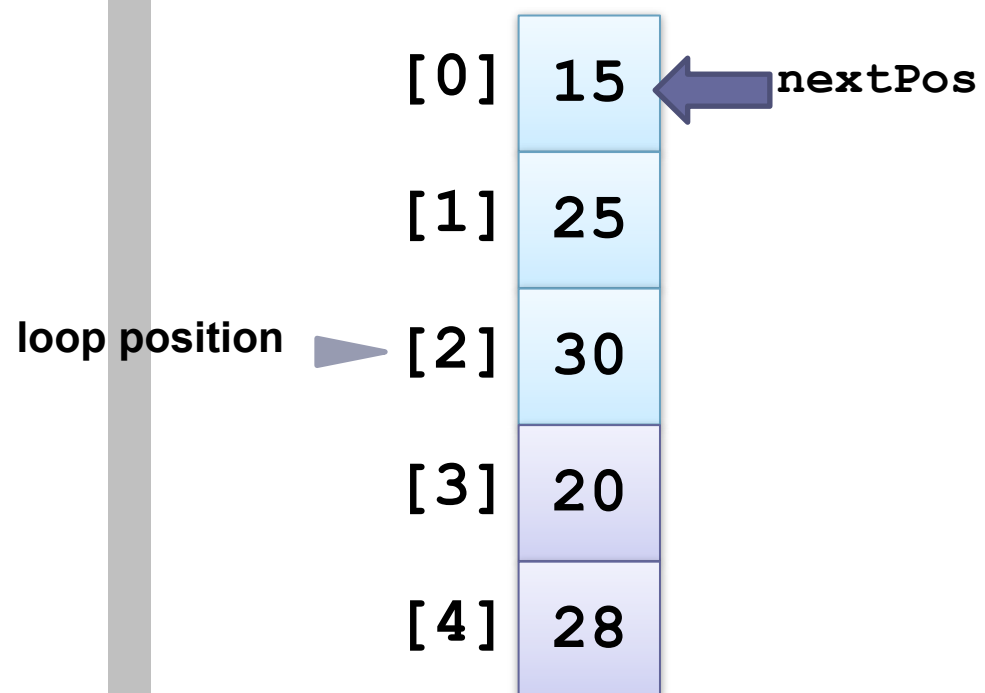
nextPos	0
nextVal	15



1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

nextPos	0
nextVal	15



1. for each array element from the second (`nextPos = 1`) to the last
2. `nextPos` is the position of the element to insert
3. Save the value of the element to insert in `nextVal`
4. while `nextPos > 0` and the element at `nextPos - 1 > nextVal`
5. Shift the element at `nextPos - 1` to position `nextPos`
6. Decrement `nextPos` by 1
7. Insert `nextVal` at `nextPos`

Trace of Insertion Sort Refinement (cont.)

nextPos	0
nextVal	15

[0]	15	← nextPos
[1]	25	
[2]	30	
[3]	20	
[4]	28	

loop position ►

- ▶ 1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

nextPos	3
nextVal	15

	[0]	15	
	[1]	25	
	[2]	30	
loop position	[3]	20	← nextPos
	[4]	28	

1. for each array element from the second ($\text{nextPos} = 1$) to the last
- ▶ 2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

nextPos	3
nextVal	20

	[0]	15	
	[1]	25	
	[2]	30	
loop position	[3]	20	← nextPos
	[4]	28	

1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
- ▶ 3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

nextPos	3
nextVal	20

	[0]	15	
	[1]	25	
	[2]	30	
loop position	[3]	20	← nextPos
	[4]	28	

1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

nextPos	3
nextVal	20

	[0]	15	
	[1]	25	
	[2]	30	
loop position	[3]	30	← nextPos
	[4]	28	

1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

nextPos	2
nextVal	20

	[0]	15	
	[1]	25	
	[2]	30	← nextPos
loop position	[3]	30	▶
	[4]	28	

1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

nextPos	2
nextVal	20

	[0]	15	
	[1]	25	
	[2]	30	← nextPos
loop position	[3]	30	▶
	[4]	28	

1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
- ▶ 4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

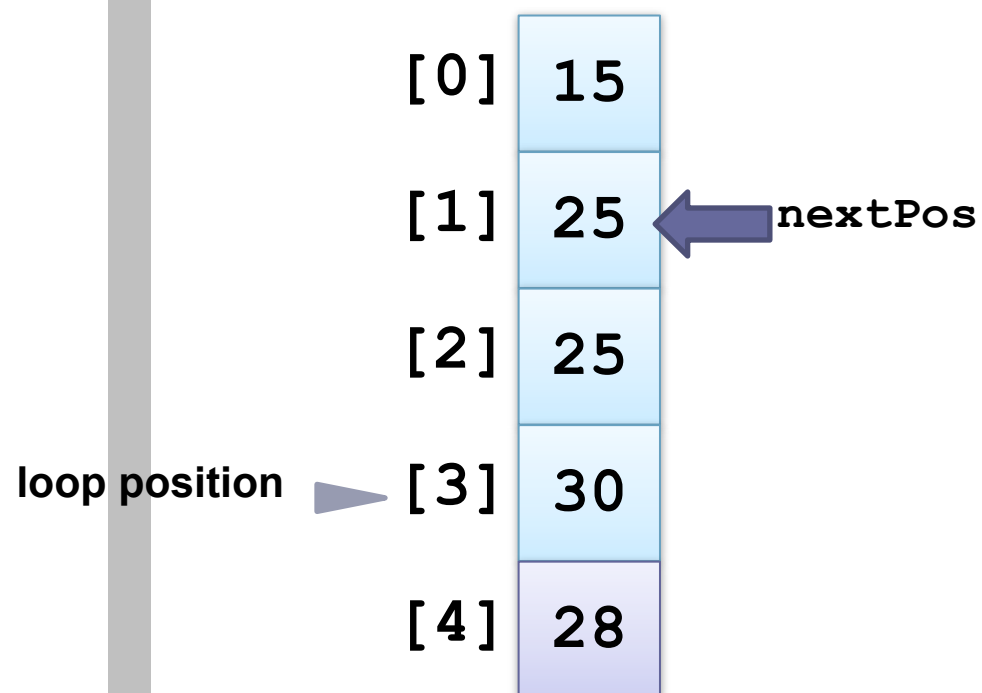
nextPos	2
nextVal	20

	[0]	15	
	[1]	25	
	[2]	25	← nextPos
loop position	[3]	30	▶
	[4]	28	

1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

nextPos	1
nextVal	20



1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

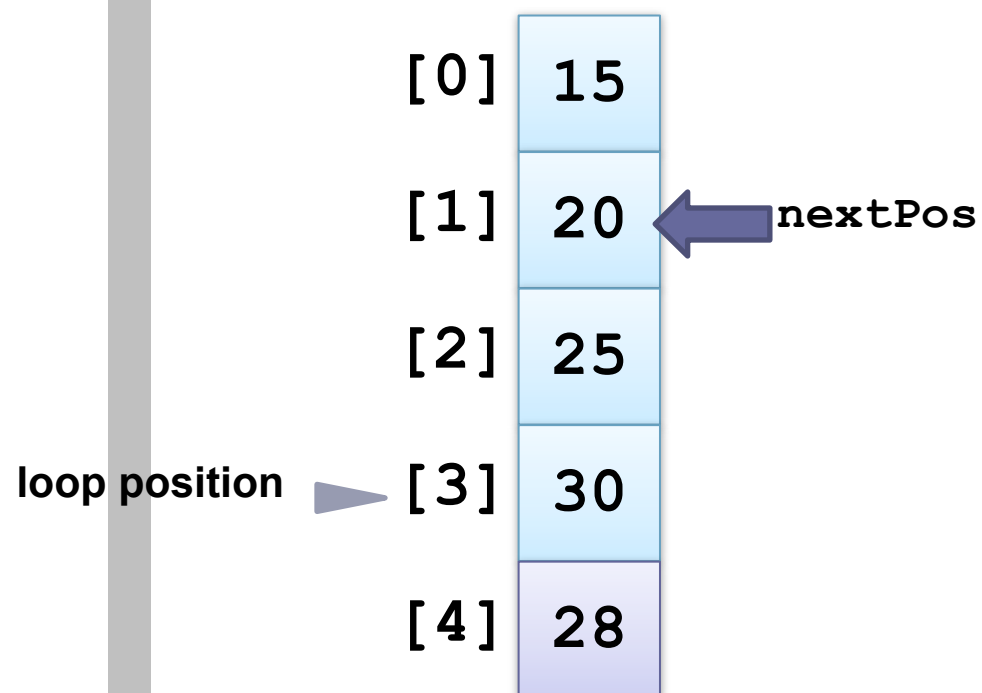
nextPos	1
nextVal	20

[0]	15	
[1]	25	← nextPos
[2]	25	
[3]	30	loop position ▶
[4]	28	

1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
- ▶ 4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

nextPos	1
nextVal	20



1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

nextPos	1
nextVal	20

[0]	15
[1]	20
[2]	25
[3]	30
[4]	28

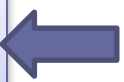
loop position

- ▶ 1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

nextPos	4
nextVal	20

[0]	15
[1]	20
[2]	25
[3]	30
[4]	28

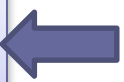
loop position   nextPos

1. for each array element from the second ($\text{nextPos} = 1$) to the last
- ▶ 2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

nextPos	4
nextVal	28

[0]	15
[1]	20
[2]	25
[3]	30
[4]	28

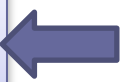
loop position   nextPos

1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
- ▶ 3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

nextPos	4
nextVal	28

[0]	15
[1]	20
[2]	25
[3]	30
[4]	28

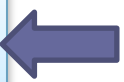
loop position   nextPos

1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

nextPos	4
nextVal	28

[0]	15
[1]	20
[2]	25
[3]	30
[4]	30

loop position   nextPos

1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5.  Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

nextPos	3
nextVal	28

[0]	15
[1]	20
[2]	25
[3]	30
[4]	30

← nextPos

loop position ►

1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

nextPos	3
nextVal	28

[0]	15
[1]	20
[2]	25
[3]	30
[4]	30

← nextPos

loop position ►

1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

nextPos	3
nextVal	28

[0]	15
[1]	20
[2]	25
[3]	28
[4]	30

← nextPos

loop position ►

1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Trace of Insertion Sort Refinement (cont.)

nextPos	3
nextVal	28

[0]	15
[1]	20
[2]	25
[3]	28
[4]	30

1. for each array element from the second ($\text{nextPos} = 1$) to the last
2. nextPos is the position of the element to insert
3. Save the value of the element to insert in nextVal
4. while $\text{nextPos} > 0$ and the element at $\text{nextPos} - 1 > \text{nextVal}$
5. Shift the element at $\text{nextPos} - 1$ to position nextPos
6. Decrement nextPos by 1
7. Insert nextVal at nextPos

Komplexitetsanalys

Två nästade loopar
som varje är $O(n)$

 komplexiteten är
alltså kvadratisk,
 $O(n^2)$

1. **for each array element from the second (`nextPos = 1`) to the last**
2. **`nextPos` is the position of the element to insert**
3. **Save the value of the element to insert in `nextVal`**
4. **while `nextPos > 0` and the element at `nextPos-1 > nextVal`**
5. **Shift the element at `nextPos-1` to position `nextPos`**
6. **Decrement `nextPos` by 1**
7. **Insert `nextVal` at `nextPos`**

Urvalssortering

Kursboken, avsnitt 8.2

Algoritmen är väldigt lik insättningsortering, fast "tvärtom":

- leta upp det minsta elementet
- lägg till det i slutet av den nya listan
- fortsätt tills den gamla listan är tom

Urvalssortering, exempel

n = number of elements in the array

- 1. for $fill = 0$ to $n - 2$ do**
- 2. Set $posMin$ to the subscript of a smallest item in the subarray starting at subscript $fill$**
- 3. Exchange the item at $posMin$ with the one at $fill$**

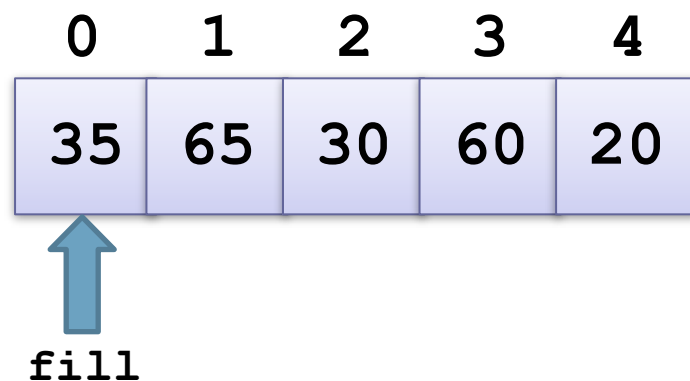
0	1	2	3	4
35	65	30	60	20

n	5
$fill$	
$posMin$	

Urvalssortering, exempel

n = number of elements in the array

- ▶ 1. for $fill = 0$ to $n - 2$ do
2. Set $posMin$ to the subscript of a smallest item in the subarray starting at subscript $fill$
3. Exchange the item at $posMin$ with the one at $fill$

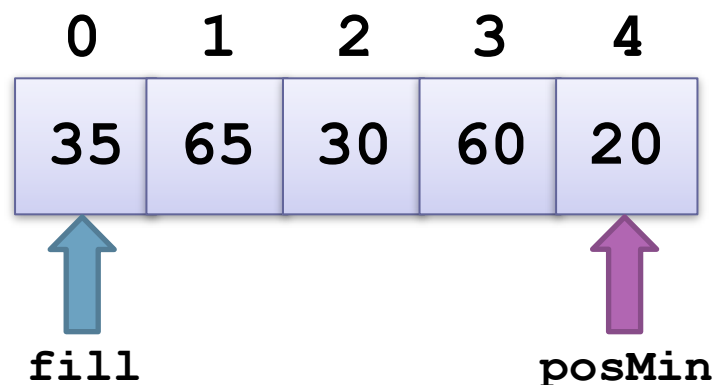


n	5
fill	0
posMin	

Urvalssortering, exempel

n = number of elements in the array

1. for $fill = 0$ to $n - 2$ do
2. Set $posMin$ to the subscript of a smallest item in the subarray starting at subscript $fill$
3. Exchange the item at $posMin$ with the one at $fill$

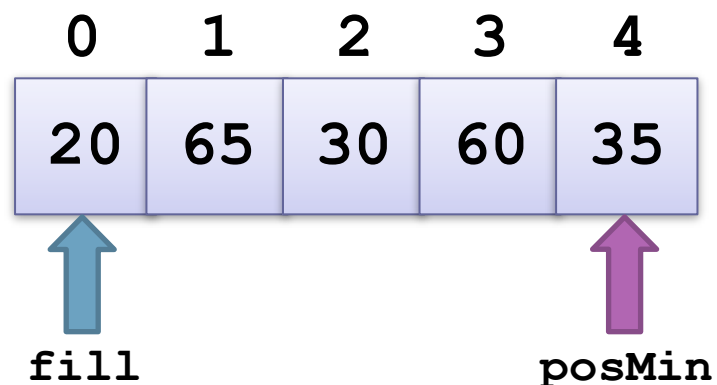


n	5
$fill$	0
$posMin$	4

Urvalssortering, exempel

n = number of elements in the array

1. **for** $fill = 0$ to $n - 2$ **do**
2. Set $posMin$ to the subscript of a smallest item in the subarray starting at subscript $fill$
- ▶ 3. Exchange the item at $posMin$ with the one at $fill$

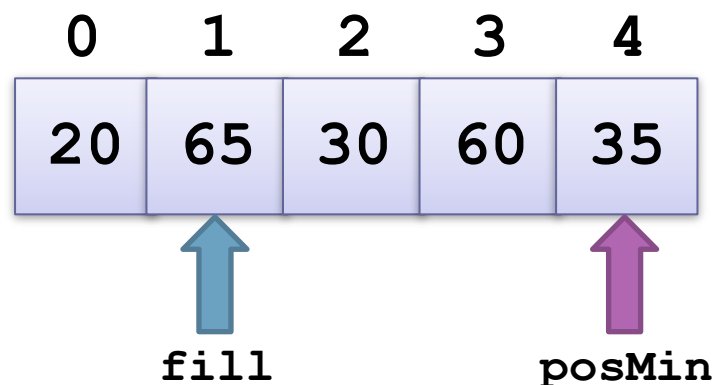


n	5
$fill$	0
$posMin$	4

Urvalssortering, exempel

n = number of elements in the array

- ▶ 1. for $fill = 0$ to $n - 2$ do
2. Set $posMin$ to the subscript of a smallest item in the subarray starting at subscript $fill$
3. Exchange the item at $posMin$ with the one at $fill$

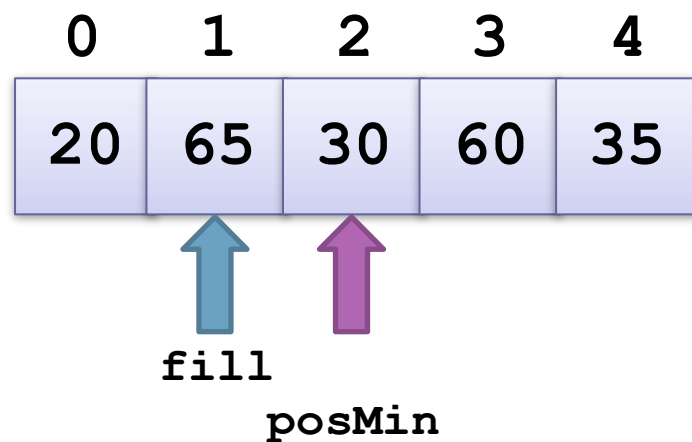


n	5
$fill$	1
$posMin$	4

Urvalssortering, exempel

n = number of elements in the array

1. for $fill = 0$ to $n - 2$ do
- ▶ 2. Set $posMin$ to the subscript of a smallest item in the subarray starting at subscript $fill$
3. Exchange the item at $posMin$ with the one at $fill$

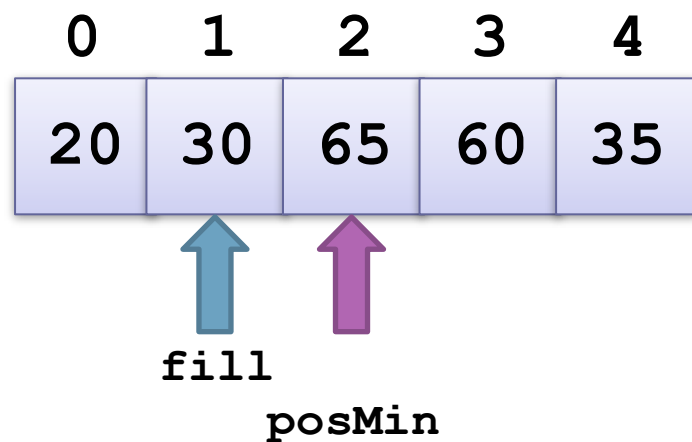


n	5
fill	1
posMin	2

Urvalssortering, exempel

n = number of elements in the array

1. **for** $fill = 0$ to $n - 2$ **do**
2. Set $posMin$ to the subscript of a smallest item in the subarray starting at subscript $fill$
- ▶ 3. Exchange the item at $posMin$ with the one at $fill$

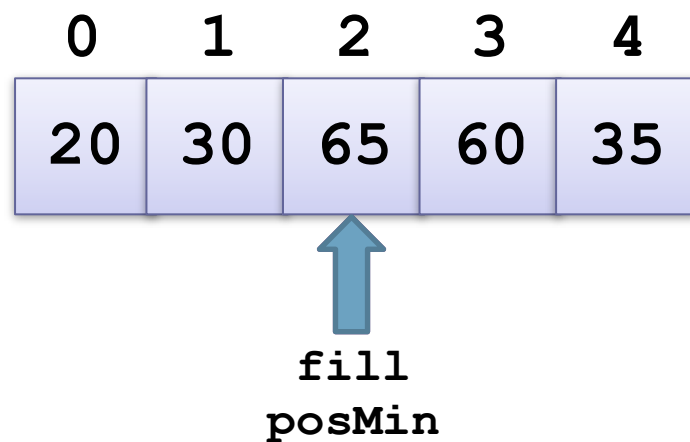


n	5
$fill$	1
$posMin$	2

Urvalssortering, exempel

n = number of elements in the array

1. **for** $fill = 0$ to $n - 2$ **do**
2. Set $posMin$ to the subscript of a smallest item in the subarray starting at subscript $fill$
3. Exchange the item at $posMin$ with the one at $fill$

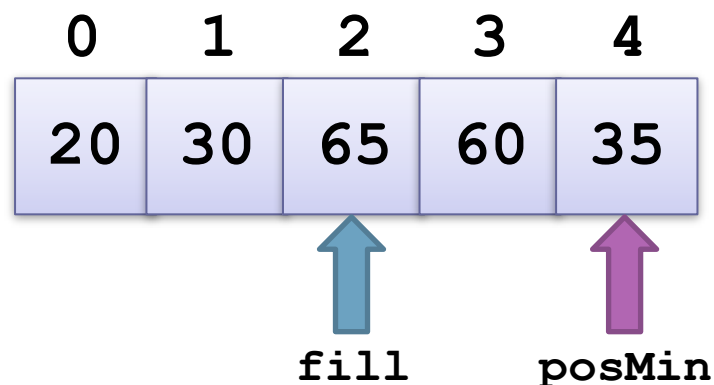


n	5
$fill$	2
$posMin$	2

Urvalssortering, exempel

n = number of elements in the array

1. for $fill = 0$ to $n - 2$ do
- ▶ 2. Set $posMin$ to the subscript of a smallest item in the subarray starting at subscript $fill$
3. Exchange the item at $posMin$ with the one at $fill$



n	5
$fill$	2
$posMin$	4

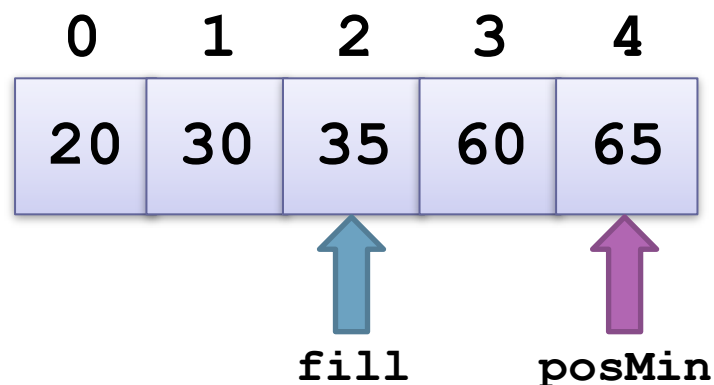
Urvalssortering, exempel

n = number of elements in the array

1. for $fill = 0$ to $n - 2$ do

2. Set $posMin$ to the subscript of a smallest item in the subarray starting at subscript $fill$

▶ 3. Exchange the item at $posMin$ with the one at $fill$

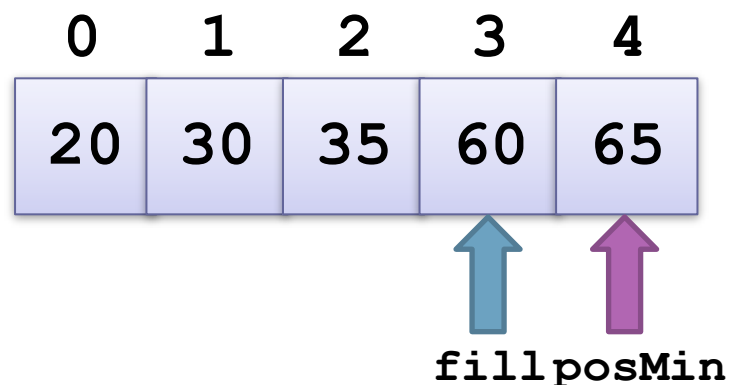


n	5
fill	2
posMin	4

Urvalssortering, exempel

n = number of elements in the array

- ▶ 1. for $fill = 0$ to $n - 2$ do
2. Set $posMin$ to the subscript of a smallest item in the subarray starting at subscript $fill$
3. Exchange the item at $posMin$ with the one at $fill$

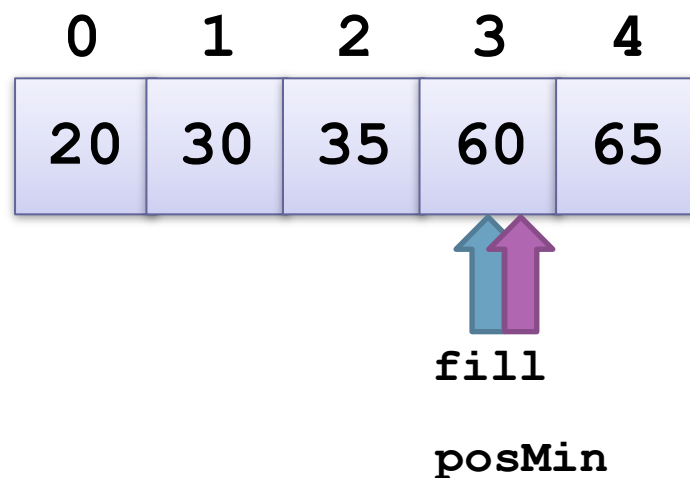


n	5
fill	3
posMin	4

Urvalssortering, exempel

n = number of elements in the array

1. for $fill = 0$ to $n - 2$ do
- ▶ 2. Set $posMin$ to the subscript of a smallest item in the subarray starting at subscript $fill$
3. Exchange the item at $posMin$ with the one at $fill$

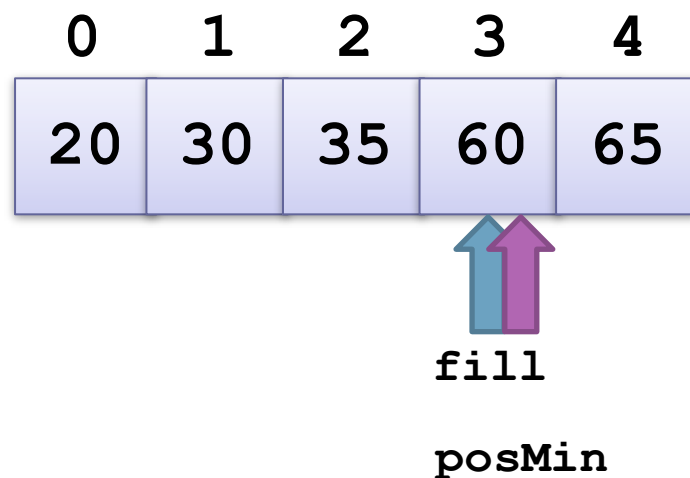


n	5
$fill$	3
$posMin$	3

Urvalssortering, exempel

n = number of elements in the array

1. for $fill = 0$ to $n - 2$ do
2. Set $posMin$ to the subscript of a smallest item in the subarray starting at subscript $fill$
3. Exchange the item at $posMin$ with the one at $fill$



n	5
$fill$	3
$posMin$	3

Urvalssortering, exempel

n = number of elements in the array

1. **for** *fill* = 0 to *n* - 2 **do**
2. Set *posMin* to the subscript of a smallest item in the subarray starting at subscript *fill*
3. Exchange the item at *posMin* with the one at *fill*

0	1	2	3	4
20	30	35	60	65

<i>n</i>	5
<i>fill</i>	3
<i>posMin</i>	3

Samma exempel, förfinad version

Den här raden:

Set posMin to the subscript of a smallest item
in the subarray starting at subscript fill

kan förfinas till en for-loop:

Initialize posMin to fill

for next = fill + 1 to n - 1 do:

if the item at next is less than the item at posMin:

Reset posMin to next

Trace of Selection Sort Refinement (cont.)

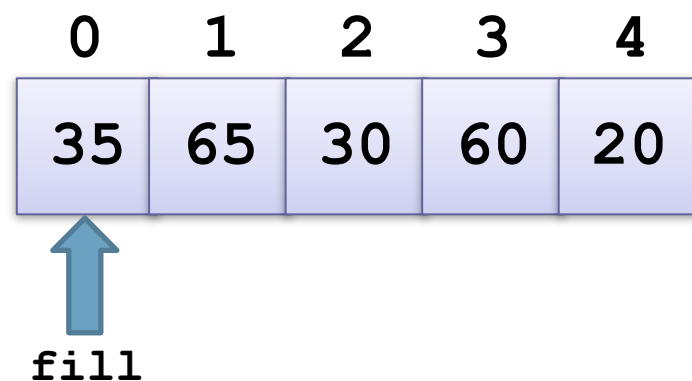
n	5
fill	
posMin	
next	

0	1	2	3	4
35	65	30	60	20

1. **for** fill = 0 to n - 2 **do**
2. **Initialize** posMin to fill
3. **for** next = fill + 1 to n - 1 **do**
4. **if** the item at next is less than the
 item at posMin
5. **Reset** posMin to next
6. **Exchange** the item at posMin with the
 one at fill

Trace of Selection Sort Refinement (cont.)

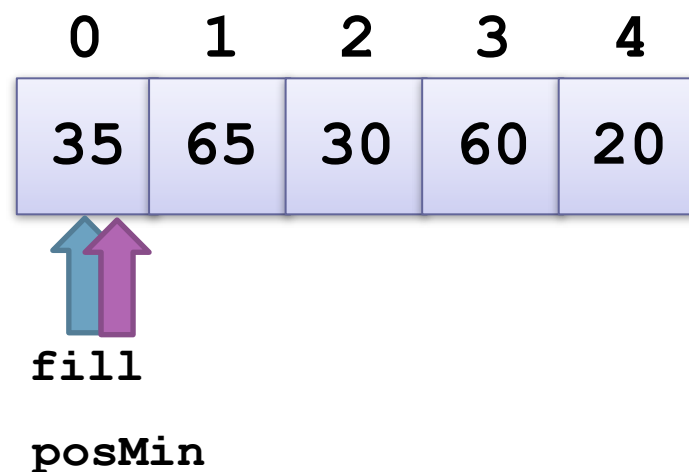
n	5
fill	0
posMin	
next	



- ▶ 1. for $fill = 0$ to $n - 2$ do
- 2. Initialize $posMin$ to $fill$
- 3. for $next = fill + 1$ to $n - 1$ do
- 4. if the item at $next$ is less than the item at $posMin$
- 5. Reset $posMin$ to $next$
- 6. Exchange the item at $posMin$ with the one at $fill$

Trace of Selection Sort Refinement (cont.)

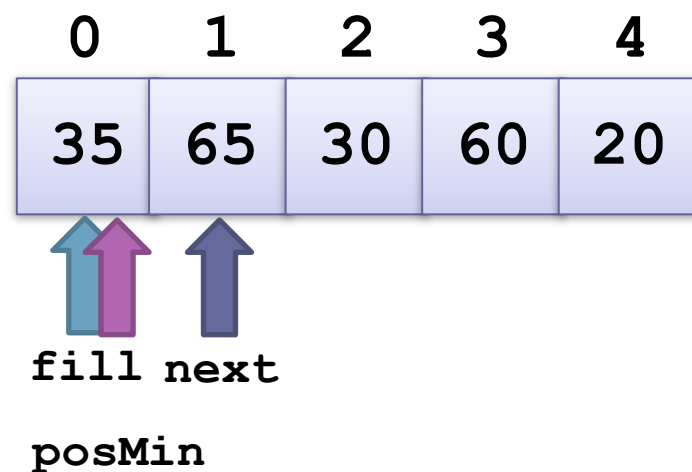
n	5
fill	0
posMin	0
next	



1. `for fill = 0 to n - 2 do`
- ▶ 2. Initialize `posMin` to `fill`
3. `for next = fill + 1 to n - 1 do`
4. **if the item at `next` is less than the item at `posMin`**
5. **Reset `posMin` to `next`**
6. **Exchange the item at `posMin` with the one at `fill`**

Trace of Selection Sort Refinement (cont.)

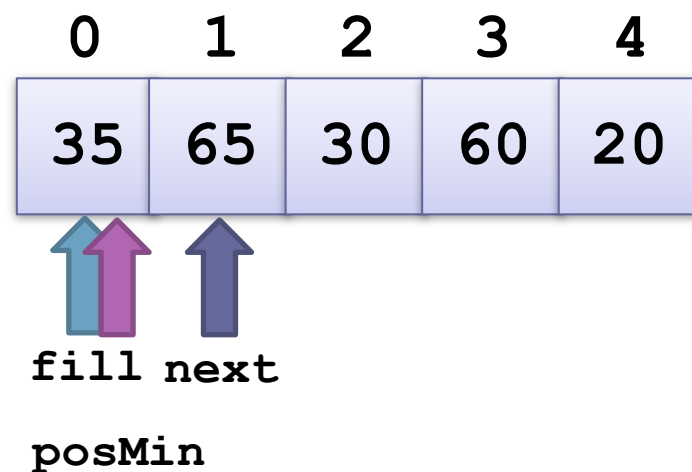
n	5
fill	0
posMin	0
next	1



1. for $fill = 0$ to $n - 2$ do
2. Initialize **posMin** to **fill**
- ▶ 3. for $next = fill + 1$ to $n - 1$ do
4. if the item at **next** is less than the item at **posMin**
5. Reset **posMin** to **next**
6. Exchange the item at **posMin** with the one at **fill**

Trace of Selection Sort Refinement (cont.)

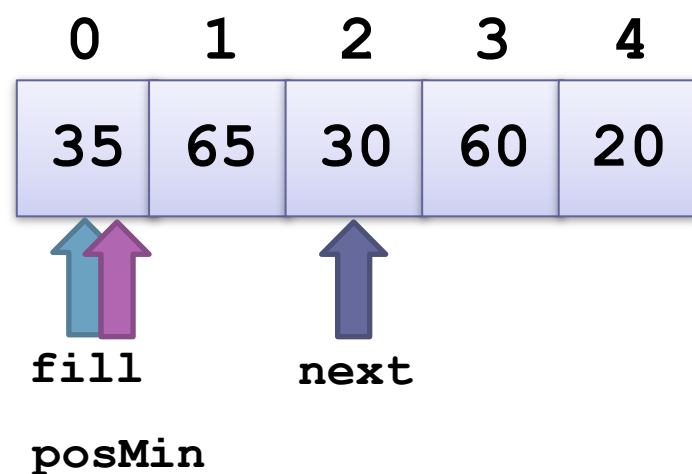
n	5
fill	0
posMin	0
next	1



1. **for** fill = 0 to n - 2 **do**
2. **Initialize** posMin to fill
3. **for** next = fill + 1 to n - 1 **do**
4. **if** the item at next is less than the item at posMin
5. **Reset** posMin to next
6. **Exchange** the item at posMin with the one at fill

Trace of Selection Sort Refinement (cont.)

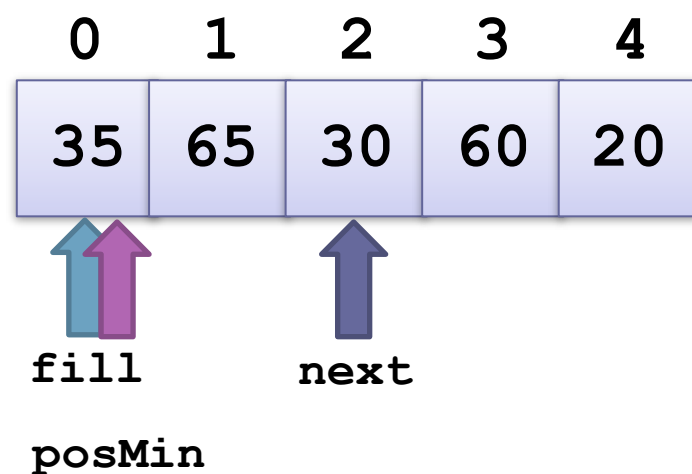
n	5
fill	0
posMin	0
next	2



1. for $fill = 0$ to $n - 2$ do
2. Initialize **posMin** to **fill**
- ▶ 3. for $next = fill + 1$ to $n - 1$ do
4. if the item at **next** is less than the item at **posMin**
5. Reset **posMin** to **next**
6. Exchange the item at **posMin** with the one at **fill**

Trace of Selection Sort Refinement (cont.)

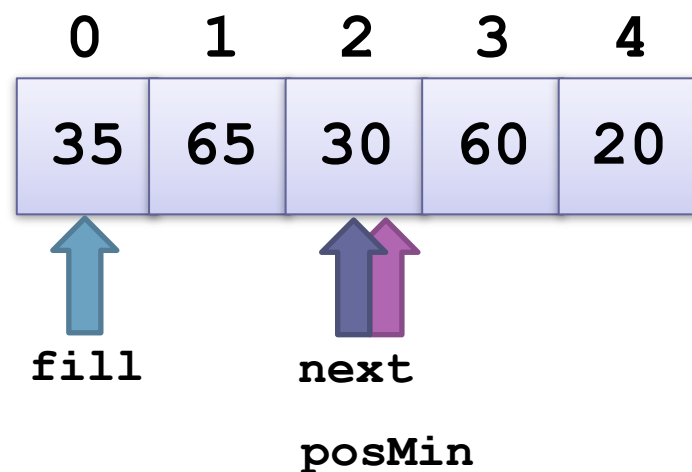
n	5
fill	0
posMin	0
next	2



1. **for** fill = 0 to n - 2 **do**
2. **Initialize** posMin to fill
3. **for** next = fill + 1 to n - 1 **do**
4. **if** the item at next is less than the item at posMin
5. **Reset** posMin to next
6. **Exchange** the item at posMin with the one at fill

Trace of Selection Sort Refinement (cont.)

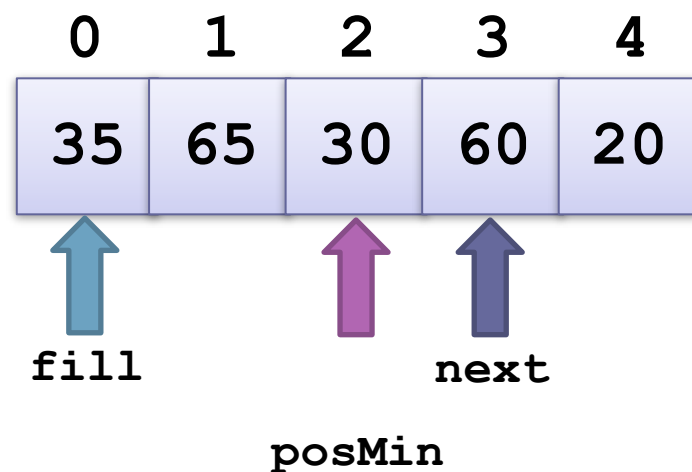
n	5
fill	0
posMin	2
next	2



1. **for** `fill = 0` to `n - 2` **do**
2. **Initialize** `posMin` to `fill`
3. **for** `next = fill + 1` to `n - 1` **do**
4. **if** the item at `next` is less than the item at `posMin`
5. **Reset** `posMin` to `next`
6. **Exchange** the item at `posMin` with the one at `fill`

Trace of Selection Sort Refinement (cont.)

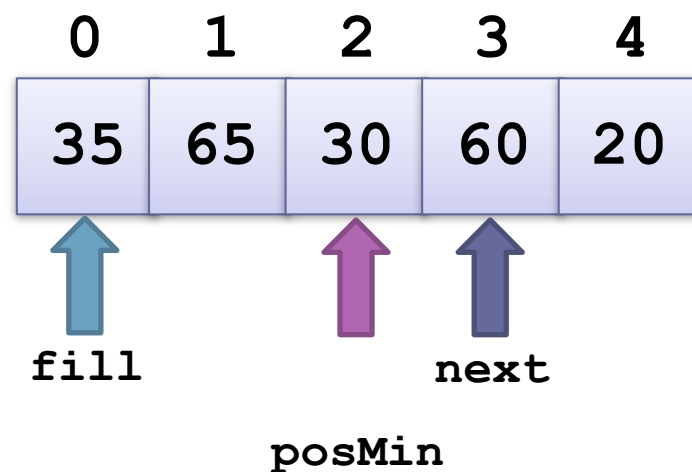
n	5
fill	0
posMin	2
next	3



1. for $fill = 0$ to $n - 2$ do
2. Initialize $posMin$ to $fill$
- ▶ 3. for $next = fill + 1$ to $n - 1$ do
4. if the item at $next$ is less than the item at $posMin$
5. Reset $posMin$ to $next$
6. Exchange the item at $posMin$ with the one at $fill$

Trace of Selection Sort Refinement (cont.)

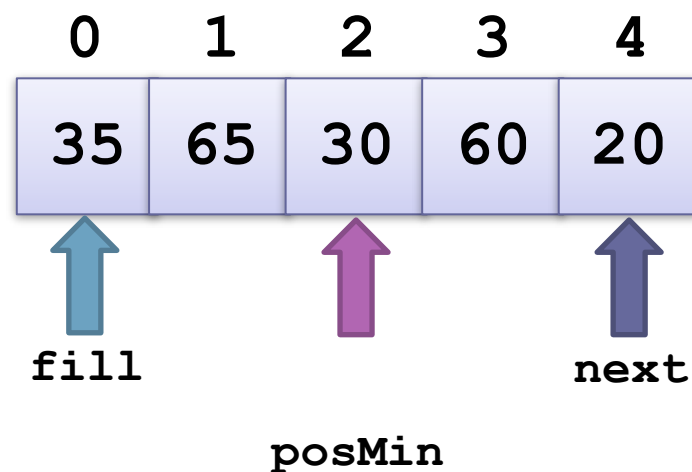
n	5
fill	0
posMin	2
next	3



1. for $fill = 0$ to $n - 2$ do
2. Initialize $posMin$ to $fill$
3. for $next = fill + 1$ to $n - 1$ do
4. if the item at $next$ is less than the item at $posMin$
5. Reset $posMin$ to $next$
6. Exchange the item at $posMin$ with the one at $fill$

Trace of Selection Sort Refinement (cont.)

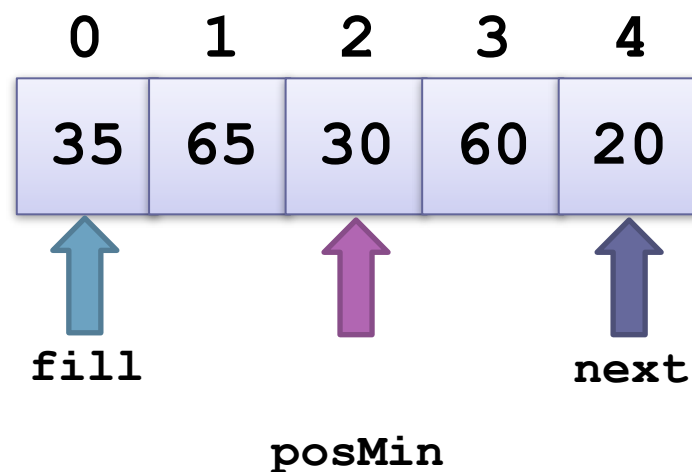
n	5
fill	0
posMin	2
next	4



1. for $fill = 0$ to $n - 2$ do
2. Initialize $posMin$ to $fill$
- ▶ 3. for $next = fill + 1$ to $n - 1$ do
4. if the item at $next$ is less than the item at $posMin$
5. Reset $posMin$ to $next$
6. Exchange the item at $posMin$ with the one at $fill$

Trace of Selection Sort Refinement (cont.)

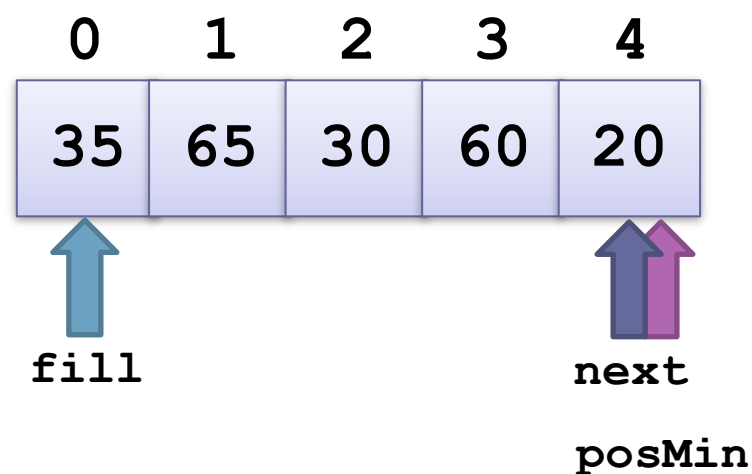
n	5
fill	0
posMin	2
next	4



1. for $fill = 0$ to $n - 2$ do
2. Initialize `posMin` to `fill`
3. for $next = fill + 1$ to $n - 1$ do
4. if the item at `next` is less than the item at `posMin`
5. Reset `posMin` to `next`
6. Exchange the item at `posMin` with the one at `fill`

Trace of Selection Sort Refinement (cont.)

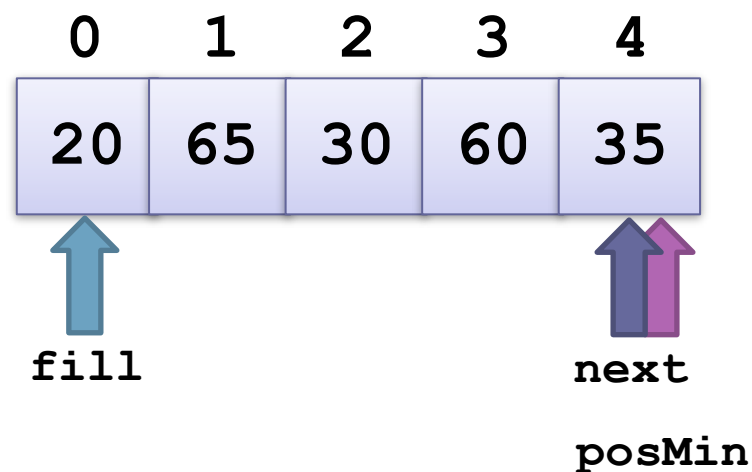
n	5
fill	0
posMin	4
next	4



1. `for fill = 0 to n - 2 do`
2. Initialize `posMin` to `fill`
3. `for next = fill + 1 to n - 1 do`
4. if the item at `next` is less than the item at `posMin`
5. Reset `posMin` to `next`
6. Exchange the item at `posMin` with the one at `fill`

Trace of Selection Sort Refinement (cont.)

n	5
fill	0
posMin	4
next	4

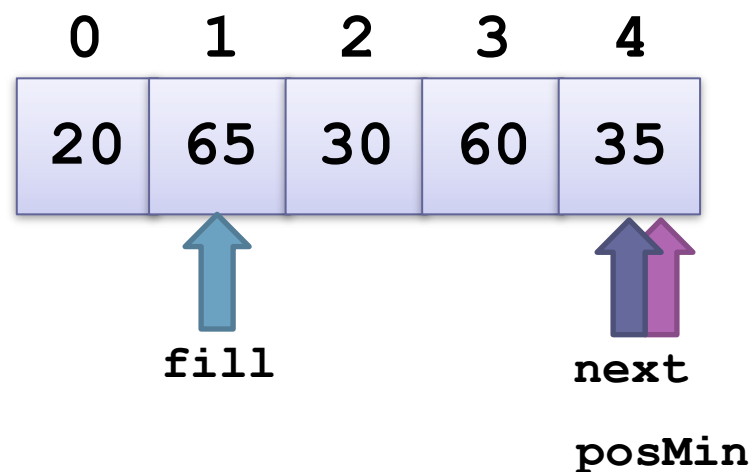


1. for $fill = 0$ to $n - 2$ do
2. Initialize $posMin$ to $fill$
3. for $next = fill + 1$ to $n - 1$ do
4. if the item at $next$ is less than the item at $posMin$
5. Reset $posMin$ to $next$
6. Exchange the item at $posMin$ with the one at $fill$

Trace of Selection Sort Refinement (cont.)

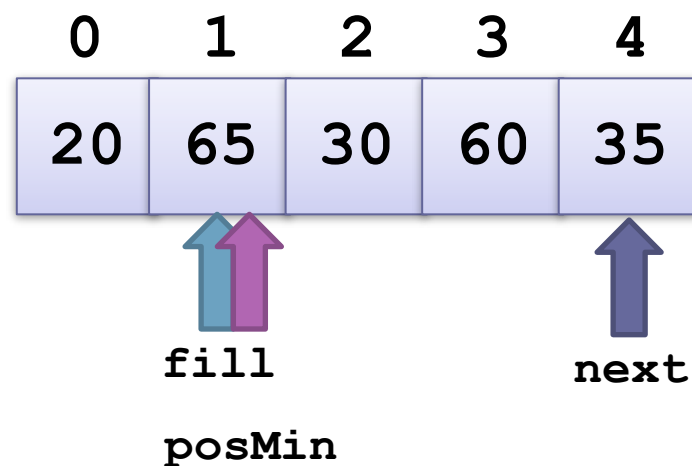
n	5
fill	1
posMin	4
next	4

- ▶ 1. for $fill = 0$ to $n - 2$ do
- 2. Initialize `posMin` to `fill`
- 3. for $next = fill + 1$ to $n - 1$ do
- 4. if the item at `next` is less than the item at `posMin`
- 5. Reset `posMin` to `next`
- 6. Exchange the item at `posMin` with the one at `fill`



Trace of Selection Sort Refinement (cont.)

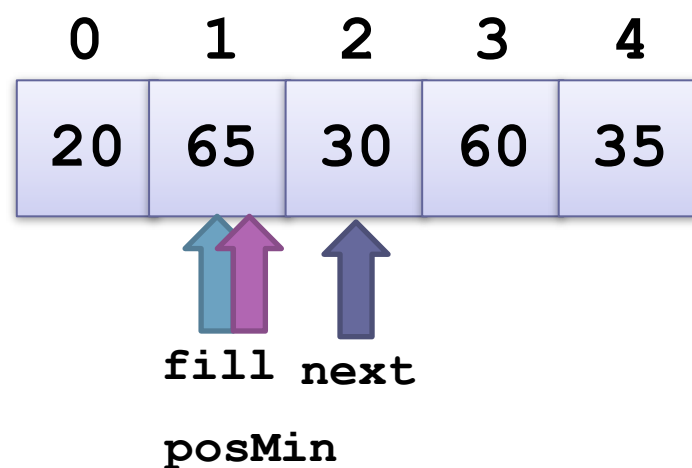
n	5
fill	1
posMin	1
next	4



1. for `fill = 0` to `n - 2` do
- ▶ 2. Initialize `posMin` to `fill`
3. for `next = fill + 1` to `n - 1` do
4. if the item at `next` is less than the item at `posMin`
5. Reset `posMin` to `next`
6. Exchange the item at `posMin` with the one at `fill`

Trace of Selection Sort Refinement (cont.)

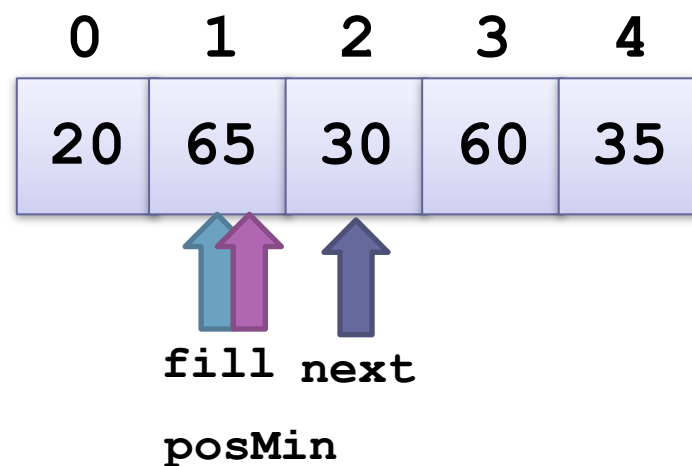
n	5
fill	1
posMin	1
next	2



1. for $fill = 0$ to $n - 2$ do
2. Initialize $posMin$ to $fill$
- ▶ 3. for $next = fill + 1$ to $n - 1$ do
4. if the item at $next$ is less than the item at $posMin$
5. Reset $posMin$ to $next$
6. Exchange the item at $posMin$ with the one at $fill$

Trace of Selection Sort Refinement (cont.)

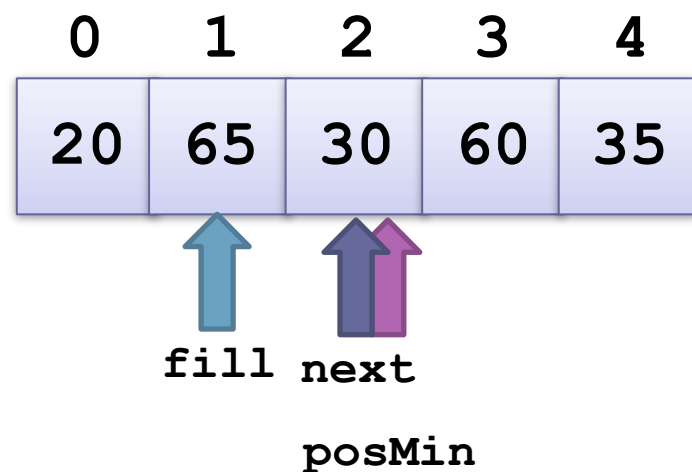
n	5
fill	1
posMin	1
next	2



1. for `fill = 0` to `n - 2` do
2. Initialize `posMin` to `fill`
3. for `next = fill + 1` to `n - 1` do
4. if the item at `next` is less than the item at `posMin`
5. Reset `posMin` to `next`
6. Exchange the item at `posMin` with the one at `fill`

Trace of Selection Sort Refinement (cont.)

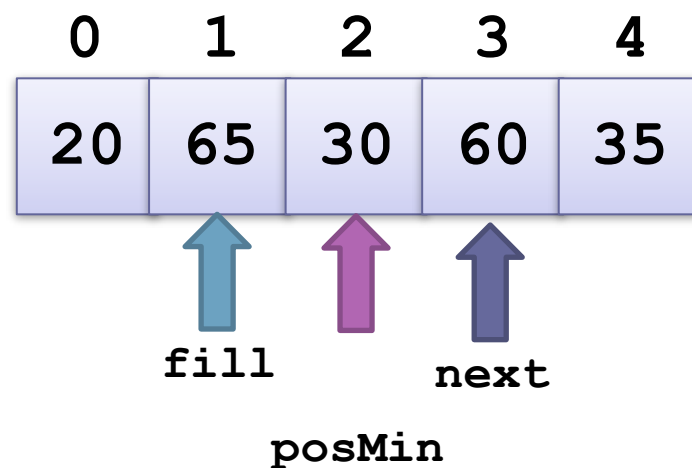
n	5
fill	1
posMin	2
next	2



1. **for** fill = 0 to n - 2 **do**
2. **Initialize** posMin to fill
3. **for** next = fill + 1 to n - 1 **do**
4. **if** the item at next is less than the item at posMin
5. **Reset** posMin to next
6. **Exchange** the item at posMin with the one at fill

Trace of Selection Sort Refinement (cont.)

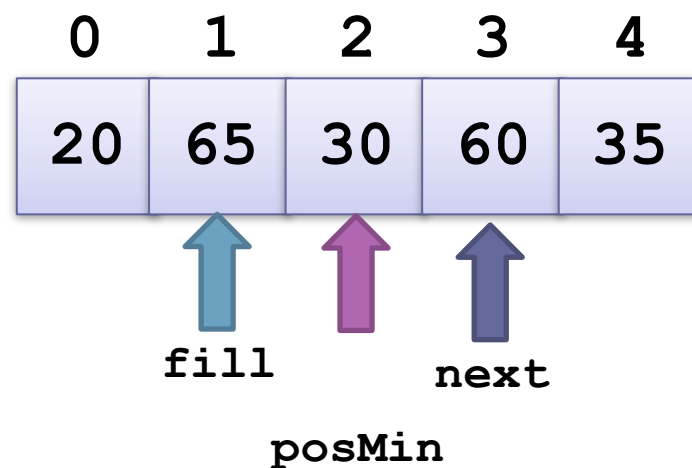
n	5
fill	1
posMin	2
next	3



1. for `fill = 0 to n - 2` do
2. Initialize `posMin` to `fill`
- ▶ 3. for `next = fill + 1 to n - 1` do
4. if the item at `next` is less than the item at `posMin`
5. Reset `posMin` to `next`
6. Exchange the item at `posMin` with the one at `fill`

Trace of Selection Sort Refinement (cont.)

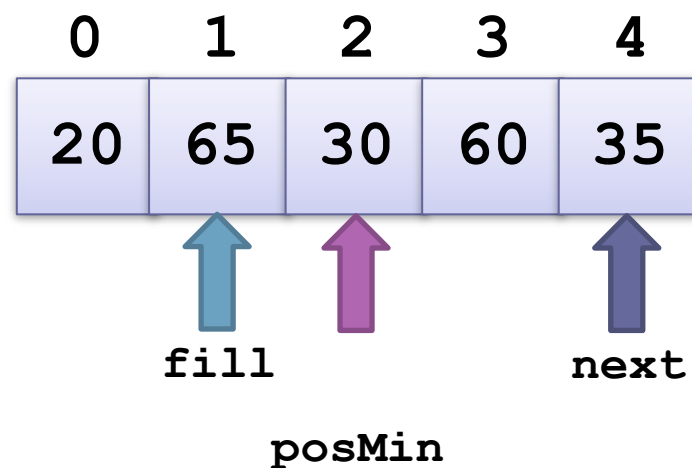
n	5
fill	1
posMin	2
next	3



1. for `fill = 0` to `n - 2` do
2. Initialize `posMin` to `fill`
3. for `next = fill + 1` to `n - 1` do
4. if the item at `next` is less than the item at `posMin`
5. Reset `posMin` to `next`
6. Exchange the item at `posMin` with the one at `fill`

Trace of Selection Sort Refinement (cont.)

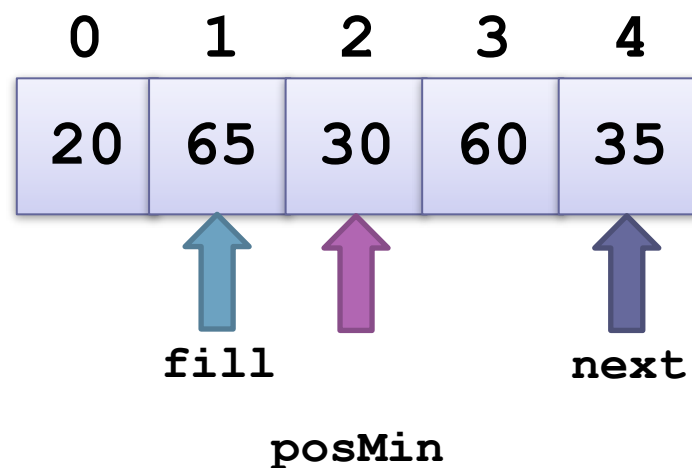
n	5
fill	1
posMin	2
next	4



1. for `fill = 0` to `n - 2` do
2. Initialize `posMin` to `fill`
- ▶ 3. for `next = fill + 1` to `n - 1` do
4. if the item at `next` is less than the item at `posMin`
5. Reset `posMin` to `next`
6. Exchange the item at `posMin` with the one at `fill`

Trace of Selection Sort Refinement (cont.)

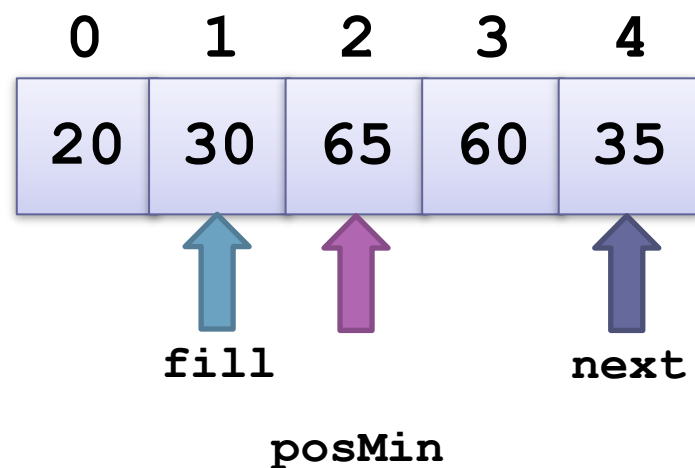
n	5
fill	1
posMin	2
next	4



1. for `fill = 0` to `n - 2` do
2. Initialize `posMin` to `fill`
3. for `next = fill + 1` to `n - 1` do
4. if the item at `next` is less than the item at `posMin`
5. Reset `posMin` to `next`
6. Exchange the item at `posMin` with the one at `fill`

Trace of Selection Sort Refinement (cont.)

n	5
fill	1
posMin	2
next	4

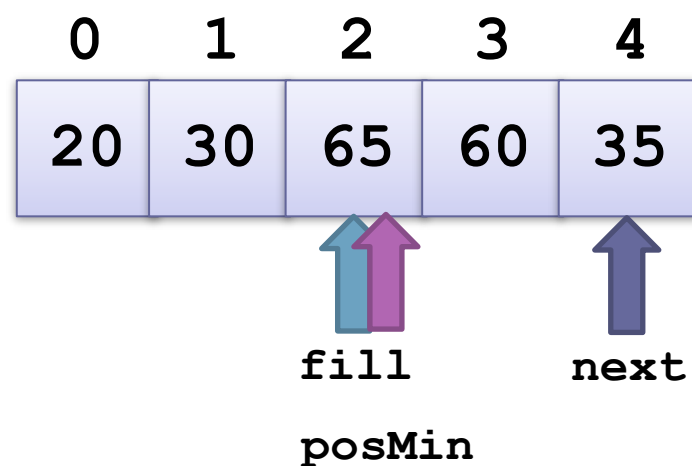


1. for **fill** = 0 to **n** - 2 do
2. Initialize **posMin** to **fill**
3. for **next** = **fill** + 1 to **n** - 1 do
4. if the item at **next** is less than the item at **posMin**
5. Reset **posMin** to **next**
6. Exchange the item at **posMin** with the one at **fill**

Trace of Selection Sort Refinement (cont.)

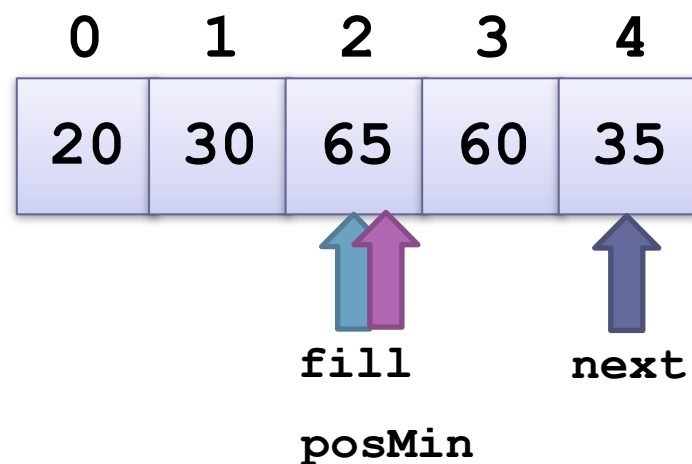
n	5
fill	2
posMin	2
next	4

- ▶ 1. for $fill = 0$ to $n - 2$ do
- 2. Initialize `posMin` to `fill`
- 3. for $next = fill + 1$ to $n - 1$ do
- 4. if the item at `next` is less than the item at `posMin`
- 5. Reset `posMin` to `next`
- 6. Exchange the item at `posMin` with the one at `fill`



Trace of Selection Sort Refinement (cont.)

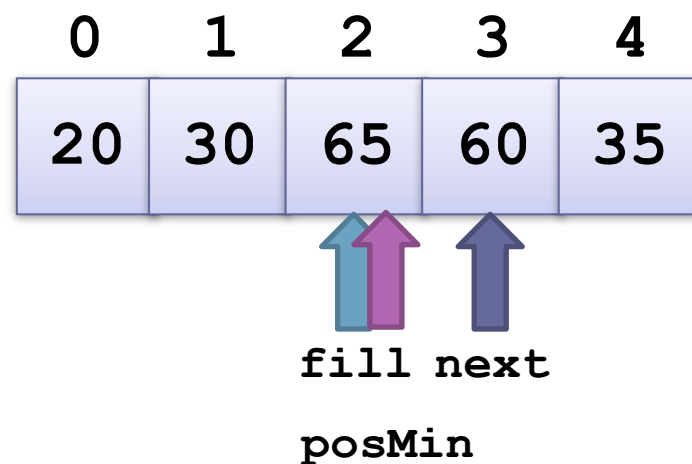
n	5
fill	2
posMin	2
next	4



1. for `fill = 0` to `n - 2` do
- ▶ 2. Initialize `posMin` to `fill`
3. for `next = fill + 1` to `n - 1` do
4. if the item at `next` is less than the item at `posMin`
5. Reset `posMin` to `next`
6. Exchange the item at `posMin` with the one at `fill`

Trace of Selection Sort Refinement (cont.)

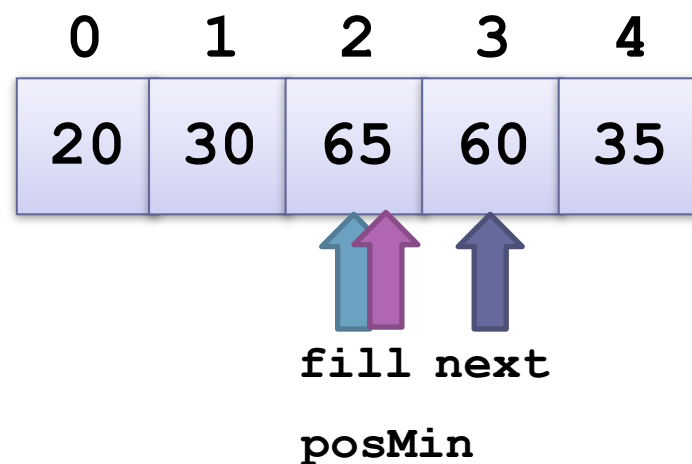
n	5
fill	2
posMin	2
next	3



1. **for** fill = 0 to n - 2 **do**
2. **Initialize** posMin to fill
- ▶ 3. **for** next = fill + 1 to n - 1 **do**
4. **if** the item at next is less than the item at posMin
5. **Reset** posMin to next
6. **Exchange** the item at posMin with the one at fill

Trace of Selection Sort Refinement (cont.)

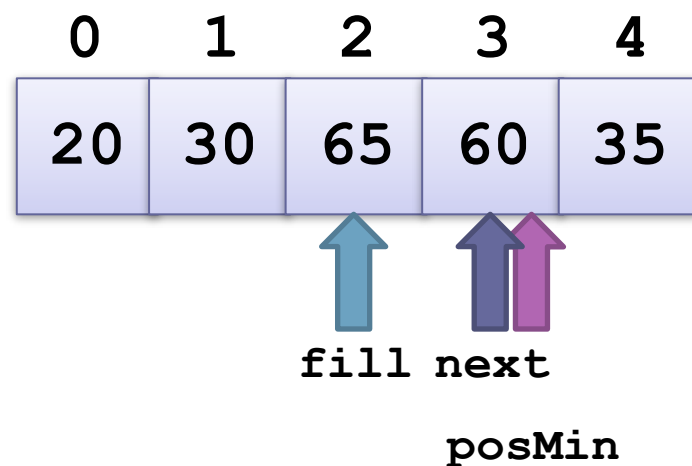
n	5
fill	2
posMin	2
next	3



1. **for** fill = 0 to n - 2 **do**
2. **Initialize** posMin to fill
3. **for** next = fill + 1 to n - 1 **do**
4. **if** the item at next is less than the item at posMin
5. **Reset** posMin to next
6. **Exchange** the item at posMin with the one at fill

Trace of Selection Sort Refinement (cont.)

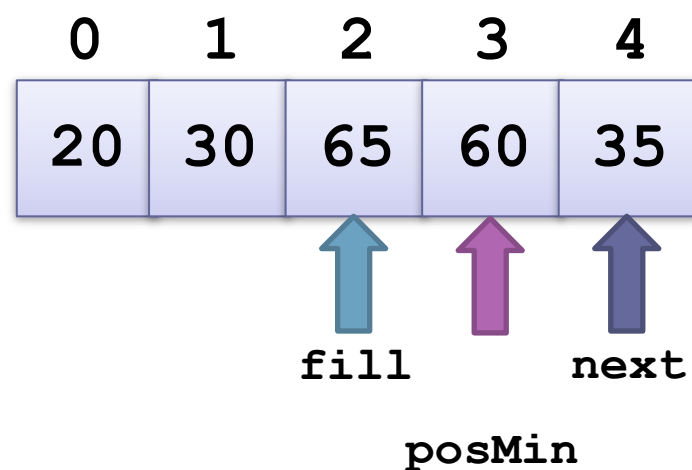
n	5
fill	2
posMin	3
next	3



1. **for** `fill = 0` to `n - 2` **do**
2. **Initialize** `posMin` to `fill`
3. **for** `next = fill + 1` to `n - 1` **do**
4. **if** the item at `next` is less than the item at `posMin`
5. **Reset** `posMin` to `next`
6. **Exchange** the item at `posMin` with the one at `fill`

Trace of Selection Sort Refinement (cont.)

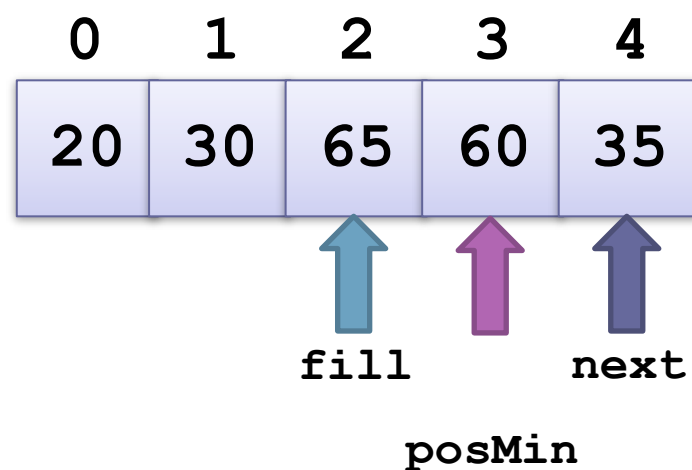
n	5
fill	2
posMin	3
next	4



1. for `fill = 0` to `n - 2` do
2. Initialize `posMin` to `fill`
- ▶ 3. for `next = fill + 1` to `n - 1` do
4. if the item at `next` is less than the item at `posMin`
5. Reset `posMin` to `next`
6. Exchange the item at `posMin` with the one at `fill`

Trace of Selection Sort Refinement (cont.)

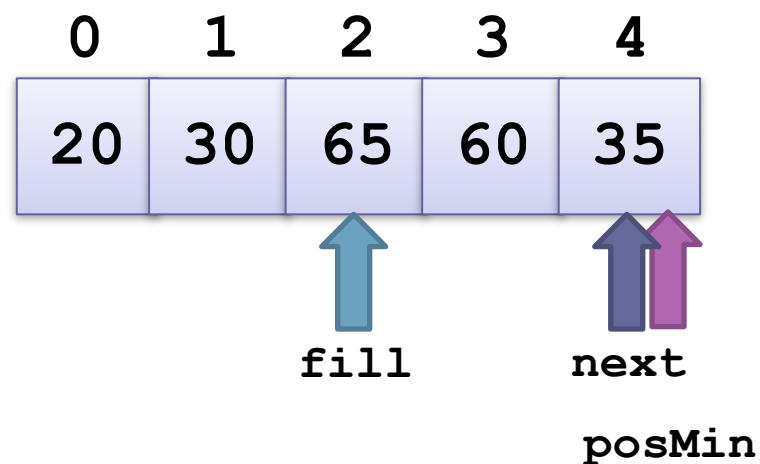
n	5
fill	2
posMin	3
next	4



1. for $fill = 0$ to $n - 2$ do
2. Initialize $posMin$ to $fill$
3. for $next = fill + 1$ to $n - 1$ do
4. if the item at $next$ is less than the item at $posMin$
5. Reset $posMin$ to $next$
6. Exchange the item at $posMin$ with the one at $fill$

Trace of Selection Sort Refinement (cont.)

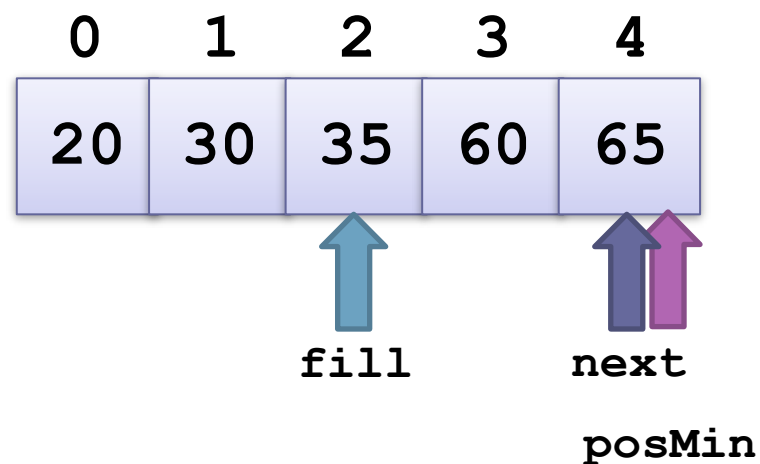
n	5
fill	2
posMin	4
next	4



1. for $fill = 0$ to $n - 2$ do
2. Initialize $posMin$ to $fill$
3. for $next = fill + 1$ to $n - 1$ do
4. if the item at $next$ is less than the item at $posMin$
5. Reset $posMin$ to $next$
6. Exchange the item at $posMin$ with the one at $fill$

Trace of Selection Sort Refinement (cont.)

n	5
fill	2
posMin	4
next	4

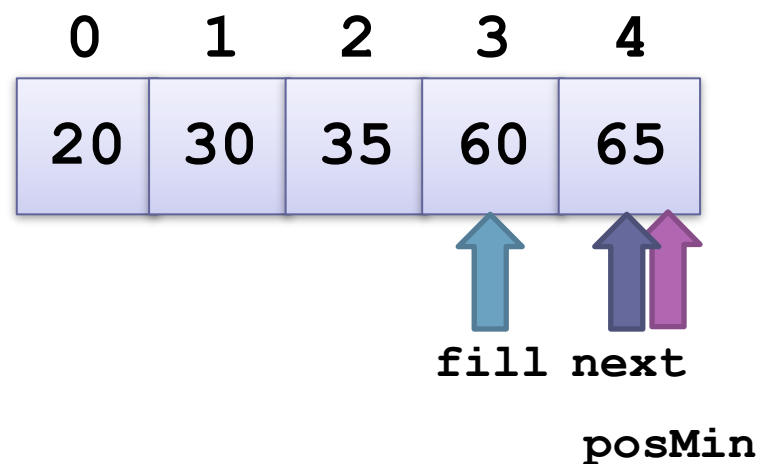


1. **for** `fill = 0` to `n - 2` **do**
2. **Initialize** `posMin` to `fill`
3. **for** `next = fill + 1` to `n - 1` **do**
4. **if** the item at `next` is less than the item at `posMin`
5. **Reset** `posMin` to `next`
6. **Exchange** the item at `posMin` with the one at `fill`

Trace of Selection Sort Refinement (cont.)

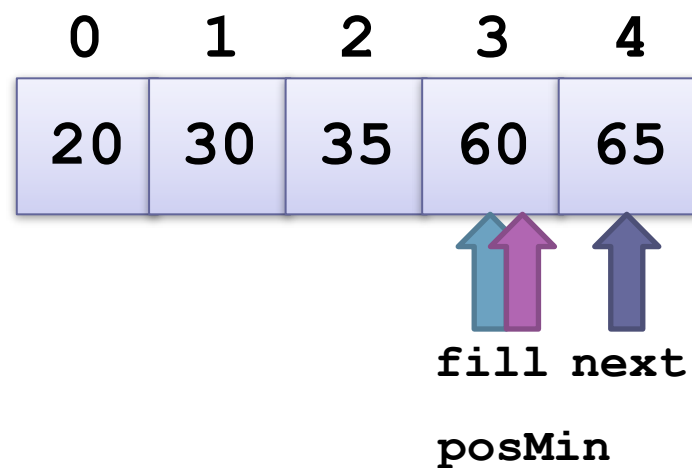
n	5
fill	3
posMin	4
next	4

- ▶ 1. for $fill = 0$ to $n - 2$ do
- 2. Initialize `posMin` to `fill`
- 3. for $next = fill + 1$ to $n - 1$ do
- 4. if the item at `next` is less than the item at `posMin`
- 5. Reset `posMin` to `next`
- 6. Exchange the item at `posMin` with the one at `fill`



Trace of Selection Sort Refinement (cont.)

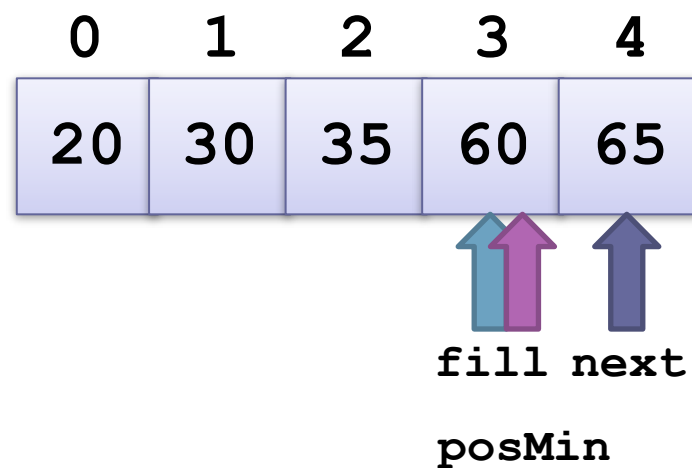
n	5
fill	3
posMin	3
next	4



1. for $fill = 0$ to $n - 2$ do
- ▶ 2. Initialize **posMin** to **fill**
3. for $next = fill + 1$ to $n - 1$ do
4. **if** the item at **next** is less than the item at **posMin**
5. **Reset posMin to next**
6. **Exchange** the item at **posMin** with the one at **fill**

Trace of Selection Sort Refinement (cont.)

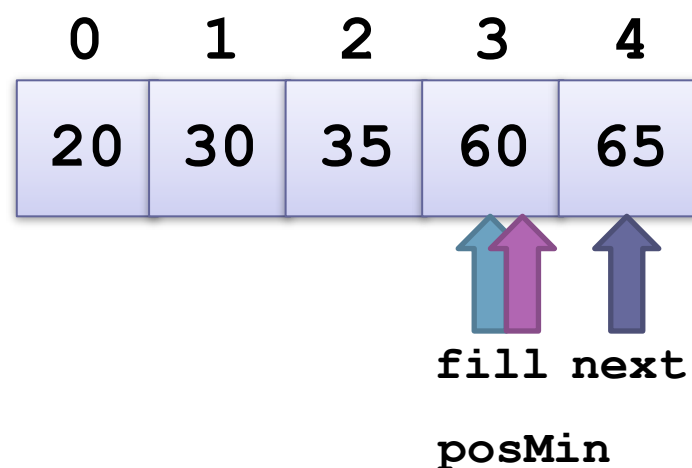
n	5
fill	3
posMin	3
next	4



1. **for** `fill = 0` to `n - 2` **do**
2. **Initialize** `posMin` to `fill`
- ▶ 3. **for** `next = fill + 1` to `n - 1` **do**
4. **if** the item at `next` is less than the item at `posMin`
5. **Reset** `posMin` to `next`
6. **Exchange** the item at `posMin` with the one at `fill`

Trace of Selection Sort Refinement (cont.)

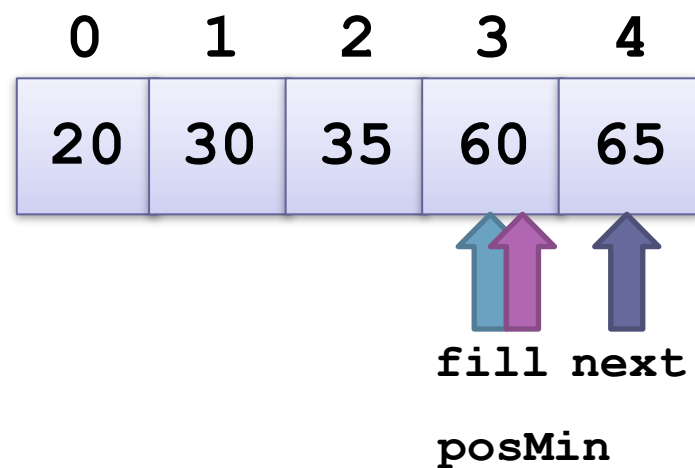
n	5
fill	3
posMin	3
next	4



1. for $fill = 0$ to $n - 2$ do
2. Initialize **posMin** to **fill**
3. for $next = fill + 1$ to $n - 1$ do
4. if the item at **next** is less than the item at **posMin**
5. Reset **posMin** to **next**
6. Exchange the item at **posMin** with the one at **fill**

Trace of Selection Sort Refinement (cont.)

n	5
fill	3
posMin	3
next	4



1. for $fill = 0$ to $n - 2$ do
2. Initialize $posMin$ to $fill$
3. for $next = fill + 1$ to $n - 1$ do
4. if the item at $next$ is less than the item at $posMin$
5. Reset $posMin$ to $next$
6. Exchange the item at $posMin$ with the one at $fill$

Trace of Selection Sort Refinement (cont.)

n	5
fill	3
posMin	3
next	4

0	1	2	3	4
20	30	35	60	65

1. **for** fill = 0 to n - 2 **do**
2. **Initialize** posMin to fill
3. **for** next = fill + 1 to n - 1 **do**
4. **if** the item at next is less than the item at posMin
5. **Reset** posMin to next
6. **Exchange** the item at posMin with the one at fill

Komplexitetsanalys

Två nästade loopar
som varje är $O(n)$

 komplexiteten
är alltså
kvadratisk,
 $O(n^2)$

1. **for** `fill = 0 to n - 2` **do**
2. **Initialize** `posMin` to `fill`
3. **for** `next = fill + 1 to n - 1` **do**
4. **if** the item at `next` is less than the
 item at `posMin`
5. **Reset** `posMin` to `next`
6. **Exchange** the item at `posMin` with the
 one at `fill`

Bubbelsortering

Kursboken, avsnitt 8.3

- Idén är att jämföra grannelement med varandra, och byta plats på dem ifall de är oordnade
- Mindre värden "bubblar" upp till toppen av listan, och större värde "sjunker" till botten
- Även denna algoritm har kvadratisk komplexitet

In-place-sortering

Alla dessa tre algoritmer är *in-place*:

- inget extra minne behövs
- det är originallistan som ändras

In-place är mycket svårare i Haskell eftersom man inte kan ändra värden:

- Haskell's insättningssortering bygger alltså en ny sorterad lista
- den gamla listan försvinner i skräpsamlingen, men det sker inte direkt, så det krävs en del extraminne

Sorteringsalgoritmer

	Number of Comparisons		
	Best	Average	Worst
Selection sort	$O(n^2)$	$O(n^2)$	$O(n^2)$
Bubble sort	$O(n)$	$O(n^2)$	$O(n^2)$
Insertion sort	$O(n)$	$O(n^2)$	$O(n^2)$
Merge sort	$O(n \log n)$	$O(n \log n)$	$O(n \log n)$
Heapsort	$O(n \log n)$	$O(n \log n)$	$O(n \log n)$
Quicksort	$O(n \log n)$	$O(n \log n)$	$O(n^2)$

n^2 vs $n \log n$

n	n^2	$n \log n$
8	64	24
16	256	64
32	1,024	160
64	4,096	384
128	16,384	896
256	65,536	2,048
512	262,144	4,608