Software Engineering using Formal Methods

Verification with Spin

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6 September 2011

SPIN: Previous Lecture vs. This Lecture

Previous lecture

SPIN appeared as a PROMELA simulator

This lecture

Intro to SPIN as a model checker

What Does A Model Checker Do?

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⇒ Finding no counter example proves stated correctness properties.

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exhaustive search

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two kinds of non-determinism to be resolved:

- explicit, local:
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:: guardX -> ...
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- implicit, global:
  scheduling of concurrent processes
  (see next lecture)

Model Checker for This Course: Spin

Spin: "Simple Promela Interpreter"

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verifier generated by Spin is a C program performing model checking:

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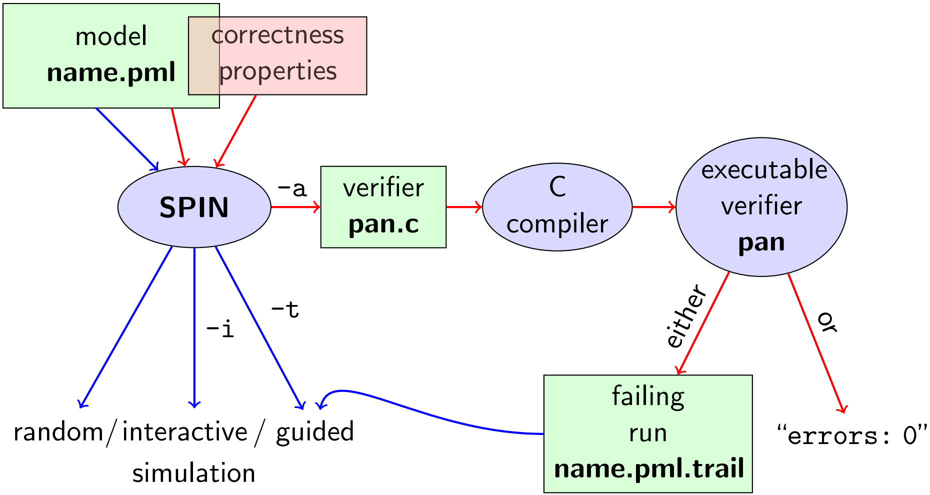
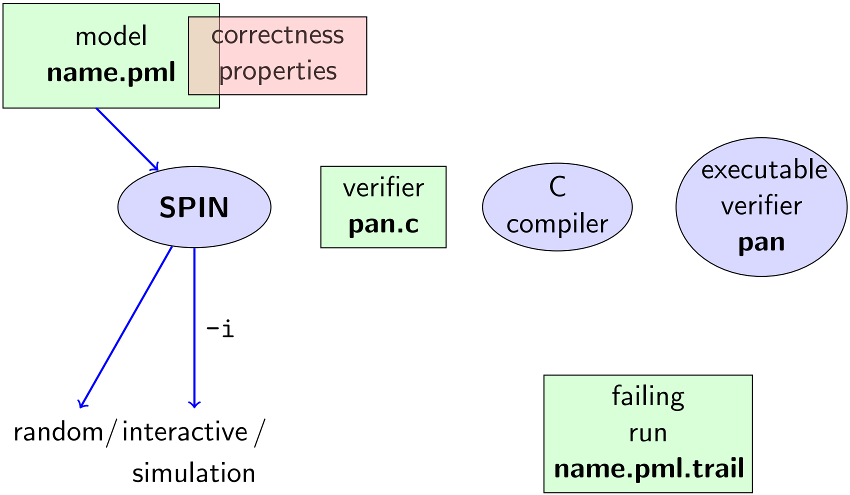
- in case the check is negative:
  generates a failing run of the model, to be simulated by Spin

SPIN Workflow: Overview



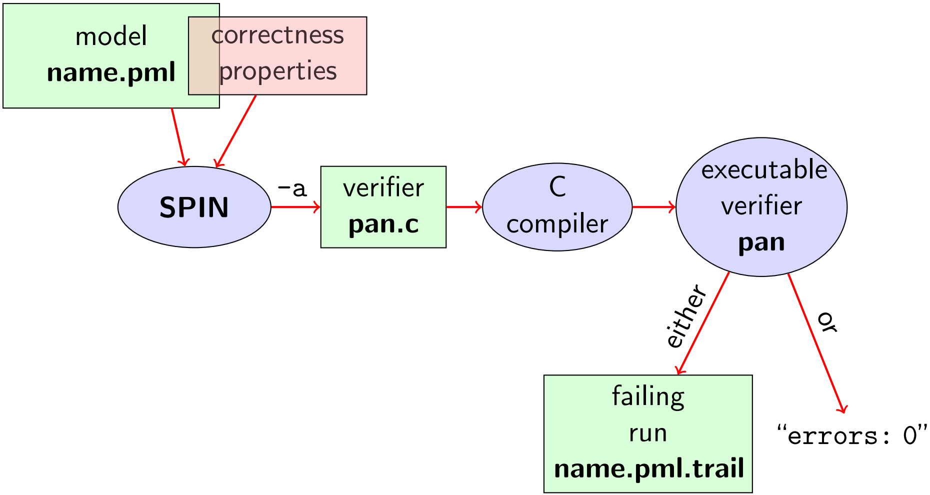
Plain Simulation with SPIN



Rehearsal: Simulation Demo

- run example, random and interactive
  `interleave.pml`, `zero.pml`

Model Checking with SPIN



Meaning of Correctness w.r.t. Properties

Given PROMELA model M, and correctness properties $C_1, \ldots, C_n$.

- Be R_M the set of all possible runs of M.
- For each correctness property C_i,
  R_{M,C_i} is the set of all runs of M satisfying C_i.
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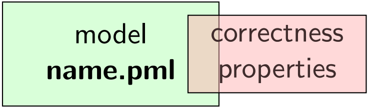
We know how to write models M.
But how to write Correctness Properties?

Stating Correctness Properties



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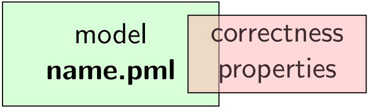

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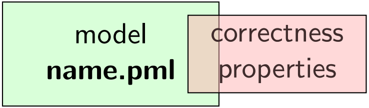

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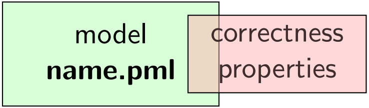

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  - `end` labels
  - `accept` labels
  - `progress` labels

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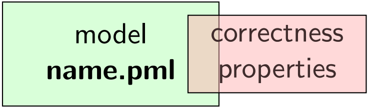

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- temporal logic formulas

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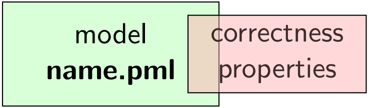

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Assertion Statements

Definition (Assertion Statements)

Assertion statements in PROMELA are statements of the form

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stmt1;
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...
stmt1;
assert(max == a);
stmt2;
...
```

```
...
if
  :: b1 -> stmt3;
           assert(x < y)
  :: b2 -> stmt4
...
```

Meaning of Boolean Assertion Statements

assert(*expr*)

- has no effect if *expr* evaluates to true
- triggers an error message if *expr* evaluates to false

This holds in both, simulation and model checking mode.

Meaning of General Assertion Statements

assert(*expr*)

- has no effect if *expr* evaluates to non-zero value
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Recall:

bool true false is syntactic sugar for

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⇒ general case covers Boolean case

Instead of using 'printf's for Debugging ...

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/* after choosing a,b from {1,2,3} */
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  :: a >= b -> max = a
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Command Line Execution

(simulate, inject faults, add assertion, simulate again)

```
> spin [-i] max.pml
```

... we can employ Assertions

quoting from file **max.pml**:

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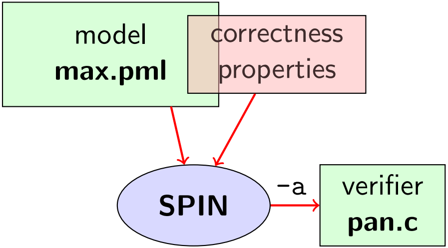
(Historic moment in the course.)

Generate Verifier in C



Command Line Execution

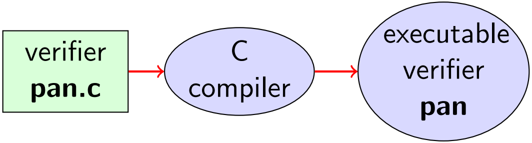
Generate Verifier in C

```
> spin -a max.pml
```

SPIN generates Verifier in C, called **pan.c**

(plus helper files)

Compile To Executable Verifier



Command Line Execution

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> gcc -o pan pan.c
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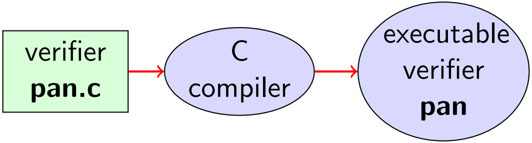

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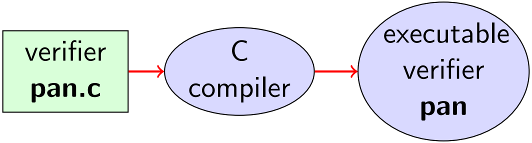

Command Line Execution

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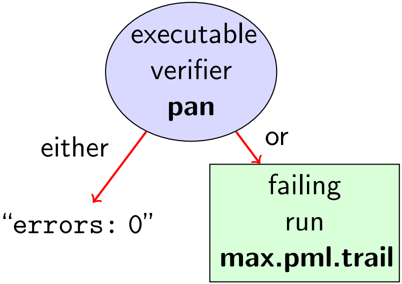
pan: historically "**p**rotocol **an**alyzer", now "**p**rocess **an**alyzer"

Run Verifier (= Model Check)



Command Line Execution

run verifier **pan**

`> ./pan` *or* `> pan`

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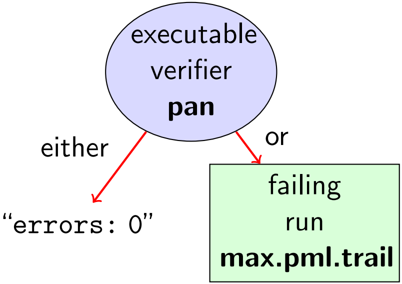

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- prints “errors: 0”

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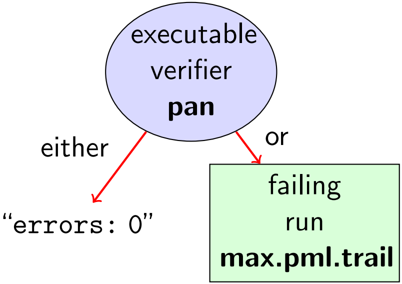

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- prints "`errors: 0`" $\Rightarrow$ Correctness Property verified!

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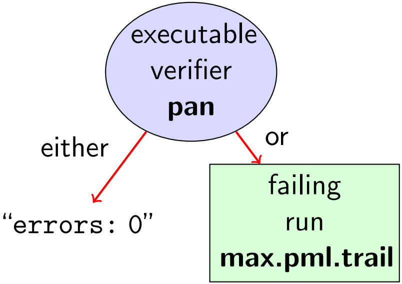

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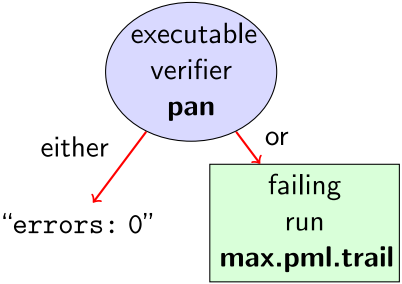

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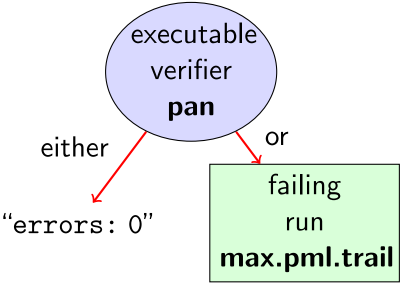

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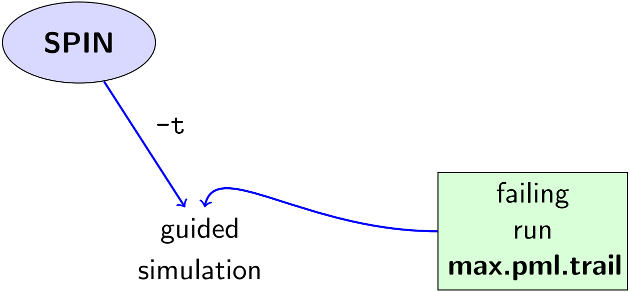
  records failing run in **max.pml.trail**

Guided Simulation

To examine failing run: employ simulation mode, “guided” by trail file.



Command Line Execution

inject a fault, re-run verification, and then:

```
> spin -t -p -l max.pml
```

Output of Guided Simulation

can look like:

```
Starting P with pid 0
1: proc 0 (P) line  8 "max.pml" (state 1) [a = 1]
                P(0):a = 1
2: proc 0 (P) line 14 "max.pml" (state 7) [b = 2]
                P(0):b = 2
3: proc 0 (P) line 23 "max.pml" (state 13) [((a<=b))]
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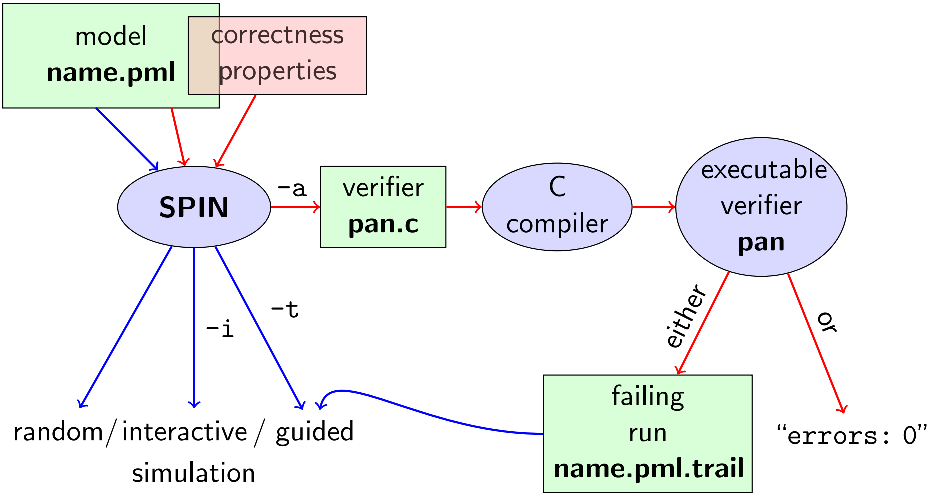
assignments in the run

values of variables whenever updated

What did we do so far?

following whole cycle (most primitive example, assertions only)



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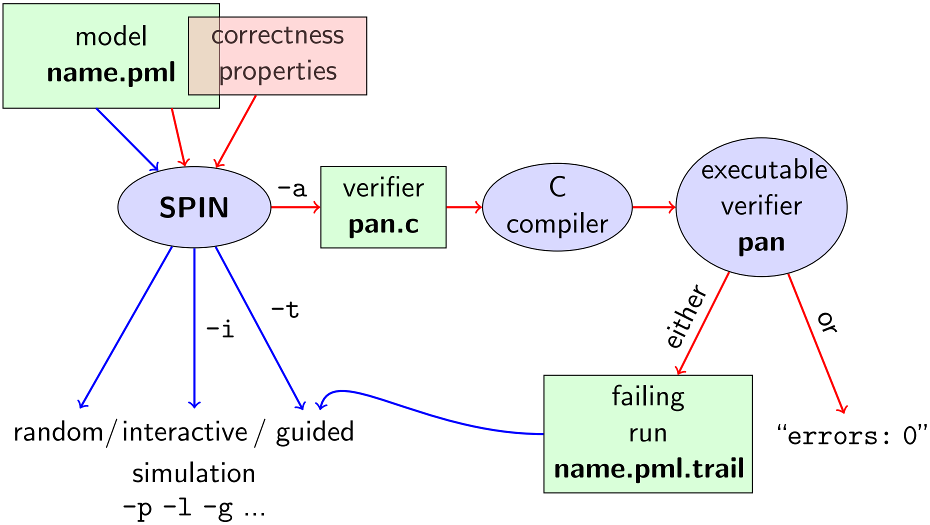

Further Examples: Integer Division

```
int dividend = 15;
int divisor  = 4;
int quotient, remainder;

quotient = 0;
remainder = dividend;
do
  :: remainder > divisor ->
     quotient++;
     remainder = remainder - divisor
  :: else ->
     break
od;
printf("%d␣divided␣by␣%d␣=␣%d,␣remainder␣=␣%d\n",
       dividend, divisor, quotient, remainder)
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simulate, put assertions, verify, change values, ...

Further Examples: Greatest Common Divisor

```
int x = 15, y = 20;
int a, b;
a = x; b = y;
do
  :: a > b -> a = a - b
  :: b > a -> b = b - a
  :: a == b -> break
od;
printf("The␣GCD␣of␣%d␣and␣%d␣=␣%d\n", x, y, a)
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Further Examples: Greatest Common Divisor

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⇒ typical for model checking

Typical Command Lines

typical command line sequences:

random simulation

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and in case of error

```
spin -t -p -l -g name.pml
```

SPIN Reference Card

Ben-Ari produced Spin Reference Card, summarizing

- typical command line sequences
- options for
  - SPIN
  - gcc
  - pan
- PROMELA
  - datatypes
  - operators
  - statements
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⇒ available from course page (see ‘Links, Papers, and Software’)

Why SPIN?

- SPIN targets software, instead of hardware verification ("*Software* Engineering using Formal Methods")
- 2001 ACM Software Systems Award (other winning software systems include: Unix, TCP/IP, WWW, Tcl/Tk, Java)
- used for safety critical applications
- distributed freely as research tool, well-documented, actively maintained, large user-base in academia and in industry
- annual SPIN user workshops series held since 1995
- based on standard theory of ω-automata and linear temporal logic

Why SPIN? (Cont'd)

- PROMELA and SPIN are rather simple to use
- good to understand a few systems really well, rather than many systems poorly
- availability of good course book (Ben-Ari)
- availability of front end JSPIN (also Ben-Ari)

What is jSPIN?

- graphical user interface for SPIN
- developed for pedagogical purposes
- written in JAVA
- simple user interface
- SPIN options automatically supplied
- fully configurable
- supports graphics output of transition system

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- graphical user interface for Spin
- developed for pedagogical purposes
- written in Java
- simple user interface
- Spin options automatically supplied
- fully configurable
- supports graphics output of transition system
- makes back-end calls transparent

jSpin **Demo**

Command Line Execution

calling jSpin

```
> java -jar /usr/local/jSpin/jSpin.jar
```

(with path adjusted to your setting)

or use shell script:

```
> jspin
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jSpin Demo

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play around with similar examples ...

Catching A Different Type of Error

quoting from file **max2.pml**:

```
/* after choosing a,b from {1,2,3} */
if
  :: a >= b -> max = a;
  :: b <= a -> max = b;
fi;
printf("the maximum of %d and %d is %d\n",
       a, b, max)
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⇒ crazy "`timeout`" message sometimes

generate and execute **pan**
⇒ reports "`errors: 1`"

Note: no assert in **max2.pml**.

Catching A Different Type of Error

Further inspection of **pan** output:

```
...
pan: invalid end state (at depth 1)
pan: wrote max2.pml.trail
...
```

Legal and Illegal Blocking

A process may legally block, as long as some other process can proceed.

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$\Rightarrow$ "Deadlock"

in **max2.pml**, there exists a run where no process can take over.

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- each location marked with an end label: "`end`*xxx*`:`"

End labels not useful in **max2.pml**, but elsewhere, they are.
Example: `end.pml`

Literature for this Lecture

Ben-Ari Chapter 2, Sections 4.7.1, 4.7.2