Software Engineering using Formal Methods Proof Obligations

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making the connection between

JML

and

Dynamic Logic / KeY

making the connection between

JML

 $\quad \text{and} \quad$

Dynamic Logic / KeY



making the connection between

JML

 and

Dynamic Logic / KeY

- ▶ generating,
- understanding,

making the connection between

JML

 and

Dynamic Logic / KeY

- generating,
- understanding,
- and proving

DL proof obligations from JML specifications

we follow 'KeY Quicktour for JML' (cited below as [KQJ])

paper + sources: see 'KeY Quicktour' on course page, under 'Links, Papers, and Software'

scenario: simple PayCard

Inspecting JML Specification

inspect quicktour/jml/paycard/PayCard.java

follow [KQJ, 2.2]

New JML Feature I: Nested Specification Cases

```
method charge() has nested specification case:
@ public normal behavior
@ requires amount > 0;
0 {
0
    requires amount + balance < limit && isValid()==true;
    ensures \result == true:
0
    ensures balance == amount + \old(balance);
0
0
    assignable balance;
0
0
    also
0
0
    requires amount + balance >= limit;
0
    ensures \result == false;
0
    ensures unsuccessfulOperations
0
            == \old(unsuccessfulOperations) + 1;
0
    assignable unsuccessfulOperations;
```

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nested specification cases allow to factor out common preconditions

```
@ public normal_behavior
@ requires R;
0 {
0
    requires R1;
0
    ensures E1;
0
    assignable A1;
0
0
    also
0
    requires R2;
0
0
    ensures E2;
0
    assignable A2;
0
  1}
expands to ... (next page)
```

```
(previous page) ... expands to
@ public normal_behavior
@ requires R;
@ requires R1;
@ ensures E1:
@ assignable A1;
0
 also
0
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@ public normal_behavior
@ requires R;
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                                                              8 / 34
```

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SEFM: Proof Obligations
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method charge() has exceptional behavior case:

- @ public exceptional_behavior
- @ requires amount <= 0;</pre>
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- ▶ pure is method-global, also prohibits non-termination & exceptions
- assignable clause is local to specification case (here, there is only one)
- pure not usable in this particular context

generate EnsuresPost PO for normal behavior of charge()

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follow [KQJ, 3.1+3.2]

summary:

- start KeY prover
- in quicktour/jml, open paycard
- select charge and EnsuresPost
- inspect Assumed Invariants

generate EnsuresPost PO for normal behavior of charge()

follow [KQJ, 3.1+3.2]

summary:

- start KeY prover
- in quicktour/jml, open paycard
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- inspect Assumed Invariants assuming less invariants:
 - is fully sound
 - can compromise provability

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Current Goal pane displays proof obligation as DL sequent

for loading more proof obligations: re-open **Proof Obligation Browser** under **Tools** menu (or **Ctrl-B**)

generate **EnsuresPost** PO for normal behavior of isValid()

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generate **PreservesOwnInv** PO for charge()

expressing that charge() preserves all invariants (of its own class)

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generate EnsuresPost PO for normal behavior of isValid()

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expressing that charge() preserves all invariants (of its own class)

follow [KQJ, 4.3.1+4.3.2]

in the following:

principles of translating JML to proof obligations in DL

- issues in translating arithmetic expressions
- translating this
- identifying the method's implementation
- translating boolean JML expressions to first-order logic formulas
- translating preconditions
- translating class invariants
- translating postconditions
- storing \old fields prior to method invocation
- storing actual parameters prior to method invocation
- expressing that 'exceptions are (not) thrown'
- putting everything together

WARNING:

following presentation is

- incomplete
- not fully precise
- simplifying
- omitting details/complications
- deviating from exact implementation in KeY

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(notational remark: stick to ASCII syntax of KeY logic in this lecture)

Issues on Translating Arithmetic Expressions

often:

 KeY replaces arithmetic JAVA operators by generalized operators, generic towards various integer semantics (JAVA, Math).
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(no need to memorize this)

Translating this

both

- explicit
- implicit

this reference translated to self

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this reference translated to self

```
e.g., given class
public class MyClass {
    ...
    private int f;
    ...
}
```
Translating this

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e.g., given class
public class MyClass {
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```

- f translated to self.f
- this.f translated to self.f

Identifying the Method's Implementation

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KeY models selection of implementation from package.Class by m(*args*)@package.Class

example:

charge(x)@paycard.PayCard

executes class paycard.PayCard's implementation of method call charge(x)

Translating Boolean JML Expressions

first-order logic treated fundamentally different in JML and KeY logic

JML

- formulas no separate syntactic category
- instead:

JAVA's **boolean** expressions extended with first-order concepts (i.p. quantifiers)

KeY logic

- formulas and expressions completely separate
- truth constants true, false are formulas,
 boolean constants TRUE, FALSE are expressions
- atomic formulas take expressions as arguments; e.g.:

▶ x - y < 5

 \blacktriangleright b = TRUE

${\mathcal F}$ Translates <code>boolean JML</code> Expressions to Formulas

$$\begin{array}{rcl} \mathcal{F}(v) & = & v = \text{TRUE} \\ \mathcal{F}(f) & = & \mathcal{T}(f) = \text{TRUE} \\ \mathcal{F}(m()) & = & \mathcal{T}(m)() = \text{TRUE} \\ \mathcal{F}(!b_{-}0) & = & !\mathcal{F}(b_{-}0) \\ \mathcal{F}(b_{-}0 \&\& b_{-}1) & = & \mathcal{F}(b_{-}0) \& \mathcal{F}(b_{-}1) \\ \mathcal{F}(b_{-}0 & || & b_{-}1) & = & \mathcal{F}(b_{-}0) & | & \mathcal{F}(b_{-}1) \\ \mathcal{F}(b_{-}0 & ==> & b_{-}1) & = & \mathcal{F}(b_{-}0) & | & \mathcal{F}(b_{-}1) \\ \mathcal{F}(b_{-}0 & ==> & b_{-}1) & = & \mathcal{F}(b_{-}0) & | & -> & \mathcal{F}(b_{-}1) \\ \mathcal{F}(b_{-}0 & ==> & b_{-}1) & = & \mathcal{F}(b_{-}0) & | & -> & \mathcal{F}(b_{-}1) \\ \mathcal{F}(e_{-}0 & == & e_{-}1) & = & \mathcal{E}(e_{-}0) & = & \mathcal{E}(e_{-}1) \\ \mathcal{F}(e_{-}0 & == & e_{-}1) & = & \mathcal{E}(e_{-}0) & > = & \mathcal{E}(e_{-}1) \\ \mathcal{F}(e_{-}0 & >= & e_{-}1) & = & \mathcal{E}(e_{-}0) & > = & \mathcal{E}(e_{-}1) \end{array}$$

v/f/m() boolean variables/fields/pure methods b_0, b_1 boolean JML expressions e_0, e_1 JAVA expressions

 \mathcal{T} may add 'self.' or '@ClassName' (see pp. 16, 17) \mathcal{E} may add casts, transform operators (see p. 15)

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${\mathcal F}$ Translates boolean JML Expressions to Formulas

$$\mathcal{F}((\langle \mathbf{forall } T x; e_{-}0)) = \langle \mathbf{forall } T x; \\ !x = \mathbf{null} \rightarrow \mathcal{F}(e_{-}0)$$

$$\mathcal{F}((\langle \mathbf{exists } T x; e_{-}0; e_{-}1)) = \langle \mathbf{exists } T x; \\ !x = \mathbf{null} \& \mathcal{F}(e_{-}0)$$

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Translating Preconditions

if selected contract Contr has preconditions

```
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@ ...
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$$\mathcal{PRE}(Contr) = \\ \mathcal{F}(b_1) \& \dots \& \mathcal{F}(b_n)$$

Translating Class Invariants

```
the invariant
class C {
    ...
    //@ invariant inv_i;
    ...
}
is translated to
```

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```
the invariant
class C {
  . . .
  //@ invariant inv_i;
  . . .
}
is translated to
                            \mathcal{INV}(inv_i)
forall C o: ((o.<created> = TRUE & !o = null) ->
                                                {self:=o}F(inv_i))
```

Translating Postconditions

if selected contract Contr has postconditions
@ ensures b_1;
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```
\mathcal{POST}(Contr) = \\ \mathcal{F}(b_1) \& \dots \& \mathcal{F}(b_n)
```

Translating Postconditions

```
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@ ensures b_1;
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special treatment of expressions in post-condition: see next slide

Translating Expressions in Postconditions

below, we assume the following assignable clause

@ assignable <assignable_fields>;

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translating expressions in postconditions (interesting cases only):

 $\mathcal{E}(\mathbf{result}) = result$

$$\mathcal{E}(\texttt{old}(e)) = \mathcal{E}_{old}(e)$$

 $\mathcal{E}_{\textit{old}}$ defined like $\mathcal{E},$ with the exception of:

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 $\mathcal{E}_{\textit{old}}$ defined like $\mathcal{E}_{\text{-}}$ with the exception of:

 $\mathcal{E}_{old}(e.f) = fAtPre(\mathcal{E}_{old}(e))$ $\mathcal{E}_{old}(f) = fAtPre(self)$ for $f \in \langle assignable_fields \rangle$

'fAtPre' meant to refer to field 'f' in the pre-state

```
given an assignable field f of class C
class C {
    ...
    private T f;
    ...
}
```

translation of postcondition replaced **f** in **\old**(...) by **f**AtPre (p. 24) left to do: store pre-state values of **f** in **f**AtPre

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```
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\for C o; fAtPre(o) := o.f
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note: not a formula, but

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STORE(f)
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note: not a formula, but a quantified update (more proper explanation tomorrow)

Storing Pre-State of All Assignable Fields

if selected contract Contr has assignable clause:

```
@ assignable f_1, ..., f_n;
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then pre-state of all assignable fields can be stored by

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STORE(Contr) = { STORE(f_1) || ... || STORE(f_n) }

how can you express in DL: method call m() will not throw an exception

how can you express in DL: method call m() will not throw an exception (if method body from class C in package p is invoked)

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how can you express in DL:
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```
<{ exc = null;

try {

    m()@p.C;

} catch (Throwable e) {

    exc = e;

}

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note difference:

- JAVA assignments
- equation, i.e., formula

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        exc = e;
     }
} \> !exc = null & <typing of exc>
```

PO for Normal Behavior Contract

PO for a normal behavior contract *Contr* for void method m(), with chosen assumed invariants inv_1, ..., inv_n

```
==>
       \mathcal{INV}(inv_1)
     & . . .
    & \mathcal{INV}(inv_n)
     & \mathcal{PRE}(Contr)
 -> STORE(Contr)
       < exc = null;
             try {
               m()@p.C;
             } catch (Throwable e) {
               exc = e;
             }
           \geq exc = null \& \mathcal{POST}(Contr)
```

PO for Normal Behavior Allowing Non-Termination

```
PO for a normal behavior contract Contr for method m().
where Contr has clause diverges true;
==>
       \mathcal{INV}(inv_1)
     & . . .
    & \mathcal{INV}(inv_n)
     & PRE(Contr)
 \rightarrow STORE(Contr)
       [{ exc = null;}
            try {
               m()@p.C;
            } catch (Throwable e) {
               exc = e;
            }
          \left( = null \& \mathcal{POST}(Contr) \right)
```

PO for Normal Behavior of Non-Void Method

PO for a normal behavior contract *Contr* for non-void method m(), ==> $\mathcal{INV}(inv_1)$ & . . . & $\mathcal{INV}(inv_n)$ & PRE(Contr) -> STORE(Contr) \leq exc = null; trv { result = m()@p.C; } catch (Throwable e) { exc = e;} } > exc = null & $\mathcal{POST}(Contr)$

PO for Normal Behavior of Non-Void Method

PO for a normal behavior contract *Contr* for non-void method m(), ==> $\mathcal{INV}(inv_1)$ & . . . & *INV*(inv_n) & PRE(Contr) -> STORE(Contr) \leq exc = null; trv { result = m()@p.C; } catch (Throwable e) { exc = e;} $\rightarrow exc = null \& POST(Contr)$

recall: $\mathcal{POST}(Contr)$ translates \result to result (p. 24)

PO for Preserving Invariants

assume method m() has contracts *Contr*₁, ..., *Contr_j* PO stating that:

> Invariants inv_1, ..., inv_n are preserved in all cases covered by a contracts.

don't fit on slide: execute quicktour with KeY instead

Literature for this Lecture

Essential

KeY Quicktour see course page, under 'Links, Papers, and Software'