

Graphics hardware – why?

- Often said to be "100x" faster than CPU.
 - Reason: Simple to parallelize triangle rendering :
 - over individual triangles, pixels, (even over x,y,z,w, and r,g,b,a)
 - Hardware fixed functions: clipping, rasterizer, texture filtering, fragment-merge, ...

Current hardware:

- Triangle rasterization with programmable shading.
- Massive parallel general-purpose computations:
 - CUDA/OpenCL/Compute Shaders (~10.000 ALUs)
- Al computations:
 - ~500 tensor cores, each performing a 4x4-matrix mul+add.
- GPU Ray tracing:
 - NVIDIA RTX (via OptiX, Vulcan, Microsoft DXR api)
 - Although, can write your own GPU ray-tracer (e.g., CUDA or shader based)
 - or even WebGPU

Perspective-correct interpolation of texture coordinates

(and actually all screen-space-interpolated pervertex data)

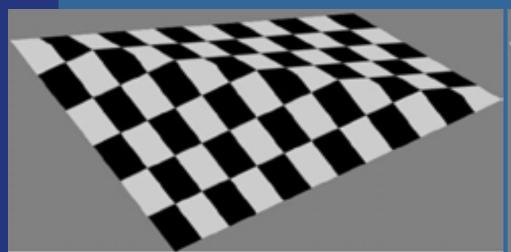


Horizon Forbidden West, 2022

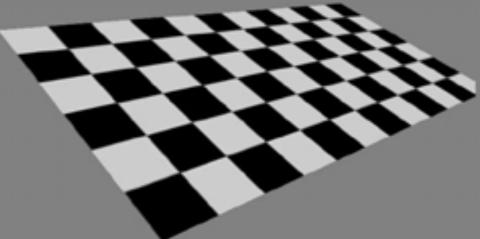


Perspective-correct texturing

- How is texture coordinates interpolated over a triangle?
- Linearly?

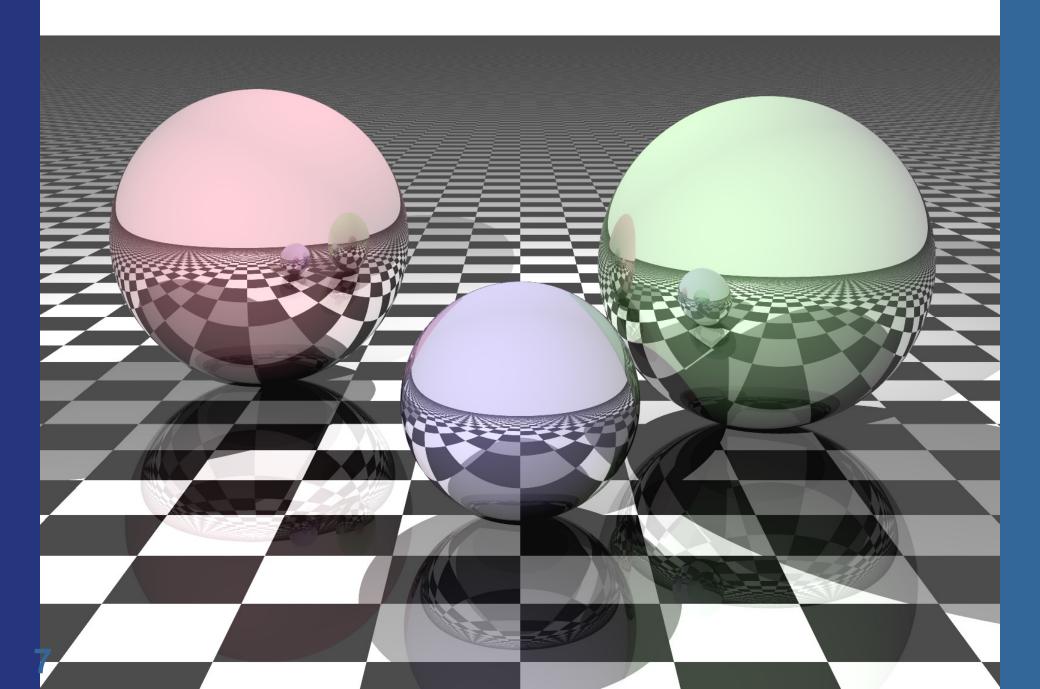


Linear interpolation



Perspective-correct interpolation

- Perspective-correct interpolation gives foreshortening effect!
- Hardware does this for you, but you need to understand this anyway!



Recall the following

Vertices are projected onto screen by non-linear transform. Hence, tex coords cannot be linearly interpolated in screen space (just like a 3D-position cannot be).

- Perspective projection introduces a non-linear transform by the homogenization step:
 - Projection: $\mathbf{p} = \mathbf{M}\mathbf{v}$
 - After projection p_w is not 1!
 - Homogenization: $(p_x/p_w, p_y/p_w, p_z/p_w, 1)$
 - Gives (x, y, z, 1), where x, y are the screen-space coordinates and z is depth

$$\mathbf{p} = \mathbf{M}\mathbf{v} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & -1/d & 0 \end{pmatrix} \begin{pmatrix} v_x \\ v_y \\ v_z \\ 1 \end{pmatrix} = \begin{pmatrix} v_x \\ v_y \\ v_z \\ -v_z/d \end{pmatrix}$$

Perspective-correct interpolation



- Linear interpolation in screen space does not work for u,v
- Why:
 - We have applied a non-linear transform to each vertex position (x/w, y/w, z/w, w/w).
 - Non-linear due to 1/w factor from the homogenisation
 - Surprisingly, we can screen-space interpolate any vertex attribute a/w (including 1/w) perspective correctly.
 - For a proof, see Jim Blinn,"W Pleasure, W Fun", IEEE Computer Graphics and Applications, p78-82, May/June 1998

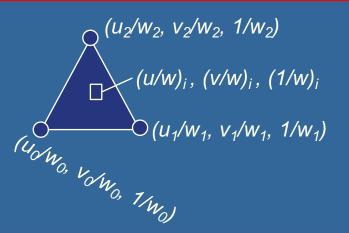
Solution:

- Interpolate (u/w, v/w, 1/w), from each vertex,
 where w is from homogeneous coordinate (x,y,z,w). (Screen-space coord is (x/w, y/w, z/w, 1))
 - Then at each pixel, get u_i,v_i as:

$$- w_i = 1 / (1/w)_i$$

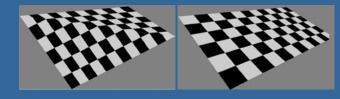
$$- u_i = (u/w)_i * w_i$$

$$- v_i = (v/w)_i * w_i$$



Shading is automatically interpolated this way too (though, not as annoying as textures). Perspective correct interpolation nowadays handled automatically by the GPU.

Perspective-correct interpolation



"Intuitive explanation" (but not proof):

- Linear interpolation in screen space does not work for u,v
- Why:
 - We have applied a non-linear transform to each vertex position (x/w, y/w, z/w, w/w).
 - Non-linear due to 1/w factor from the homogenisation
- Solution:
 - We must apply the same non-linear transform to u,v as for x,y,z
 - E.g. (u/w, v/w). This can now be correctly screenspace interpolated since it follows the same non-linear (1/w) transform (and interpolation) as (x/w, y/w, z/w).
 - So, linearly interpolate (u/w, v/w, 1/w), which is computed in screenspace at each vertex.
 - Then at each pixel:
 - $u_i = (u/w)_i / (1/w)_i$
 - $v_i = (v/w)_i / (1/w)_i$

Overview of GPU architecture

- -History / evolution
- GPU design: Several **cores** consisting of many **ALU**s (NVIDIA terminology: **Streaming Multiprocessors (SMs)** of many **cores**
- GPU vs CPU

Take-away: bandwidth (cost of memory accesses) is often the main problem

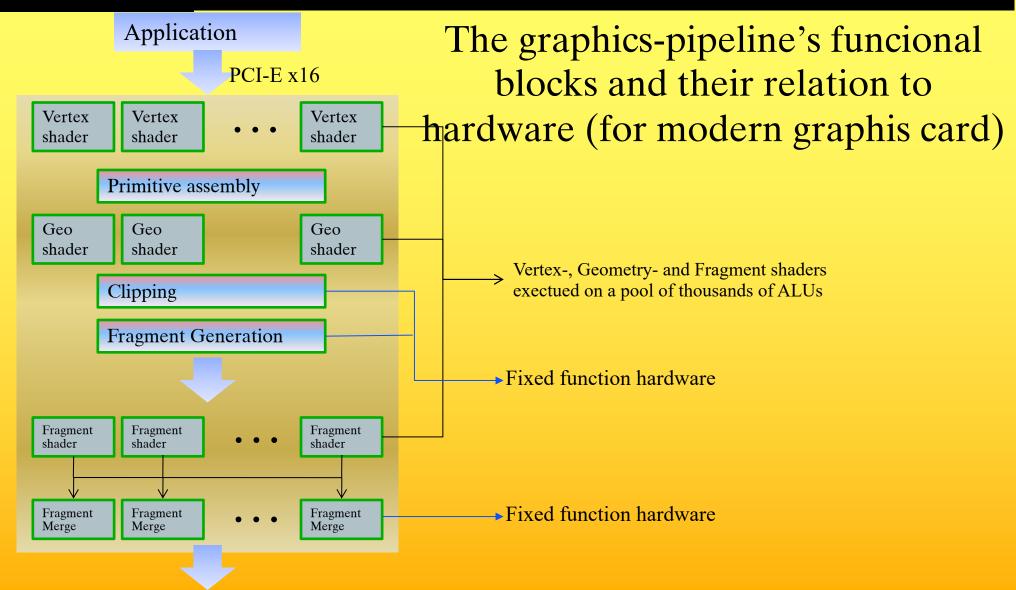
Background: Graphics hardware architectures

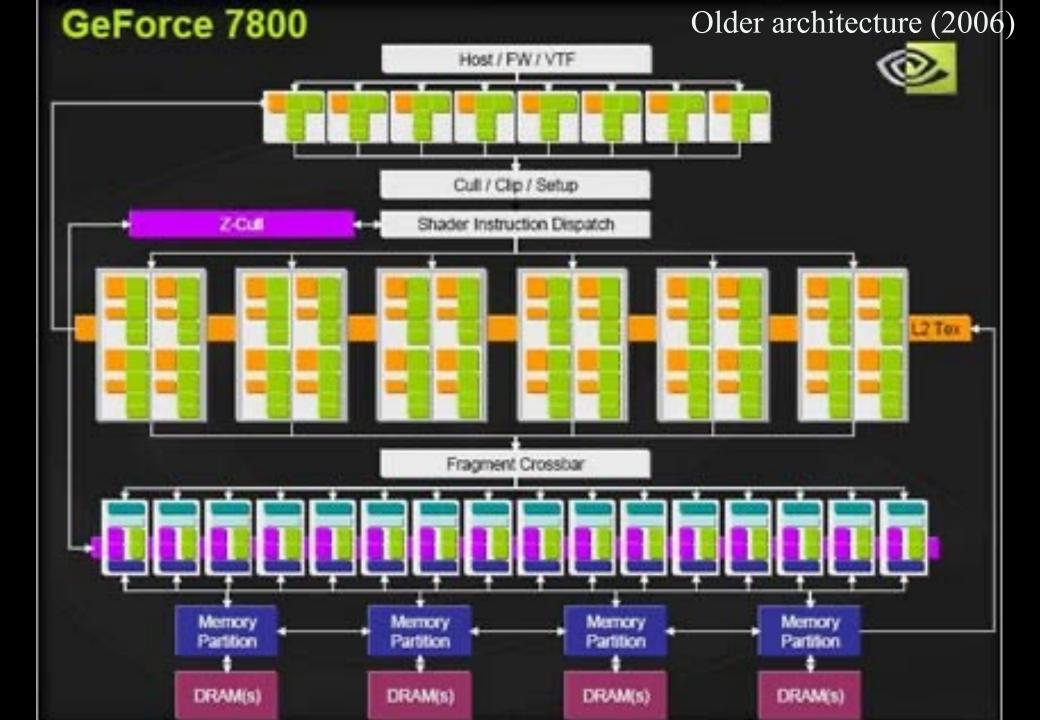
- Evolution of graphics hardware has started from the end of the pipeline
 - Rasterizer was put into hardware first (most performance to gain from this)
 - Then the geometry stage
 - Application will not be put into GPU hardware (?)

Application (A)

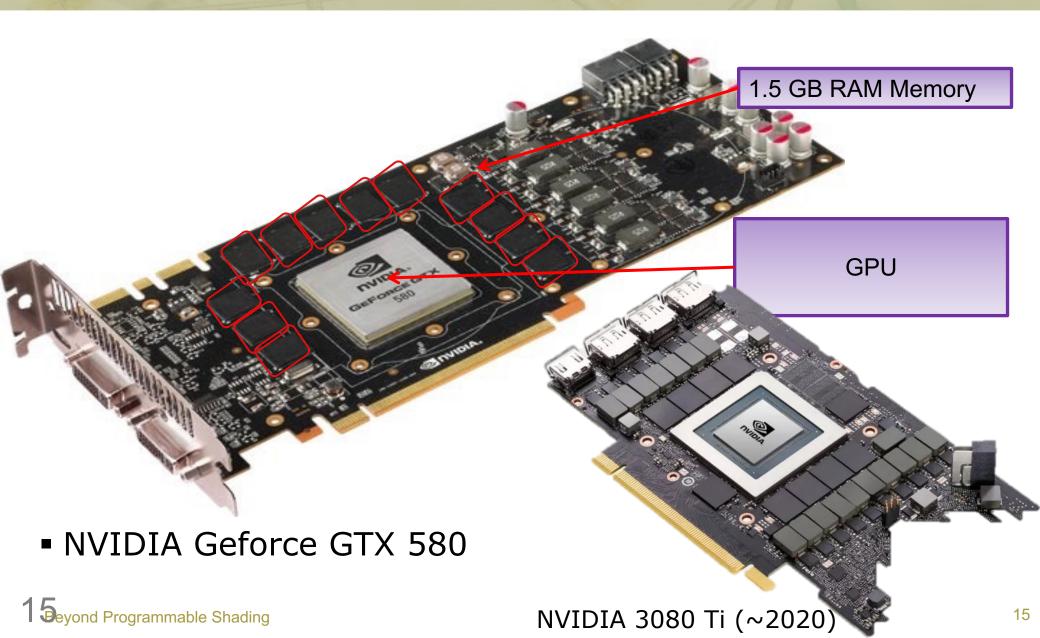
Display

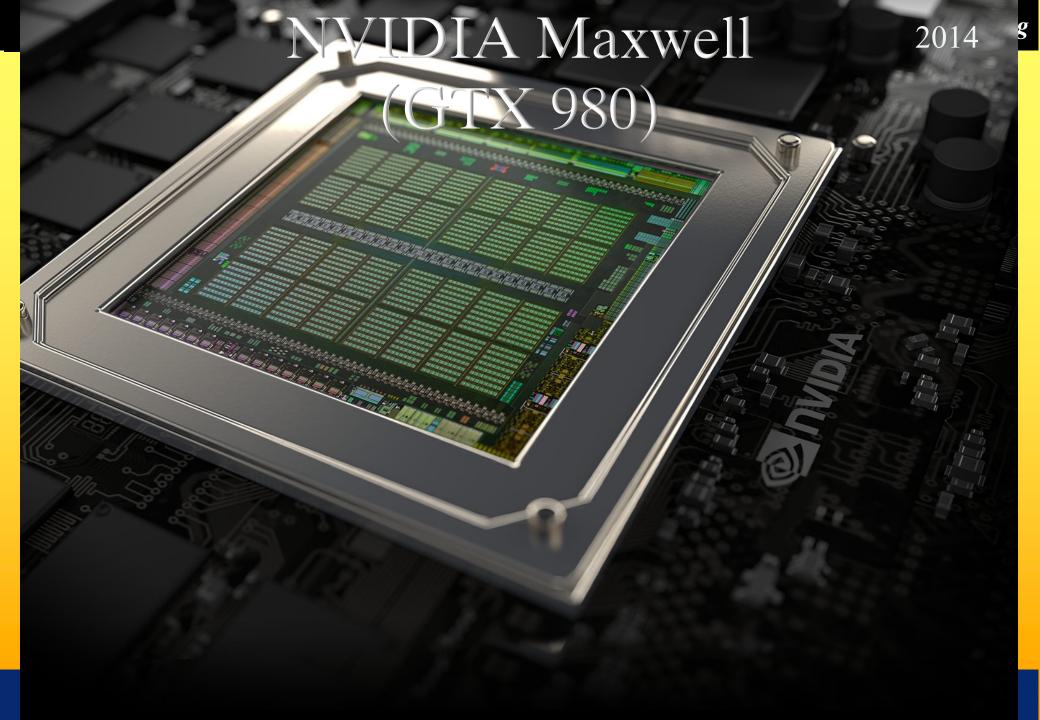
- Two major ways of getting better performance:
 - Pipelining
 - Parallellization
 - Combinations of these are often used

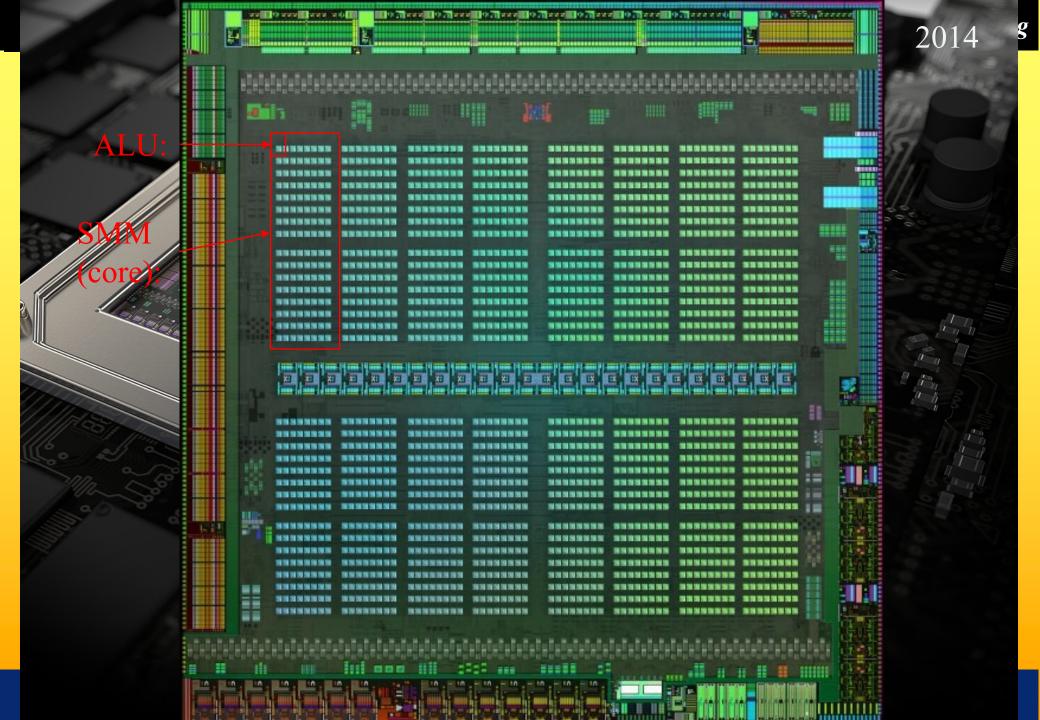




Graphics Processing Unit - GPU







CHALMERS

16 Cores ("SMM") 2MB L2 cache 64 output pixels / clock (i.e., 64 ROPs) 2048 ALUs ("cores") ~6 Tflops

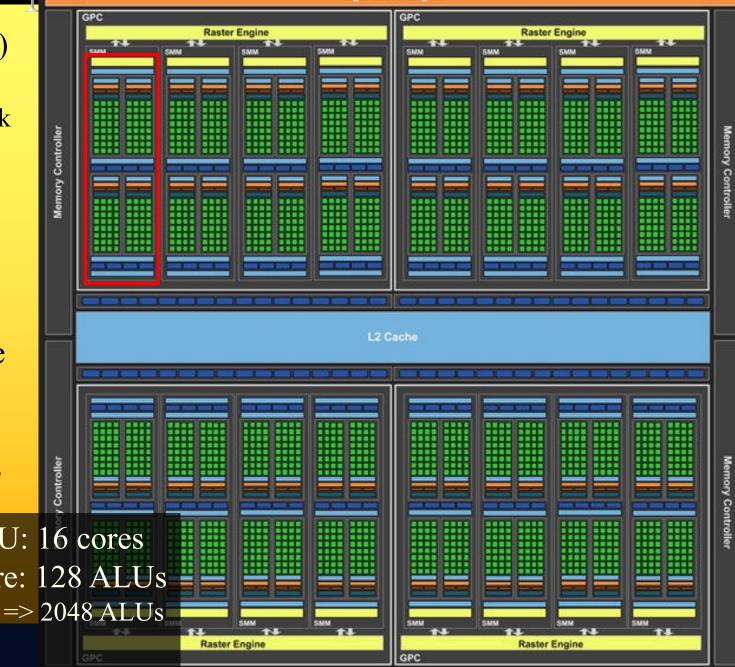
Each Core:

- 128 ALUs
- 96KB L1 cache
- 8 TexUnits

memory

32 Load/Store units for access to global

GPU: 16 cores Core: 128 ALUs



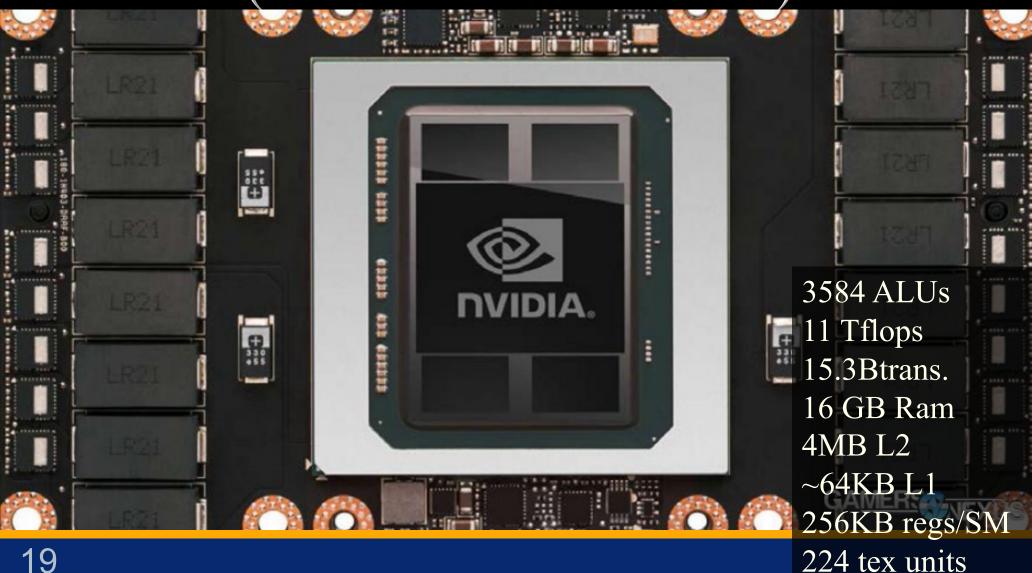
PCI Express 3.0 Host Interface

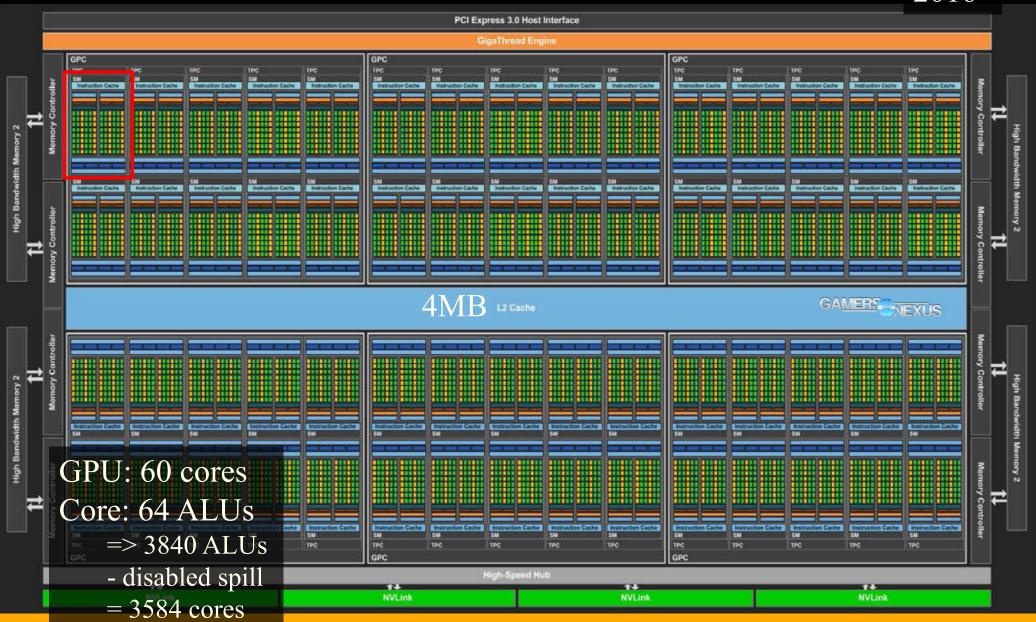
GigaThread Engine

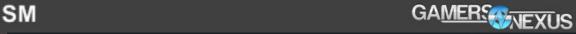
NVIDIA Pascal GP100

2016

 $(GTX \overline{1080} / Titan X)$







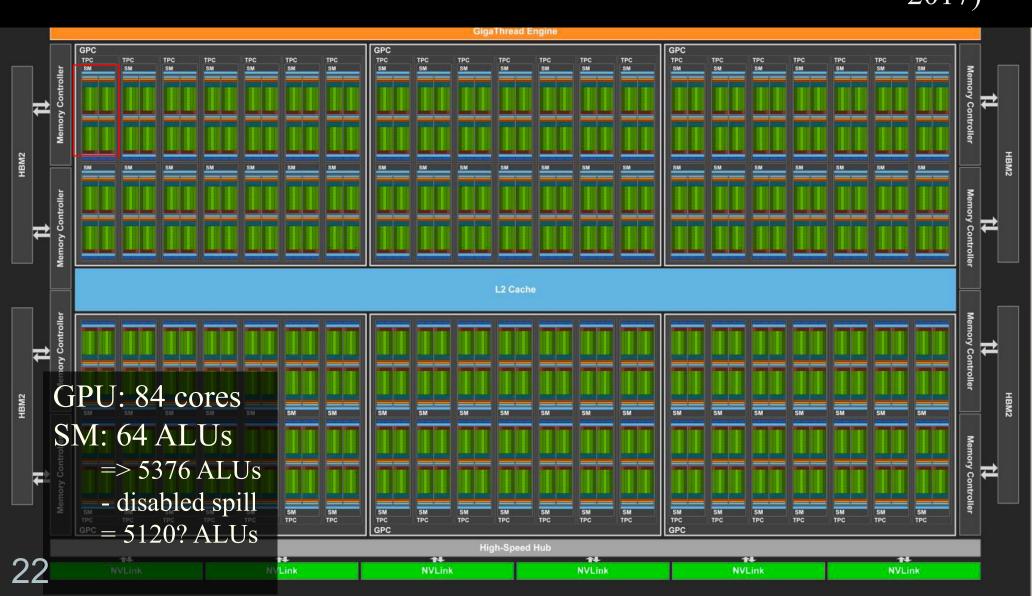
Instruction Cache



64KB Shared Memory

NVIDIA Volta GV100

2018 (Dec. 2017)



NVIDIA Volta GV100



NVIDIA Turing TU102

GPU: 36 cores

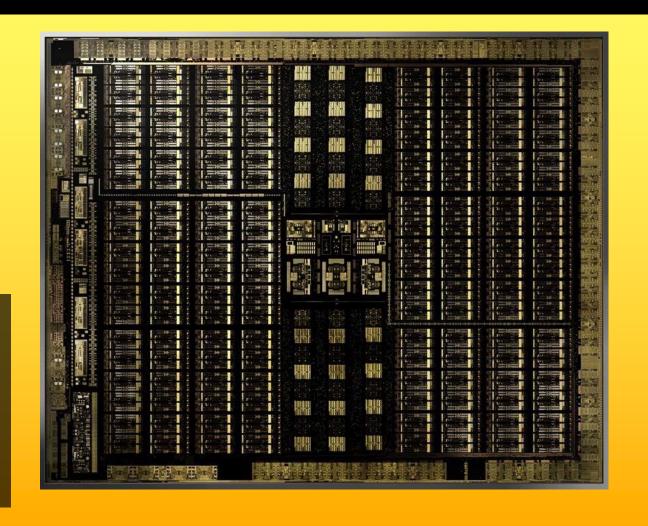
Core: 128 ALUs

=> 4608 ALUs

 $+\sim$ 550 tensor cores

+ 72 RT cores

18.6 billion transistors



NVIDIA Turing TU102

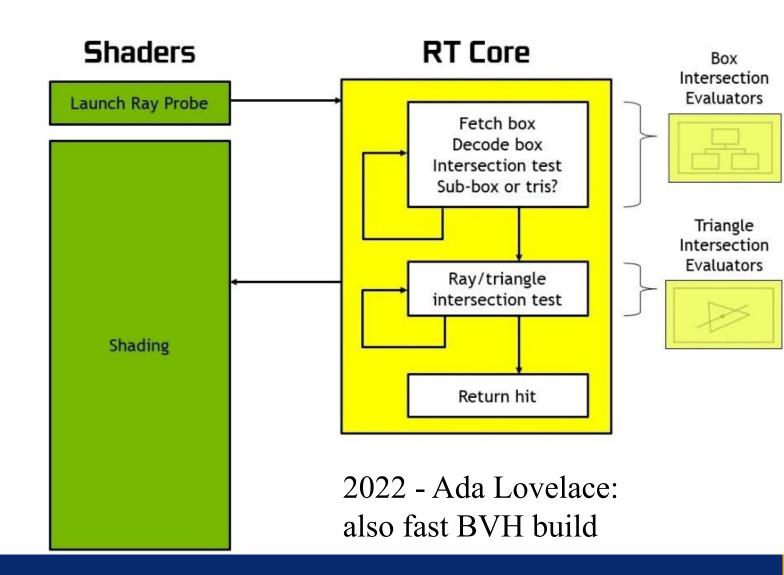


NVIDIA Turing TU102

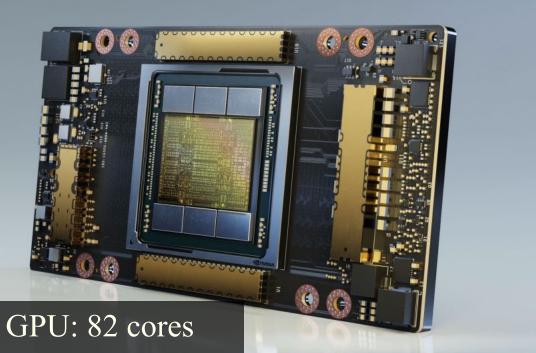
Hardware Acceleration Replaces Software Emulation







NVIDIA Ampere



Core: 128 ALUs

=> 10496 ALUs

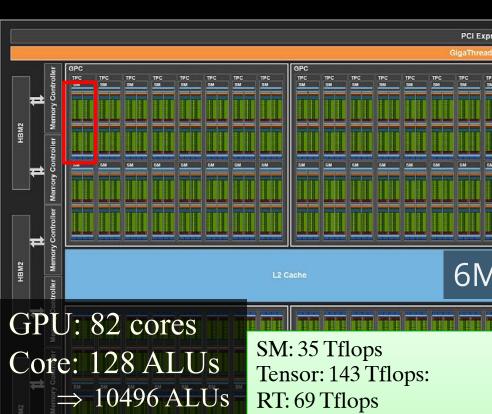
+~328 tensor cores

+82 RT cores

28.3 billion transistors



NVIDIA



~128KB L1\$

 $+\sim$ 328 tensor cores

28.3 billion transistors

+82 RT cores

Sum: ~250 Tflops.
INT8 allows for 624
 TOPS (1248 TOPS with sparsity).
INT4 doubles that to

1248 / 2496 TOPS.

SM **L0 Instruction Cache** L0 Instruction Cache Warp Scheduler (32 thread/clk Warp Scheduler (32 thread/clk Dispatch Unit (32 thread/clk) Dispatch Unit (32 thread/clk) Register File (16,384 x 32-bit) Register File (16,384 x 32-bit) NT32 INT32 FP64 NT32 INT32 FP64 FP32 FP32 NT32 INT32 NT32 INT32 FP64 FP64 NT32 INT32 FP64 NT32 INT32 FP32 FP32 FP64 **TENSOR CORE TENSOR CORE** FP64 NT32 INT32 FP64 256 FP16/FP32 FP64 NT32 INT32 FMA per clock FP64 NT32 INT32 SFU SFU

192KB L1 Data Cache / Shared Memory

Tex

Tex



Tex



Tex

NVIDIA Ada Lovelace

NVIDIA ADA LOVELACE

76 Billion Transistors | TSMC 4N Process | Micron G6X Memory

Shaders
New Streaming Multiprocessor
90 Shader TFLOPs
2X Power Efficiency

GPU: 144 cores

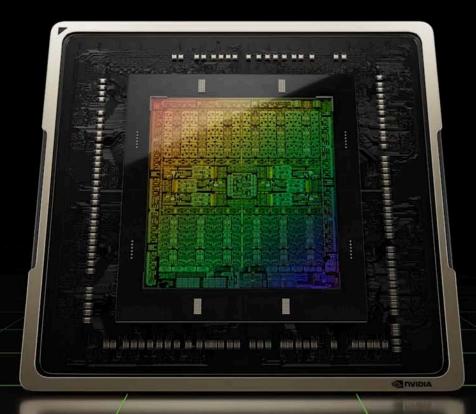
Core: 128 ALUs

=> 18432 ALUs

 $+ \sim 576$ tensor cores

+ 144 RT cores

76.3 billion transistors

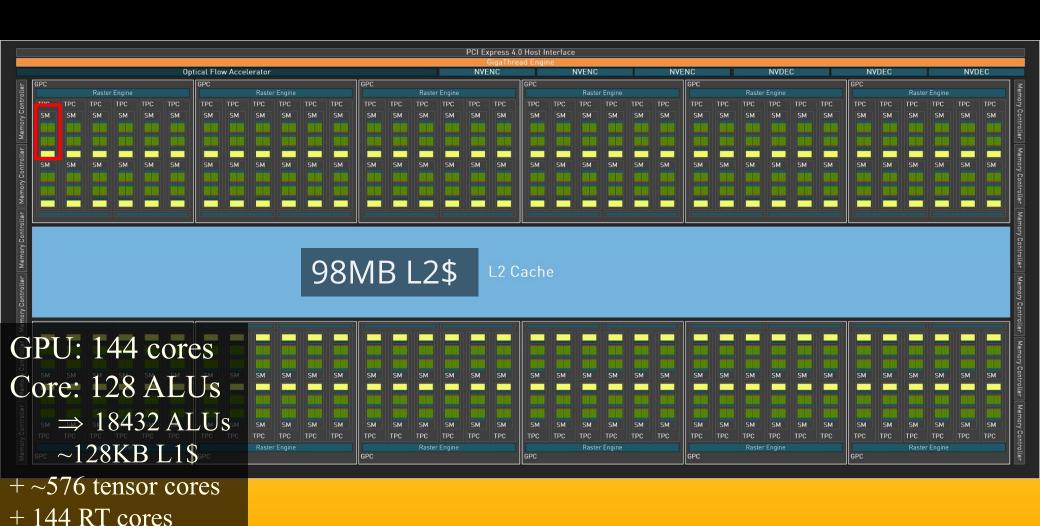


Ray Tracing
3rd-Gen RT Cores
200 RT TFLOPs
2X Ray-Triangle Intersection

Deep Learning 4th-Gen Tensor Cores 1,400 Tensor TFLOPs Optical Flow Accelerator



NVIDIA Ada Lovelace



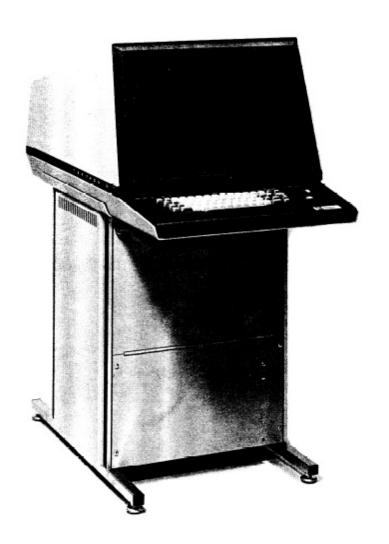
30

76.3 billion transistors

Graphics Hardware History

Direct View Storage Tube:

- Created by Tektronix (early 70's)
 - -First with "frame buffer" (moveto/lineto)
 - Did not require constant refresh
 - -Standard interface to computers
 - Allowed for standard software
 - Plot3D in Fortran
 - -Relatively inexpensive
 - Opened door to use of computer graphics for CAD community
 - -4096 * 4096 addressable points (4096 * 3120 viewable).



Graphics Hardware History - functionality

- 80's:
 - linear interpolation of color over a scanline
 - Vector graphics
- 91' Super Nintendo, Neo Geo,
 - SN: Rasterization of 1 single 3D rectangle per frame (FZero)
- 95-96': Playstation 1, 3dfx Voodoo 1
 - Rasterization of whole triangles (Voodoo 2, 1998)
- 99' Geforce (256)
 - Transforms and Lighting (geometry stage)
- 02' 3DLabs WildCat Viper, P10
 - Pixel shaders, integers,
- 02' ATI Radion 9700, GeforceFX
 - Vertex shaders and Pixel shaders with floats
- 06' Geforce 8800 also unified architecture (Radion already was).
 - Geometry shaders, integers and floats, logical operations
- Then: More general multiprocessor systems, higher SIMD-width, more cores
- 09' Tesselation Shaders (Direct3D '09, OpenGL '10). (ATI 2007)
- 17' Tensor cores
- 18' RT cores, Mesh Shaders





Graphics Hardware History - specs

- 2001 GeForce3: 600-800 pipeline stages! 57 million transistors.
 - First Pentium IV: 20 stages, 42 million transistors,

E.g., since 2004:

- #trans: ~200x increase
- Bandwidth: ~30x
- Clock freq: $\sim 2x$

- 2004 ATI X800: 165M transistors
- 2005 ATI X1800: 320M trans, 625 MHz, 750 Mhz mem, 10Gpixels/s, 1.25G verts/s
- 2004 GeForce 6800: 222 M transistors, 400 MHz, 400 MHz core/550 MHz mem
- 2005 GeForce 7800: 302M trans, 13Gpix/s, 1.1Gverts/s, 430 MHz core, mem bw 54GB/s, 650MHz(1.3GHz)
- 2006 GeForce 8800: 681M trans, 39.2Gpix/s, 10.6Gverts/s, 612/1500 MHz core, 103.7 GB/s, 1080/2160GDDR3
- 2008 Geforce 280 GTX: 1.4G trans, 65nm, 602/1296 MHz core, 142GB/s, 1107(*2)MHz mem, 48Gtex/s
- 2007 ATI Radeon HD 5870: 2.15G trans, 40nm, 850 MHz, 153GB/s, GDDR5, 256bit mem bus,
- 2010 Geforce GTX480: 3Gtrans, 700/1401 MHz core, Mem 177.4GB/s, 1.848G(*2)GHz, 384bit mem bus, 40Gtex/s
- 2011 GXT580: 3Gtrans, 772/1544, Mem: 192.4GB/s, 2004/4008 MHz, GDDR5, 384bit mem bus, 49.4 Gtex/s
- 2012 GTX680: 3.5Gtrans (7.1 for Tesla), 1006/1058, 192.2GB/s, 6GHz GDDR5, 256-bit mem bus.
- 2013 GTX780: 7.1G, core clock: 837MHz, 336 GB/s, Mem clock: 6GHz GDDR5, 384-bit mem bus
- 2014 GTX980: 7.1G?, core clock: ~1200MHz, 224GB/s, Mem clock: 7GHz GDDR5, 256-bit mem bus
- 2015 GTX Titan X: 8Gtrans, core clock: ~1000MHz, 336GB/s, Mem clock: 7GHz GDDR5, 384-bit mem bus
- 2016 Titan X: 12/15Gtrans, core clock: ~1500MHz, 480GB/s, Mem clock: 10Gbps GDDR5X, 4096-HBM2
- 2018 Nvidia Volta: 21.1Gtrans, core clock: ~1500MHz. 600GB/s, Mem: 14Gbps 4096-bit HBM2 (or GDDR6)
- 2020 Nvidia Ampere: 54 Gtrans, ~1500MHz, 1008 GB/s, Mem: 21Gbps, 4096-bit HBM2, (or GDDR6)
- 2022 Nvidia Ada Lovelace: 76 Gtrans, 2.2-2.5 GHz, 1008 GB/s, Mem: 21Gbps, GDDR6X, 384-bit mem bus

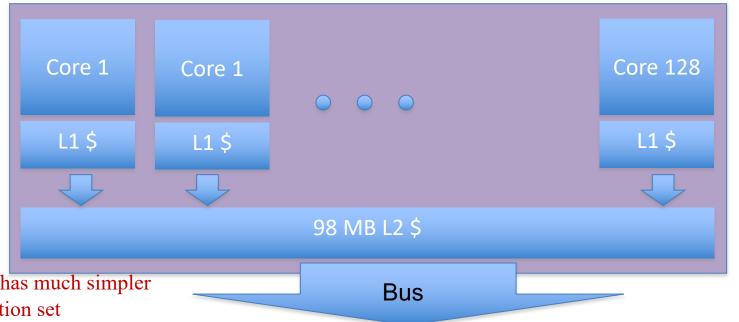
Lesson learned: #trans doubles ~per 2 years. Core clock increases slowly. Mem clock –increases with new technology DDR2, DDR3, GDDR5/6, HBM2, GDDR6X. We use the fastest memory available, despite costs.

- We want as fast memory as possible! Why?
 - Parallelization can cover for slow core clock. Parallelization more energy efficient than high clock frequency; power consumption is proportional to freq².
 - Memory transfers are often the bottleneck

GPU- Nvidia's Ada Lovelace 2022

RTX 4090:

Overview:



128 cores à **128 ALUs**

~128 KB L1\$ per core

Bandwidth ~1 TB/s

Bus: 384 bits

GPU core has much simpler

- instruction set
- cache hierarchy

than a CPU core.

High parallelism, but

bandwidth is a major problem.

Wish:

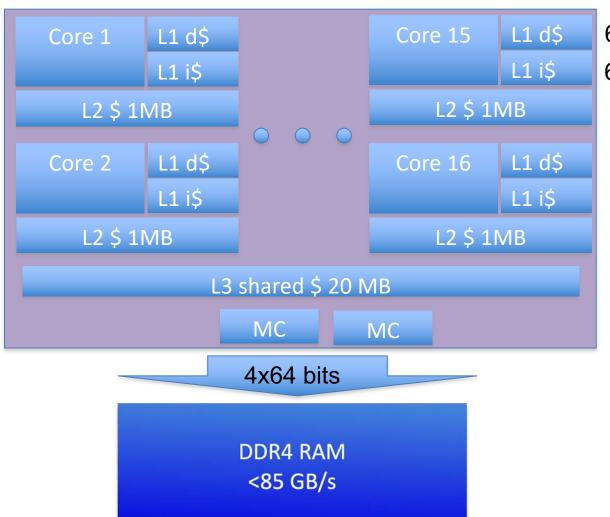
~16.384 ALUs à 1 float.op/clock => 64KB/clock cycle

~2.2GHz core clock => 144 TB/s request

We have ~1TB/s. Hence, would need to do ~144 computations between each RAM–read/write. Ameliorated by L1\$ + L2\$ + latency hiding (warp switching) but still a main problem!

RAM – GDDR6X

CPU - 2021



- 64 KB ~16 cores à 8 SIMD floats
 - With 16 cores à 8 floats
 - ⇒ We want **512** bytes/clock (e.g. from RAM).
 - 3GHz CPU => 1.5 TByte/s.
 (In addition x2, both for GPU & CPU, since:

$$r1 = r2 + r3;$$
)

We only have **85** GB/s due to cheaper DDR4 RAM and only 4x64 bits buses.

Solved by \$-hierarchy + registers + thread switching

- Wish: GPU 144TB/s vs CPU 1.5 TB/s ≈ 100x diff.
- You could say bandwidth is 2 orders of magnitude more important on GPU than CPU, due to parallelism. And GPU is ~10x more bandwidth limited than CPU (GPU has 10x higher bandwidth).

Memory bandwidth usage is huge!!

- On top of that bandwith usage is never 100%.
- However, there are many techniques to reduce bandwith usage:
 - Texture caching with prefetching
 - Texture compression
 - Hierarchical Z-occlusion testing
 - E.g., for every 8x8 pixel block of frame buffer, store its z_{min} , z_{max} .
 - If triangle is behind pixel block, skip rasterize it.
 - If triangle is in front, skip accessing 8x8 individual z-values.



Taxonomy of hardware design

for how to resynchronize (sort) parallelized work.

Outputs to frame buffers must respect incoming triangle order.

Take-aways: Sort-first, Sort-middle, Sort-Last Fragment, Sort-Last Image

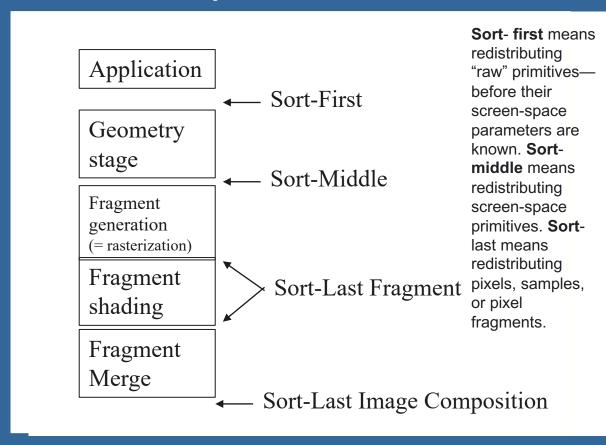
Taxonomy of Hardware

- We can do many computations in parallel:
 - Pixel shading, vertex shading, geometry shading
- But result on screen must be as if each triangle were rendered one by one in their incoming order (according to OpenGL spec)
 - I.e., for every pixel, the rasterized fragments must be merged to the buffers in the original input triangle order
 - E.g., for blending/transparency, (z-culling + stencil test)
- Hence, results need to be sorted somewhere before reaching the screen...

Taxonomy of hardware

Need to sort the results of the parallelization

- Gives four major architectures:
 - Sort-first
 - Sort-middle
 - Sort-Last Fragment
 - Sort-Last Image



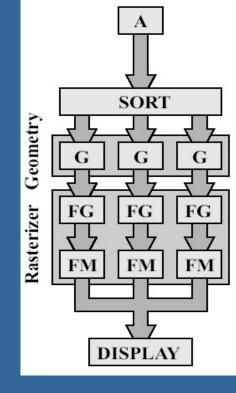
 Will describe these briefly. Sort-last fragment (and sort middle) are most common in
 commercial hardware

Sorting/dividing work to parallel execution units.

Sort-First



- Sorts primitives before geometry stage
 - E.g., screen in divided into large regions
 - Blocks or scanlines
 - A separate pipeline is responsible for each region (or many)
- Not explored much at all, since:
 - Poor load balancing if uneven triangle distribution between regions.
 - Vertex shader can change triangle position
 - GPUs are not pipelined like this any longer

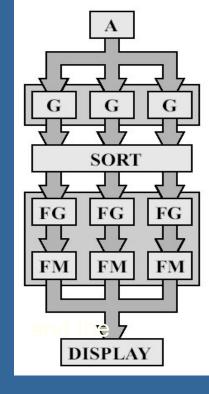


Explanation of image: G is geometry, FG & FM is part of rasterizer (R)

- A fragment is all the generated information for a pixel on a triangle
- FG is Fragment Generation (finds which pixels are inside triangle)
- FM is Fragment Merge (merges the created fragments with various buffers (Z, color))

Sort-Middle

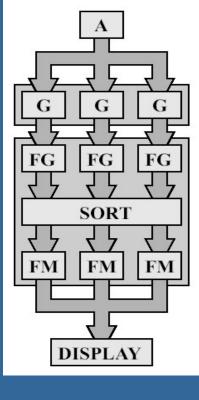
- A B A B A
- Sorts betwen G and R stage
 - i.e., after vertex and geometry shader
 - Pretty natural, since after G, we know the screen-space positions of the triangles
- Older cheaper hardware used this
 - Examples include InfiniteReality (from SGI)
 KYRO architecture (from Imagination)
- Spread work arbitrarily among G pipelines
- Then depending on screen-space position, sort to different R's
 - Screen can be split into "tiles". For example:
 - Rectangular blocks (8x8 pixels)
 - Or every n scanlines
- The R is responsible for rendering inside tile
- Bads (same as Sort-First):
 - A triangle can be sent to many FG's depending on overlap (over tiles)
 - May give poor load balancing if triangles are unevenly distributed over the screen tiles



Sort-Last Fragment

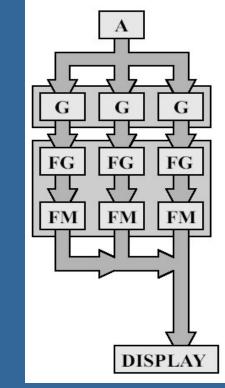


- Sorts between FG and FM
 - After rasterization
- Most graphics cards use this somehow.
 - Each pixel block is responsible for sorting its fragments according to original triangle render order.
 - One typical block size: 4x8 pixels
- Example how it could work:
 - Take pixel block from queue, based on triangle order
 - test hiearchical z-culling
 - Execute shaders
 - Merge
- Good load balancing for all stages before FM.
- Small pixel blocks give good load balancing on screen
- With triangle sizes roughly similar to block sizes, there are not so many more blocks to sort vs sorting triangles in Sort-First and Sort-Middle.



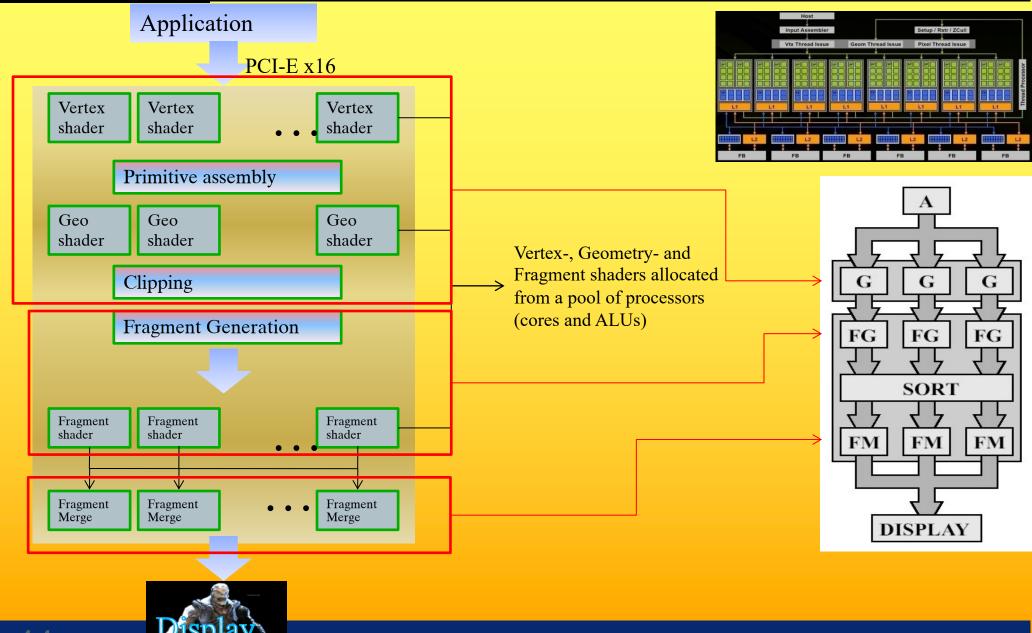
Sort-Last Image

- Sorts after entire pipeline
- So each FG & FM has a separate frame buffer for entire screen (Z and color)
 - Typically: one whole graphics card per pipeline.



- After all primitives have been sent to the pipeline, the z-buffers and color buffers are merged into one color buffer
- Can be seen as a set of independent pipelines
- Huge memory requirements!
- Used in research, but not much commerically.
- Problematic for transparency.

Functional layout of the graphics pipeline and relation to a graphics card:



The history implies the future

- Cell 2005, Sony Playstation 3
 - 8 cores à 4-float SIMD, 256KB L2 cache/core, 3.2 GHz
- NVIDIA 8800 GTX Nov 2006
 - 16 cores à 8-float SIMD (GTX 280 30 cores à 8, june '08)
 - 16 KB L1 cache, 64KB L2 cache
 - 1.2-1.625 GHz
- NVIDIA Fermi GF100 2010, (GF110 2011)
 - 16 cores à 2x16-float SIMD (1x16 double SIMD)
 - 16/48 KB L1 cache, 768 KB L2 cache
- NVIDIA Kepler 2012 16 cores à 2x3x16=96 float SIMD
- NVIDIA Kepler 2013 16 cores à 2x6x16=192 float SIMD
- NVIDIA Titan X 2016 60 cores à 2x4x8=64 float SIMD
- NVIDIA Volta 2018 84 cores à 64 float SIMD + 640 tensor cores (16-bit matrix mul+add)

 NVIDIA Turing 2018 36 cores à 128 float SIMD + ~550 tensor cores (16-bit matrix mul+add) + 72 RT cores
- NVIDIA Ampere 2020 82 cores à 128 ALUs + ~328 tensor cores + 82 RT cores
- NVIDIA Ada Lovelace 2022 144 cores à 128 ALUs + ~576 tensor cores + 144 RT cores

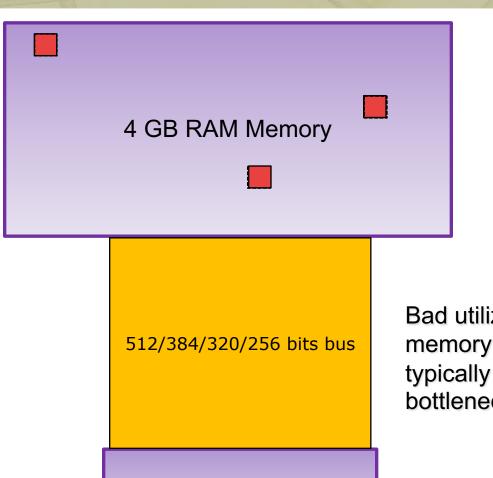
If we have time...

How create efficient GPU programs?

Answer: coallesced memory accesses

Graphics Processing Unit - GPU

Conceptual layout:

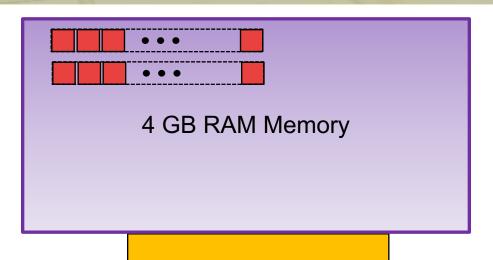


GPU

Bad utilization of the memory bus, which typically is the bottleneck!

= memory element (32 bits)

Graphics Processing Unit - GPU



Read 32 coallesced floats for max bandwidth usage

512/384/320/256 bits bus

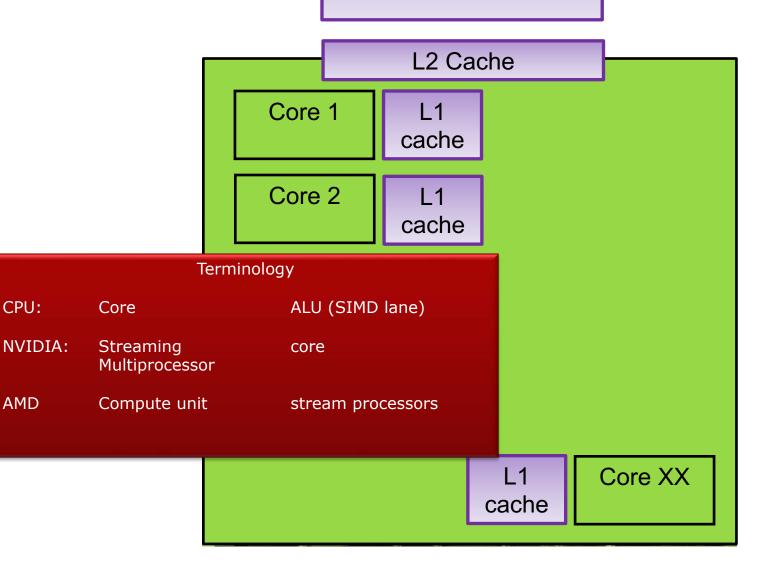
GPU

Much better utilization of the memory bus!

= memory element (32

Let's look a

Lots of GB RAM



Core X

N*32 ALUs or "lanes" or threads. Nx32 mul/add per ~1 clock cycle

In principle, all must do the same instruction (add/mul), but on different data.

CPU:

AMD

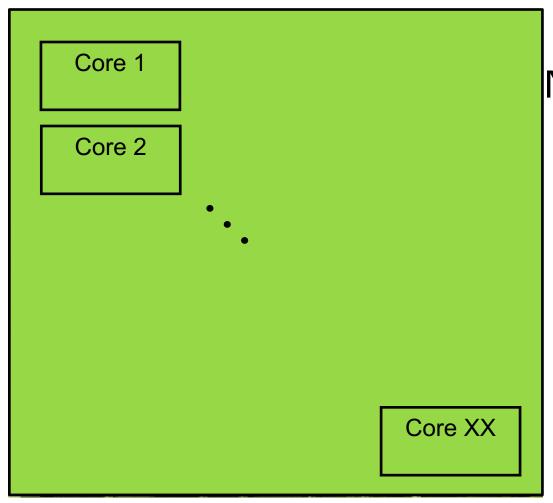
Let's look at the GPU

Each core:

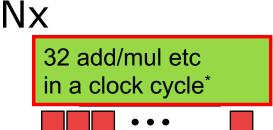
executes one program (=shader).

Each cycle:

• N*32 flops
These days, can
be a few different
instr.



From RAM or L1/L2 cache



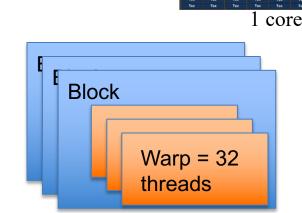
To RAM or L1/L2 cache

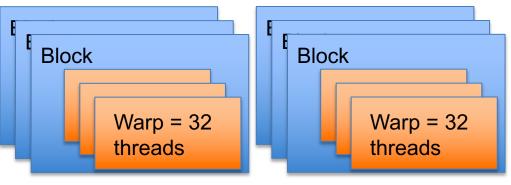
Low level APIs for GPU programming

- CUDA
 - C++ compiler
 - Works best for NVIDIA GPUs
 - CUDA SDK
 - Numerous examples and documentation (most for single GPU)
 - Has most functionality
- OpenCL
 - C compiler
 - Platform independent
 - AMD
 - NVIDIA
 - Less control/functionality than CUDA
- Compute Shaders (DirectX, OpenGL).

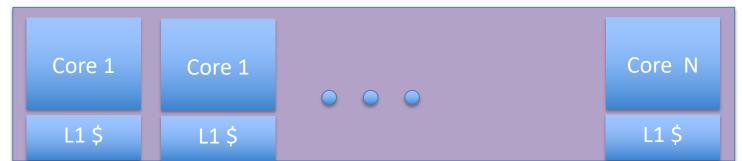
CUDA

- A kernel (=CUDA program) is executed by 100:s-1M:s
 - threads
 - A "warp" = 32 threads, one thread per ALU
 - Warps (one to ~32) are grouped into one block
 - Block: executed on one core
 - One to 48 warps execute on a core





Max one program per block.
One program counter per warp.



Read coalesced blocks

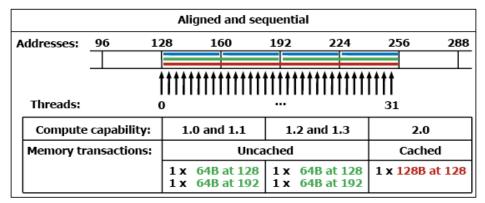
Global mem accesses.

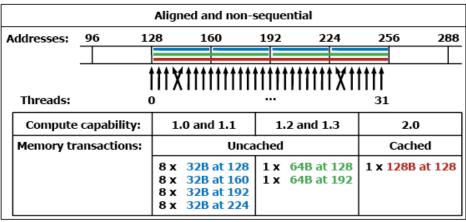
One transaction:

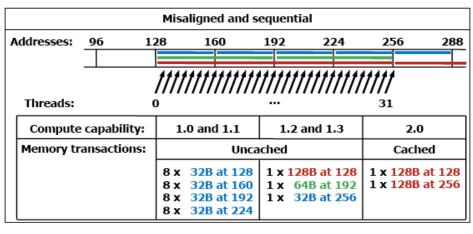
Bandwidth to GPU RAM is the most precious resource, so two transactions is often bad.

Two transactions:

Global memory instructions support reading or writing words of size equal to 1, 2, 4, 8, or 16 bytes. Any access (via a variable or a pointer) to data residing in global memory compiles to a single global memory instruction if and only if the size of the data type is 1, 2, 4, 8, or 16 bytes and the data is naturally aligned (i.e., its address is a multiple of that size).



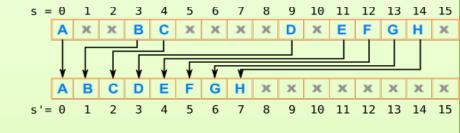


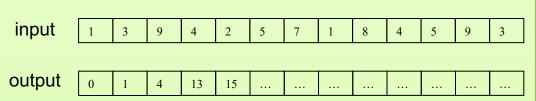


Fermi: Examples of Global Memory Accesses by a Warp, 4-Byte Word per Thread, and Associated Memory Transactions Based on Compute Capability

Efficient Programming

- If your program can be constructed this way, you are a winner!
- More often possible than anticipated
 - Stream compaction
 - Prefix sums
 - Sorting



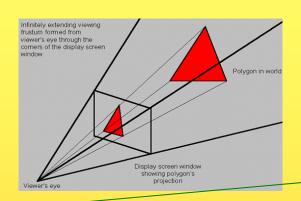


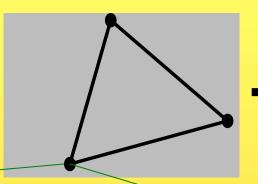


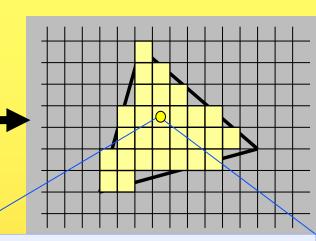
19 5 100 1 63 79 1 5 19 63 79 100

Fermi: 16 multi-processors à 2x16 SIMD width

Shaders







```
// Vertex Shader
#version 130

in vec3 vertex;
in vec3 color;
out vec3 outColor;
uniform mat4 modelViewProjectionMatrix;

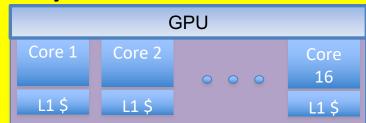
void main()
{
    gl_Position = modelViewProjectionMatrix*vec4(vertex,1);
    outColor = color;
}
```

```
// Fragment Shader:
#version 130
in vec3 outColor;
out vec4 fragColor;

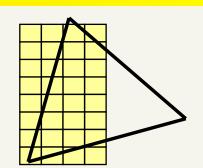
void main()
{
    fragColor = vec4(outColor,1);
}
```

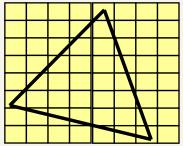
Shaders and coallesced memory accesses

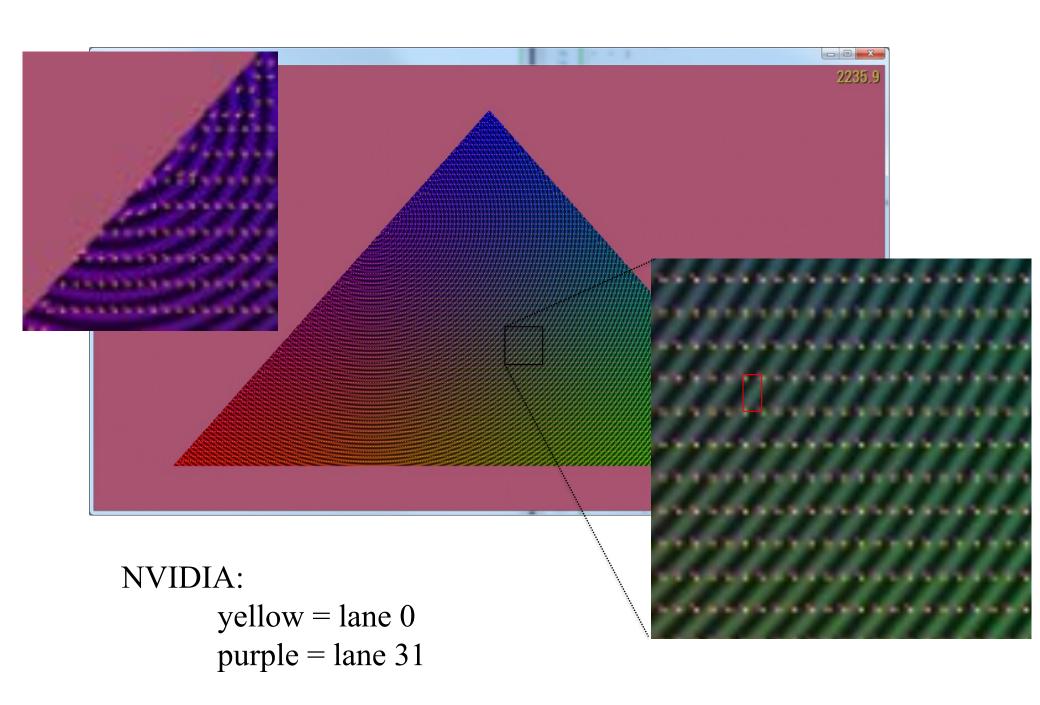
• Each core (e.g. 128-SIMD) typically executes the same instruction per clock cycle for either a:



- Vertex shader:
 - E.g. 128 vertices
- Geometry shader
 - E.g. 128 triangles
- or Fragment shader:
 - E.g. 128 pixels
 in blocks of at least 2x2 pixels
 (to compute texture filter derivatives) .
 Here is an example of blocks
 4x8 = 32 pixels:
- However, many architectures can execute different instructions, of the same shader, for different warps (warp = group of 32 ALUs)

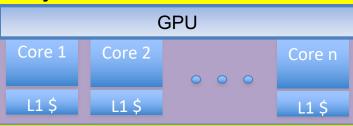


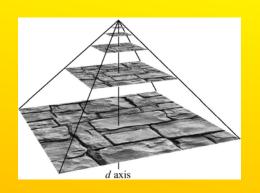


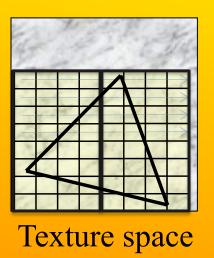


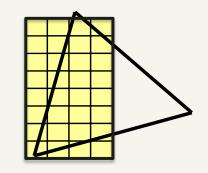
Shaders and coallesced memory accesses

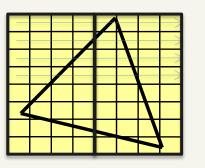
 For mipmap-filtered texture lookups in a fragment shader, this can provide decently coallesced memory accesses.











Thread utilization

- Each core executes one program (=shader)
- Each of the 192 ALUs execute one "thread" (a shader for a vertex or fragment)
- Since the core executes the same instruction for at least 32 threads (as far as the programmer is concerned)...
- If (...)
 - Then, a = b + c;
 - **–** ...
- Else

$$- a = c + d;$$

...the core must execute both paths if any of the 32 threads need the if and else-path.

But not if all need the same path.

Summary

Need to know:

- Linearly interpolate $(u_i/w_i, v_i/w_i, 1/w_i)$ in screenspace from each triangle vertex i. Then at each pixel:
 - $u_{ip} = (u/w)_{ip} / (1/w)_{ip}$ $v_{ip} = (v/w)_{ip} / (1/w)_{ip}$

where ip = screen-space interpolated value from the triangle vertices.

- Perspective correct interpolation (e.g. for textures)
- Taxonomy:
 - Sort first
 - sort middle
 - sort last fragment
 - sort last image
- Bandwidth
 - Why it is a problem and how to "solve" it
 - L1 / L2 caches
 - Texture caching with prefetching, (warp switching)
 - Texture compression, Z-compression, Z-occlusion testing (HyperZ)
- Be able to sketch the functional blocks and relation to hardware for a modern graphics card (next slide→)

