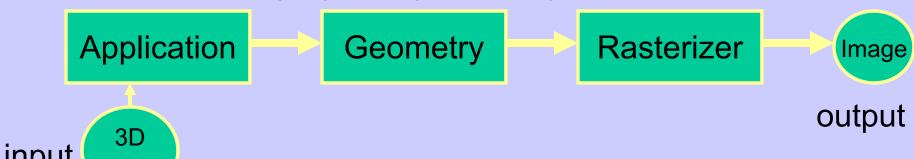
Full-time wrapup

Lecture 1

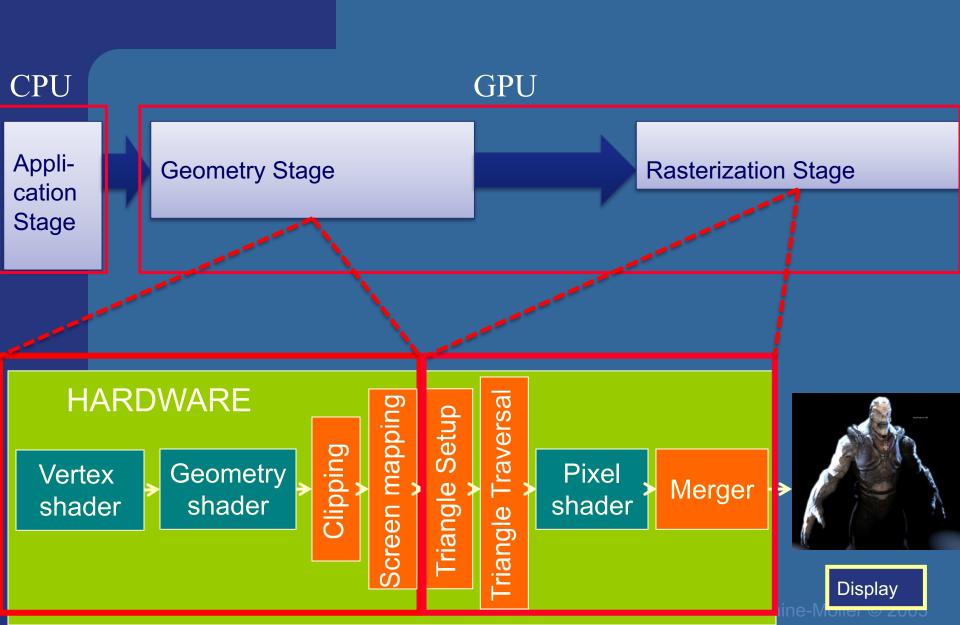
- Application-, geometry-, rasterization stage
- Real-time Graphics pipeline
- Modelspace, worldspace, viewspace, clip space, screen space
- Z-buffer
- Double buffering
- Screen tearing

Lecture 1: Real-time Rendering The Graphics Rendering Pipeline

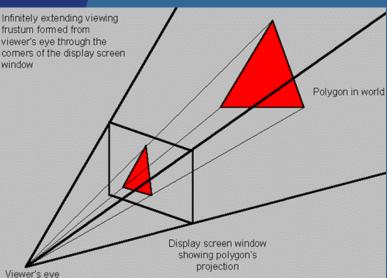
- Three conceptual stages of the pipeline:
 - Application (executed on the CPU)
 - logic, speed-up techniques, animation, etc...
 - Geometry
 - Executing vertex and geometry shader
 - Vertex shader:
 - lighting computations per triangle vertex
 - Project onto screen (3D to 2D)
 - Rasterizer
 - Executing fragment shader
 - Interpolation of per-vertex parameters (colors, texcoords etc) over triangle
 - Z-buffering, fragment merge (i.e., blending), stencil tests...



Rendering Pipeline and Hardware

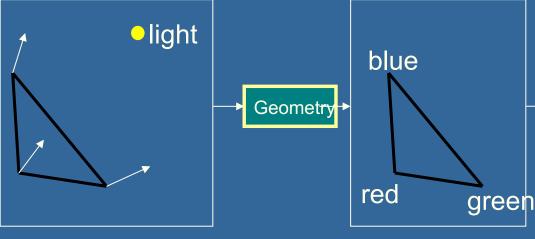


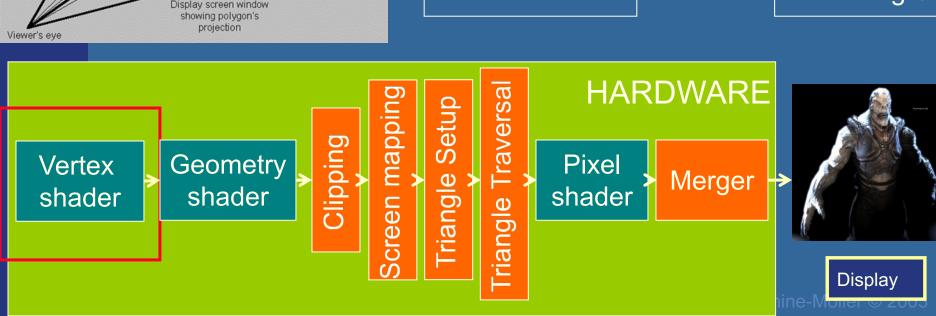
Geometry Stage

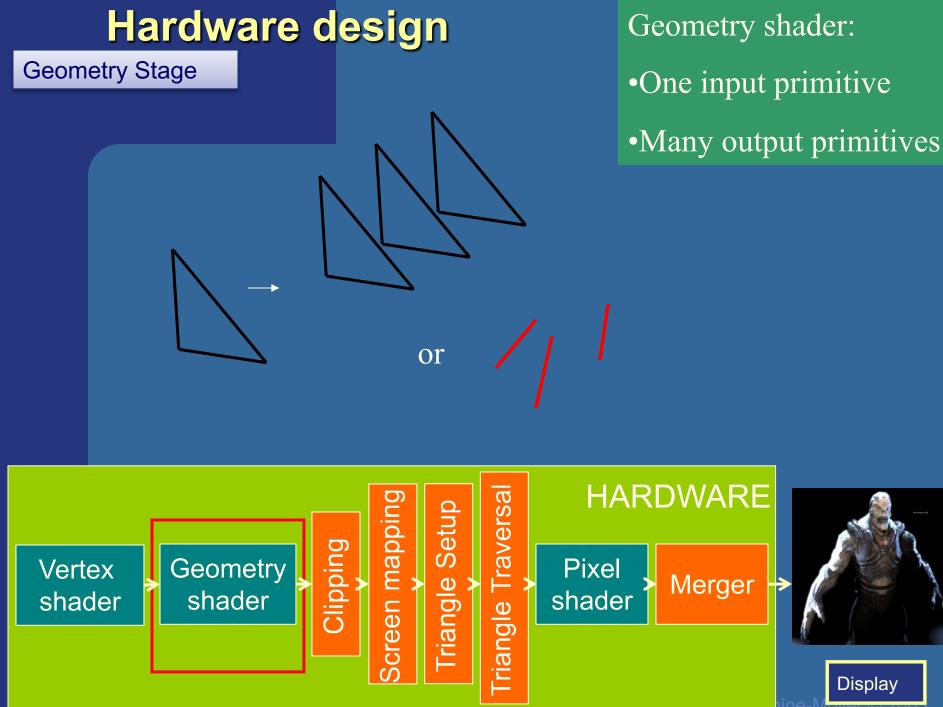


Vertex shader:

- Lighting (colors)
- •Screen space positions

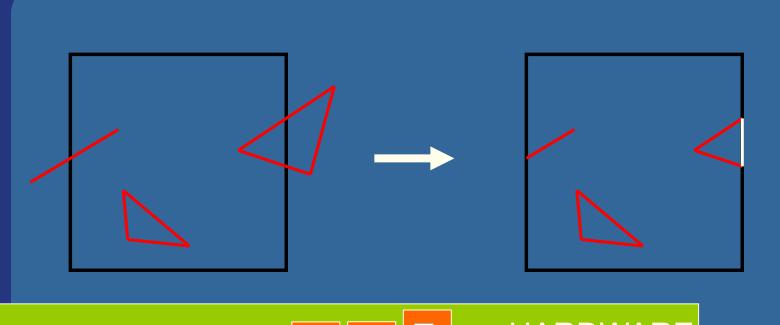






Geometry Stage

Clips triangles against the unit cube (i.e., "screen borders")



Setup

Triangle

Vertex shader Shader

Clipping Screen mapping

riangle Trav

HARDWARE

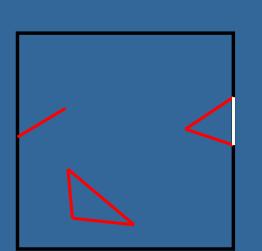
Pixel shader

Merger



Display

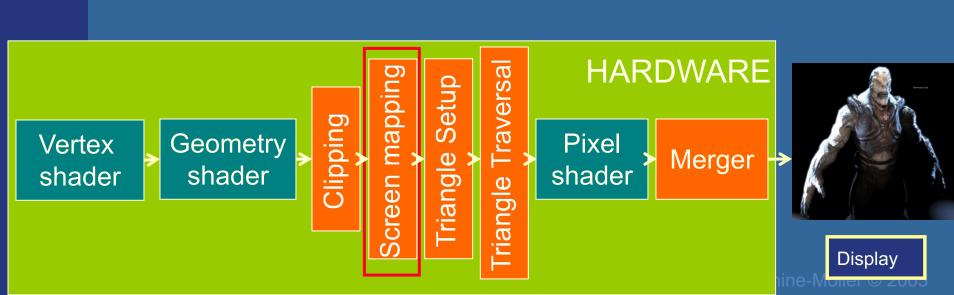
Rasterizer Stage



Maps window size to unit cube

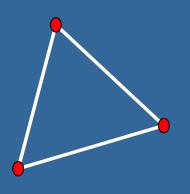
Geometry stage always operates inside a unit cube [-1,-1,-1]-[1,1,1] Next, the rasterization is made against a draw area corresponding to window dimensions.

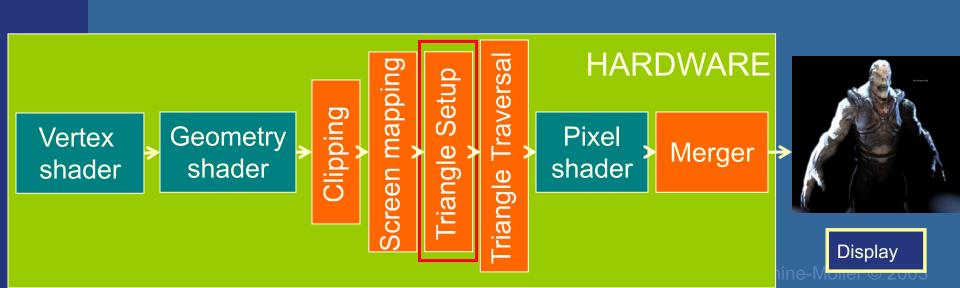




Rasterizer Stage

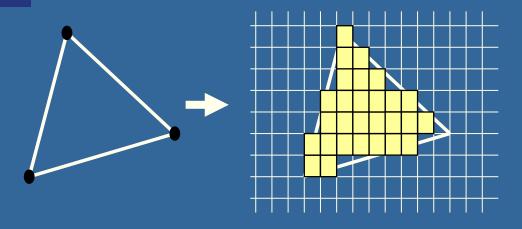
Collects three vertices into one triangle

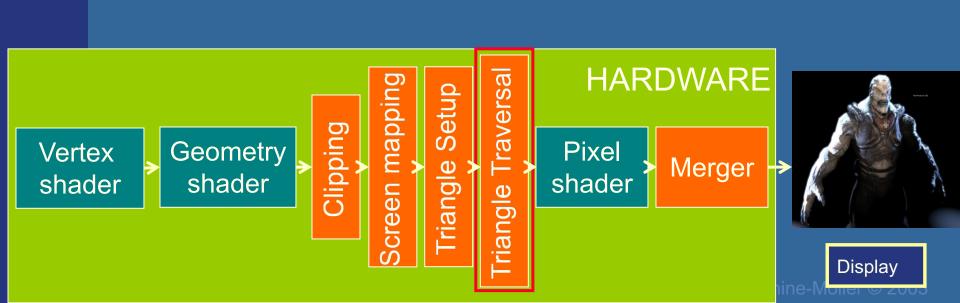


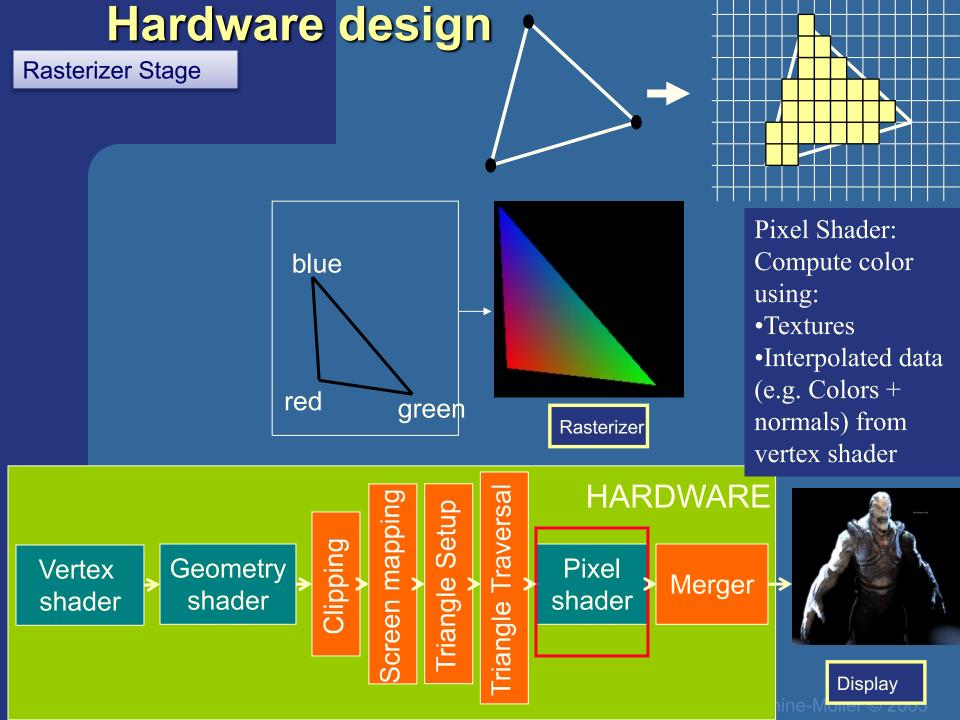


Rasterizer Stage

Creates the fragments/pixels for the triangle







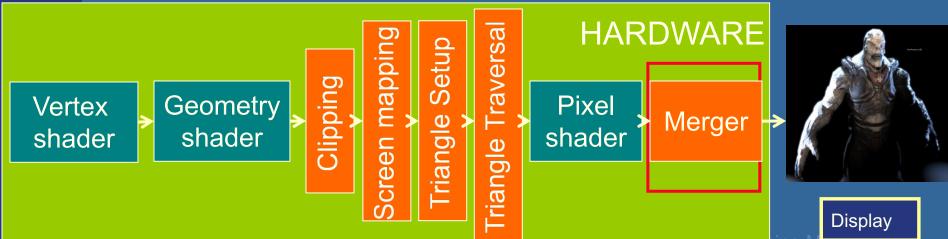
Rasterizer Stage

The merge units update the frame buffer with the pixel's color

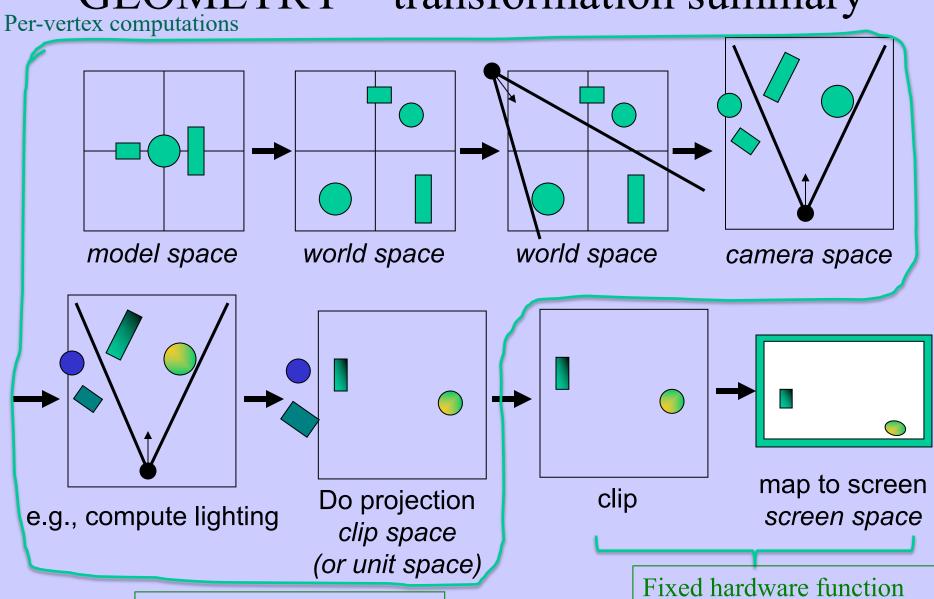


Frame buffer:

- Color buffers
- Depth buffer
- Stencil buffer



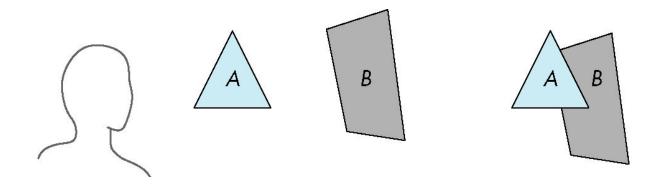
GEOMETRY – transformation summary



Done in vertex shader

Painter's Algorithm

 Render polygons a back to front order so that polygons behind others are simply painted over



B behind A as seen by viewer

- Requires ordering of polygons first
 - –O(n log n) calculation for ordering
 - –Not every polygon is either in front or behind all other polygons

Fill B then A

I.e., : Sort all triangles and render them back-to-front.

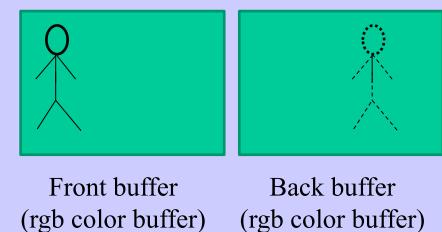
z-Buffer Algorithm

- Use a buffer called the z or depth buffer to store the depth of the closest object at each pixel found so far
- As we render each polygon, compare the depth of each pixel to depth in z buffer
- If less, place shade of pixel in color buffer and update z buffer

Also know double buffering!

The RASTERIZER double-buffering

 We do not want to show the image until its drawing is finished.



The front buffer is displayed

rate.

Last fully finished drawn frame.

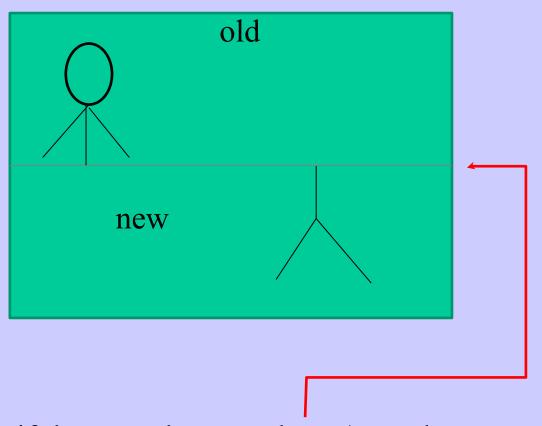
Application

Color buffer we draw to.

Not displayed yet.

- The back buffer is rendered to
- When new image has been created in back buffer, swap the Front-/Back-buffer pointers.
- Use vsynch or screen tearing will occur...
 i.e., when the swap happens in the middle of the screen with respect to the screen refresh

The RASTERIZER Application Geometry double-buffering — screen tearing



Example if the swap happens here (w.r.t the screen refresh rate). Solution: use vsynch to swap buffers after monitor has "updated" the screen. See page 1011-1012.

Screen Tearing

Swapping

back/front buffers



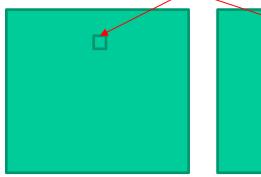
Screen tearing is solved by using V-Sync.

V-Sync: swap front/back buffers during vertical blank (vblank) instead.

The default frame buffer:

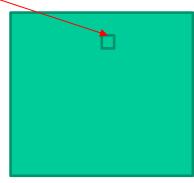
Typically: Front + Back color buffers + Z buffer + (Stencil buffer)

Stores rgb(a) value per pixel. Default: 8 bits per r,g,b channel.



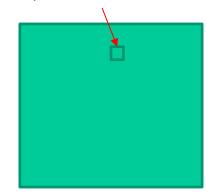
Front buffer (rgb color buffer)

Last fully finished drawn frame.
Is displayed.



Back buffer (rgb color buffer)

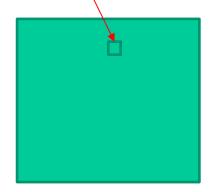
Color buffer we draw to. Not displayed yet. Stores fragment's depth value per pixel, typically: (16), 24, or 32 bits.



Z buffer (depth)

To resolve visibility

Stencil buffer can be asked for. 8-bits per pixel.



Stencil buffer

Used for masking rendering to only where pixel's stencil value = some specific value.

Lecture 2: Transforms

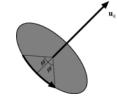
- Transformation pipeline: ModelViewProjection matrix
- Scaling, rotations, translations, projection
- Cannot use same matrix to transform normals

Use:
$$\mathbf{N} = (\mathbf{M}^{-1})^T$$
 instead of \mathbf{M} $(\mathbf{M}^{-1})^T = \mathbf{M}$ if rigid-body transform

- Homogeneous notation
- Rigid-body transform, Euler rotation (head,pitch,roll)
- Change of frames
- Quaternions $\hat{\mathbf{q}} = (\sin \phi \mathbf{u}_q, \cos \phi)$
 - Know what they are good for. Not knowing the mathematical rules.

$$\hat{\mathbf{q}}\hat{\mathbf{p}}\hat{\mathbf{q}}^{-1}$$

...represents a rotation of 2φ radians around axis
 uq of point p

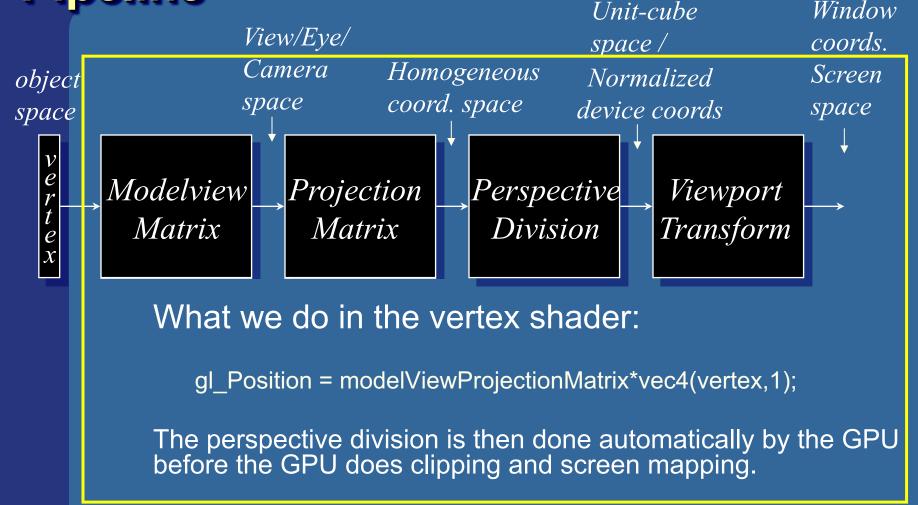


- Understand the simple DDA algorithm
- Bresenhams line-drawing algorithm

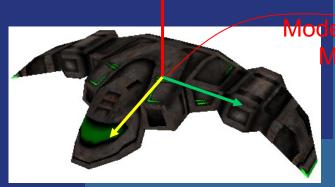
Lecture 2:

Transformation Pipeline

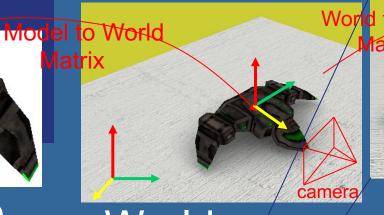
Clip space: clipping is nowadays typically done in homogeneous space. However, it used to be done in unit-cube space. Both terminologies are still used.



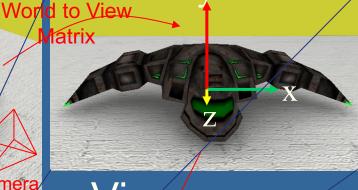
OpenGL | Geometry stage | done on GPU



Model space



World space

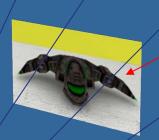


View space

ModelViewMtx = "Model to View Matrix"

ModelViewMtx * $v = (M_{V \leftarrow W} * M_{W \leftarrow M}) * v$

 $v_{\text{view_space}} = ModelViewMtx * v_{\text{model_space}}$



Projection Matrix

Full projection:

V_{clip_sp} = projectionMatrix * ModelViewMatrix * v_{model_space}

Or simply: v_{clip} space = $M_{ModelViewProjection} * v$, where $M_{ModelViewProjection}$ = projectionMatrix * ModelViewMatrix

02. Vectors and Transforms

Rotation

part

Homogeneous notation

- A point: $\mathbf{p} = (p_x \quad p_y \quad p_z)$
- Translation becomes:

Translation part

- A vector (direction): $\mathbf{d} = (d_x \quad d_y \quad d_z)$

Translation of vector: Td = d

Change of Frames

• How to get the M_{model-to-world} matrix:

$$\mathbf{P} = (0,5,0,1) \bullet$$

$$\mathbf{M}_{\text{model-to-world}} = \begin{bmatrix} a_x & b_x & c_x & o_x \\ a_y & b_y & c_y & o_y \\ a_z & b_z & c_z & o_z \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 \\ 5 \\ 0 \\ 1 \end{bmatrix}$$
world space

The basis vectors $\mathbf{a}, \mathbf{b}, \mathbf{c}$

are expressed in the world coordinate system

(Both coordinate systems are right-handed)

E.g.:
$$\mathbf{p}_{\text{world}} = \mathbf{M}_{\text{m}\to\text{w}} \mathbf{p}_{\text{model}} = \mathbf{M}_{\text{m}\to\text{w}} (0,5,0,1)^{\text{T}} = 5 \mathbf{b} \ (+ \mathbf{o})$$

Same example, just explained differently:

Change of Frames

$$\mathbf{M}_{\text{model-to-world}} = \begin{bmatrix} a_x & b_x & c_x & o_x \\ a_y & b_y & c_y & o_y \\ a_z & b_z & c_z & o_z \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\mathbf{M}_{\text{model-to-world}} = \begin{bmatrix} a_x & b_x & c_x & o_x \\ a_y & b_y & c_y & o_y \\ a_z & b_z & c_z & o_z \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\mathbf{M}_{\text{model-to-world}} = \begin{bmatrix} a_x & b_x & c_x & o_x \\ a_y & b_y & c_y & o_y \\ a_z & b_z & c_z & o_z \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Let's initially disregard the translation **o**. I.e., $\mathbf{o} = [0,0,0]$

X: One step along a results in a_x steps along world space axis x.

One step along **b** results in \mathbf{b}_{x} steps along world space axis x.

One step along c results in c_x steps along world space axis x.

The x-coord for **p** in world space (instead of modelspace) is thus $[a_x b_x c_x]$ **p**.

The y-coord for \mathbf{p} in world space is thus $[\mathbf{a}_y \ \mathbf{b}_y \ \mathbf{c}_y]\mathbf{p}$.

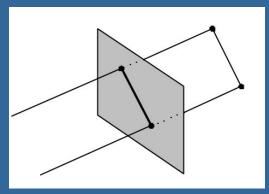
The z-coord for \mathbf{p} in world space is thus $[\mathbf{a}_z \ \mathbf{b}_z \ \mathbf{c}_z]\mathbf{p}$.

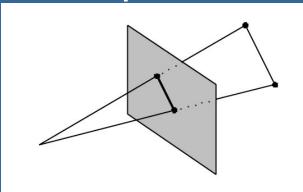
With the translation \mathbf{o} we get $\mathbf{p}_{\text{worldspace}} = \mathbf{M}_{\text{model-to-world}} \mathbf{p}_{\text{modelspace}}$

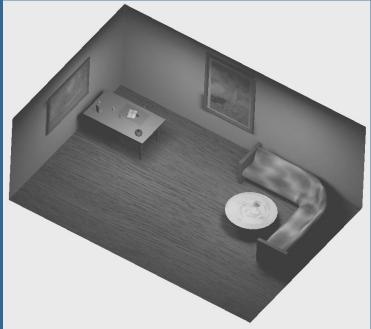
02. Vectors and Transforms

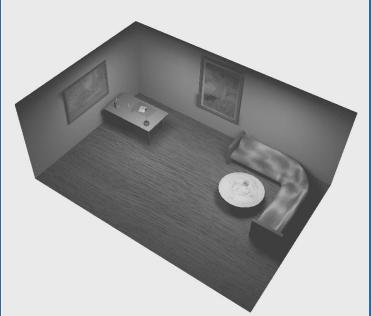
Projections

Orthogonal (parallel) and Perspective

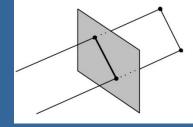








02. Vectors and Transforms



Orthogonal projection

- Simple, just skip one coordinate
 - Say, we're looking along the z-axis
 - Then drop z, and render

$$\mathbf{M}_{ortho} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \quad \Rightarrow \quad \mathbf{M}_{ortho} \begin{pmatrix} p_x \\ p_y \\ p_z \\ 1 \end{pmatrix} = \begin{pmatrix} p_x \\ p_y \\ 0 \\ 1 \end{pmatrix}$$



DDA Algorithm

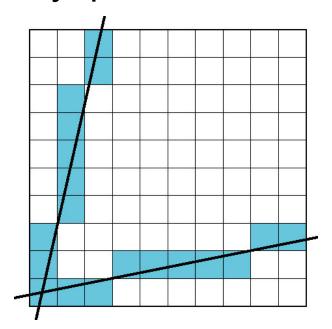
 (x_2, y_2) Δy (x_1, y_1) Δx

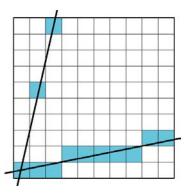
- <u>Digital Differential Analyzer</u>
 - DDA was a mechanical device for numerical solution of differential equations
 - -Line y=kx+ m satisfies differential equation $dy/dx = k = \Delta y/\Delta x = y_2-y_1/x_2-x_1$
- Along scan line $\Delta x = 1$

```
y=y1;
For(x=x1; x<=x2,ix++) {
   write_pixel(x, round(y), line_color)
   y+=k;
}</pre>
```

Using Symmetry

- Use for $1 \ge k \ge 0$
- For k > 1, swap role of x and y
 - –For each y, plot closest x





Otherwise we get problem for steep slopes

02. Vectors and Transforms

Very Important!

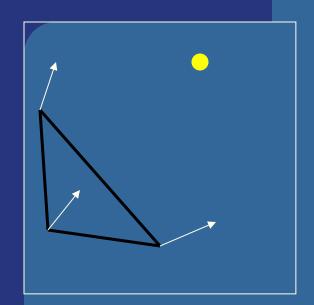
- The problem with DDA is that it uses floats which was slow in the old days
- Bresenhams algorithm only uses integers

You do not need to know Bresenham's algorithm by heart. It is enough that you **understand** it if you see it.

Lecture 3.1: Shading

- Ambient, diffuse, specular, emission
 - Formulas,
 - Phongs vs Blinns highlight model.
- Half vector: $h = \frac{l+v}{||l+v||}$
- Flat, Goraud, and Phong shading
- Fog
- Transparency
- Gamma correction

Lighting



Material:

- •Ambient (r,g,b,a)
- •Diffuse (r,g,b,a)
- •Specular (r,g,b,a)
- •Emission (r,g,b,a) ="självlysande färg"

Light:

- •Ambient (r,g,b,a)
- •Diffuse (r,g,b,a)
- •Specular (r,g,b,a)

DIFFUSE	Base color
SPECULAR	Highlight Color
AMBIENT	Low-light Color
EMISSION	Glow Color
SHININESS	Surface Smoothness

Lecture 3: Shading

The ambient/diffuse/specular/emission model

Summary of formulas:

Ambient: $\mathbf{i}_{amb} = \mathbf{m}_{amb} \mathbf{l}_{amb}$

Diffuse: $(n \cdot l) m_{\text{diff}} l_{\text{diff}}$

Specular:

• Phong: $(r \cdot v)^{shininess}$ \mathbf{m}_{spec} \mathbf{I}_{spec}

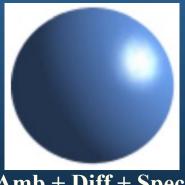
Blinn: $(n \cdot h)^{shininess}$ \mathbf{m}_{spec} \mathbf{l}_{spec}

Emission: m_{emission}





Amb + Diff



Amb + Diff + Spec



Amb + Diff + Spec + Em

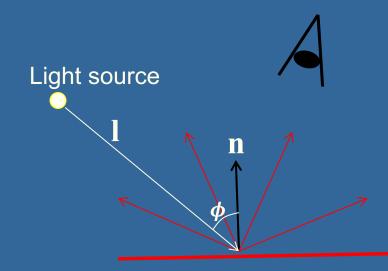
The ambient/diffuse/specular/emission model

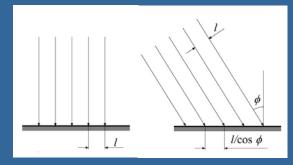
- The most basic real-time model:
- Light interacts with material and change color at bounces:

$$\mathbf{outColor}_{rgb} \sim \mathbf{material}_{rgb} \otimes \mathbf{lightColor}_{rgb}$$

- Ambient light: incoming background light from all directions and spreads in all directions (view-independent and light-position independent color)
- **Diffuse** light: the part that spreads equally in **all** directions (view independent) due to that the surface is very **rough** on microscopic level









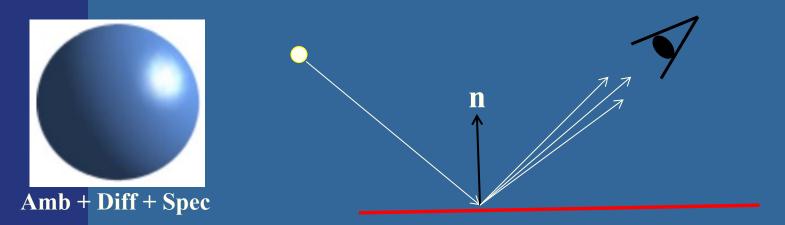
$$\mathbf{i}_{diff} = (\mathbf{n} \cdot \mathbf{l}) \mathbf{m}_{diff} \otimes \mathbf{s}_{diff}$$
$$(\mathbf{n} \cdot \mathbf{l}) = \cos \phi$$

The ambient/diffuse/specular/emission model

- The most basic real-time model:
- Light interacts with material and change color at bounces:

$$\mathbf{outColor}_{rgb} \sim \mathbf{material}_{rgb} \otimes \mathbf{lightColor}_{rgb}$$

- Ambient light: incoming background light from all directions and spreads in all directions (view-independent and light-position independent color)
- Diffuse light: the part that spreads equally in all directions (view independent) due to that the surface is very rough on microscopic level
- **Specular** light: the part that spreads mostly in the reflection direction (often same color as light source)

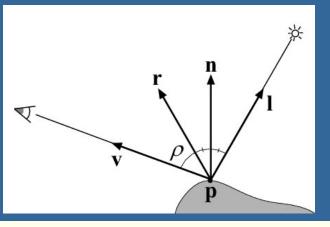


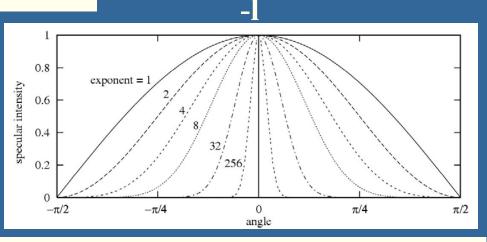
Specular: Phong's model

- Phong specular highlight model
- Reflect I around n:

$$\mathbf{r} = -\mathbf{l} + 2(\mathbf{n} \cdot \mathbf{l})\mathbf{n}$$

$$i_{spec} = (\mathbf{r} \cdot \mathbf{v})^{m_{shi}} = (\cos \rho)^{m_{shi}}$$

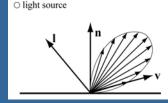




 $(\mathbf{n} \cdot \mathbf{l})\mathbf{n}$

$$\mathbf{i}_{spec} = ((\mathbf{n} \cdot \mathbf{l}) < 0) ? 0 : \max(0, (\mathbf{r} \cdot \mathbf{v}))^{m_{shi}} \mathbf{m}_{spec} \otimes \mathbf{s}_{spec}$$

Next: Blinns highlight formula: (n·h)^m



n must be unit vector

Specular: Blinn's specular highlight model

Blinn proposed replacing $\mathbf{v} \cdot \mathbf{r}$ by $\mathbf{n} \cdot \mathbf{h}$ where

$$\mathbf{h} = (\mathbf{l} + \mathbf{v})/|\mathbf{l} + \mathbf{v}|$$

h is halfway between I and v

If **n**, **l**, and **v** are coplanar:

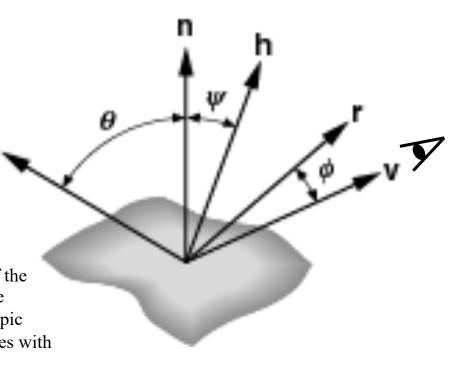
$$\psi = \phi/2$$

Must then adjust exponent

so that
$$(\mathbf{n} \cdot \mathbf{h})^{e'} \approx (\mathbf{r} \cdot \mathbf{v})^{e}$$
, $(e' \approx 4e)$

If the surface is rough, there is a probability distribution of the microscopic normals **n**. This means that the intensity of the reflection is decided by how many percent of the microscopic normals are aligned with **h**. And that probability often scales with how close **h** is to the macroscopic surface normal **n**.

$$\mathbf{i}_{spec} = \max(0, (\mathbf{h} \cdot \mathbf{n})^{m_{shi}}) \mathbf{m}_{spec} \otimes \mathbf{s}_{spec}$$



03. Shading:

Shading

- Flat, Goraud, and Phong shading:
 - Flat shading: one normal per triangle. Lighting computed once for the whole triangle.

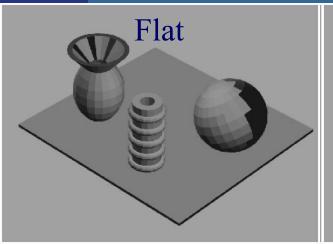
Flat

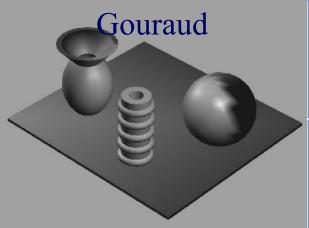
shading

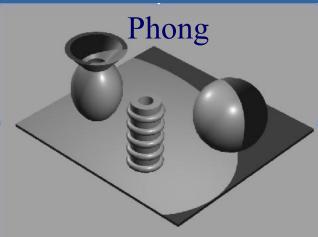
Gouraud

shading

- Gouraud shading: the lighting is computed per triangle vertex and for each pixel, the <u>color is interpolated</u> from the colors at the vertices.
- Phong Shading: the lighting is <u>not</u> computed per vertex. Instead the <u>normal</u> <u>is interpolated</u> per pixel from the normals defined at the vertices and <u>full</u> <u>lighting is computed per pixel</u> using this normal. This is of course more expensive but looks better.

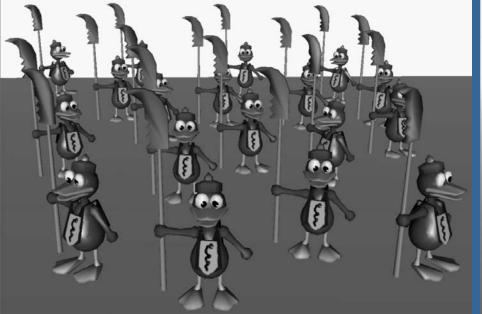


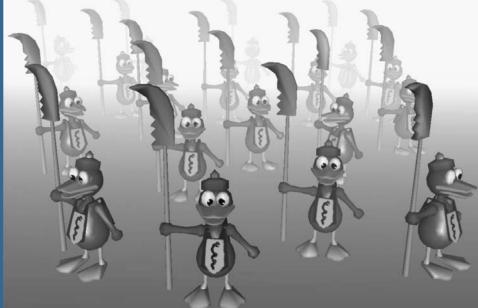




Phong

shading





• Color of fog: \mathbf{c}_f color of surface: \mathbf{c}_s

$$\mathbf{c}_p = f\mathbf{c}_s + (1 - f)\mathbf{c}_f \qquad f \in [0,1]$$

- How to compute f?
- E.g., linearly:

$$f = \frac{z_{end} - z_{p}}{z_{end} - z_{start}}$$

Transparency and alpha

- Transparency
 - Very simple in real-time contexts
- The tool: alpha blending (mix two colors)
- Alpha (α) is another component in the frame buffer, or on triangle
 - Represents the opacity
 - 1.0 is totally opaque
 - 0.0 is totally transparent
- The over operator: (Blending)

$$\mathbf{c}_o = \alpha \mathbf{c}_s + (1 - \alpha) \mathbf{c}_d$$

03. Shading:

Transparency

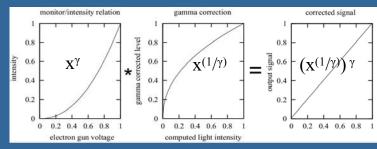
- Need to sort the transparent objects
 - First, render all non-transparent triangles as usual.
 - Then, sort all transparent triangles and render back-to-front with blending enabled. (and using standard depth test)
 - The reason is to avoid problems with the depth test and because the blending operation (i.e., over operator) is order dependent.

If we have high frame-to-frame coherency regarding the objects to be sorted per frame, then Bubble-sort (or Insertion sort) are really good! Superior to Quicksort.

Because, they have expected runtime of resorting already almost sorted input in O(n) instead of $O(n \log n)$, where n is number of elements.

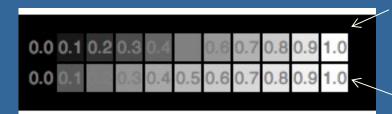
$$c = c_i^{(1/\gamma)}$$

Gamma correction



- Reasons for wanting gamma correction (standard is 2.2):
- 1. Screen has non-linear color intensity
 - We often want linear output (e.g. for correct antialiasing)
- Also happens to give more efficient color space (when compressing intensity from 32-bit floats to 8-bits). Thus, often desired when storing textures.

 Gamma of 2.2. Better



Gamma of 2.2. Better distribution for humans. Perceived as linear.

Truly linear intensity increase.

A linear intensity output (bottom) has a large jump in perceived brightness between the intensity values 0.0 and 0.1, while the steps at the higher end of the scale are hardly perceptible.

A nonlinearly-increasing intensity (upper), will show much more even steps in perceived brightness.

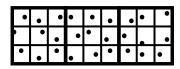
Leture 3.2: Sampling, filtrering, and Antialiasing

- When does it occur?
 - In 1) pixels, 2) time, 3) texturing

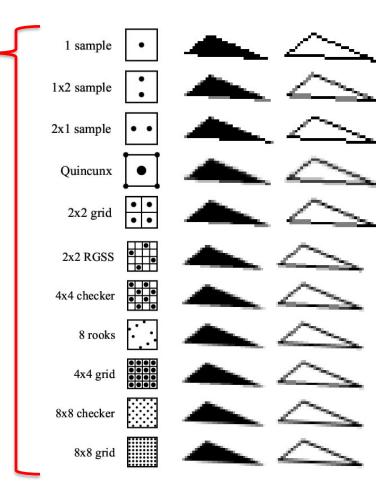




- Supersampling schemes:
- Quincunx + weights
- Jittered sampling
 - Why is it good?



Supersampling vs multisampling vs coverage sampling



SSAA, MSAA and CSAA

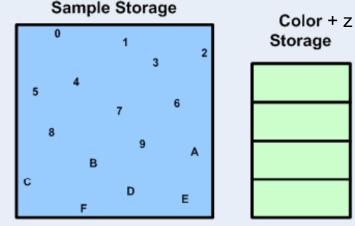


- Super Sampling Anti Aliasing
 - Stores duplicate information (color, depth, stencil) for each sample and fragment shader is run for each sample.
 - Corresponds to rendering to an oversized buffer and downfiltering.
- <u>Multi</u> Sampling Anti Aliasing
 - Shares some information between samples. E.g.
 - Result of Frament shader Frag. shader is only run once per rasterized fragment.
 - But stores a color per sample and typically also a stencil and depth-value per sample
- **Coverage Sampling Anti Aliasing**

Idea: Don't even store unique color and depth per sample. In each subsample, store index into a per-pixel list of 4-8 colors+depths.

- I.e., for 4-8 polygons, store their coverage.
- Fragment shader executed once per rasterized fragment
- E.g., Each sample holds a 2-bit index into a table (a storage of up to four colors per pixel)

16x CSAA Sample Storage



04. Texturing

Texturing:

- Real-time Filtering:
 - Magnification nearest neightbor, linear
 - Minification nearest neighbor, bilinear, bilinear mipmap filtering & trilinear-filtered mipmap lookup.
 - Why not sinc filter as real-time filter?
 - Mipmaps + their memory cost
 - How compute bilinear/trilinear filtering
 - Number of texel accesses for trilinear filtering
 - Anisotropic filtering take several trilinear-filtered mipmap lookups along the line of anisotropy (e.g., up to 16 lookups)
- Environment mapping cube maps. How compute lookup.
- Bump mapping
- 3D-textures what is it?
- Sprites
- Billboards/Impostors, viewplane vs viewpoint oriented, axial billboards, how to handle depth buffer for fully transparent texels.
- Particle systems

Filtering

FILTERING:

For magnification: Nearest or Linear (box vs Tent filter)

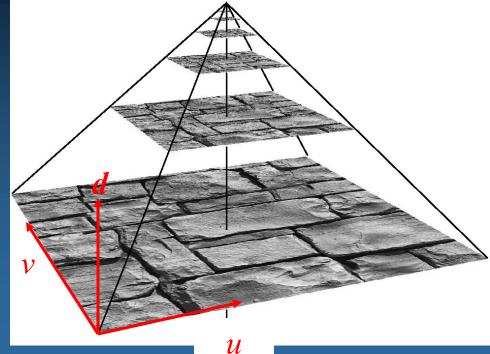




- For minification: nearest, linear and...
 - Bilinear using mipmapping
 - Trilinear using mipmapping
 - Anisotropic up to 16 mipmap lookups along line of anisotropy

Mipmapping

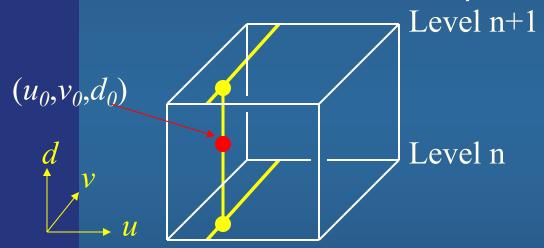
- Image pyramid
- Half width and height when going upwards



- Average over 4 "parent texels" to form "child texel"
- Depending on amount of minification, determine which image to fetch from
- Compute d first, gives two images
 - Bilinear interpolation in each

Mipmapping

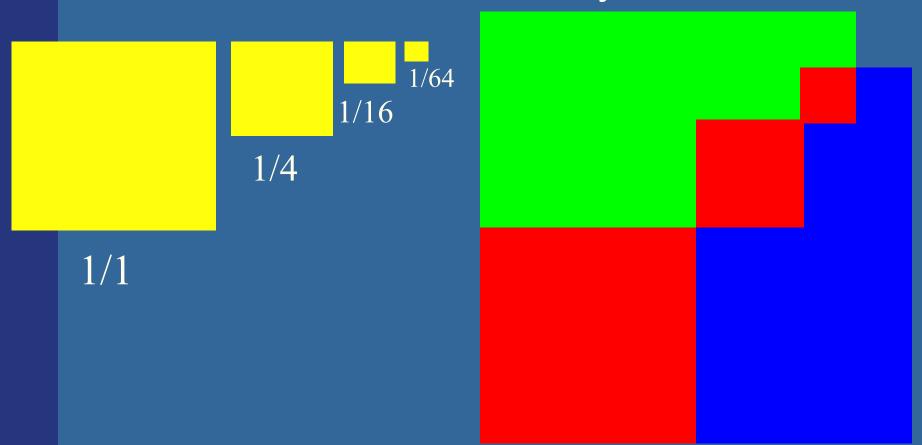
- Interpolate between those bilinear values
 - Gives trilinear interpolation



Constant time filtering: 8 texel accesses

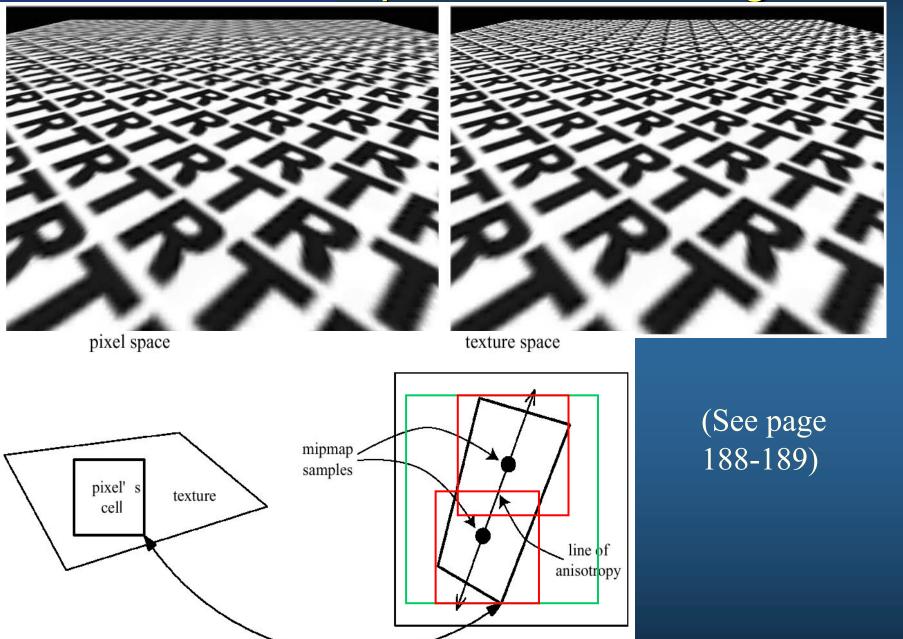
Mipmapping: Memory requirements

Not twice the number of bytes…!

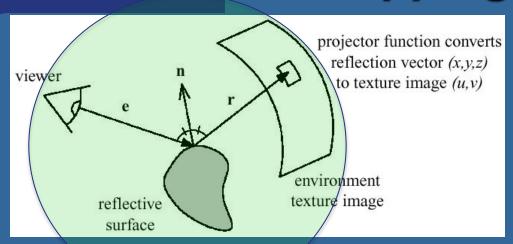


• Rather 33% more — not that much Modified by Ulf Assarsson 2004

Anisotropic texture filtering



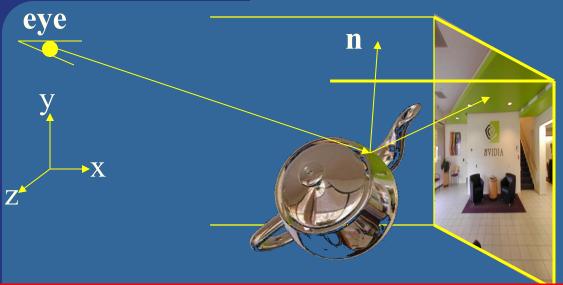
Environment mapping





- Assumes the environment is infinitely far away
- Cube mapping is the norm nowadays

Cube mapping



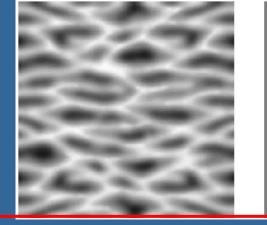


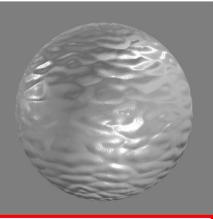
- Simple math: compute reflection vector, **r**
- Largest abs-value of component, determines which cube face.
 - Example: r=(5,-1,2) gives POS_X face
- Divide r by abs(5) gives (u,v)=(-1/5,2/5)
- Also remap from [-1,1] to [0,1] by (u,v) = ((u,v)+vec2(1,1))*0.5;
- Your hardware does all the work for you. You just have to compute the reflection vector.

Bump mapping

• by Blinn in 1978

geometry





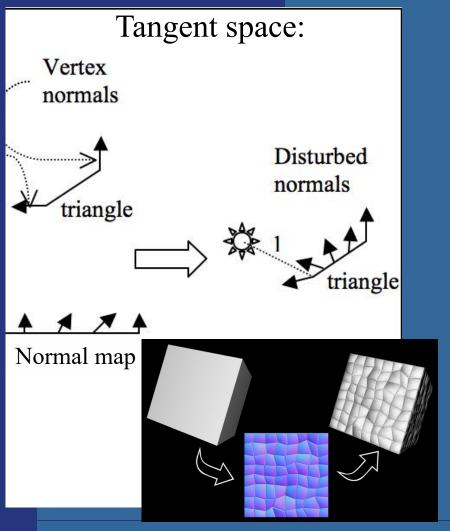
- Inexpensive way of simulating wrinkles and bumps on geometry
 - Expensive to model these geometrically
- Instead <u>let a texture modify the normal at</u> each pixel, and then use this normal to compute lighting per pixel

Bump map

Stores heights: can derive normals

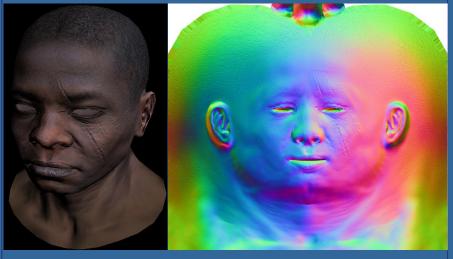
Bump mapped geometry

Normal mapping in tangent vs object space



Object space:

•Normals are stored directly in model space. I.e., as including both face orientation plus distorsion.



Tangent space:

•Normals are stored as distorsion of face orientation. The same bump map can be tiled/repeated and reused for many faces with different orientation

More...

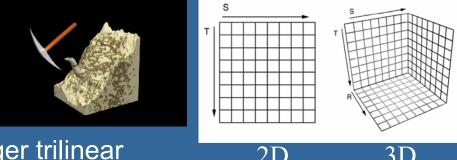
• 3D textures:



- Rather quadlinear
 - (trilinear interpolation in both 3D-mipmap levels + between mipmap levels)
- Enables new possibilities
 - Can store light in a room, for example

Displacement Mapping

- Like bump/normal maps but truly offsets the surface geometry (not just the lighting).
- Gfx hardware cannot offset the fragment's position
 - Offsetting per vertex is easy in vertex shader but requires a highly tessellated surface.
 - Tesselation shaders are created to increase the tessellation of a triangle into many triangles over its surface. Highly efficient.
 - (Can also be done using Geometry Shader (e.g. Direct3D 10) by ray casting in the displacement map, but tessellation shaders are generally more efficient for this.)



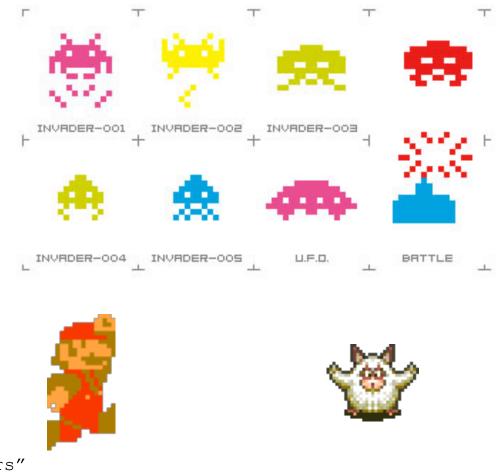


Sprites

Just know what "sprites" are and that they are very similar to a billboard

```
GLbyte M[64]=
   127,0,0,127, 127,0,0,127,
   127,0,0,127, 127,0,0,127,
   0,127,0,0, 0,127,0,127,
   0,127,0,127, 0,127,0,0,
   0,0,127,0, 0,0,127,127,
   0,0,127,127, 0,0,127,0,
   127, 127, 0, 0, 127, 127, 0, 127,
   127, 127, 0, 127, 127, 127, 0, 0 };
void display(void) {
   glClearColor(0.0,1.0,1.0,1.0);
   glClear(GL COLOR BUFFER BIT);
   glEnable (GL BLEND);
   glBlendFunc (GL SRC ALPHA,
         GL ONE MINUS SRC ALPHA);
   glRasterPos2d(xpos1, ypos1);
   qlPixelZoom(8.0,8.0);
   glDrawPixels(width, height,
         GL RGBA, GL BYTE, M);
   qlPixelZoom(1.0,1.0);
   SDL GL SwapWindow //"Swap buffers"
```

Sprites (=älvor) was a technique on older home computers, e.g. VIC64. As opposed to billboards, sprites do not use the frame buffer. They are rasterized directly to the screen using a special chip. (A special bit-register also marked colliding sprites.)

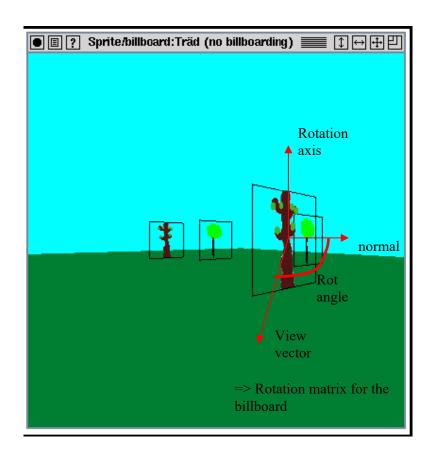


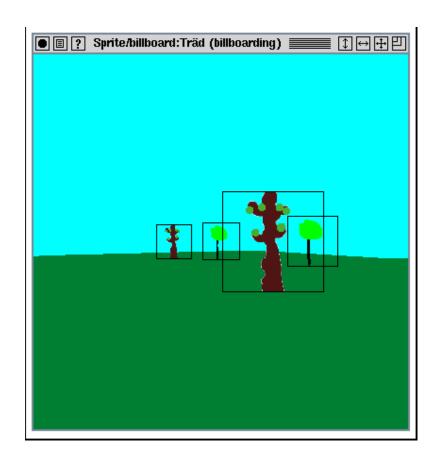
Billboards

- 2D images used in 3D environments
 - Common for trees, explosions, clouds, lens flares



Billboards





- Rotate them towards viewer
 - Either by rotation matrix (see OH 288), or
 - by orthographic projection

Billboards

- Fix correct transparency by blending AND using alphatest
 - In fragment shader:if (color.a < 0.1) discard;

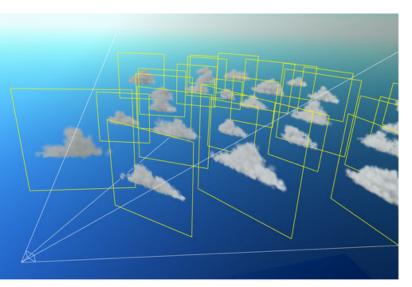
If alpha value in texture is lower than this threshold value, the pixel is not rendered to. I.e., neither frame buffer nor z-buffer is updated, which is what we want to achieve.

Color Buffer Depth Buffer

With blending

With alpha test

E.g. here: so that objects behind is visible through the hole





(Also called *Impostors*)



axial billboarding
The rotation axis is fixed and disregarding the view position

Lecture 5: OpenGL

- How to use OpenGL (or DirectX)
 - Will not ask about syntax. Know how to use.
 - I.e. functionality
 - E.g. how to achieve
 - Blending and transparency
 - Fog how would you implement in a fragment shader?
 - pseudo code is enough
 - Specify a material, a triangle, how to translate or rotate an object.
 - Triangle vertex order and facing

Buffers

- Frame buffer
 - Back/front/left/right glDrawBuffers()
 - Offscreen buffers (e.g., framebuffer objects, auxiliary buffers)

Frame buffers can consist of:

- Color buffer rgb(a)
- Depth buffer (z-buffer)
 - For correct depth sorting
 - Instead of BSP-algorithm or painters algorithm...
- Stencil buffer
 - E.g., for shadow volumes or only render to frame buffer where stencil = certain value (e.g., for masking).

Lecture 6: Intersection Tests

• Analytic test:

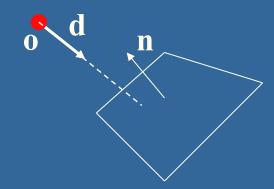
- Be able to compute ray vs sphere or other similar formula
- Ray/triangle, ray/plane
- Point/plane, Sphere/plane,
- Know expressions for ray, sphere, cylinder, plane, triangle

Geometrical tests

- Ray/box with slab-test
- Ray/polygon (3D->2D)
- box/plane
- AABB/AABB
- View frustum vs spheres/AABB:s/BVHs.
- Separating Axis Theorem (SAT)
- Know what a dynamic test is

Analytical: Ray/plane intersection

- Ray: **r**(*t*)=**o**+*t***d**
- Plane formula: n•p + d = 0



• Replace **p** by **r**(*t*) and solve for t:

$$n \cdot (o+td) + d = 0$$

 $n \cdot o+tn \cdot d + d = 0$
 $t = (-d - n \cdot o) / (n \cdot d)$

Here, one scalar equation and one unknown -> just solve for t.

Analytical: Ray/sphere test

d

- Sphere center: c, and radius r
- Ray: **r**(*t*)=**o**+*t***d**
- Sphere formula: ||**p**-**c**||=*r*
- Replace **p** by **r**(*t*): ||**r**(*t*)-**c**||=*r*



$$(\mathbf{r}(t)-\mathbf{c})\cdot(\mathbf{r}(t)-\mathbf{c})-r^2=0$$

$$(\mathbf{o} + t\mathbf{d} - \mathbf{c}) \cdot (\mathbf{o} + t\mathbf{d} - \mathbf{c}) - r^2 = 0$$

$$(\mathbf{d} \cdot \mathbf{d})t^2 + 2((\mathbf{o} - \mathbf{c}) \cdot \mathbf{d})t + (\mathbf{o} - \mathbf{c}) \cdot (\mathbf{o} - \mathbf{c}) - r^2 = 0$$

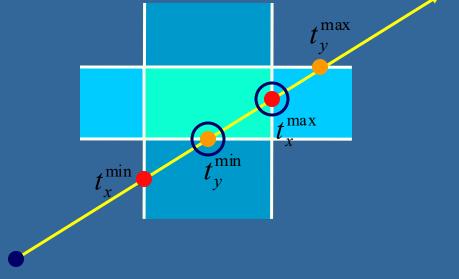
$$t^{2} + 2((\mathbf{o} - \mathbf{c}) \cdot \mathbf{d})t + (\mathbf{o} - \mathbf{c}) \cdot (\mathbf{o} - \mathbf{c}) - r^{2} = 0 \quad ||\mathbf{d}|| = 1$$

This is a standard quadratic equation. Solve for the nine-Möller © 2003

Geometrical: Ray/Box Intersection (2)

Intersect the 2 planes of each slab with

the ray



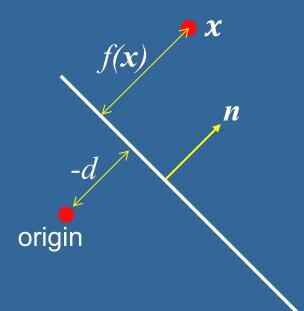
- Keep max of t^{min} and min of t^{max}
- If $t^{min} < t^{max}$ then we got an intersection
- Special case when ray parallell to slab

The Plane Equation Plane: $\pi : \mathbf{n} \cdot \mathbf{p} + d = 0$

If $\mathbf{n} \cdot \mathbf{x} + d = 0$, then \mathbf{x} lies in the plane.

The function $f(\mathbf{x}) = \mathbf{n} \cdot \mathbf{x} + d$ gives the signed distance of \mathbf{x} from the plane. (\mathbf{n} should be normalized.)

- f(x) > 0 means above the plane
- f(x) < 0 means below the plane



-d is how far the origin is behind the plane

Sphere/Plane Box/Plane

Plane: $\pi : \mathbf{n} \cdot \mathbf{p} + d = 0$

Sphere: c r

 $AABB: \mathbf{b}^{min} \mathbf{b}^{max}$

- Sphere: compute $f(\mathbf{c}) = \mathbf{n} \cdot \mathbf{c} + d$
- $f(\mathbf{c})$ is the signed distance (n normalized)
- $abs(f(\mathbf{c})) > r$ no collision
- $abs(f(\mathbf{c})) = r$ sphere touches the plane
- $abs(f(\mathbf{c})) < r$ sphere intersects plane

- Box: insert all 8 corners
- If all f's have the same sign, then all points are on the same side, and no collision









AABB/plane

OBB almost as easy. Just first project

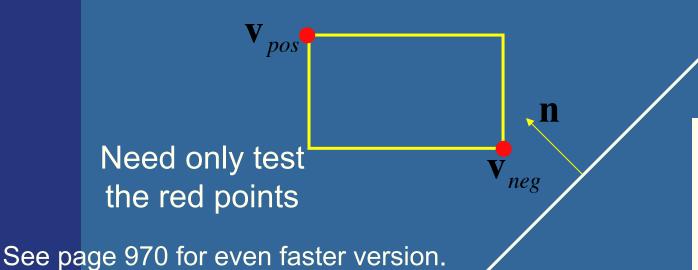
n on OBB's axes – see p: 972

Plane: $\pi : \mathbf{n} \cdot \mathbf{p} + d = 0$

Sphere: $\mathbf{c} r$

Box: \mathbf{b}^{min} \mathbf{b}^{max}

- The smart way (shown in 2D)
- Find the two vertices that have the most positive and most negative value when tested againt the plane



 $\mathbf{v}_{pos_x} = (\mathbf{n}_x > 0)? \mathbf{b}_{max_x} : \mathbf{b}_{min_x}$ $\mathbf{v}_{pos_y} = (\mathbf{n}_y > 0)? \mathbf{b}_{max_y} : \mathbf{b}_{min_y}$ $\mathbf{v}_{pos_z} = (\mathbf{n}_z > 0)? \mathbf{b}_{max_z} : \mathbf{b}_{min_z}$ $\mathbf{v}_{neg_x} = (\mathbf{n}_x < 0)? \mathbf{b}_{max_x} : \mathbf{b}_{min_x}$ $\mathbf{v}_{neg_y} = (\mathbf{n}_y < 0)? \mathbf{b}_{max_y} : \mathbf{b}_{min_y}$ $\mathbf{v}_{neg_z} = (\mathbf{n}_z < 0)? \mathbf{b}_{max_z} : \mathbf{b}_{min_z}$

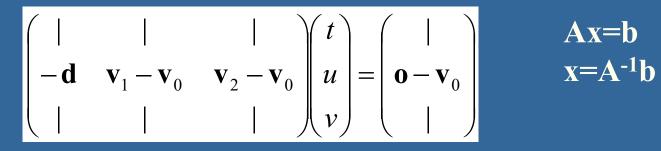
Another analytical example: Ray/Triangle in detail

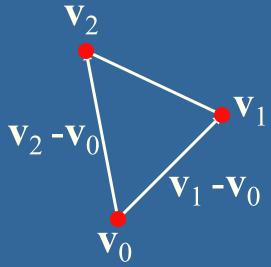
- Ray: $\mathbf{r}(t) = \mathbf{o} + t\mathbf{d}$
- Triangle vertices: v_0 , v_1 , v_2
- A point in the triangle:

$$\mathbf{t}(u,v) = \mathbf{v}_0 + u(\mathbf{v}_1 - \mathbf{v}_0) + v(\mathbf{v}_2 - \mathbf{v}_0)$$
where $[u,v>=0, u+v<=1]$ is inside triangle

• Set t(u,v)=r(t), and solve for t, u, v:

$$\mathbf{v}_{0}+u(\mathbf{v}_{1}-\mathbf{v}_{0})+\nu(\mathbf{v}_{2}-\mathbf{v}_{0}) = \mathbf{o}+t\mathbf{d}$$
=> -t\mathbf{d} + u(\mathbf{v}_{1}-\mathbf{v}_{0}) + \nu(\mathbf{v}_{2}-\mathbf{v}_{0}) = \mathbf{o}-\mathbf{v}_{0}
=> [-\mathbf{d}, (\mathbf{v}_{1}-\mathbf{v}_{0}), (\mathbf{v}_{2}-\mathbf{v}_{0})] [t, u, v]^{T} = \mathbf{o}-\mathbf{v}_{0}

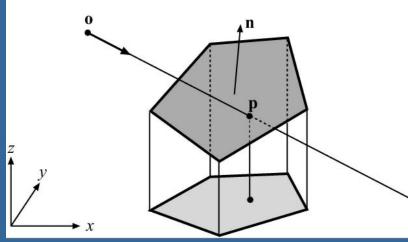


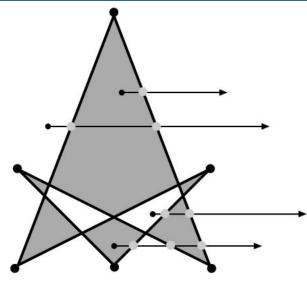


$$Ax=b$$
$$x=A^{-1}b$$

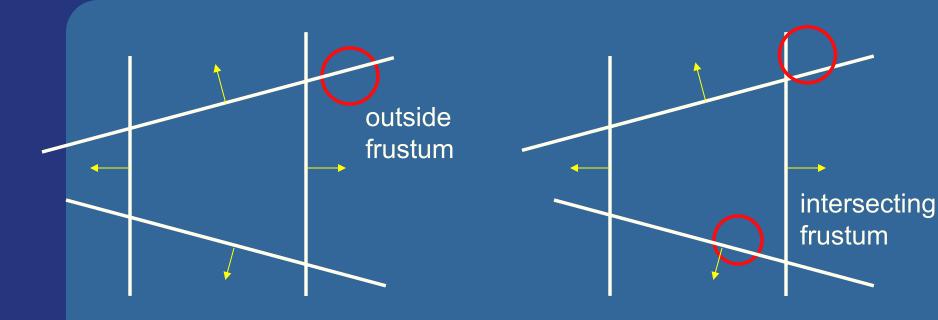
Ray/Polygon: very briefly

- Intersect ray with polygon plane
- Project from 3D to 2D
- How?
- Find $\max(|n_x|,|n_y|,|n_z|)$
- Skip that coordinate!
- Then, count crossing in 2D





View frustum testing example



Algorithm:

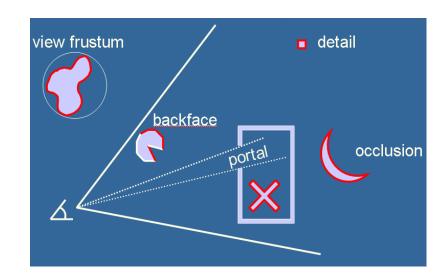
- if sphere is outside any of the 6 frustum planes -> report "outside".
- Else report intersect.
- Not exact test, but not incorrect, i.e.,
 - A sphere that is reported to be inside, can be outside
 - Not vice versa, so test is conservative.

Lecture 7.1: Spatial Data Structures and Speed-Up Techniques

- Speed-up techniques
 - Culling
 - Backface
 - View frustum (hierarchical)
 - Portal
 - Occlusion Culling
 - Detail
 - Levels-of-detail:

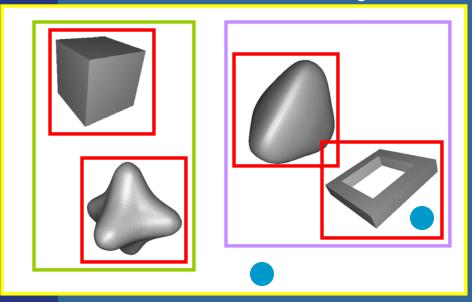


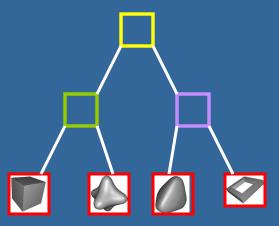
- How to construct and use the spatial data structures
 - BVH, BSP-trees (polygon aligned + axis aligned), quadtree/octree



Axis Aligned Bounding Box Hierarchy - an example

 Assume we click on screen, and want to find which object we clicked on





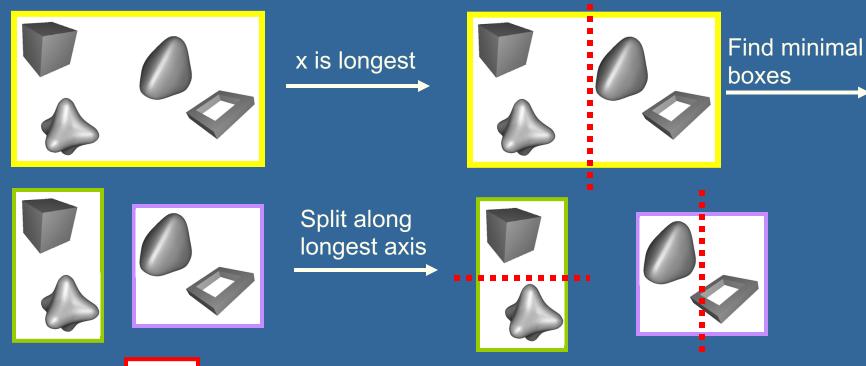


- 1) Test the root first
- 2) Descend recursively as needed
- 3) Terminate traversal when possible In general: get O(log n) instead of O(n)

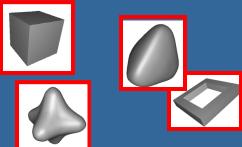
How to create a BVH? Example: using AABBs

AABB = Axis Aligned
Bounding Box
BVH = Bounding Volume
Hierarchy

Find minimal box, then split along longest axis



Find minimal boxes



Called TOP-DOWN method Similar for other BVs

Axis-aligned BSP tree Rough sorting

- Test the planes, recursively from root, against the point of view. For each traversed node:
 - If node is leaf, draw the node's geometry
 - else
 - Continue traversal on the "hither" side with respect to the eye to sort front to back
- Then, continue on the farther side.

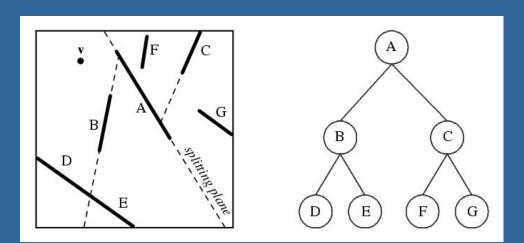
 Then, continue o

 Works in the same way for polygonaligned BSP trees --- but that gives exact sorting

Polygon-aligned BSP tree

- Allows exact sorting
- Very similar to axis-aligned BSP tree
 - But the splitting plane are now located in the planes of the triangles

```
Drawing Back-to-Front {
    recurse on farther side of P;
    Draw P;
    Recurse on hither side of P;
}// farther/hither is with respect to eye pos.
```

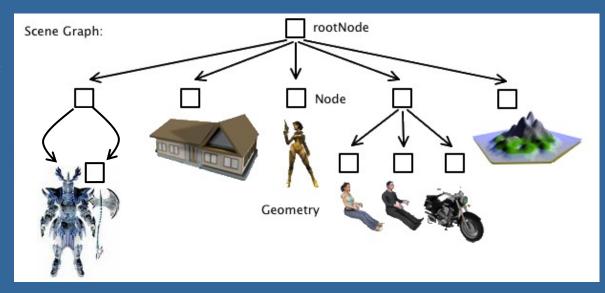


Know how to build it and how to traverse back-to-front or front-to-back with respect to the eye position (here: v)

A Scene Graph is a hierarchical scene description – more typically a **logical** hierarchy (than e.g. **spatial**)

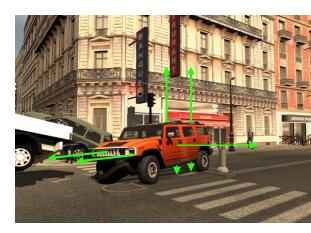
Scene graphs

- a node hierarchy
- A scene graph is a node hierarchy, which often reflects a logical hierarchical scene description
 - often in combination with a BVH such that each node has a BV.
- Common hierarchical features include:
 - Lights
 - Materials
 - Transforms
 - Transparency
 - Selection



Lecture 7.2: Collision Detection

- 3 types of algorithms:
 - With rays
 - Fast but not exact
 - With BVH
 - Slower but exact
 - You should be able to write pseudo code for BVH/BVH test for coll det between two objects.
 - For many many objects.
 - Course pruning of "obviously" non-colliding objects
 - E.g., Use a grid with an object list per cell, storing the objects that intersect that cell. For each cell with list length > 1, test those against each other with a more exact method.
 - (Sweep-and-prune is interesting but you can skip it.)

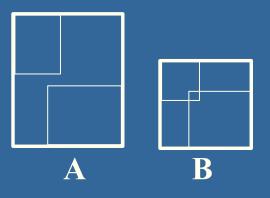


Pseudo code for BVH against BVH

```
FindFirstHitCD(A, B)
if(not overlap(A, B)) return false;
if(isLeaf(A) and isLeaf(B))
   for each triangle pair T_A \in A_c and T_B \in B_c
      if(overlap(T_A, T_B)) return TRUE;
else if(isNotLeaf(A) and isNotLeaf(B))
   if(Volume(A) > Volume(B))
      for each child C_A \in A_c
       if \mathbf{FindFirstHitCD}(C_A, B) return true;
   else
      for each child C_B \in B_c
       if FindFirstHitCD(A, C_B) return true;
else if(isLeaf(A) and isNotLeaf(B))
   for each child C_B \in B_c
    if \mathbf{FindFirstHitCD}(C_B, A) return true;
else
   for each child C_A \in A_c
    if \mathbf{FindFirstHitCD}(C_A, B) return true;
return FALSE;
```

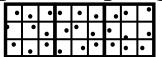
Pseudocode deals with 4 cases:

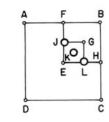
- 1) Leaf against leaf node
- 2) Internal node against internal node
- 3) Internal against leaf
- 4) Leaf against internal



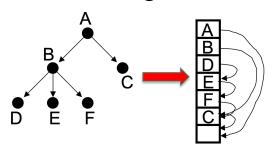
Lecture 8+9: Ray tracing

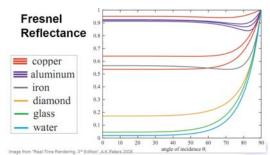
- Compute reflection ray
- Adaptive Super Sampling scheme:
- Jittering:





- How to stop ray tracing recursion? Send weight...
- Spatial data structures super important:
 - Draw: BVH: AABB/OBB/sphere. BSP-trees: polygon-aligned +
 AABSP=kd-tree. Octree/quadtree. Grids, hierarchical/recursive grids.
- Speedup techniques
 - Optimizations for BVHs: skippointer tree
 - Ray BVH-traversal
 - Grids: mailboxing purpose and how it works.
 - (You do not need to learn the <u>ray</u> traversal algorithms for Grids nor AA-BSP trees)
 - Shadow cache
- Material: Metall: rgb-dependent Fresnel effect Dielectrics: not rgb-dependent.
- Constructive Solid Geometry how to implement



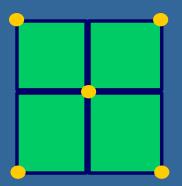


Adaptive Supersampling

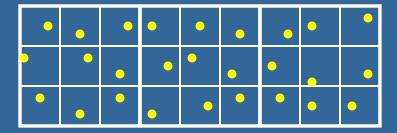
Pseudo code:

Color AdaptiveSuperSampling() {

- Make sure all 5 samples exist
 - (Shoot new rays along diagonal if necessary)
- Color col = black;
- For each quad i
 - If the colors of the 2 samples are fairly similar
 - col += (1/4)*(average of the two colors)
 - Else
 - col +=(1/4)*
 adaptiveSuperSampling(quad[i])
- return col;



Jittered sampling



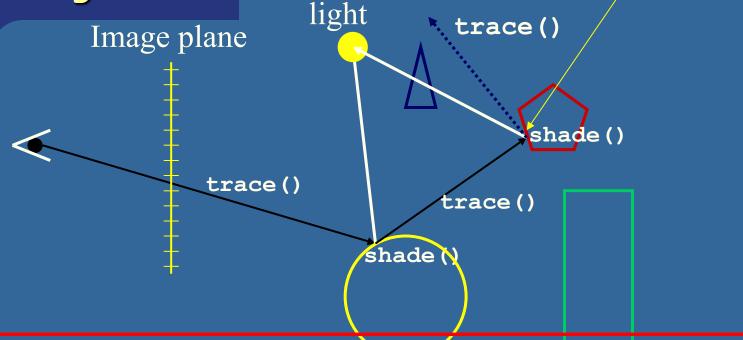
- Works as before
 - Replaces aliasing with noise
 - Our visual system likes that better
- This is often a preferred solution
- Can use adaptive strategies as well

08 + 09. Ray Tracing

Summary of the Ray tracing-

algorithm:

Point is in shadow



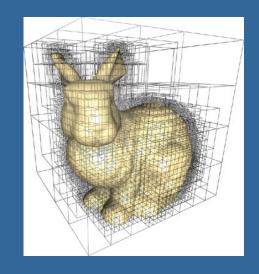
- main()-calls trace() for each pixel
- trace(): should return color of closest hit point along ray.
 - 1. calls findClosestIntersection()
 - 2. If any object intersected \rightarrow call shade().
- Shade(): should compute color at hit point
 - 1. For each light source, shoot shadow ray to determine if light source is visible If not in shadow, compute diffuse + specular contribution.
 - 2. Compute ambient contribution
 - 3. Call trace() recursively for the reflection- and refraction ray.

One of the most important slides in the whole course:

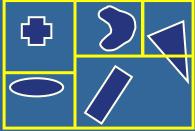
Data structures

Octree



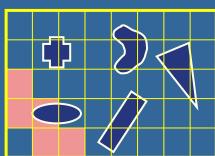


Kd tree

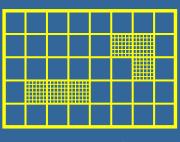


Kd-tree = Axis-Aligned BSP tree with fixed recursive split plane order (e.g. x,y,z,x,y,z...)

• Grids
Including mail
boxing

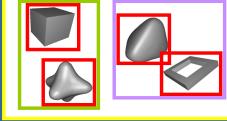






Recursive grid

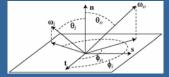




Lecture 10 – Global Illumination

The rendering equation + BRDF

$$L_o = L_e + \int_{\Omega} f_r(\mathbf{x}, \mathbf{\omega}, \mathbf{\omega}') L_i(\mathbf{x}, \mathbf{\omega}') (\mathbf{\omega}' \cdot \mathbf{n}) d\mathbf{\omega}'$$



- Be able to explain all its components
- Monte Carlo sampling:
 - The naïve way (an exponentially growing ray tree)
 - Path tracing
 - Why it is good, compared to naive monte-carlo sampling
 - The overall algorithm (on a high level as in these slides).

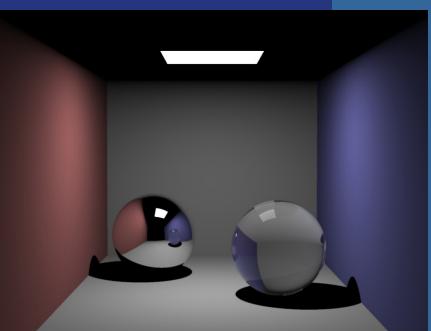


- Shoot photons from light source, and let them bounce around in the scene, and store them where they land (e.g. in a kD-tree).
- Ray-tracing pass from the eye. Estimate photon density at each ray hit, by growing a sphere (at the hit point in the kD-tree) until it contains a predetermined #photons. Sphere radius is then the inverse measure of the light intensity at the point.
- Bidirectional Path Tracing, Metropolis Light Transport
 - Just their names. Don't need to know the algorithms.

Denoising by Final Gather or Al

- Final Gather sample indirect illumination carefully at some positions in the world (final-gather points). At each ray hit, estimate indirect illumination by interpolation from nearby final-gather points.
- AI: use some existing Deep Neural Network solution that denoises your images for your kind of scenes.

Isn't ray tracing enough?



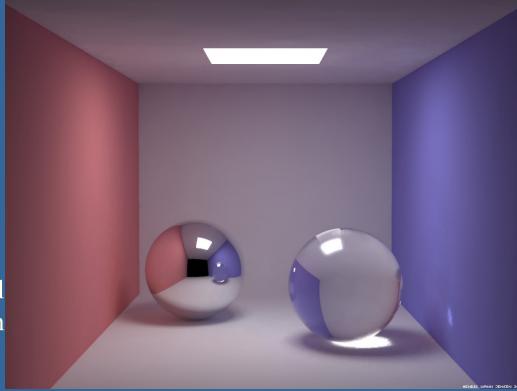
Ray tracing

Which are the differences?

Global Illumination

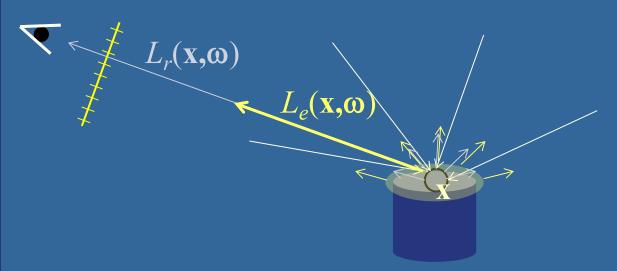
Effects to note in Global Illumination image:

- 1) Indirect lighting (light reaches the roof)
- 2) Soft shadows (light source has area)
- 3) Color bleeding (example: roof is red near red wall) (same as 1)
- 4) Caustics (concentration of refracted light through glass ball)
- 5) Materials have no ambient component



The rendering equation

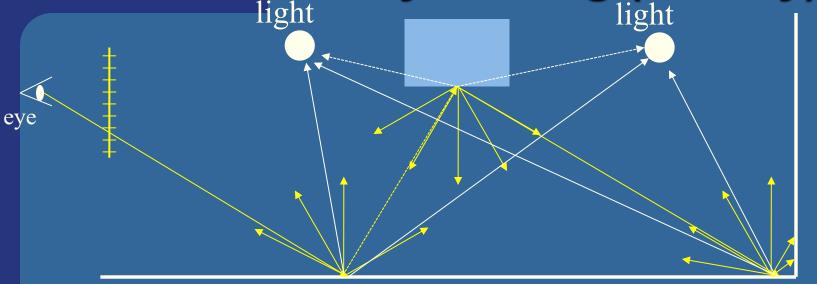
- Paper by Kajiya, 1986.
- Is the basis for all global illumination algorithms
- $L_o(\mathbf{x}, \mathbf{\omega}) = L_e(\mathbf{x}, \mathbf{\omega}) + L_r(\mathbf{x}, \mathbf{\omega})$
 - outgoing=emitted+reflected radiance



$$L_o = L_e + \int_{\Omega} f_r(\mathbf{x}, \mathbf{\omega}, \mathbf{\omega}') L_i(\mathbf{x}, \mathbf{\omega}') (\mathbf{\omega}' \cdot \mathbf{n}) d\mathbf{\omega}'$$

• f_r is the BRDF, ω ' is incoming direction, \mathbf{n} is normal at point \mathbf{x} , Ω is hemisphere "around" \mathbf{x} and \mathbf{n} , L_i is incoming radiance

Monte Carlo Ray Tracing (naïvely)



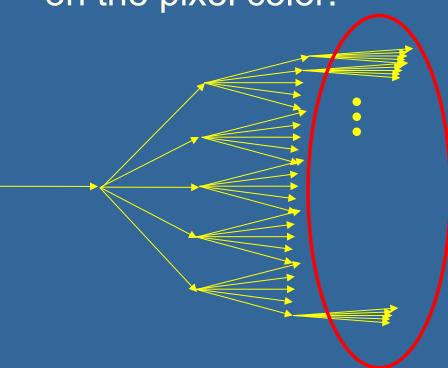
diffuse floor and wall

- (Compute local lighting as usual, with a shadow ray per light.)
- Sample indirect illumination by shooting sample rays over the hemisphere, at each hit.

$$L_o = L_e + \int_{\Omega} f_r(\mathbf{x}, \mathbf{\omega}, \mathbf{\omega}') L_i(\mathbf{x}, \mathbf{\omega}') (\mathbf{\omega}' \cdot \mathbf{n}) d\mathbf{\omega}'$$

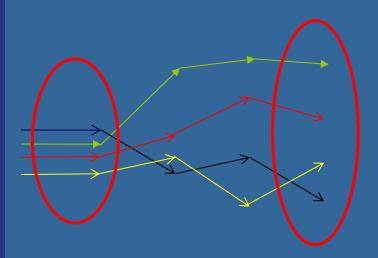
Monte Carlo Ray Tracing (naïvely)

 The indirect-illumination sampling gives a ray tree with most rays at the bottom level. This is bad since these rays have the lowest influence on the pixel color.



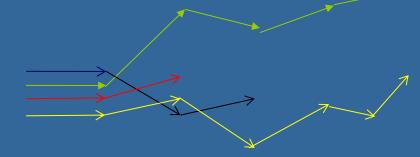
PathTracing

- one efficient Monte-Carlo Ray-Tracing solution
- Path Tracing instead only traces one of the possible ray paths at a time. This is done by randomly selecting only one sample direction at a bounce. Hundreds of paths per pixel are traced.



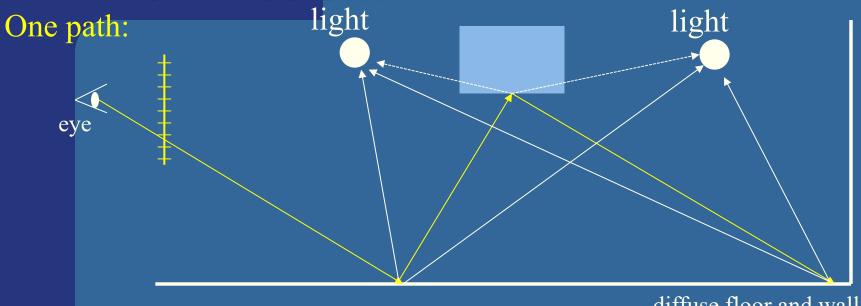
Equally number of rays are traced at each level

Or:



Even smarter: terminate path with some probablility after each level, since they have decreasing importance to final pixel color.

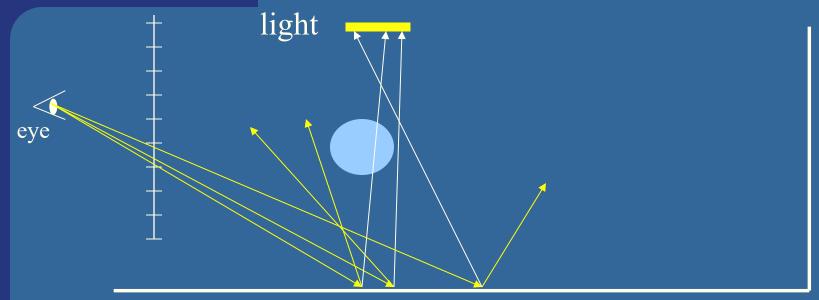
Path Tracing – indirect + direct illumination.



diffuse floor and wall

- Shoot many paths per pixel (the image just shows one light path).
 - At each intersection,
 - Shoot one shadow ray per light source
 - at random position on light, for area/volumetric light sources
 - and randomly select one new ray direction.

Path Tracing and area lights



diffuse floor and wall

- For area light sources, shoot the shadow ray to one random position on the area light. This gives soft shadows when many paths are averaged for the pixel.
- Example: Three paths for one pixel
 - At each ray intersection,
 - Pick one random position on light source
 - Send one random ray bounce to continue the path...

Path tracing: Summary

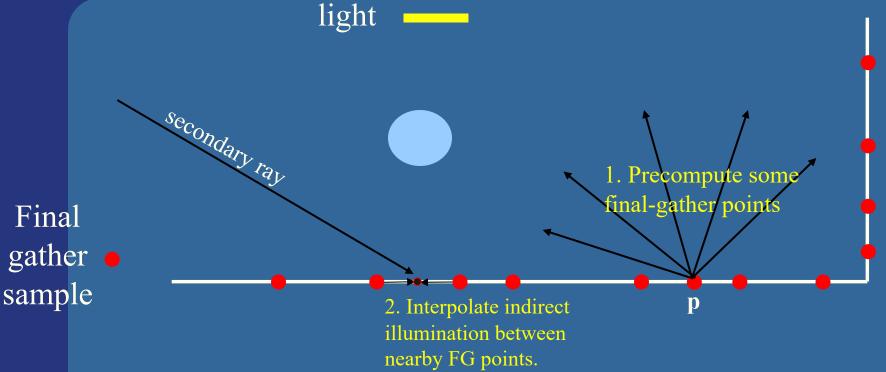
- Uses Monte Carlo sampling to solve integration:
 - by shooting many random ray paths over the integral domain.
 - Algorithm:
 - For each pixel, // we will shoot a number of paths:
 - For each path, generate the primary ray:
 - Repeat {
 - 1. Trace the ray. At hitpoint:
 - 2. Shoot one shadow ray and compute local lighting.
 - 3. Sample indirect illumination randomly over the possible reflection/refraction directions by generating **one** such new ray.
 - } until the path is randomly terminated (or the ray does not hit anything).
- Shorter summary: shoot many paths per pixel, by randomly choosing
 one new ray at each interaction with surface + one shadow ray per light.
 Terminate the path with a random probability

Final Gather

Popular for ray tracing and photon mapping but not path tracing

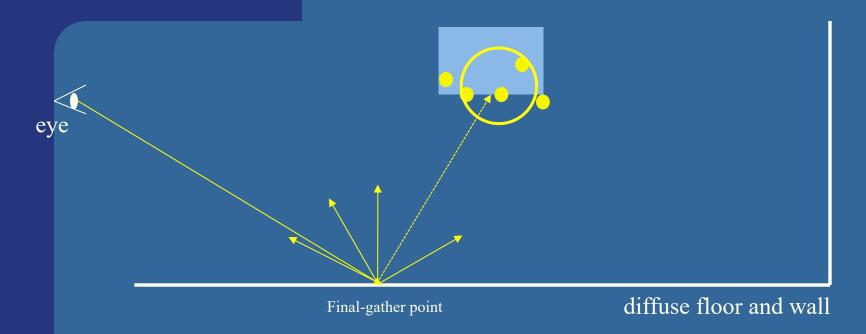
Idea and good answer:

- Compute indirect illumination somehow, but only at a few positions (final gather points) in the scene.
- Estimate indirect illumination for other positions by interpolation from nearby final-gather points



- Many versions of Final Gathering exist.
- E.g., to compute final-gather point p:
 - Send thousand(s) random rays out from p to sample indirect illumination
- To use during ray tracing: interpolate global illumination between nearby Final Gather points, to estimate incoming radiance at the ray's intersection point.
- Does not matter much if indirect illumination is blotchy for secondary rays.

Final Gather with Photon Mapping



- Too noicy to use the <u>global</u> map for direct visualization
- Remember: eye rays are recursively traced (via reflections/refractions) until a diffuse hit, **p**. There, we want to estimate slow-varying indirect illumination.
 - Instead of growing sphere in global map at p, Final Gather shoots 100-1000 indirect rays from p and grows sphere in the global map and also caustics map, where each of those rays end at a diffuse surface. Or interpolate from nearby already computed final-gather points.

Photon Mapping - Summary

Creating Photon Maps:

Trace photons (~100K-1M) from light source. Store them in kd-tree when they hit diffuse enough surface (e.g., not 100% specular). Then, use russian roulette to decide if the photon should be absorbed or specularly or diffusively reflected. Create both global map and caustics map. For the Caustics map, we send more of the photons towards reflective/refractive objects.

Ray trace from eye:

- As usual: I.e., shooting primary rays and recursively shooting reflection/refraction rays, and at each intersection point p, compute direct illumination (shadow rays + local shading).
- Also grow sphere around each p in caustics map to get caustics contribution and in global map to get slow-varying indirect illumination.
- If final gather is used: At the first diffuse hit, instead of using global map directly, sample the indirect illumination around **p** by sampling the hemisphere with ~100–1000 rays and **then** use the two photon maps where those rays hit a surface.

Growing sphere:

Uses the kd-tree to grow a sphere around **p** until a fixed amount (e.g. 50) photons are inside the sphere.
 Estimate outgoing radiance by using the material's brdf and the photons' powers and incoming directions.

Or shorter summary:

- 1. Shoot photons from light source, and let them bounce around in the scene, and store them where they land (e.g. in a kD-tree).
- 2. Ray-tracing pass from the eye. Estimate radiance at each ray hit, by growing a sphere (at the hit point in the kD-tree) until it contains a predetermined #photons. Use a caustics map and a global map.

Lecture 11: Shadows + Reflection

- Point light / Area light
- Three ways of thinking about shadows
 - The basis for different algorithms.
- Shadow mapping
 - Be able to describe the algorithm
 - Percentage closer filtering
 - Cascaded shadow maps
- Shadow volumes
 - Be able to describe the algorithm
 - Stencil buffer, 3-pass algorithm, Z-pass, Z-fail,
 - Creating quads from the silhouette edges as seen from the light source, etc
- Pros and cons of shadow volumes vs shadow maps
- Planar reflections how to do. Why not using environment mapping?

Ways of thinking about shadows

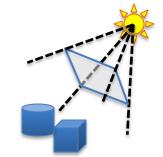
- As separate objects (like Peter Pan's shadow) This corresponds to planar shadows
- As volumes of space that are dark
 - This corresponds to shadow volumes
- As places not seen from a light source looking at the scene. This corresponds to shadow maps
- Note that we already "have shadows" for objects facing away from light

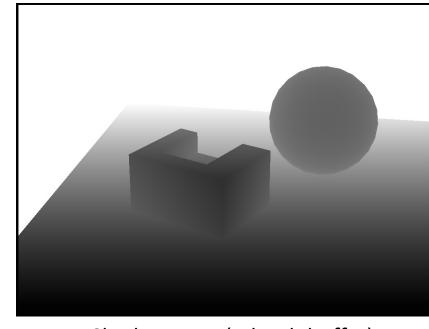
Shadow Maps - Summary

Shadow Map Algorithm:

- Render a z-buffer from the light source
 - Represents geometry in light
- Render from camera
 - For every fragment:
 - Transform(warp) its 3D-pos (x,y,z) into shadow map (i.e. light space) and compare depth with the stored depth value in the shadow map
 - If depth greater-> point in shadow
 - Else -> point in light
 - Use a bias at the comparison

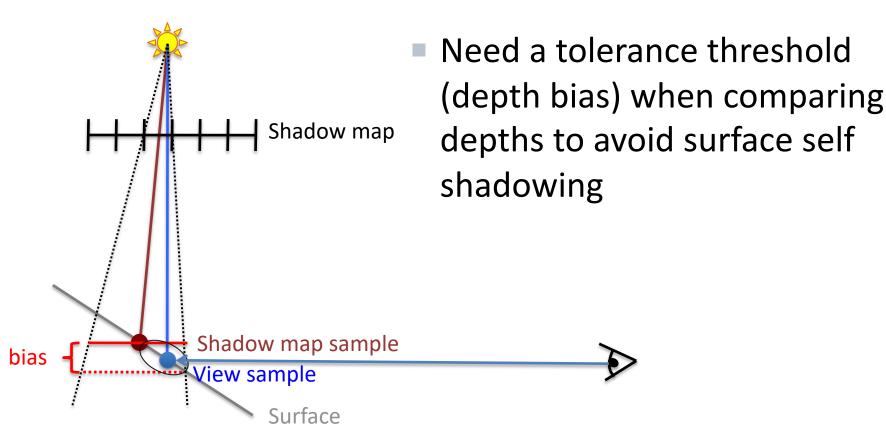
Understand z-fighting and light leaks





Shadow Map (=depth buffer)

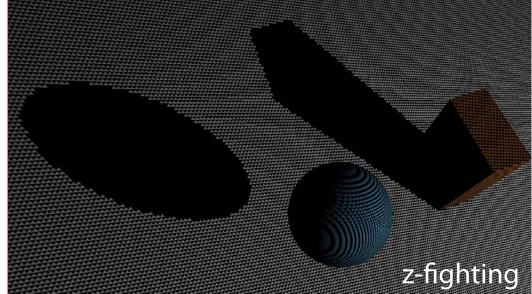
Bias



Bias

Shadow map Shadow map sample bias View sample Surface

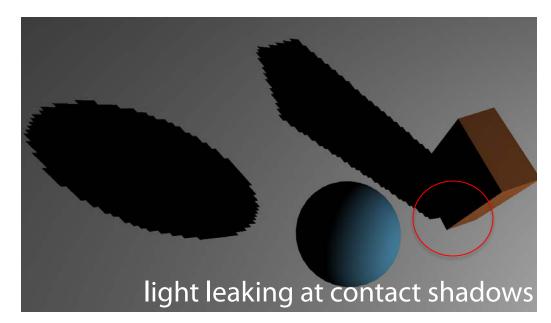
 Need a tolerance threshold (depth bias) when comparing depths to avoid surface self shadowing



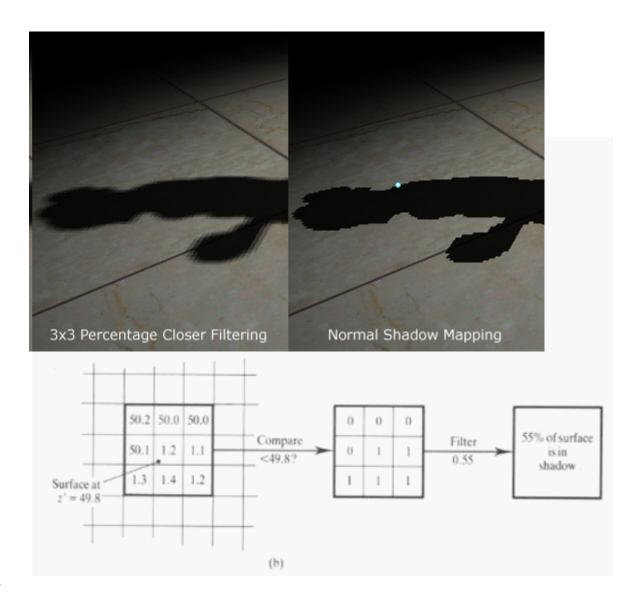
Bias

Shadow map Shadow map sample bias View sample Surface Surface that should be in shadow

 Need a tolerance threshold (depth bias) when comparing depths to avoid surface self shadowing



Percentage Closer Filtering



Use a neighborhood of the SM pixel (e.g., 3x3 region) to compute an averaged shadow result of this region.

Cascaded Shadow Maps

You need high SM resolution close to the camera and can use lower further away. So create a separate SMs per depth region of the view frustum, with higher spatial resolution closer to camera.

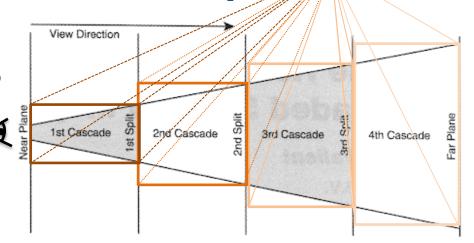
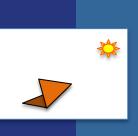


FIGURE 4.1.1 2D visualization of view frustum split (uniformly) into separate cascade frustums.

Shadow volumes

Create shadow quads for all silhouette edges (as seen from the light source). (The normals are pointing outwards from the shadow volume.)



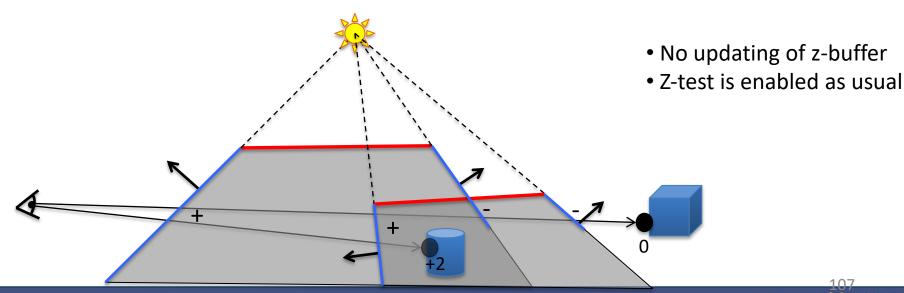


Edges between one triangle front facing the light source and one triangle back facing the light source are considered silhouette edges.

Then...

Shadow Volumes - concept

- Perform counting with the stencil buffer
 - Render front facing shadow quads to the stencil buffer
 - Inc stencil value, since those represents entering shadow volume
 - Render back facing shadow quads to the stencil buffer
 - Dec stencil value, since those represents exiting shadow volume

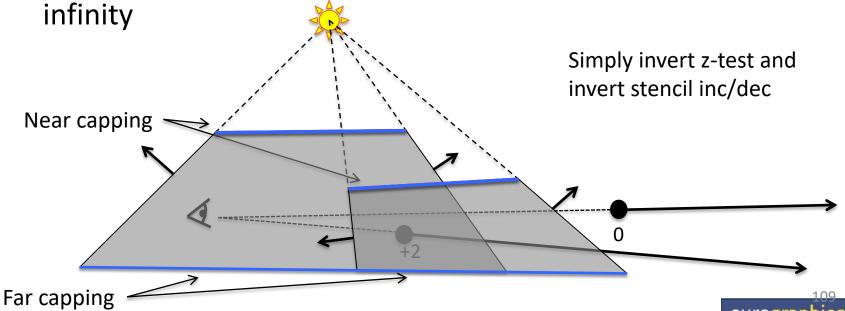


Shadow Volumes with the Stencil Buffer

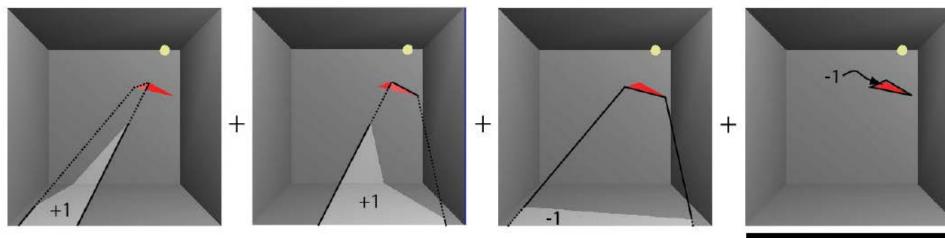
- A three pass process:
 - 1st pass: Render ambient lighting
 - 2nd pass:
 - Draw to stencil buffer only
 - Turn off updating of z-buffer and writing to color buffer but still use standard depth test
 - Set stencil operation to
 - » incrementing stencil buffer count for frontfacing shadow volume quads, and
 - » decrementing stencil buffer count for backfacing shadow volume quads
 - 3rd pass: Render diffuse and specular where stencil buffer is 0.

The Z-fail Algorithm

- Z-pass must offset the stencil buffer with the number of shadow volumes that the eye is inside. Problematic.
- Count to infinity instead of to the eye
 - We can choose any reference location for the counting
 - A point in light avoids any offset
 - Infinity is always in light if we cap the shadow volumes at infinity



Z-fail by example

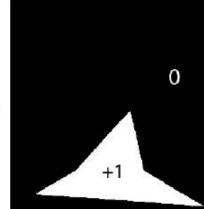


Compared to Z-pass:

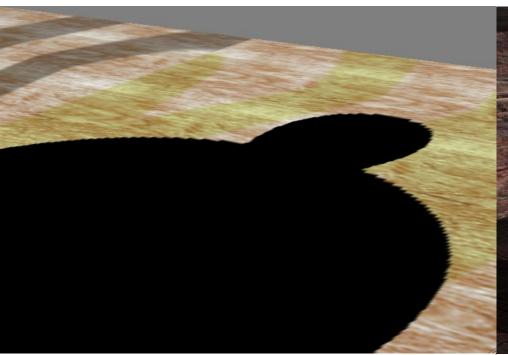
Invert z-test

Invert stencil inc/dec

I.e., count to infinity instead of from eye.



Shadow Maps vs Shadow Volumes





- Good: Handles any rasterizable geometry, constant cost regardless of complexity, map can sometimes be reused. Very fast.
- Bad: Frustum limited. Jagged shadows if restoo low, biasing headaches.
 - Solution:
 - 6 SM (cube map), high res., use filtering (huge topic)



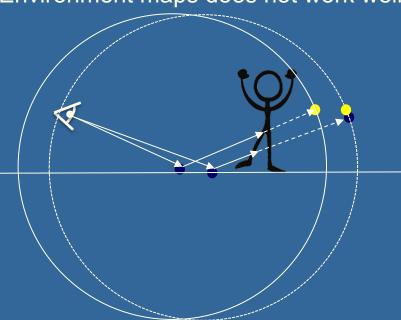
Shadow Volumes

- Good: shadows are **sharp**. Handles omnidirectional lights.
- Bad: 3 passes, shadow polygons must be generated and rendered → lots of polygons & fill
 - Solution: culling & clamping

Planar reflections

- We've already done reflections in curved surfaces with environment mapping. But the env.map is assumed to have an infinite radius, such that only the reflection ray's direction (not origin) matters. Hence...
- ...Environment maps does not work well for reflections in planar surfaces:

For two adjacent screen pixels, the cube map returns a too small uv change. Hence the reflection will be smeared out.





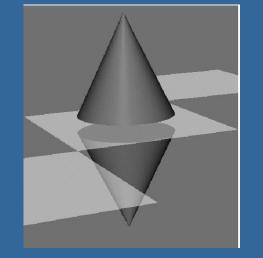
Standar (sheubey) map Parallax correcte d

 Parallax corrected cube maps fix this, but has its own problems. Ray tracing solves all but is slower. Purely planar reflections are actually easy to get by reflecting the geometry or camera as we will see on the next slide...

Planar reflections

Two methods:

- 1. Reflecting the object:
 - If reflection plane is z=0 (else somewhat more complicated – see page 504)
 - Apply glScalef(1,1,-1);
 - Backfacing becomes front facing!
 - i.e., use frontface culling instead of backface culling
 - Lights should be reflected as well
- 2. Reflecting the camera in the reflection plane



Planar reflections

- Assume plane is z=0
- Then apply glScalef(1,1,-1);
- Effect:

Z

Important:

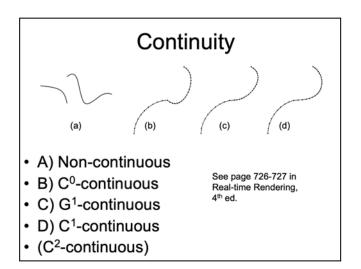
- render scaled (1,1,-1) model
- · with reflected light pos.
- using front face culling

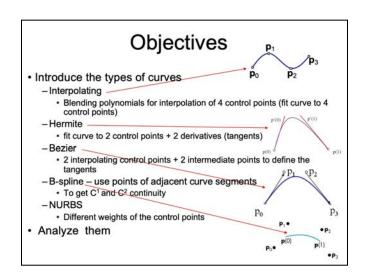
Or reflect camera position instead of the object:

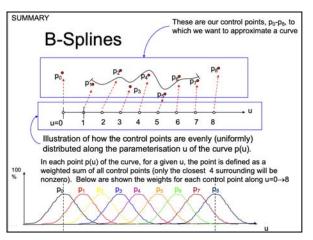
Right-hand sided coordinate system pepts puerl-tyan

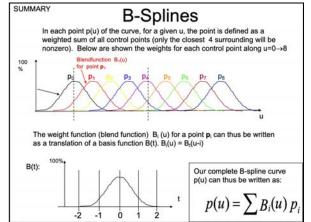
- Render reflection:
 - 1. Render reflective plane to stencil buffer
 - 2. Reflect camera including camera axes ← The important part!
 - 3. Set user clip plane in mirror plane to cull anything between mirror and reflected camera
 - 4. Render scene from reflected camera.
- Render scene as normal from original camera

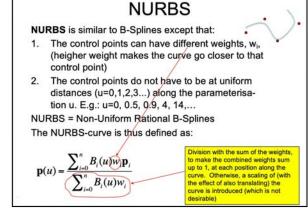
12. Curves and Surfaces – what you need to know:









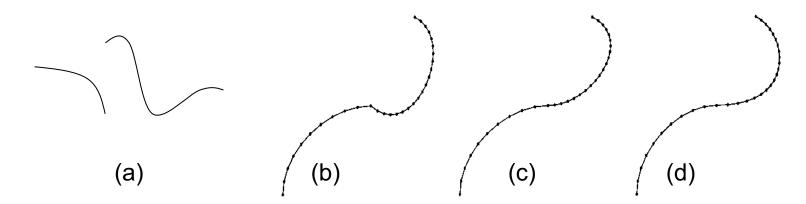


Curves and Surfaces - outline

Goal is to explain NURBS curves/surfaces...

- Introduce types of curves and surfaces
 - Explicit not general, easy to compute.
 - Implicit general, non-easy to compute.
 - Parametric general + simple to compute. We choose this.
- A complete curve is split into curve segments, each defined by a cubical polynomial.
 - Introducing Interpolating/Hermite/Bezier curves.
- Adjacent segments should have C² continuity.
 - Leads to B-Splines with a blending function (a spline) per control point
 - Each spline consists of 4 cubical polynomials, forming a bell shape translated along u.
 - (Also, four bells will overlap at each point on the complete curve.)
- NURBS a generalization of B-Splines:
 - Control points at non-uniform locations along parameter u.
 - Individual weights (i.e., importance) per control point

Continuity



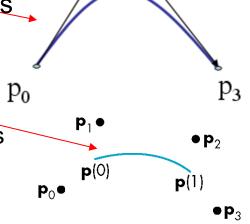
- A) Non-continuous
- B) C⁰-continuous
- C) G¹-continuous
- D) C¹-continuous
- (C²-continuous)

See page 726-727 in Real-time Rendering, 4th ed.

Types of Curves p₁

 \mathbf{p}_0

- Introduce the types of curves
 - Interpolating
 - Blending polynomials for interpolation of 4 control points (fit curve to 4 control points)
 - Hermite
 - fit curve to 2 control points + 2 derivatives (tangents)
 - Bezier
 - 2 interpolating control points + 2 intermediate points to define the tangents
 - B-spline use points of adjacent curve segments
 - To get C¹ and G² continuity
 - -NURBS
 - Different weights of the control points
 - The control points can be at non-uniform intervalls



Splines and Basis

- If we examine the cubic B-spline from the perspective of each control (data) point, each interior point contributes (through the blending functions) to four segments
- We can rewrite p(u) in terms of the data points as

$$p(u) = \sum B_i(u) p_i$$

defining the basis functions {B_i(u)}

B-Splines

These are our control points, p_0 p_8 , to which we want to approximate a curve

u

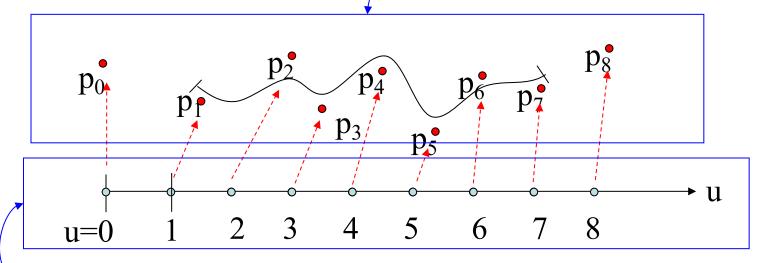
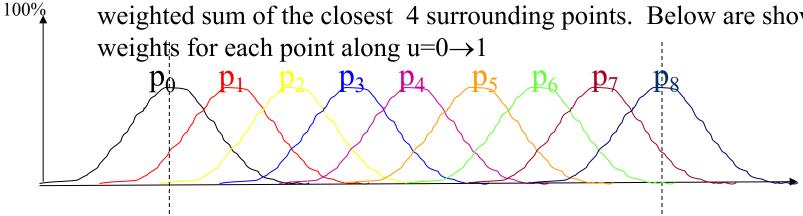


Illustration of how the control points are evenly (uniformly) distributed along the parameterisation u of the curve p(u).

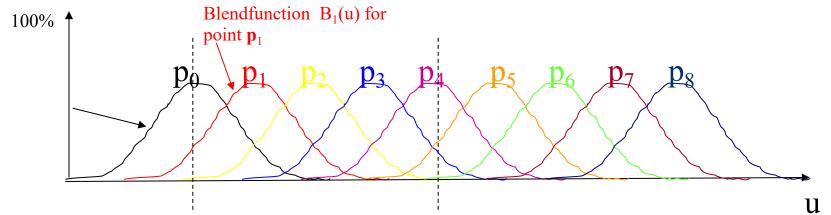
In each point p(u) of the curve, for a given u, the point is defined as a weighted sum of the closest 4 surrounding points. Below are shown the



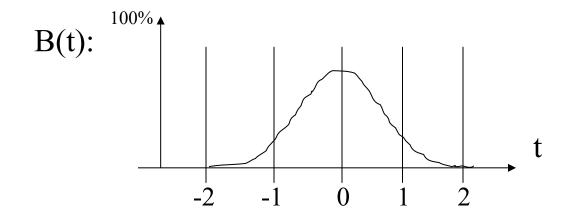
SUMMARY

B-Splines

In each point p(u) of the curve, for a given u, the point is defined as a weighted sum of the closest 4 surrounding points. Below are shown the weights for each point along $u=0\rightarrow 1$



The weight function (blend function) $B_{pi}(u)$ for a point p_i can thus be written as a translation of a basis function B(t). $B_{pi}(u) = B(u-i)$



Our complete B-spline curve p(u) can thus be written as:

$$p(u) = \sum B_i(u) p_i$$

NURBS

NURBS is similar to B-Splines except that:

- The control points can have different weights, w_i, (heigher weight makes the curve go closer to that control point)
- 2. The control points do not have to be at uniform distances (u=0,1,2,3...) along the parameterisation u. E.g.: u=0, 0.5, 0.9, 4, 14,...

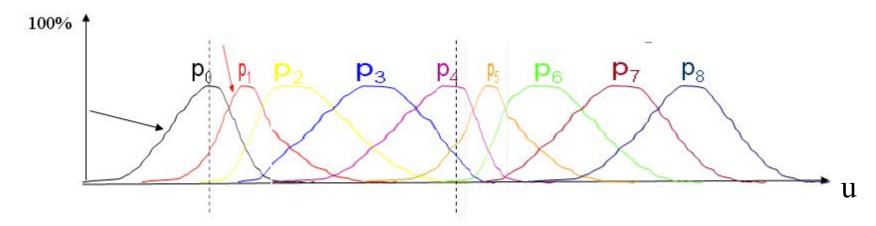
NURBS = Non-Uniform Rational B-Splines
The NURBS-curve is thus defined as:

$$\mathbf{p}(u) = \frac{\sum_{i=0}^{n-1} B_i(u) w_i \mathbf{p}(i)}{\sum_{i=0}^{n-1} B_i(u) w_i}$$

Division with the sum of the weights, to make the combined weights sum up to 1, at each position along the curve. Otherwise, a translation of the curve is introduced (which is not desirable)

NURBS

- Allowing control points at non-uniform distances means that the basis functions B_{pi}() are being streched and non-uniformly located.
- E.g.:



Each curve $B_{pi}()$ should of course look smooth and C^2 –continuous. But it is not so easy to draw smoothly by hand...(The sum of the weights are still =1 due to the division in previous slide)

Lecture 13:

Linearly interpolate $(u_i/w_i, v_i/w_i, 1/w_i)$ in screenspace from each triangle vertex i.

Then at each pixel:

$$u_{ip} = (u/w)_{ip} / (1/w)_{ip}$$

 $v_{ip} = (v/w)_{ip} / (1/w)_{ip}$

where ip = screen-space interpolated value from the triangle vertices.

- Perspective correct interpolation (e.g. for textures)
- Taxonomy:
 - Sort first
 - sort middle
 - sort last fragment
 - sort last image
- Bandwidth
 - Why it is a problem and how to "solve" it
 - L1 / L2 caches
 - Texture caching with prefetching, (warp switching)
 - Texture compression, Z-compression, Z-occlusion testing (HyperZ)
- Be able to sketch the functional blocks and relation to hardware for a modern graphics card (next slide→)

