Parsing Expressions

Slides by Koen Lindström Claessen & David Sands

Expressions

- Such as
 - 5*2+12
 17+3*(4*3+75)
- Can be modelled as a datatype

data Expr = Num Int | Add Expr Expr | Mul Expr Expr

Showing and Reading

built-in show

function produces

ugly results

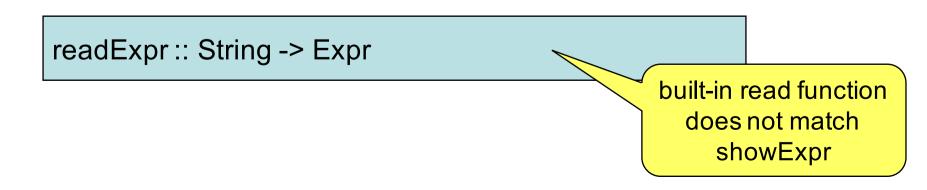
• We have seen how to write

showExpr :: Expr -> String

Main> showExpr (Add (Num 2) (Num 4))

"2+4" **Main>** *showExpr (Mul (Add (Num 2) (Num 3)) (Num 4)* (2+3)*4

• This lecture: How to write



Parsing

- Transforming a "flat" string into something with a richer structure is called *parsing*
 - expressions

— ...

- programming languages
- natural language (swedish, english, dutch)
- Very common problem in computer science
 - Many different solutions

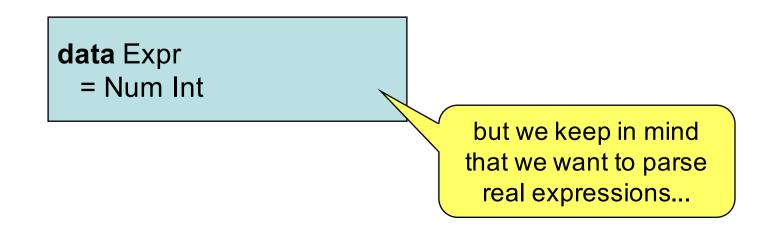
Parser libraries

- Haskell has many nice libraries that make it easy to write parsers
 - E.g. parsec included in the Haskell Platform: http://hackage.haskell.org/package/parsec
- In this lecture we will do it from scratch

Expressions

data Expr = Num Int | Add Expr Expr | Mul Expr Expr

- Let us start with a simpler problem
- How to parse



Parsing Numbers

number :: String -> Int

Main> number "23" 23 Main> number "apa" ? Main> number "23+17" ?

Parsing Numbers

- Parsing a string to a number, there cases:
 - (1) the string is a number, e.g. "23"

how to model

these?

- (2) the string is not a number at all, e.g. "apa"
- (3) the string *starts* with a number, e.g. "17+24"

Case(1)

and (3) are

similar...

A Parser

String -> Maybe (a, String)

type Parser a = String -> Maybe (a, String)



A Parser for things is a function from Strings to Maybe a thing and a String

G Hutton, Programming in Haskell

Parsing Numbers

Parsing a string to a number, there are three cases:

(1) the string is a number, e.g. "23"

Just(23,"")

(2) the string is not a number at all, e.g. "apa" Nothing

(3) the string *starts* with a number, e.g. "17+24" Just(17,"+24")

Parsing Numbers

number :: Parser Int

Main> number "23" Just (23, "") Main> number "apa" Nothing Main> number "23+17" Just (23, "+17")

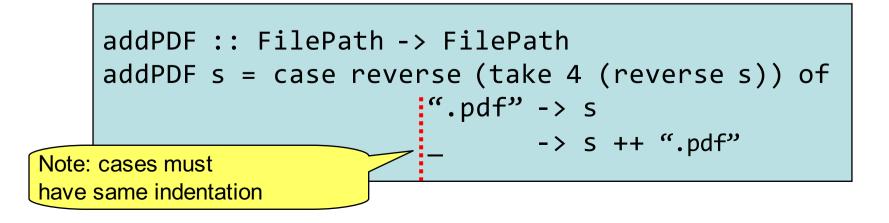
how to implement?

Case expressions

• We have seen many examples of pattern matching in function definitions

rank (Card r _) = r

Sometimes we just want to match on a local value given by an expression Use case expressions for this

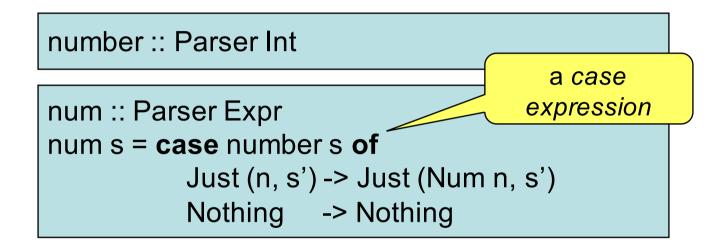


Parsing Numbers

import Data.Char(isDigit)

```
number :: Parser Int
number (c:s)
| isDigit c = Just (numb,rest)
| otherwise = Nothing
where
numb = read (takeWhile isDigit (c:s))
rest = dropWhile isDigit (c:s)
```

Parsing Numbers



Main> num "23" Just (Num 23, "") Main> num "apa" Nothing Main> num "23+17" Just (Num 23, "+17")

The structure of expression strings

- An expression must be of the forn " $t_1 + t_2 + ... + t_m$ "
 One or more terms with '+' between them
- Each term t_i must be of the form " $f_1 * f_2 * ... * f_n$ "
- Each factor f_i must be a number

We're currently ignoring parentheses

• We need four different parsers, one for each category: expression, term, factor, number

Parsing strategy

Solves the problem of where to split the string

Each parser will eat as much of the input as "makes sense" to it, and leave the rest untouched

- Parse "1*2+3asd" as an expression
 - result: Add (Mul (Num 1) (Num 2)) (Num 3)
 - rest: "asd"
- Parse "1*2+3asd" as a term
 - result: Mul (Num 1) (Num 2)
 - rest: "+3asd"
- Parse "1*2+3asd" as a factor
 - result: Num 1
 - rest: "*2+3asd"

Parsing example

- Parse "1+2" as an expression
 - Should have the form " $t_1 + t_2 + ... + t_m$ ", so we start by looking for a term
- Parse "1+2" as a term
 - Should have the form " $f_1 * f_2 * ... * f_n$ ", so we start by looking for a factor
- Parse "1+2" as a factor

– Should be a number

... continue on the next slide

Parsing example

- Parse "1+2" as a number
 - Return the number and the rest of the string: (1, "+2")
- The factor parser returns (Num 1, "+2")
- The term parser returns (Num 1, "+2")
- The expression parser now has hold of the first term.
 - Since the rest of the string starts with "+", it goes on to look for another term.
 - Now the rest of the string is "", so there are no more terms, and it can return (Add (Num 1) (Num 2), "")

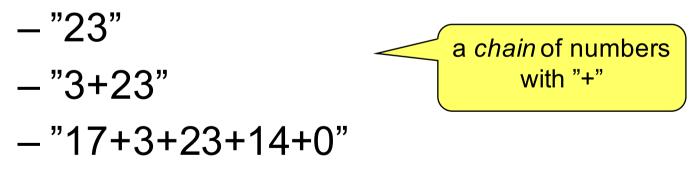
The structure of expression strings

- An expression must be of the form " $t_1 + t_2 + ... + t_m$ "
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Expressions

data Expr = Num Int | Add Expr Expr

Expressions are now of the form

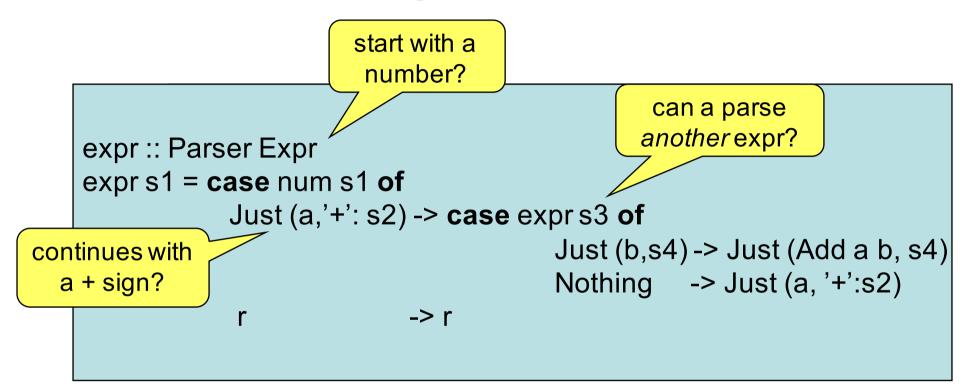


Parsing Expressions

expr :: Parser Expr

Main> expr "23" Just (Num 23, "") Main> expr "apa" Nothing Main> expr "23+17" Just (Add (Num 23) (Num 17), "") Main> expr "23+17)" Just (Add (Num 23) (Num 17), ")")

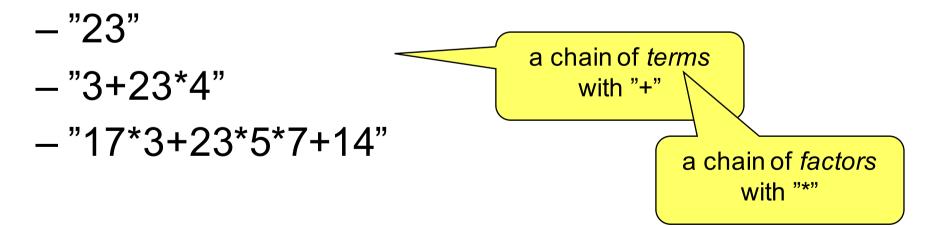
Parsing Expressions



Expressions

data Expr = Num Int | Add Expr Expr | Mul Expr Expr

Expressions are now of the form



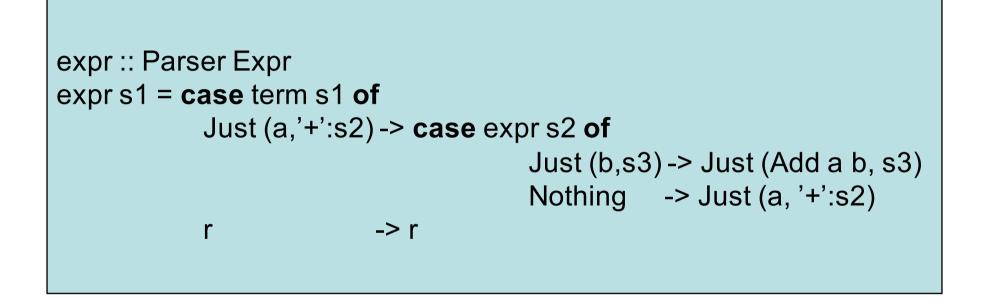
Grammar for Expressions

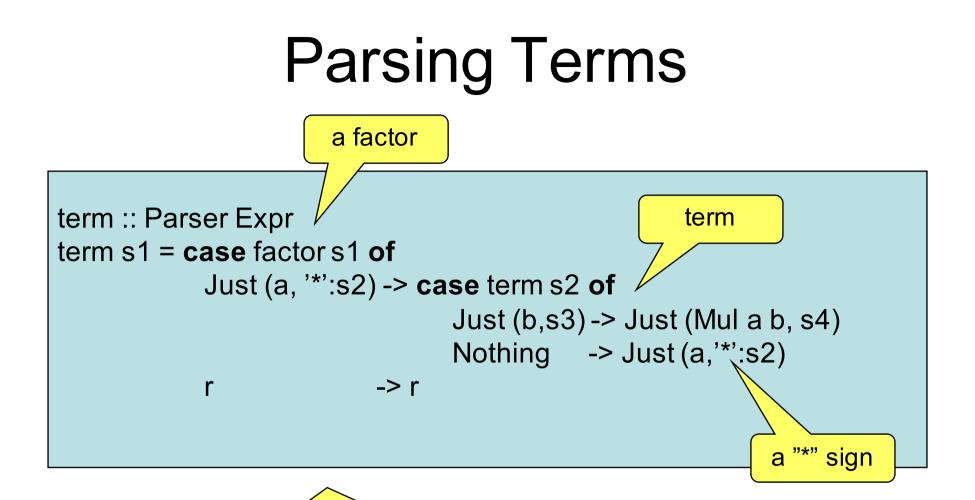
 Parse Expressions according to the following BNF grammar:

<expr></expr>	::= <term></term>	<term></term>	"+" <expr></expr>
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- <term> ::= <factor> | <factor> "*" <term>
- <factor> ::= "(" <expr> ")" | <number>

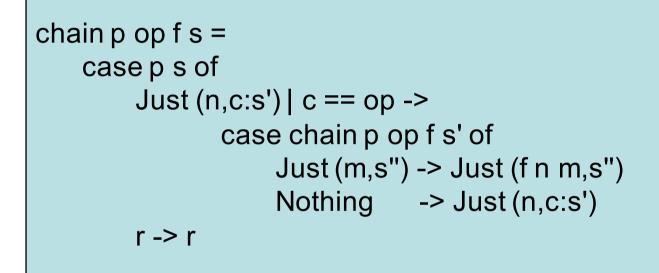
Parsing Expressions





Horrible cut-and-paste programming! Better: abstract over the differences between term and expr and make a more general function

Parsing Chains



expr, term :: Parser Expr expr = chain term '+' Add term = chain factor '*' Mul

Factor?

factor :: Parser Expr factor = num

Parentheses

- So far no parentheses
- Expressions look like
 - 23 - 23+5*17 - 23+5*(17+23*5+3) a factor can be a parenthesized expression again

Factor?

```
factor :: Parser Expr
factor ('(':s) =
case expr s of
Just (a, ')':s1) -> Just (a, s1)
_- -> Nothing
```

factors = num s

Reading an Expr

Main> readExpr "23" Just (Num 23) Main> readExpr "apa" Nothing Main> readExpr "23+17" Just (Add (Num 23) (Num 17))

Alternative number parsing

number :: Parser Int number (c:s) | isDigit c = Just (n,s') where n = read \$ takeWhile isDigit (c:s) s' = dropWhile isDigit s number _ = Nothing

Summary

- Parsing becomes easier when
 - Failing results are explicit
 - A parser also produces the *rest* of the string
- Case expressions
 - To look at an intermediate result
- Higher-order functions
 - Avoid copy-and-paste programming

The Code (1)

```
readExpr :: String -> Maybe Expr
readExpr s = case expr s of
Just (a,"") -> Just a
_ -> Nothing
```

```
expr, term :: Parser Expr
expr = chain term '+' Add
term = chain factor '*' Mul
```

```
factor :: Parser Expr
factor ('(':s) =
case expr s of
Just (a, ')':s1) -> Just (a, s1)
________-> Nothing
factor s = num s
```

The Code (2)

```
chain p op f s =

case p s of

Just (n,c:s2) | c == op ->

case chain p op f s2 of

Just (m,s3) -> Just (f n m,s3)

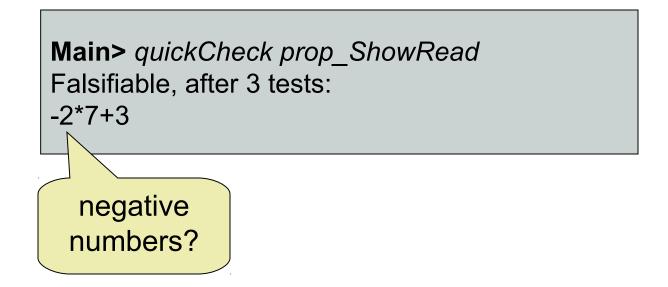
Nothing -> Just (n,c:s2)

r -> r
```

```
number :: Parser Int
number (c:s) | isDigit c = Just (digits 0 (c:s))
number _ = Nothing
digits :: Int -> String -> (Int,String)
digits n (c:s) | isDigit c = digits (10*n + digitToInt c) s
digits n s = (n,s)
```

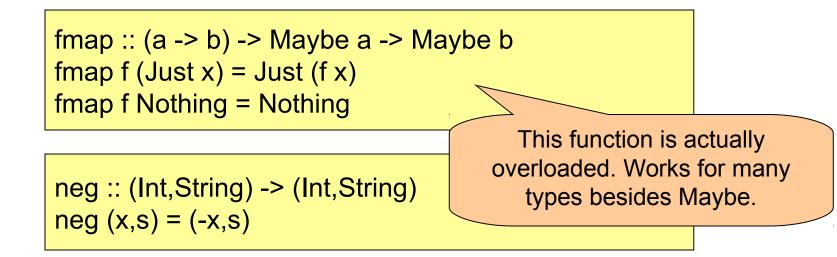
Testing readExpr

prop_ShowRead :: Expr -> Bool
prop_ShowRead a =
 readExpr (show a) == Just a



Fixing the Number Parser

```
number :: Parser Int
number (c:s) | isDigit c = Just (digits 0 (c:s))
number ('-':s) = fmap neg (number s)
number _ = Nothing
```

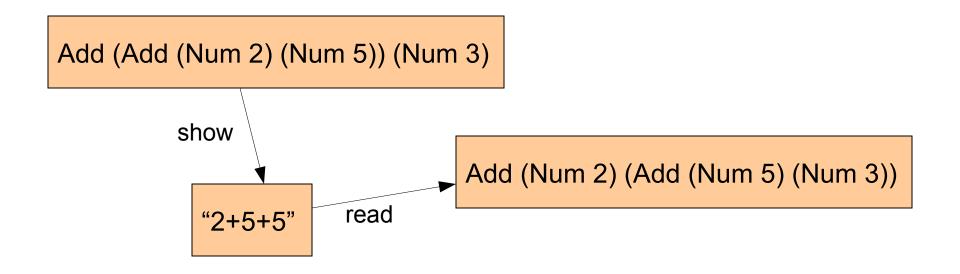


Testing again

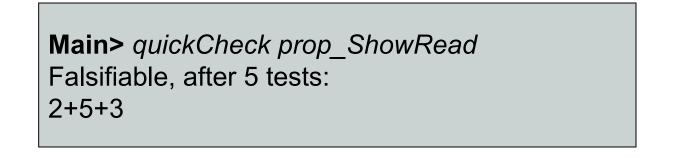
Main> quickCheck prop_ShowRead Falsifiable, after 5 tests: 2+5+3

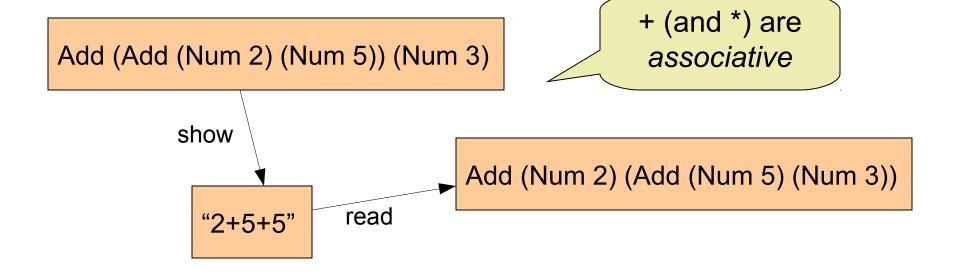
Testing again

Main> quickCheck prop_ShowRead Falsifiable, after 5 tests: 2+5+3



Testing again





Fixing the Property (1)

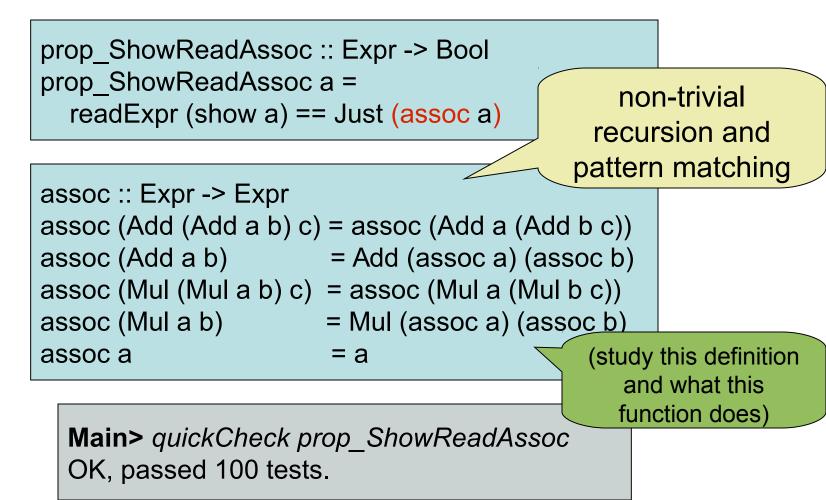
The result does not have to be *exactly* the same, as long as the *value* does not change.

prop_ShowReadEval :: Expr -> Bool
prop_ShowReadEval a =
 fmap eval (readExpr (show a)) == Just (eval a)

Main> *quickCheck prop_ShowReadEval* OK, passed 100 tests.

Fixing the Property (2)

The result does not have to be *exactly* the same, only after rearranging associative operators



Properties about Parsing

- We have checked that readExpr correctly processes anything produced by showExpr
- Is there any other property we should check?
 - What can still go wrong?
 - How to test this?

Very difficult!

Summary

- Testing a parser:
 - Take any expression,
 - convert to a String (show),
 - convert back to an expression (read),
 - check if they are the same
- Some structural information gets lost
 - associativity!
 - -use "eval"
 - use "assoc"