### Recursive Datatypes and Lists

data Suit = Spades | Hearts | Diamonds | Clubs

Interpretation:

"Here is a new type Suit. This type has four possible values: Spades, Hearts, Diamonds and Clubs."

data Suit = Spades | Hearts | Diamonds | Clubs

This definition introduces five things:

– The type Suit

– The Constructors

Spades	:: Suit
Hearts	:: Suit
Diamonds	:: Suit
Clubs	:: Suit

data Rank = Numeric Integer | Jack | Queen | King | Ace

Interpretation:

"Here is a new type Rank. Values of this type have five possible possible forms: Numeric n, Jack, Queen, King or Ace, where n is a value of type Integer"

data Rank = Numeric Integer | Jack | Queen | King | Ace

This definition introduces six things:

- The type Rank
- The Constructors

Numeric	::???
Jack	::???
Queen	::???
King	::???
Ace	::???

data Rank = Numeric Integer | Jack | Queen | King | Ace

This definition introduces six things:

- The type Rank
- The Constructors

Numeric:: Integer  $\rightarrow$  RankJack:: ???Queen:: ???King:: ???Ace:: ???

data Rank = Numeric Integer | Jack | Queen | King | Ace

This definition introduces six things:

- The type Rank
- The Constructors
  - Jack
  - Queen :: Rank
  - King
  - Ace

- Numeric :: Integer  $\rightarrow$  Rank
  - :: Rank

  - :: Rank
  - :: Rank



data Card = Card Rank Suit

Interpretation:

"Here is a new type Card. Values of this type have the form Card r s, where r and s are values of type Rank and Suit respectively."

data Card = Card Rank Suit

This definition introduces two things:
The type Card
The Constructor Card :: ???

data Card = Card Rank Suit

This definition introduces two things:
– The type Card
– The Constructor
Card :: Rank → Suit → Card



data Hand = Empty | Add Card Hand

Interpretation:

"Here is a new type Hand. Values of this type have two possible forms: Empty or Add c h where c and h are of type Card and Hand respectively."

data Hand = Empty | Add Card Hand

Alternative interpretation:

"A hand is either empty or consists of a card on top of a smaller hand."

data Hand = Empty | Add Card Hand

This definition introduces three things: – The type Hand – The Constructors Empty :: ??? Add :: ???

data Hand = Empty | Add Card Hand

This definition introduces three things: – The type Hand – The Constructors Empty :: Hand Add :: ???

data Hand = Empty | Add Card Hand

This definition introduces three things: – The type Hand – The Constructors Empty :: Hand Add :: Card  $\rightarrow$  Hand  $\rightarrow$  Hand



Define functions by stating their results for all possible forms of the input

size :: Num a => Hand  $\rightarrow$  a

Define functions by stating their results for all possible forms of the input

size :: Num a => Hand  $\rightarrow$  a size Empty = 0 size (Add Card hand) = 1 + size hand

Interpretation:

"If the argument is Empty, then the result is 0. If the argument consists of a card **card** on top of a hand hand, then the result is 1 + the size of the rest of the hand."

size :: Num a => Hand  $\rightarrow$  a size Empty = 0 size (Add Card hand) = 1 + size hand

Patterns have two purposes:

- 1. Distinguish between forms of the input (e.g. Empty and Add)
- 2. Give names to parts of the input (In the definition of size, card is the first card in the argument, and hand is the rest of the hand.)



### Construction/destruction

When used in an expression (RHS), Add *constructs* a hand:

aHand :: Hand aHand = Add c1 (Add c2 Empty)

When used in a pattern (LHS), Add *destructs* a hand:

size (Add Card hand) = ...

#### Lists – how they work

data List = Empty | Add ?? List

- Can we generalize the Hand type to lists with elements of arbitrary type?
- What to put on the place of the ??

data List a = Empty | Add a (List a)

A parameterized type

Constructors: Empty :: ??? Add :: ???

data List a = Empty | Add a (List a)

A parameterized type

Constructors: Empty :: List a Add :: ???

**data** List a = Empty | Add a (List a)

A parameterized type

Constructors: Empty :: List a Add ::  $a \rightarrow List a \rightarrow List a$ 

# Built-in lists

data [a] = [] | (:) a [a]

Not a legal definition, but the built-in lists are *conceptually* defined like this

**Constructors:** 

 $\begin{array}{ll} [] & \vdots & [a] \\ (\vdots) & \vdots & a \rightarrow & [a] \rightarrow & [a] \end{array}$ 

# Built-in lists

```
Instead of
   Add 1 (Add 2 (Add 3 Empty))
we can use built-in lists and write
   (:) 1 ((:) 2 ((:) 3 []))
or, equivalently
   1:2:3:[]
or, equivalently
                              Special syntax for the
   [1,2,3]
                                  built-in lists
```

- Can represent 0, 1, 2, ... things
  -[], [3], ["apa", "katt", "val", "hund"]
- They all have the same type -[1,3,True,"apa"] is not allowed
- The order matters
  - -[1,2,3] /= [3,1,2]
- Syntax

- 5 : (6 : (3 : [])) == 5 : 6 : 3 : [] == [5,6,3] - "apa" == ['a','p','a']

# Programming Examples

See files Lists0.hs and Lists1.hs

# More on Types

- Functions can have "general" types:
  - polymorphism
  - reverse :: [a]  $\rightarrow$  [a]
  - -(:) ::  $a \rightarrow [a] \rightarrow [a]$
- Sometimes, these types can be restricted
  - Ord a  $\Rightarrow$  ... for comparisons (<, <=, >, >=, ...)
  - Eq a => ... for equality (==, /=)
  - Num a => ... for numeric operations (+, -, \*, ...)

## Do's and Don'ts



## Do's and Don'ts



## Do's and Don'ts



comparison with a boolean constant

resultIsBig :: Integer  $\rightarrow$  Bool resultIsBig n = not (isSmall (f n))



