Software Engineering using Formal Methods

Modeling Concurrency

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Concurrent Systems – The Big Picture

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Solutions to this must be carefully designed and verified, otherwise...

Concurrent Systems – The Big Picture

Focus of this Lecture

Aim of SPIN-style model checking methodology:

exhibit flaws in software systems

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exhibit design flaws in software systems

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Focus of next lecture:

- Modeling and analyzing distributed systems

Concurrent/Distributed systems difficult to get right

problems:

- hard to predict, hard to form faithful intuition

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  often impossible to analyze/debug defect
- lack of time
  exhaustive testing exhausts the testers long before it exhausts behavior of the system...

Mission of SPIN-style Model Checking

offer an efficient methodology to

- improve the design
- exhibit defects

of concurrent and distributed systems

Activities in Spin-style Model Checking

1. model (critical aspects of) concurrent/distributed system with Promela
2. state crucial properties with assertions, temporal logic, ...
3. use Spin to check all possible runs of the model
4. analyze result, possibly re-work **1.** and **2.**

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The hardest part of Model Checking are **1.** and **2.**

Seprate concerns of model vs. property! Check the property you want the model to have, not the one it happens to have.

Main Challenges of Modeling

expressiveness
: model must be expressive enough to ‘embrace’ defects the real system could have

simplicity
: model must be simple enough to be ‘model checkable’, theoretically and practically

Modeling Concurrent Systems in Promela

in the SPIN approach,
the cornerstone of modeling concurrent/distributed systems are

PROMELA processes

Initializing Processes

there is always an initial process prior to all others

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often declared *implicitly* using '**active**'

can be declared *explicitly* with key word '**init**'

```
init {
  printf("Hello␣world\n")
}
```

if *explicit*, **init** is used to start other processes with **run** statement

Starting Processes

processes can be started *explicitly* using **run**

```
proctype P() {
  byte local;
  ...
}

init {
  run P();
  run P()
}
```

each **run** operator starts copy of process (with copy of local variables)

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run `P()` does *not* wait for `P` to finish

PROMELA's **run** corresponds to JAVA's **`start`**, *not* to JAVA's **`run`**

Atomic Start of Multiple Processes

by convention, **run** operators enclosed in **atomic** block

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proctype P() {
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(more on **atomic** later)

Joining Processes

following trick allows ‘joining’, i.e., waiting for all processes to finish

```
byte result;

proctype P() {
  ...
}

init {
  atomic {
    run P();
    run P()
  }
  (_nr_pr == 1); /*blocks until join*/
  printf("result␣=%d", result)
}
```

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}
```

`_nr_pr` built-in variable holding number of running processes

`_nr_pr == 1` only 'this' process (**init**) is (still) running

Process Parameters

Processes may have formal parameters, instantiated by **run**:

```
proctype P(byte id; byte incr) {
   ...
}

init {
  run P(7, 10);
  run P(8, 15)
}
```

Active (Sets of) Processes

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  ...
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```
active [n] proctype P() {
  ...
}
```

implicit **init** will **run** *n* copies of `P`

Local and Global Data

Variables declared outside of the processes are global to all processes.

Variables declared inside a process are local to that processes.

```
byte n;

proctype P(byte id; byte incr) {
  byte t;
  ...
}
```

`n` is global

`t` is local

Modeling with Global Data

pragmatics of modeling with global data:

shared memory of concurrent systems often modeled
by global variables of numeric (or array) type

status of shared resources (printer, traffic light, ...) often modeled
by global variables of Boolean or enumeration type
(**bool**/**mtype**).

communication mediums of distributed systems often modeled
by global variables of channel type (**chan**). (next lecture)

Interference on Global Data

```
byte n = 0;

active proctype P() {
  n = 1;
  printf("Process␣P,␣n␣=␣%d\n", n)
}
```

Interference on Global Data

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byte n = 0;

active proctype P() {
  n = 1;
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}

active proctype Q() {
  n = 2;
  printf("Process␣Q,␣n␣=␣%d\n", n)
}
```

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how many outputs possible?

different processes can interfere on global data

Examples

1. `interleave0.pml`
   SPIN simulation, SPINSPIDER automata + transition system
2. `interleave1.pml`
   SPIN simulation, adding assertion, fine-grained execution model, model checking
3. `interleave5.pml`
   SPIN simulation, SPIN model checking, trail inspection

Atomicity

limit the possibility of sequences being interrupted by other processes

weakly atomic sequence

can *only* be interrupted if a statement is not executable

strongly atomic sequence

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defined in PROMELA by **atomic{ ... }**

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cannot be interrupted at all
defined in PROMELA by **d_step{ ... }**

Deterministic Sequences

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d_step:

- strongly atomic
- deterministic (like a single **step**)
- choices resolved in fixed way (always take the first possible option)
  $\Rightarrow$ avoid choices in **d_step**
- it is an error if any statement within **d_step**,
  other than the first one (called *'guard'*), blocks

```
d_step {
    stmt1; ← guard
    stmt2;
    stmt3
}
```

If `stmt1` blocks, **d_step** is not entered, and blocks as a whole.

It is an error if `stmt2` or `stmt3` block.

(Weakly) Atomic Sequences

atomic:

- weakly atomic
- can be non-deterministic

```
atomic {
    stmt1; ← guard
    stmt2;
    stmt3
}
```

If *guard* blocks, **atomic** is not entered, and blocks as a whole.

Once **atomic** is entered, control is kept until a statement blocks, and only then passed to another process.

Prohibit Interference by Atomicity

apply **atomic** or **d_step** to interference examples

Synchronization on Global Data

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Executability addresses many issues in the interplay of processes

Most known synchronization primitives (e.g. test & set, compare & swap, semaphores) can be modelled using executability and atomicity

Executability

Each statement has the notion of executability.
Executability of basic statements:

statement type	*executable*
assignment	always
assertion	always
print statement	always
expression statement	iff value not 0/**false**
send/receive statement	(next lecture)

Executability (Cont'd)

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any of its alternatives is executable

an alternative is executable
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its guard (the first statement) is executable

(recall: in alternatives, "->" syntactic sugar for ";")

Executability and Blocking

Definition (Blocking)

A statement blocks iff it is *not* executable.
A process blocks iff its location counter points to a blocking statement.

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Executability, resp. blocking are the key to PROMELA-style modeling of solutions to synchronization problems.
(to be discussed in the following)

The Critical Section Problem

archetypical problem of concurrent systems

given a number of looping processes, each containing a critical section

design an algorithm such that:

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Absence of Deadlock If *some* processes are trying to enter their critical sections, then *one* of them must eventually succeed.

Absence of (individual) Starvation If *any* process tries to enter its critical section, then *that* process must eventually succeed.

Critical Section Pattern

for demonstration and simplicity:
(non)critical sections only **printf** statements

```
active proctype P() {
  do :: printf("P␣non-critical␣actions\n");
        /* begin critical section */
        printf("P␣uses␣shared␣recourses\n")
        /* end critical section */
  od
}

active proctype Q() {
  do :: printf("Q␣non-critical␣actions\n");
        /* begin critical section */
        printf("Q␣uses␣shared␣recourses\n")
        /* end critical section */
  od
}
```

No Mutual Exclusion Yet

More infrastructure to achieve ME.

Adding two Boolean flags:

```
bool P_in_CS = false;
bool Q_in_CS = false;

active proctype P() {
  do :: printf("P␣non-critical␣actions\n");
        P_in_CS = true;
        /* begin critical section */
        printf("P␣uses␣shared␣recourses\n");
        /* end critical section */
        P_in_CS = false
  od
}

active proctype Q() {
  ...correspondingly...
}
```

Show Mutual Exclusion VIOLATION with SPIN

adding assertions

```
bool P_in_CS = false;
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  do :: printf("P␣non-critical␣actions\n");
        P_in_CS = true;
        /* begin critical section */
        printf("P␣uses␣shared␣recourses\n");
        assert(!Q_in_CS);
        /* end critical section */
        P_in_CS = false
  od
}

active proctype Q() {
    ........assert(!P_in_CS);........
}
```

Mutual Exclusion by Busy Waiting

```
bool P_in_CS = false;
bool Q_in_CS = false;

active proctype P() {
  do :: printf("P␣non-critical␣actions\n");
        P_in_CS = true;
        do :: !Q_in_CS -> break
           :: else -> skip
        od;
        /* begin critical section */
        printf("P␣uses␣shared␣recourses\n");
        assert(!Q_in_CS);
        /* end critical section */
        P_in_CS = false
  od
}

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Mutual Exclusion by Blocking

instead of Busy Waiting, process should

- yield control
- continuing to run only when exclusion properties are fulfilled

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We can use expression statement `!Q_in_CS`,
to let process `P` block where it should not proceed!

Mutual Exclusion by Blocking

```
active proctype P() {
  do :: printf("P␣non-critical␣actions\n");
        P_in_CS = true;
        !Q_in_CS;
        /* begin critical section */
        printf("P␣uses␣shared␣recourses\n");
        assert(!Q_in_CS);
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Verify Mutual Exclusion of this

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SPIN still reports assertion violation(!)

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- `P/Q_in_CS` *not* sufficient for *proving* ME

need more infrastructure:
ghost variables, only for proving / model checking

Show Mutual Exclusion with Ghost Variable

```
int critical = 0;

active proctype P() {
  do :: printf("P non-critical actions\n");
        P_in_CS = true;
        !Q_in_CS;
        /* begin critical section */
        critical++;
        printf("P uses shared recourses\n");
        assert(critical < 2);
        critical--;
        /* end critical section */
        P_in_CS = false
  od
}

active proctype Q() {
  ...correspondingly...
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SPIN (`./pan -E`) shows no assertion is violated
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Still SPIN (without `-E`) reports (`invalid end state`)
⇒ deadlock

Deadlock Hunting

Invalid End State:

- A process does not finish at its end
- OK if it is not crucial to continue – see last lecture
- If it is crucial to continue:
  Real deadlock

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Find Deadlock with SPIN:

- Verify to produce a failing run trail
- Simulate to see how the processes get to the interlock
- Fix the code, not using the `end...:` labels or `-E` switch ;)

Atomicity against Deadlocks

solution:

checking and setting the flag in one atomic step

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```
atomic {
  !Q_in_CS;
  P_in_CS = true
}
```

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  - writers exclude each other and readers
    readers exclude writers, but not other readers
  - FIFO queue semaphores, for fairly choosing processes to enter

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  modeling possibilities include:
  - counters instead of booleans
  - semaphores (see demo)
- more fine grained exclusion conditions, e.g.
  - several critical sections (Leidestraat in Amsterdam)
  - writers exclude each other and readers
    readers exclude writers, but not other readers
  - FIFO queue semaphores, for fairly choosing processes to enter
- ... and many more

Why Not Critical Section in Single Atomic Block?

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Actually possible in this case.
Also in interleaving example (counting via `temp`, see above).
But:

- does not carry over to variations (see previous slide)
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- **d_step** excludes any nondeterminism!

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Using **atomic** and **d_step** too heavily, for too large blocks, can result in well-behaved models, while modelling the wrong system.