A Better Facet of Dynamic Information Flow Control

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ABSTRACT
Multiple Facets (MF) is a dynamic enforcement mechanism which has proved to be a good fit for implementing information flow security for JavaScript. It relies on multi executing the program, once per each security level or view, to achieve soundness. By looking inside programs, MF encodes the views to reduce the number of needed multi-executions.

In this work, we extend Multiple Facets in three directions. First, we propose a new version of MF for arbitrary lattices, called Generalised Multiple Facets, or GMF. GMF strictly generalizes MF, which was originally proposed for a specific lattice of principals. Second, we propose a new optimization on top of GMF that further reduces the number of executions. Third, we strengthen the security guarantees provided by Multiple Facets by proposing a termination sensitive version that eliminates covert channels due to termination.

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1 INTRODUCTION
JavaScript has become the de facto programming language of the Web. Web browsers daily execute thousands of JavaScript lines which usually have access to confidential information, for example, cookies that mark that the user in a web session is authenticated. It is not surprising that JavaScript is a common target for attacks.

While browsers deploy security measures in the form of access control (e.g., SOP and CSP), they are insufficient [12, 17, 30] to protect confidentiality of data.

Information flow control (IFC) is a promising technology which provides a systematic solution to handle unintentional or malicious leaks of confidential information. Recently, dynamic IFC analyses have received a lot of attention [1–3, 5, 7, 9, 10, 14, 26, 33], due, in part, to its applicability to JavaScript—where static analyses are rather an awkward fit [29].

In order to scale, a suitable IFC technique for the web not only needs to be dynamic but also needs to reduce to the minimum the modifications required to existing JavaScript code. In this light, an interesting dynamic IFC technique which fulfills both of these requirements consists in executing several copies of a program: one execution per each security level or view. In that manner, each copy of the program (view) depends only on information observable to the corresponding security level, where no leaks are therefore possible. Secure Multi Execution (SME) [14] and Multiple Facets (MF) [3] are two techniques based on this idea.

Both techniques have been proved to be a good fit for information flow security in the web since they have been successfully implemented as extensions of the Firefox browser [13, 33]. Although both SME and MF are based on multi-executions, they present important differences [7]. On one hand, SME is black-box [24], i.e., it is a mechanism that does not look inside programs but rather change the semantics of inputs and outputs to ensure security. For a moment, we assume a scenario where security levels are simply sets of principals (e.g., web origins) which denote those authorities with confidentiality concerns over data. In such a scenario, SME needs to spawn one execution for any possible set of principals—where the number of executions grows exponentially with respect to the number of principals! Instead, MF [3] is designed to reduce the number of multi-executions and the memory footprint of SME. It does so by inspecting programs code and multi-executing instructions and multiplexing memory only when needed. While MF is more resource-friendly than SME, SME provides stronger security guarantees when it comes to leaks via abnormal termination [7].

Our broad goal is to augment the efficiency of techniques based on MF and SME to general cases. In particular, we discovered that MF might sometimes spawn more multi-executions than SME—something that is counter-intuitive when considering the purpose of MF (see Section 2). Our first contribution consists on a novel technique to further reduce the number of multi-executions (and memory footprint) of MF. Our second contribution is to generalize MF to work for arbitrary finite lattices (see Section 3) rather than being restricted to the security lattice of principals as in the original proposal [3]. This becomes useful when, for instance, a program depends on 5 security levels. In such case, as stated originally, MF will need to encode them by using (at least) 3 principals ($2^3 > 5$), and thus execute the program $2^3 = 8$ times, while SME will execute it only 5 times (one per security level). Finally, we combine MF and SME into a single new dynamic IFC mechanism in order to provide security guarantees as strong as SME (i.e., termination sensitive...
if with only two elements
where values as 1
rule ˆ semantics, obtained by projection of
and one corresponding to the
of 2 (possibly different) values: one corresponding to the
level. For the sake of simplicity, let’s consider first a security lattice
maps each variable to an array of values, one value per security

MF may use fewer resources than SME (programs)
(P, H(µ)) ⊑ µ₁
(P, L(µ)) ⊑ µ₂
SME-TINI
(P, H(µ)) ⊑ µ₁
(P, L(µ)) ⊑ µ₂
SME-TINI
µ₁ ⊕ µ₂
where ⊕ combines two normal memories into a SME memory in such a way that H(µ₁ ⊕ µ₂) = µ₁ and L(µ₁ ⊕ µ₂) = µ₂. The SME mechanism will blindly execute the program as many times as possible views (or positions of the array) may exist.

Consider a program h = I where initial views for variables l and h are given by: h(µ) = (1 : 0) and h(l) = (1 : 1). In SME, using the SME-TINI rule, the assignment will be executed twice: once with H(µ) = [h → 1, l → 1] for the high view and once with L(µ) = [h → 0, l → 1] for the low view. After execution, the final SME memory will map h to (1 : 1). One way to reduce the number of executions is to exploit the knowledge that the high and the low view for variable l are equal, i.e., H(µ(l)) = L(µ(l)). Since the semantics is deterministic, there is no need to execute the program twice. We can use this knowledge by specialising SME at the granularity of commands and include the following assignment rule:

Non-interference) while avoiding multi-executions as much as our
optimized version of MF allows it. All proofs can be found in [23].

2 BACKGROUND ON SME AND MF
In this section, we discuss how on one hand, the underpinning mechanism in MF reduces the number of executions compared to SME, and on the other hand, may run more multi executions than SME because of the security lattice based on principals. Our goal here is partly pedagogical and partly to motivate and provide intuition on the optimization proposed in Section 4.

Language and Semantics To investigate the foundation of multiple facets, we use a simple, deterministic while language. Its syntax includes programs P, variables x, expressions e, and values v. We use the symbol ⊕ for binary expression operators. A value is either an integer value or a boolean value.

1 We give here the termination insensitive version of SME.
Hence when encoding of an SME memory can be reduced effectively, multi executions are reduced accordingly. As shown in the following sections, preservation of MF memories encoding through execution requires: to represent arrays of values as trees called faceted values and to evaluate expressions depending on faceted values. In particular, the definition of the evaluation of expressions on faceted values depends highly on the shape of expressions and their values according to different views, and thus is contradictory to the blackbox property of a monitor.

**MF may run more multi executions than SME** Original MF has one limitation with respect to SME: it was designed only for a security lattice of principals: for 3 principals, such a lattice contains $2^n$ security levels. The following Ad Exchange platform [35] example demonstrates that MF may be less efficient than SME in practice, when the security lattice is not based on principals.

**Example 2.1.** An Ad Exchange platform needs to put an advertisement on a publisher’s website. For that, it implements a Real-time Bidding (RTB) system [36], where advertisers can bid for the space on the publisher’s website to get their ad published. The system receives as input all the bid offers from bidders and sorts them. According to the RTB algorithm, the second best offer wins.

We present the lattice of 5 elements for this example in Fig. 2. For simplicity, we consider only 3 bidders called $B_1$, $B_2$, and $B_3$, an Ad Exchange ($\top$ level) which is able to see all the bids, and a public view $\bot$. Because MF is designed for a principal lattice, to encode 5 security levels, it uses 3 principals $k_1$, $k_2$, and $k_3$, and create a lattice of $8 = 2^3$ levels, and thus has a potential to run some parts of the program 8 times, while SME always executes the program 5 times.

We consider one test that naively checks the order of bid offers and decides the winner. The encoding of the lattice is: $T = \{k_1, k_2, k_3\}$, $B_1 = \{k_1\}$, and $\bot = \emptyset$.

1: $\text{winner} := 0$;
2: $\text{test} := (x_1 \leq x_2)$ and $(x_2 \leq x_3)$;
3: if $\text{test}$ then $\text{winner} := 2$ else skip

The bid values from bidders are $x_1 = (k_1 \leq 10 \cdot 0)$, $x_2 = (k_2 \leq 5 \cdot 0)$, and $x_3 = (k_3 \leq 7 \cdot 0)$. Thus, the resulting value of test at line 2 is $\langle k_1 \leq (k_2 \leq (k_3 \leq tt : ff)) \bowtie (k_2 \leq (k_3 \leq tt : ff)) \bowtie (k_3 \leq tt : ff) \bowtie (k_3 \leq tt : tt) \rangle$.

Therefore, the original MF executes the if instruction 8 times with 3 useless executions for levels $\{k_1, k_2\}$, $\{k_2, k_3\}$, and $\{k_1, k_3\}$.

Moreover, because different views of a variable may contain the same values, MF may execute the same statement several times. For example, in the execution described above, original MF executes the then branch 3 times, while it only needs to run once since the three executions for the then branch can be merged into one.

### 3 MF FOR ARBITRARY SECURITY LATTICE

We present an extension to the original Multiple Facets mechanism [3] for an arbitrary security lattice $(L, \sqsubseteq)$, which we call Generalised Multiple Facets mechanism, or GMF. Similarly to Multiple Facets, GMF operates over a faceted memory $\hat{\mu}$ that maps variables to simple values or faceted values. A faceted value is of the form $\langle l \sqcup V_1 : V_2 \rangle$ where $l \in \mathcal{L}$ is a security level, and $V_1$ can be either a faceted value or a simple value. The first facet $V_1$ of $\langle l ? V_1 : V_2 \rangle$ is called private, and visible to the observers at security level $l$ or higher levels in the lattice; the second facet $V_2$ is called public, and visible to security levels that are lower or incomparable to $l$. We use $V$ as a meta-variable for faceted values or simple values. Every evaluation in GMF (see Fig. 6) is marked with a set of security levels $pc$, for which the current computation is visible.

#### 3.1 Expression evaluation

By $\hat{\mu}^{PC}(e)$ we denote the evaluation of expression $e$ in faceted memory $\hat{\mu}$ with set of security levels $pc$. The definition of $\hat{\mu}^{PC}(e)$ is presented in Fig. 4. For example, consider the evaluation of $x$ when the faceted value $x$ in memory $\hat{\mu}$ is $\langle l ? V_1 : V_2 \rangle$. To define which facet is useful given a $pc$, we consider the following cases:

- All the levels in $pc$ are greater than or equal to $l$, denoted $l \leq pc$ (i.e. $\forall l' \in pc. l \sqsubseteq l'$): the evaluation can use the private facet $V_1$ because the public facet $V_2$ is anyway not useful for every level in this $pc$.
- All the levels in $pc$ are lower than or incomparable to $l$, denoted $l \nleq pc$ (i.e. $\forall l' \in pc. l \nsubseteq l'$): the evaluation can only use the public facet $V_2$ because $V_2$ is a facet visible to any view that is lower than or incomparable to $l$.
- Otherwise, we say that $l$ and $pc$ are incomparable and denote it by $l \parallel pc$ (i.e. $\forall l' \in pc. l \nsubseteq l' \land l' \nsubseteq l$): we first evaluate $V_1$ with $pc_1 = \{l' \in pc \mid l \sqsubseteq l'\}$ - the set of all levels in $pc$ which are greater than or equal to $l$. Then, we evaluate $V_2$ with $pc_2 = pc \setminus pc_1$ which is the set of all levels in $pc$ which are lower than or incomparable to $l$. Finally, we combine the two results in a new faceted value.

To evaluate a variable $x$, we use a special unary operator $\otimes^{PC}(\hat{\mu}(x))$, which returns the value that is visible to all the levels in the $pc$. Let’s consider the case of $\otimes^{PC}(\{l ? V_1 : V_2\})$. Notice that, if $pc$ and $l$ are incomparable, meaning that there are some levels in $pc$ that are higher than or equal to $l$ and other levels in $pc$ that are lower than or incomparable to $l$, denoted by $l \parallel pc$, then the evaluation returns the faceted value $\langle l ? \otimes^{PC_1}(V_1) : \otimes^{PC_2}(V_2)\rangle$. The form of the result of $\hat{\mu}^{PC}(e)$ is described in Lemma 3.1.

**Lemma 3.1.** If $\hat{\mu}^{PC}(e) = \langle l ? V_1 : V_2 \rangle$, then $l \parallel pc$.

**Example 3.2 (Expression evaluation).** Consider the lattice $(L, \sqsubseteq)$ from Fig. 3, and the evaluation of $x + y$ in $\hat{\mu}$, where $\hat{\mu}(x) = (M_1 ? 10 \cdot 0)$ and $\hat{\mu}(y) = (M_2 ? 5 \cdot 0)$.

Suppose that $pc = \{M_1, H\}$. Since all the levels in $pc$ are higher than or equal to $M_1$, the evaluation of $x$ returns $\hat{\mu}^{PC}(x) = 10$. Since $pc$ and $M_2$ are incomparable, the evaluation of $y$ returns $\hat{\mu}^{PC}(y) = (M_2 ? 5 \cdot 0)$. Next, the evaluation of $10 + \otimes^{PC}(M_2 ? 5 \cdot 0)$ is split into two: one uses a facet visible to $M_2$ (and hence $H$), and another one
We abuse the notation and use $\hat{\mu}$ as the projection function.

The projection function $\hat{\mu}$ keeps the original value of each variable.

$\hat{\mu}(pc(e_1 \oplus e_2)) = \hat{\mu}(pc(e_1) \oplus \hat{\mu}(pc(e_2))$.

$\hat{\mu} = \phi(pc(x))$

$L$ is split into $M_1$.

$\hat{\mu}(x + y) = \hat{\mu}(pc(x) + pc(\hat{\mu}(y)))$

$\hat{\mu} = \phi(pc((M_1 ? 10 : 0) + pc((M_2 ? 5 : 0)))$

$I(u) = \phi(pc((M_2 ? 5 : 0) + pc((M_1 ? 5 : 10 + \Gamma) = (M_2 ? 15 : 10))$

The projection function $I$ is used in the definition of $\hat{\mu}_{\Gamma}$ function that converts a faceted memory to a simple memory (see Fig. 5).

The semantics of GMF is defined in Sec. 3 as a big-step evaluation relation $\Gamma \vdash (P, \mu) \downarrow_{GMF} \mu'$, where program $P$ is executed in a memory $\mu$ and a security environment $\Gamma$ that maps variables to security levels in a given security lattice $(L, \sqsubseteq)$.

The main rule GMF first constructs a faceted memory from the standard memory using the transformation $\mu \triangleright_{\Gamma}$, as shown in Fig. 5, where $\triangleright L$ is the greatest lower bound of $L$. The resulting faceted memory keeps original value of each variable $x$ in a private facet, and adds default values (defined by def function) to a public facet. In a special case when the level of $x$ is the smallest level in a lattice, we keep only a simple value $\mu(x)$ that is visible to all security levels. We then evaluate the program with the constructed faceted memory and $pc = L$. The resulting faceted memory is transformed back to a normal memory by using the projection function $\hat{\mu}_{\Gamma}$.

The semantics rules for skip, sequence, while, and and loop are straightforward. The GAssign rule uses a faceted evaluation $\hat{\mu}^pc(e)$ defined in Section 3.1.

Before describing the semantics of if instruction, we first define several auxiliary functions. Let dom(\hat{\mu}) be the domain of $\hat{\mu}$ and $y$ be a fresh variable, i.e. $y \not\in$ dom(\hat{\mu}). By $\hat{\mu} \oplus (y \mapsto V)$ we denote a new memory $\hat{\mu}'$, such that dom(\hat{\mu}') = dom(\hat{\mu}) \cup \{y\}, $\hat{\mu}'(y) = V$ and for all $x \in$ dom(\hat{\mu}) we have $\hat{\mu}'(x) = \hat{\mu}(x)$. By $\hat{\mu} \| y$, we remove $y$ from the domain of $\hat{\mu}$, that is, $\hat{\mu} \| y$ constructs a new memory $\hat{\mu}'$, where dom($\hat{\mu}'$) = dom($\hat{\mu}$) \{y\} and for all $x \neq y$, $\hat{\mu}'(x) = \hat{\mu}(x)$.

The semantics of if instruction is defined as $\mathbf{if \ then \ P \ else \ P'}$, with $\hat{\mu}$ and $pc$. If $\hat{\mu}$ is evaluated to a constant value (tt or ff), then only P1 or P2 is evaluated (see rule GIf-C).

When $e$ is evaluated to a faceted value $(\Gamma ? V_1 : V_2)$, we construct a new program if $\mathbf{if \ then \ P_1 \ else \ P_2}$, where $y$ is a fresh variable. From Lemma 3.1, we have that $\Gamma \| pc$, and hence $pc_1 = \{l' \in pc \mid l' \leq l\}$ and $pc_2 = pc \| pc_1$ are non-empty. In this case, we run the new program if $\mathbf{if \ then \ P_1 \ else \ P_2}$ twice: once with the “higher view” than $\Gamma$, i.e., with $pc_1 = \{l' \in pc \mid l' \leq l\}$ and $y$ set to a private facet $V_1$, and another time with “lower or incomparable view” than $\Gamma$, i.e., with $pc_2 = pc \| pc_1$ and $y$ set to a public facet $V_2$. We then combine the resulting memories using the $\downarrow_{\Gamma}$ operator. The combination of faceted memories is based on the fact that when $pc$ is split into $pc_1$ and $pc_2$ in the GIf-S rule, all levels in $pc_1$ is larger than or equal to $\Gamma$, and all levels in $pc_2$ is smaller or incomparable to $\Gamma$.
pc \{ V \} = \nu
\begin{cases} 
\nu & \text{if } V = V_2, \\
\{ V \} & \text{if } V_1 \equiv I, I \not\equiv I, V_1 = \{ I_1 \not\equiv V_1 : V_1 \}, \\
\{ V \} & \text{if } V_1 \equiv I, I \not\equiv I, V_1 = \{ I_1 \not\equiv V_1 : V_1 \}, \\
\{ V \} & \text{if } I \not\equiv I, V_2 = \{ I_2 \not\equiv V_2 : V_2 \}, \\
\{ I \} & \text{if } I \not\equiv I, V_2 = \{ I_2 \not\equiv V_2 : V_2 \}, \\
\{ I \} & \text{otherwise}. 
\end{cases}

\text{Figure 7: Optimisation of a faceted value.}

Notice that the form of a faceted value constructed by combining values can be reduced. For example, a faceted value of the form \(<(H \otimes V_1) : V_2>\) can be reduced to \(<(H \otimes V_1) : V_2>\) because \(V_1 \not\equiv H\) and the projection of the original value at any level is either \(V_1\) or \(V_2\). We use the optimisation on the constructed faceted values from Fig. 7.

Therefore, in the GIF-S rule after the evaluation of \(P^*\) in two contexts, we combine the resulting faceted memories \(\hat{\mu}_1^f\langle y\rangle\) and \(\hat{\mu}_2^f\langle y\rangle\) and apply an optimisation operator \(\{\}\) for each newly constructed faceted value. The correctness of \(\{\}\) used to optimize faceted values is proven in Lemma 3.3.

Lemma 3.3. For all \(I, I, V\), it follows that \(\Gamma(V) = \Gamma(\{\nu\})\).

Example 3.4 (Evaluation of if instruction). Consider the security lattice \(\langle L_0, \sqsubseteq \rangle\) from Fig. 3 and the evaluation of the following program \(P\) with \(pc = L_0\) and \(\mu\), where \(\mu(x) = \langle M_1 \mid \langle H \otimes \text{tt} : \text{ff} \rangle : \text{tt} \rangle\).

1. if \(x\) then \(z := 10\) else \(z := 5\).

The evaluation follows the GIF-S rule since \(M_1 \| L_0\). We construct \(P^* = if\ y_1\ then\ P_1\ else\ P_2\ and\ first\ evaluate\ P^*\) with \(pc_1 = \{ I \in pc \mid M_1 \not\sqsubseteq I' \} = \{ M_1, H \}\) and \(\mu_1\) and \(\mu_2\) with \(y \mapsto (H \otimes \text{ff})\), and then evaluate \(P^*\) with \(pc_2 = pc\ \cap\ pc_1 = \{ M_2, L\}\), \(\hat{\mu}_2 = \hat{\mu} \upharpoonright (y \mapsto \text{tt})\).

Since \(pc_1 = \{ M_1, H\}\) and \(\hat{\mu}_1(y) = (H \otimes \text{ff})\), the evaluation of \(P^* \) with \(pc_1\) and \(\mu_1\) is split again to two evaluations: one with \(P'' = if\ then\ P_1\ else\ P_2\) and \(pc_{11} = \{ H\}\), and \(\hat{\mu}_{11} = \hat{\mu} \upharpoonright (y \mapsto \text{tt})\); and the other one with \(P'''\), \(pc_{12} = \{ M_1\}\), and \(\hat{\mu}_{12} = \hat{\mu} \upharpoonright (y \mapsto \text{ff})\).

The evaluation of \(P''\) with \(pc_{11}\) and \(\mu_1\) follow the GIF-C rule and we get two faceted memories \(\hat{\mu}''_{1,1}\) and \(\hat{\mu}''_{1,2}\), where \(\hat{\mu}''_{1,1}(z) = 10\) and \(\hat{\mu}''_{1,2}(z) = 5\). Then, \(\hat{\mu}''_{1,1} \upharpoonright \{ y \} \) and \(\hat{\mu}''_{1,2} \upharpoonright \{ y \} \) where \(\hat{\mu}''_{1,1}(x) = (H \otimes \text{ff})\).

The evaluation of \(P_2\) with \(pc_2\) follows the GIF-C rule and the result is \(\hat{\mu}''_{2,1}\), where \(\hat{\mu}''_{2,1}(z) = 10\). At this point, \(\hat{\mu}'' \upharpoonright \{ y \} \) and \(\hat{\mu}'' \upharpoonright \{ y \} \) are combined and the result is \(\hat{\mu}''\), where \(\hat{\mu}'' = \langle M_1 \mid (H \otimes \text{ff}) \rangle\).

Example 3.5 (Evaluation with the GFM rule). Consider the lattice \(\langle L_0, \sqsubseteq \rangle\) from Fig. 3 and program \(P\) from Example 3.4 with one more instruction \(x := x_1 > x_2\). Suppose that \(\Gamma(x_1) = M_1, \Gamma(x_2) = H, \Gamma(z) = H, \mu(x_1) = 10, \mu(x_2) = 5\), the default values for \(x_1\) and \(x_2\) are respectively 100 and 20. Let \(\mu = a^\text{def}^l\). It follows that \(\hat{\mu}(x_1) = \langle M_1 \mid (H \otimes \text{ff}) \rangle\). We establish the relation between the execution with GFM semantics and the execution with the standard semantics.

Lemma 3.9. \((P, \mu) \xrightarrow{\text{GFM}} (P, \hat{\mu}) \iff (P, \mu) \xrightarrow{\text{def}} (P, \hat{\mu})\) for all \(l \in \text{pc}\).

Thanks to Lemma 3.9, we now prove the equivalence of GFM and SME-TINI.

Theorem 3.10. GFM and SME-TINI are equivalent.

As a consequence, we have that GFM is TINI.

Remark 3.1. MF [3] is constructed for a set of principals. When the set of principals is fixed, we can use GFM to encode MF: we construct the lattice \(\langle P, \sqsubseteq \rangle\), where each element is a set of principals; we prove that GFM for \(\langle P, \sqsubseteq \rangle\) and MF for \(P\) are equivalent [23].
4 OPTIMIZING GMF

In Section 3, we presented the semantics of Generalised Multiple Facets (GMF) for arbitrary lattice and have proven it to be equivalent to SME-TINI. However, GMF from Fig. 6 can be further optimised and avoid repeating evaluations of the same commands. The following example demonstrates the sub-optimality of GMF.

Example 4.1 (GMF is not optimal). We consider the below program from Example 2.1. The lattice is \(\langle L_B, \sqsubseteq \rangle\) from Fig. 2.

1. \(\text{winner} := 0\);
2. \(\text{test} := (x_1 \leq x_2) \land (x_2 \leq x_3)\);
3. \(\text{if test then } \text{winner} := 2 \text{ else skip}\)

Suppose that the bid offers of \(B_1, B_2, B_3\) are respectively 10, 5, and 7, and the default values for \(B_1\) are 0. W.r.t. this setting, the initial faceted memory is \(\hat{\mu}\), where \(\hat{\mu}(x_1) = (B_1 \equiv 10 \cdot 0), \hat{\mu}(x_2) = (B_2 \equiv 5 \cdot 0)\), and \(\hat{\mu}(x_3) = (B_3 \equiv 7 \cdot 0)\). We consider the execution of the program with GMF.

After line 2, \(\text{test} = (B_1 \equiv B_2 \equiv \text{ff} \equiv \text{ff}) \equiv (B_2 \equiv \text{ff} \equiv B_3 \equiv \text{tt} \equiv \text{tt})\). Following the semantics of GMF, the assignment \(\text{winner} := 2\) is evaluated twice with \(pc_3 = \{B_1\}\) and \(pc_1 = \{1\}\); the \text{skip} instruction is evaluated three times with \(pc_T = \{\text{tt}\}, pc_B = \{B_1\}\), and \(pc_B = \{B_2\}\).

The main idea of our optimisation lays in reducing the number of sub-evaluations and hence the number of faceted memory combinations. For Example 4.1, we propose a mechanism that merges the evaluations corresponding to \(pc_{B_3} \land pc_{\perp}\) into one evaluation with \(pc_1 = \{B_3, \bot\}\). This simplification is possible since \(\text{test}\) denotes the same value (i.e., \(\text{tt}\)) under \(pc_{B_3}\) and \(pc_{\perp}\). Similarly, our simplification merges the evaluations corresponding to \(pc_T, pc_{B_1}\), and \(pc_{B_2}\), where \(\text{test}\) denotes \(\text{ff}\), into one evaluation with \(pc_2 = \{\text{tt}, B_1, B_2\}\), and thus evaluates each branch of the if command only once.

In this section, we propose semantics of \emph{optimized GMF} (OGMF) that reduces the number of sub-evaluations, and hence is more resource-friendly than GMF.

4.1 Semantics

The ideas behind the OGMF rule, and the rules for skip, assignment, sequence, and while instructions are similar to the corresponding ones of GMF. The functions \(\mu \mapsto x^\mathrm{def}\) (x) and \(\mu\rbr{\mid x}\) are defined in Fig. 5. We now explain the semantic rules for the conditional instruction.

Consider evaluation of the program \(\text{if } e \text{ then } P_1 \text{ else } P_2\) with \(pc\) and memory \(\hat{\mu}\), and \(\hat{\mu}^{pc}(e) = V\). In order to evaluate each branch of the conditional only once, we split the \(pc\) in two subsets: in the first subset \(pc_1\) the visible value of \(V\) is true, and in the remaining subset \(pc_2\), \(V\) is false. We now have three distinct cases.

If \(pc_1 = pc\), meaning that for all levels in \(pc\), the visible value of \(V\) is true, then \(P_1\) is evaluated (rule OIf-T). If \(pc_2 = pc\), then for all levels in \(pc\), the visible value of \(V\) is false, and only \(P_2\) is evaluated (rule OIf-F). Finally, when \(pc\) is split in non-empty \(pc_1\) and \(pc_2\), then both \(P_1\) and \(P_2\) are evaluated, and their results \(\hat{\mu}_1'(e)\) and \(\hat{\mu}_2'(e)\) are combined by \(\hat{\mu}' = \hat{\mu}_1'^{pc_1} \uplus \hat{\mu}_2'^{pc_2}\) (rule OIf-S) to a new faceted memory. The intuition behind this combination is that the projection of \(\hat{\mu}_1'\) at \(l \in pc_1\) is taken from the evaluation of \(P_1\) and its projection at \(l \in pc_2\) is taken from the evaluation of \(P_2\).

\[\begin{align*}
\text{OGMF} & \quad (P, \mu)^{oc} \quad \hat{\mu}'^l
\end{align*}\]

OAssign \(x := e, \hat{\mu}\) \(\hat{\mu}[x \mapsto \hat{\mu}^{pc}(e)]\)

OSkip \((\text{skip}, \hat{\mu}) \hat{\mu}''\)

OSkip \(\Gamma = (P, \hat{\mu}) \quad \hat{\mu}''\)

\(\hat{\mu}^{pc}(e) = V\)

OIf-T \(pc_1 = \{l \in pc(l(V) = \text{tt})\} \quad pc_1 = pc\quad (P, \hat{\mu}) \quad \hat{\mu}'\)

OIf-F \(pc_2 = \{l \in pc(l(V) = \text{tt})\} \quad pc_2 = pc\quad (P, \hat{\mu}) \quad \hat{\mu}'\)

OIf-S \(pc_1 \neq \emptyset \quad pc_2 \neq \emptyset \quad (P, \hat{\mu}) \quad \hat{\mu}'\quad (P, \hat{\mu}) \quad \hat{\mu}'\quad (P, \hat{\mu}) \quad \hat{\mu}'\)

OWhile \(\text{if } e \text{ then } P\\text{ while } e \text{ do } P\text{ else }\) skip \(P', \hat{\mu}'\)

\(\hat{\mu}'(x) = \hat{\mu}_1'(x)\) otherwise.

Figure 8: Optimized multiple facets for arbitrary lattice

In the definition of combination of memories for OGMF (bottom of Fig. 8), we distinguish two cases. If for some variable \(x\), its value in both faceted memories is the same, \(\hat{\mu}_1'(x) = \hat{\mu}_2'(x)\), then we do not need to construct a new faceted value. Instead, we optimize the current value using the optimisation operator from Fig. 7.

If the values of \(x\) in \(\hat{\mu}_1'(x)\) and \(\hat{\mu}_2'(x)\) are different, then we construct a new faceted value \(V = [V_1, V_2, pc_1, pc_2]\) and apply further optimisation on the resulting value \(V\) using a new optimisation operator that takes into account a faceted value and the current \(pc:\) \([V, pc]\) optimizes the form of \(V\) and is described in Fig. 9. We show an example of such optimisation in Example 4.4.

To combine two faceted memories, we first construct a new faceted value by using \(\mathbb{F}(V_1, V_2, pc_1, pc_2)\):

\[\mathbb{F}(V_1, V_2, pc_1, pc_2) = \{\text{List}(pc_1 \cup pc_2), V_1, V_2, pc_1, pc_2\}\]

where \(\text{List}(S)\) is a list of security levels from a set \(S\), such that if \(I\) appears before \(I'\) in \(\text{List}(S)\) then \(I \nmid I'\). If the relation \(\nmid\) in a given security lattice is not a total order, we can transform it into a total order \(\leq_T\) provided that \(\nmid\) is a finite partial order. We can then view \(\text{List}(S)\) as a list such that for any \(l\) and \(l'\) in this list, if \(l\) appears before \(l'\), then \(l' \nmid l\).

The definition of \(\mathbb{F}(V_1, V_2, pc_1, pc_2)\) uses the following operator that creates a faceted value based on an ordered list of security
levels $L$, two faceted values, $pc_1$ and $pc_2$:

$$\langle L, V_1, V_2, pc_1, pc_2 \rangle = \begin{cases} 
(I(V_1)) & \text{if } L = l, l \in pc_1, \\
(I(V_2)) & \text{if } L = l, l \in pc_2, \\
\{\langle I(V_1) : \langle(T, V_1, V_2, pc_1, pc_2) \rangle \} & \text{if } l = (T, T \neq []), l \in pc_1, \\
\{\langle I(V_2) : \langle(T, V_1, V_2, pc_1, pc_2) \rangle \} & \text{if } l = (T, T \neq []), l \in pc_2.
\end{cases}$$

Notice that the form of the faceted value created by $F(V_1, V_2, pc_1, pc_2)$ may be suboptimal.

**Example 4.2 (Faceted value construction).** Suppose that $V_1 = 2$, $V_2 = 0$, $pc_1 = \{B_1, \bot\}$, $pc_2 = \{\top, B_1, B_2\}$, $List(pc_1 \cup pc_2)$ is $\top, B_1, B_2, \bot$, and the lattice $(\mathcal{L}_B, \sqsubseteq)$ is from Fig. 2.

Following the definition of combination of faceted memories, we have $F(2, 0, pc_1, pc_2) = \{\langle \top ? : (B_1 ? 0 : (B_2 ? 0 : (B_3 ? 2 : 2))) \}$.

This value can be further reduced to $\{B_1 ? 0 : (B_2 ? 0)\}$.

We therefore define an optimisation function $[V, pc]$ that further optimises the result $V$ of a $F$ function. The optimisation uses the observation that faceted value returned by $F$ has the form of $\langle l ? v : V' \rangle$, where $V'$ is either a simple value or a faceted value.

The function $[V, pc]$ is defined in Fig. 9. If $V$ is of the form $\langle l ? v : v' \rangle$, then the optimisation is straightforward. We now consider the case when $V$ is of the form $\langle l ? v : (l' ? v' : V') \rangle$. For demonstration, consider the lattice $(\mathcal{L}_B, \sqsubseteq)$ from Fig. 2.

If the faceted value $V$ is of the form $\langle \top ? v : (B_1 ? v : V') \rangle$ (formally, $l' \sqsubseteq l$ and $v = v'$), then it can be reduced to $\langle (B_1 ? v : V'), pc' \rangle$ (formally, $\langle (l' ? v' : V'), pc' \rangle$), where $pc' = pc \setminus \{\top\}$.

If the faceted value $V$ is of the form $\langle B_1 ? v : (B_2 ? v : V') \rangle$, $l$ and $l'$ are incomparable and $v = v'$, and moreover for all the levels in the $pc$, for which either $B_1$ or $B_2$ is visible, it is guaranteed that they observe the same value $v$ (see the definition of $\text{cond}(V, pc)$ below), then we distinguish the following two cases:

$$\text{cond}(V, pc) \equiv V = \langle (l ? v : (l' ? v' : V')) \rangle \land V_1 \in pc : \text{glb}(l, l') \sqsubseteq l_1 \implies l_1(v) = v.$$

- If all levels in $pc$ are greater than or equal to $\text{glb}(l, l')$ (i.e., $\text{glb}(l, l') \leq pc$), then $V$ is reduced to $v$. For example, if $pc = \{B_1, B_2, B_3\}$, $\text{glb}(B_1, B_2) = \bot$, then $\text{glb}(B_1, B_2) \leq pc$, and thanks to the $\text{cond}(V, pc)$ we know that $B_1(V) = B_2(V) = B_3(V) = V$, then we can reduce such faceted value to simply $v$ because value $v$ is not useful for such $pc$.

- If only some levels in $pc$ are greater than or equal to $\text{glb}(l, l')$ (i.e., $\text{glb}(l, l') \parallel pc$), then $V$ is reduced to $\langle (l ? v' : V') \rangle$ and this value is reduced further recursively. Consider that we add one more security level $L$ to the lattice $(\mathcal{L}_B, \sqsubseteq)$ such that $L \subseteq \bot$. If $pc = \{B_1, B_2, L\}$, $\text{glb}(B_1, B_2) = \bot$, then $\text{glb}(B_1, B_2) \parallel pc$ because $\bot \not\sqsubseteq L$. We then construct a set of security levels $S$ from $pc$, which are higher or equal than $\text{glb}(l, l')$, and therefore the view on $V$ from all these levels is $v$ (because $\text{cond}(V, pc)$ holds). In our example, $S = \{B_1, B_2\}$, and we construct a new faceted value $V'' = \langle L, V' \rangle = L(V')$. We then define a new $pc' = (pc \setminus S) \cup \{\text{glb}(l, l')\} = (L, \bot)$, and we need to keep $\text{glb}(l, l')$ in $pc'$ because we must ensure that all the levels present in the new faceted value are also present in $pc$. Therefore, the reduced faceted value for our example is $\{\langle \bot ? v : L(V') \rangle : (L, L)\}$.

Finally, if none of the above conditions hold then we recursively reduce the faceted $\langle l' ? v' : V' \rangle$.

The correctness of $\hat{\mu}_1 @ pc_1, pc_2 \hat{\mu}_2$ in the Olf-S rule is proven in Lemma 4.3.

**Lemma 4.3.** For all levels $l$, variables $x$, sets of security levels $pc_1$ and $pc_2$, and memories $\hat{\mu}_1$ and $\hat{\mu}_2$,

- if $l \in pc_1$, then $l(\hat{\mu}_1 @ pc_1, pc_2 \hat{\mu}_2(x)) = l(\hat{\mu}_1)(x)$,
- if $l \in pc_2$, then $l(\hat{\mu}_1 @ pc_1, pc_2 \hat{\mu}_2(x)) = l(\hat{\mu}_2(x))$.

**Example 4.4 (Optimisation of faceted value).** Consider a faceted value $\langle \top ? 0 : (B_1 ? 0 : (B_2 ? 0 : (B_3 ? 2 : 2))) \rangle$ and $pc = \{\top, B_1, B_2, B_3, \bot\}$ from Example 4.2. We show how this value is optimised with our optimisation function $[\cdot]$:

$$\langle \top ? 0 : (B_1 ? 0 : (B_2 ? 0 : (B_3 ? 2 : 2))) \rangle = \langle B_1 ? 0 : (B_2 ? 0 : (B_3 ? 2 : 2)) \rangle.$$

**Example 4.5 (OGMF is more resource-friendly than GMF).** Consider the program from Example 4.1. To show optimisation of OGMF, we evaluate it with $pc = \{\top, B_1, B_2, B_3, \bot\}$ and $\hat{\mu}$, where $\hat{\mu}(x_1) = (B_1 ? 10 : 0)$, $\hat{\mu}(x_2) = (B_2 ? 5 : 0)$, and $\hat{\mu}(x_3) = (B_3 ? 7 : 0)$. After the execution of the instruction at line 2, the faceted memory is $\hat{\mu}' = \hat{\mu}[\text{winner} \triangleright 0, \text{test} \triangleright V]$, where $V = (B_1 ? B_2 ? \text{ff} \triangleright \text{ff} : (B_2 ? \text{ff} \triangleright (B_3 ? \text{tt} \triangleright \text{tt}))$.

We consider the execution of the if instruction. For levels $pc_1 = \{B_3, \bot\}$, the evaluation of test is $\text{tt} : B_3[\hat{\mu}'(\text{test}) = \bot](\hat{\mu}'(\text{test}) = \text{tt})$. Moreover, $pc_1 \neq pc$, therefore, the rule Olf-S applies. The evaluation of the program is split to two: the first evaluation is with $P_1 = \text{winner} := 2$ and $pc_1 = \{B_3, \bot\}$; and the second evaluation is with $P_2 = \text{skip}$ and $pc_2 = \{\top, B_1, B_2\}$. Each branch of the conditional will be evaluated only once. The evaluation of $P_1$ with $pc_1$ terminates with $\hat{\mu}_1''[\text{winner} = 2]$. The evaluation of $P_2$ with $pc_2$ terminates with $\hat{\mu}_2''[\text{winner} = 0]$. These two faceted memories are combined to $\hat{\mu}'''$, where $\hat{\mu}'''[\text{winner} = (B_1 ? 0 : (B_2 ? 0 : 2))]$ (as described in Examples 4.2 and 4.4).

In the example above, OGMF has only two sub-evaluations, while GMF has five, moreover OGMF combines faceted memories once, while GMF combines them four times. Therefore, OGMF is more resource-friendly than GMF.

### 4.2 Equivalence to SME-TINI and Security Guarantee

We first establish the relation between the standard semantics and the semantics of OGMF.

**Lemma 4.6.** $(p, \hat{\mu}) \triangleright \hat{\mu}_O \hat{\mu}_G \hat{\mu}_G$ iff $(p, l(\hat{\mu})) \triangleright l(\hat{\mu})$ for all $l \in pc$.

We now can prove the semantic equivalence result for OGMF and SME-TINI.

**Theorem 4.7.** OGMF and SME-TINI are equivalent.

As a consequence, OGMF and GMF are equivalent even though OGMF is optimized. In addition, OGMF is TINI.
\[ [(l \ ? \ v : v'), pc] = \begin{cases} v & \text{if } v = v' \\ (l \ ? \ v : v') & \text{otherwise.} \end{cases} \]

\[ [(l' \ ? \ v : V'), pc'] = \begin{cases} \mu & \text{if } l' \subseteq l, v = v', \text{where } pc' = pc \setminus \{l\} \\ v & \text{if } l \parallel l', v = v', \text{cond}(V, pc) \text{ and } \text{glob}(l, l') \prec pc, \end{cases} \]

\[ [(l \ ? \ (l' \ ? \ v' : V'), pc') = \begin{cases} \text{if } l \parallel l', v = v', \text{cond}(V, pc) \text{ and } \text{glob}(l, l') \parallel pc, \text{ where } pc' = (pc \setminus S) \cup \{\text{glob}(l, l')\}, \\ \{gbl(l, l') \subseteq l_t\}, \text{ and } V = \{\text{List}(pc \setminus S), V''\}, \end{cases} \]

\[ (l \ ? \ (l' \ ? \ v' : V'), pc') \text{ otherwise, where } pc' = pc \setminus \{l\}. \]

\[ (L, V) \equiv \begin{cases} I(V) & \text{if } L = l, \\ (l \ ? \ I(V) : (T, V)) & \text{if } L = l.T, T \neq []. \end{cases} \]

**Figure 9:** Definition of \([V, pc]\), and optimisation of a faceted value \(V\) with respect to the set of security levels \(pc\).

5 A TERMINATION SENSITIVE VERSION OF MULTIPLE FACETS

A termination sensitive model assumes that an attacker can observe termination of evaluations. In [19], the model is explained further: an attacker at level \(l\) can observe the termination of evaluations at level \(l\) and lower. In the case of GMF and OGMF, an evaluation marked with \(pc\) is an evaluation at \(l\) if \(l \in pc\). Notice that an evaluation is at more than one level whenever \(pc\) is not a singleton.

As illustrated by Example 5.1, GMF and OGMF do not prevent the influence of private data at higher levels to the termination of the evaluations at lower levels. In other words, GMF and OGMF do not prevent leakage on termination channel [19].

Example 5.1. Suppose that \(L = \{L, H\}\), where \(L \subseteq H\). We look at the evaluation of \(if x \ then \ (while \ t t \ do \ skipp) \ else \ skipp\) with \(pc = L\) and \(\mu(x) = \{H ? tt : if\}\). When GMF or OGMF is used, the evaluation is split into two: one is with \(pc_1 = \{H\}\), the other one is with \(pc_2 = \{L\}\). The evaluation with \(pc_2\) converges, while the evaluation with \(pc_1\) diverges since its executing program is \(while\ tt \ do \ skipp\). Therefore, the evaluation of the whole program with \(pc = \{L, H\}\) also diverges and hence, to an attacker at \(L\), the evaluation at \(L\) diverges. However, if the program is evaluated with \(\mu'(x) = \{H ? ff : if\}\), to the attacker at \(L\), the evaluation at \(L\) converges. Based on observations on those two evaluations, an attacker at \(L\) can gain insight about the high facet of \(x\). In other words, GMF and OGMF do not prevent the influence of data at \(H\) to the termination of the evaluation at \(L\).

Therefore, we propose **Termination Sensitive Multiple Facets** (TSMF), a version of MF that takes into account the termination sensitive model. TSMF is a generalization of a version of MF presented in [8, Appendix A]. The basic idea of TSMF is that when an if instruction is evaluated, TSMF performs a bounded evaluation of the instruction by using OGMF. If the OGMF evaluation does not terminate within the given time bound, then the instruction is evaluated instead using SME semantics with a low-prio scheduler [14]. The security guarantees offered by TSMF are the same as SME with the same low-prio scheduler [19]. The semantics of TSMF and the proofs about its security guarantees can be found in [23].

6 RELATED WORK

SME. Devriese and Piessens introduce the idea of Secure Multi-Execution [14]. Since then, many researchers have developed different aspects of this approach. Close to our work, Kashyap et al. [19] discuss how schedulers might affect security guarantees (i.e., TSNI and TINI) based on the chosen scheduler and the lattice ordering. They show several schedulers and classify them according to the strength of security guarantees and according to fairness properties. This work complement theirs by providing a similar analysis but for an interplay of MF and SME semantics. SME [14] has many implementations: as a library in Haskell [18], as an experimental web browser based on Firefox [13], as a static program transformation for both Python and JavaScript [4], and as an adaptation to reactive systems [6]. In the work above, SME preserves the semantics of secure programs up to interleaving of events. To remedy that, Zanarini et al. [37] carefully leverage SME to design a precise monitor which exactly preserves semantics of secure programs up to termination. Several other works [10, 26, 33] expand SME and introduce declassification. In this work, we focus on semantics guarantees up to interleaving of events—as in the SME original formulation.

MF. Austin and Flanagan introduce MF semantics [3]—a technique often referred as an optimization for SME. However, as shown by Bielova and Rezk [7], they do not provide the same security guarantees (i.e., TINI vs. TSNI) and differ in their treatment of default values. This work provides yet another look into a comparison between both techniques to show their differences, while introducing novel value-based optimizations to MF. Another work by the same authors [9] compare and contrast five dynamic techniques, including MF and SME, to mainly reason about the preservation of semantics of secure programs, a property known as transparency. In this work, we show that GMF and OGMF enjoy the same transparency guarantees as SME-TINI (Theorems 3.10 and 4.7).

Tools. Most information flow control tools provide TINI, e.g., Jif [21], FlowCaml [25], Laminar [27], Paragon [11], and JSFlow [16]. Similarly, termination leaks are often ignored in security tools coming from the operating system research community, e.g., Asbestos [15], HiStar [38], and Flume [20]. A few exceptions to this trend are the security libraries LIO [31] and MAC [28], which provide TSNI for concurrent programs.

Decentralized label models. The decentralized label model (DLM), allows one to express the interests of mutually-distrusting principals without a central authority [22]. The set of labels forms a pre-order where the order relationship does not require to know all the points in the relationship to determine the result of comparing two labels—bearing in mind that there might be an infinite number of labels due to the dynamic creation of principals at runtime. In a similar spirit, DC-labels [32, 34] provides a decentralized label format which allows one to express rich policies dictated
by mutually-distrusting principals as propositional logic formulas (without negation). In this work, we require to know all the points in the chosen lattice in order to optimize MF as shown by OGMF. Extending our techniques to DLM or DC-labels is an interesting direction for future work.

7 CONCLUSION AND PERSPECTIVES

This work contributes to develop techniques to secure programs using dynamic information flow—a promising approach to secure existing JavaScript code. We especially focus on proposing a technique that achieves a smaller number of executions than MF (and hence smaller memory footprint) without diminishing security guarantees. We further extend our MF-based technique to work with arbitrary finite lattices (GMF) based on the observation that off-the-shelf lattices with principals are not always the most convenient ones to use. Knowing all the points in the lattice allows for further optimizations: spawning multi-executions could be done on a value-based basis (OGMF) rather than on security levels—as in original MF. Finally, we propose a hybrid approach which present an interesting balance between the number of executions and security guarantees: it behaves as OGMF as long as it can and switches to SME when termination leaks could occur (TSMF). In other words, TSMF prioritizes resource usage as long as there are no risks for termination leaks. We expect that these insights will help inform future development of multi-execution-based techniques. In fact, an intriguing question is what it would take for our optimizations (or future ones) to work on potentially infinite lattices like the DLM or DC-labels—an interesting direction for future work.

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REFERENCES