# Format used to specify the benchmark problems 

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#### Abstract

This document details the format used to specify the benchmarks problems for identification of ordinary differential equations given at http://www.odeidentification.org.

We will first describe some general characteristics of the format, and then walk through the details of the identification file format, using the problem metabol2 as an example.


## 1 General structure of the format

With the exception of the begin..end construction at the beginning and the end of the file, the format consists of statements organized in paragraphs. A paragraph can consist of one or several statements. A typical paragraph has some similarity to a record or class in a programming language:

```
person_7
has name = mary
has telephoneNumber = 1234567
has child_ = person_5 person_14
is female
```

which can be understood as the single statements

```
name of person_7 = mary
telephoneNumber of person_7 = 1234567
child of person_7 = person_5 person_14
person_7 is female
```

In principle, every single statement is independent of every other statement, so the meaning of the statements is independent of their order. The indices used are all arbitrary and may be permuted. When a list is assigned (such as for child in the example above), it is assumed to end at the end of the line.

The particular format for identification problems follows this general structure, but has its own kinds of paragraphs, specialized to the purpose of this application. A simple reader for identification problems will then only be able to read these particular paragraphs for this application.

The format has been designed to be easy to parse in the following way. The syntax of a single paragraph is keyword based, in that you read the first identifier of the paragraph (before the , ,', which is "person" in the example above), and then you know how to straightforwardly parse the entire paragraph. This can then be repeated over and over again until the end of the file.

All objects are referred to with a role and an index, eg. "variable_4". The indices are for each category consecutive beginning with 1 . This means that you can easily read the file and directly place in suitable program data structures without the use of any hash tables. Dynamic arrays can however be useful, unless the file is read twice to check required array sizes. Not having such redundant size information in the file makes it easy to manually edit and modify the file without causing inconsistencies.

A simple example parser for identification problems is available on the web site. It is written in C and should be possible to compile and run on any computer with a $C$ compiler. As it stands, it parses the identification problem file and prints it again. It can therefore be used directly as a simple verifier in that if the input and the output are identical, the file can be considered to be correct. When used in another program, the print statements can be replaced with code that loads the data into appropriate data structures.

## 2 Details about the format

We will now look at problem metabol2 in more detail. Our ambition is to make this documentation self-contained, but it can be useful to look at the full problem specification to get an impression of how all parts are combined. Finally, a general remark: ' $/ /$ ' indicates that the rest of a line is a comment.

### 2.1 Header

```
format version = 1.0
begin problem metabol2
type = reactionKinetics
date = 5-Aug-08 09:27:04
url = http://www.cs.chalmers.se/~dag/identification/
```

The current and first format version is called 1.0. The problem is encapsulated by
'begin' and 'end'. 'problem' is a keyword followed by the name of the problem, which typically but not necessarily is the same as the name of the file.

There are two available types of problems: reactionKinetics and SSystem. Date and url specify when the problem was formulated and the address to the on-line information, respectively.

### 2.2 Reaction types

The reaction types specify the building blocks of the model space for a certain problem. Note that the model space is specified subsequently.

```
reaction_1
has name = uniMolecularMassAction
has localVariableName_1 = X1
has localParameterName_1 = k1
has equation = k1*X1
reaction_2
has name = biMolecularMassAction
has localVariableName_1 = X1
has localVariableName_2 = X2
has localParameterName_1 = k1
has equation = k1*X1*X2
reaction_3
has name = michaelisMenten
has localVariableName_1 = X1
has localParameterName_1 = k1
has localParameterName_2 = k2
has equation = k1*X1/(k2+X1)
reaction_4
has name = michaelisMentenNonCompInhib
has localVariableName 1 = X1
has localVariableName_2 = X2
has localParameterName_1 = k1
has localParameterName_2 = k2
has localParameterName_3 = k3
has equation = k1*X1/(k2 +X1)/(1+X2/k3)
```

A new reaction type begins with the keyword 'reaction_' followed by an integer. Each type has a unique name (used as reference in subsequent sections), a list of local variable names, a list of local parameter names and a rate equation. In the first example above, the rate equation is

$$
k_{1} X_{1}
$$

where $k_{1}$ is a local parameter and $X_{1}$ is a local variable. In the second reaction
type, 'biMolecularMassAction', the rate equations is

$$
k_{1} X_{1} X_{2}
$$

where $k_{1}$ is a local parameters and $X_{1}$ and $X_{2}$ are local variables. In the third reaction type, 'michaelisMenten', the rate equations is

$$
\frac{k_{1} X_{1}}{k_{2}+X_{1}}
$$

where $k_{1}$ and $k_{2}$ are local parameters and $X_{1}$ is a local variable. In the fourth reaction type, 'michaelisMentenNonCompInh', the rate equations is

$$
\frac{k_{1} X_{1}}{\left(k_{2}+X_{1}\right)\left(1+\frac{X_{2}}{k_{3}}\right)}
$$

where $k_{1}, k_{2}$ and $k_{3}$ are local parameters and $X_{1}$ and $X_{2}$ are local variables.

### 2.3 Variables

Each variable has a name and is either an inputVariable or a dependent variable.

```
variable_1 has name = x1 is inputVariable
variable_2 has name = x2 is inputVariable
variable_3 has name = x3 is dependent
variable_4 has name = x4 is dependent
variable_5 has name = x5 is dependent
variable_6 has name = x6 is dependent
variable_7 has name = x7 is dependent
```

For each dependent variable there is a corresponding ODE. Hence, in the above example the system of ODEs to consider is:

$$
\begin{aligned}
x_{3}^{\prime}(t) & =f_{3}\left(x_{1}, x_{2}, x_{3}, x_{4}, x_{5}, x_{6}, x_{7}, p, t\right) \\
x_{4}^{\prime}(t) & =f_{4}\left(x_{1}, x_{2}, x_{3}, x_{4}, x_{5}, x_{6}, x_{7}, p, t\right) \\
x_{5}(t) & =f_{5}\left(x_{1}, x_{2}, x_{3}, x_{4}, x_{5}, x_{6}, x_{7}, p, t\right) \\
x_{6}^{\prime}(t) & =f_{6}\left(x_{1}, x_{2}, x_{3}, x_{4}, x_{5}, x_{6}, x_{7}, p, t\right) \\
x_{7}^{\prime}(t) & =f_{7}\left(x_{1}, x_{2}, x_{3}, x_{4}, x_{5}, x_{6}, x_{7}, p, t\right)
\end{aligned}
$$

where the $f$ 's are functions defined by the model space, $p$ is a vector of parameters and $t$ is time.

### 2.4 Ranges

A range is specified by a lower and an upper bound on the real line. Ranges are subsequently referred to when defining parameter bounds.

To specify a range we begin with the keyword 'range_' followed by an integer. Each range has a lower and upper bound.

```
range_1 has lowerBound = 0.000E+00 has upperBound = 0.500E+02
range_2 has lowerBound = -0.500E+02 has upperBound = 0.000E+00
range_3 has lowerBound = 0.100E+00 has upperBound = 0.500E+02
```


### 2.5 Variable sets

A variable set contains a set of variables. Variable sets are subsequently referred to when defining model space. A new variable set begins with the keyword 'memberOfSet_' followed by an integer, and finally a list of variables.

```
memberOfSet_1 variable_1 variable_2 variable_3 variable_4 variable_5
    variable_6 variable_7
memberOfSet_2 variable_4 variable_5 variable_6 variable_7
memberOfSet_3 variable_3 variable_5 variable_6 variable_7
memberOfSet_4 variable_3 variable_4 variable_6 variable_7
memberOfSet_5 variable_3 variable_4 variable_5 variable_7
memberOfSet_6 variable_3 variable_4 variable_5 variable_6
```

Note that the line break between 'variable_5' and 'variable_6' for 'memberOfSet_1' above is for display purpose and not part of the correct syntax.

### 2.6 Model space

The model space is defined separately for each dependent variable (ODE). Note that the model space may differ between the variables.

For each dependent variable there may be several possible reactions. A new possible reaction begins with the keyword possibleReaction_followed by an integer, and then followed by 'of' and the variable to consider. Each possible reaction has a type (must be one of the pre-specified types above), a space of allowed variables for each local variable, and ranges for all parameters.

```
possibleReaction_1 of variable_3
has type = uniMolecularMassAction
has spaceOfVariable X1 = memberOfSet_2
has rangeOfParameter k1 = range_1
possibleReaction_2 of variable_3
```

```
has type = uniMolecularMassAction
has spaceOfVariable X1 = variable_3
has rangeOfParameter k1 = range_2
possibleReaction_3 of variable_3
has type = biMolecularMassAction
has spaceOfVariable X1 = memberOfSet_2
has spaceOfVariable X2 = memberOfSet_1
has rangeOfParameter k1 = range_1
possibleReaction_4 of variable_3
has type = biMolecularMassAction
has spaceOfVariable X1 = variable_3
has spaceOfVariable X2 = memberOfSet_1
has rangeOfParameter k1 = range_2
possibleReaction_5 of variable_3
has type = michaelisMenten
has spaceOfVariable X1 = memberOfSet_2
has rangeOfParameter k1 = range_1
has rangeOfParameter k2 = range_3
possibleReaction_6 of variable_3
has type = michaelisMenten
has spaceOfVariable X1 = variable_3
has rangeOfParameter k1 = range_2
has rangeOfParameter k2 = range_3
possibleReaction_7 of variable_3
has type = michaelisMentenNonCompInhib
has spaceOfVariable X1 = memberOfSet_2
has spaceOfVariable X2 = memberOfSet_1
has rangeOfParameter k1 = range_1
has rangeOfParameter k2 = range_3
has rangeOfParameter k3 = range_3
possibleReaction_8 of variable_3
has type = michaelisMentenNonCompInhib
has spaceOfVariable X1 = variable_3
has spaceOfVariable X2 = memberOfSet_1
has rangeOfParameter k1 = range_2
has rangeOfParameter k2 = range_3
has rangeOfParameter k3 = range_3
```

The above text specifies the possible reactions of variable 3. A summary is given in table 1.

Note that is assumed that $X_{i} \neq X_{j}$. For example, the following 'michaelisMentenNonCompInhib' reaction is not part of the above model space

$$
\frac{k_{1} X_{3}}{\left(k_{2}+X_{3}\right)\left(1+\frac{X_{3}}{k_{3}}\right)}
$$

Also note that some combinations of the biMolecularMassAction reaction are equivalent, e.g. $k_{1} x_{5} x_{6}$ and $k_{1} x_{6} x_{5}$. Hence, in practice, one of them can be ignored.

| Rate equation | Variable space | Parameter range |
| :--- | :--- | :--- |
| $k_{1} X_{1}$ | $X_{1} \in\left\{x_{4}, x_{5}, x_{6}, x_{7}\right\}$ | $k_{1} \in[0.0,50.0]$ |
| $k_{1} X_{1}$ | $X_{1} \in\left\{x_{3}\right\}$ | $k_{1} \in[-50.0,0.0]$ |
| $k_{1} X_{1} X_{2}$ | $X_{1} \in\left\{x_{4}, x_{5}, x_{6}, x_{7}\right\}$ | $k_{1} \in[0.0,50.0]$ |
|  | $X_{2} \in\left\{x_{1}, x_{2}, x_{3}, x_{4}, x_{5}, x_{6}, x_{7}\right\}$ |  |
| $k_{1} X_{1} X_{2}$ | $X_{1} \in\left\{x_{3}\right\}$ | $k_{1} \in[-50.0,0.0]$ |
|  | $X_{2} \in\left\{x_{1}, x_{2}, x_{3}, x_{4}, x_{5}, x_{6}, x_{7}\right\}$ |  |
| $\frac{k_{1} X_{1}}{k_{2}+X_{1}}$ | $X_{1} \in\left\{x_{4}, x_{5}, x_{6}, x_{7}\right\}$ | $k_{1} \in[0.0,50.0]$ |
| $\frac{k_{1} X_{1}}{k_{2}+X_{1}}$ | $X_{1} \in\left\{x_{3}\right\}$ | $k_{2} \in[0.10,50.0]$ |
| $\frac{k_{1} \in X_{1}}{\left(k_{2}+X_{1}\right)\left(1+\frac{X_{2}}{k_{3}}\right)}$ | $X_{1} \in\left\{x_{4}, x_{5}, x_{6}, x_{7}\right\}$ | $k_{2} \in[0.10 .0,50.0]$ |
|  | $X_{2} \in\left\{x_{1}, x_{2}, x_{3}, x_{4}, x_{5}, x_{6}, x_{7}\right\}$ | $k_{1} \in[0.0,50.0]$ |
|  | $k_{2} \in[0.10,50.0]$ |  |
|  | $k_{3} \in[0.10,50.0]$ |  |
| $\frac{k_{1} X_{1}}{\left(k_{2}+X_{1}\right)\left(1+\frac{X_{2}}{k_{3}}\right)}$ | $X_{1} \in\left\{x_{3}\right\}$ | $k_{1} \in[-50.0,0.0]$ |
|  | $X_{2} \in\left\{x_{1}, x_{2}, x_{3}, x_{4}, x_{5}, x_{6}, x_{7}\right\}$ | $k_{2} \in[0.10,50.0]$ |
|  | $k_{3} \in[0.10,50.0]$ |  |

Table 1: Summary of possible reactions of variable 3 in the problem metabol2

Table 2 gives the list of possible reactions explicitly written out (this time without ranges for the parameters).

The ODE for variable 3 should be selected from any subset of the above 59 reaction terms. For the problem we consider as example, metabol2, the true ODE is

$$
x_{3}^{\prime}(t)=\frac{k_{1} x_{3}}{\left(k_{2}+x_{3}\right)\left(1+\frac{x_{1}}{k_{3}}\right)}+\frac{k_{4} x_{3}}{\left(k_{5}+x_{3}\right)\left(1+\frac{x_{2}}{k_{6}}\right)}+\frac{k_{7} x_{4}}{\left(k_{8}+x_{4}\right)}+\frac{k_{9} x_{5}}{\left(k_{10}+x_{5}\right)}
$$

For S-systems, the model space is simply defined by bounds for the parameters.

```
alpha has defaultLowerBound = 0.
alpha has defaultUpperBound = 20.
beta has defaultLowerBound = 0.
beta has defaultUpperBound = 20.
```

| $k_{1} x_{4}$ | $k_{1} x_{5}$ | $k_{1} x_{6}$ | $k_{1} x_{7}$ | $k_{1} x_{3}$ |
| :---: | :---: | :---: | :---: | :---: |
| $k_{1} x_{4} x_{1}$ | $k_{1} x_{4} x_{2}$ | $k_{1} x_{4} x_{5}$ | $k_{1} x_{4} x_{6}$ | $k_{1} x_{4} x_{7}$ |
| $k_{1} x_{5} x_{1}$ | $k_{1} x_{5} x_{2}$ | $k_{1} x_{5} x_{6}$ | $k_{1} x_{5} x_{7}$ | $k_{1} x_{6} x_{1}$ |
| $k_{1} x_{6} x_{2}$ | $k_{1} x_{6} x_{7}$ | $k_{1} x_{7} x_{1}$ | $k_{1} x_{7} x_{2}$ | $k_{1} x_{3} x_{1}$ |
| $k_{1} x_{3} x_{2}$ | $k_{1} x_{3} x_{4}$ | $k_{1} x_{3} x_{5}$ | $k_{1} x_{3} x_{6}$ |  |
| $\frac{k_{1} x_{4}}{k_{2}+x_{4}}$ | $\frac{k_{1} x_{5}}{k_{2}+x_{5}}$ | $\frac{k_{1} x_{6}}{k_{2}+x_{6}}$ | $\frac{k_{1} x_{7}}{k_{2}+x_{7}}$ | $\frac{k_{1} x_{3}}{k_{2}+x_{3}}$ |
| $\frac{k_{1} x_{4}}{\left(k_{2}+x_{4}\right)\left(1+\frac{x_{1}}{k_{3}}\right)}$ | $\frac{k_{1} x_{4}}{\left(k_{2}+x_{4}\right)\left(1+\frac{x_{2}}{k_{3}}\right)}$ | $\frac{k_{1} x_{4}}{\left(k_{2}+x_{4}\right)\left(1+\frac{x_{3}}{k_{3}}\right)}$ | $\frac{k_{1} x_{4}}{\left(k_{2}+x_{4}\right)\left(1+\frac{x_{5}}{k_{3}}\right)}$ | $\frac{k_{1} x_{4}}{\left(k_{2}+x_{4}\right)\left(1+\frac{x_{6}}{k_{3}}\right)}$ |
| $\frac{k_{1} x_{4}}{\left(k_{2}+x_{4}\right)\left(1+\frac{x_{7}}{k_{3}}\right)}$ | $\frac{k_{1} x_{5}}{\left(k_{2}+x_{5}\right)\left(1+\frac{x_{1}}{k_{3}}\right)}$ | $\frac{k_{1} x_{5}}{\left(k_{2}+x_{5}\right)\left(1+\frac{x_{2}}{k_{3}}\right)}$ | $\frac{k_{1} x_{5}}{\left(k_{2}+x_{5}\right)\left(1+\frac{x_{3}}{k_{3}}\right)}$ | $\frac{k_{1} x_{5}}{\left(k_{2}+x_{5}\right)\left(1+\frac{x_{4}}{k_{3}}\right)}$ |
| $\frac{k_{1} x_{5}}{\left(k_{2}+x_{5}\right)\left(1+\frac{x_{6}}{k_{3}}\right)}$ | $\frac{k_{1} x_{5}}{\left(k_{2}+x_{5}\right)\left(1+\frac{x_{7}}{k_{3}}\right)}$ | $\frac{k_{1} x_{6}}{\left(k_{2}+x_{6}\right)\left(1+\frac{x_{1}}{k_{3}}\right)}$ | $\frac{k_{1} x_{6}}{\left(k_{2}+x_{6}\right)\left(1+\frac{x_{2}}{k_{3}}\right)}$ | $\frac{k_{1} x_{6}}{\left(k_{2}+x_{6}\right)\left(1+\frac{x_{3}}{k_{3}}\right)}$ |
| $\frac{k_{1} x_{6}}{\left(k_{2}+x_{6}\right)\left(1+\frac{x_{4}}{k_{3}}\right)}$ | $\frac{k_{1} x_{6}}{\left(k_{2}+x_{6}\right)\left(1+\frac{x_{5}}{k_{3}}\right)}$ | $\frac{k_{1} x_{6}}{\left(k_{2}+x_{6}\right)\left(1+\frac{x_{7}}{k_{3}}\right)}$ | $\frac{k_{1} x_{7}}{\left(k_{2}+x_{7}\right)\left(1+\frac{x_{1}}{k_{3}}\right)}$ | $\frac{k_{1} x_{7}}{\left(k_{2}+x_{7}\right)\left(1+\frac{x_{2}}{k_{3}}\right)}$ |
| $\frac{k_{1} x_{7}}{\left(k_{2}+x_{7}\right)\left(1+\frac{x_{3}}{k_{3}}\right)}$ | $\frac{k_{1} x_{7}}{\left(k_{2}+x_{7}\right)\left(1+\frac{x_{4}}{k_{3}}\right)}$ | $\frac{k_{1} x_{7}}{\left(k_{2}+x_{7}\right)\left(1+\frac{x_{5}}{k_{3}}\right)}$ | $\frac{k_{1} x_{7}}{\left(k_{2}+x_{7}\right)\left(1+\frac{x_{6}}{k_{3}}\right)}$ | $\frac{k_{1} x_{3}}{\left(k_{2}+x_{3}\right)\left(1+\frac{x_{1}}{k_{3}}\right)}$ |
| $\frac{k_{1} x_{3}}{\left(k_{2}+x_{3}\right)\left(1+\frac{x_{2}}{k_{3}}\right)}$ | $\frac{k_{1} x_{3}}{\left(k_{2}+x_{3}\right)\left(1+\frac{x_{4}}{k_{3}}\right)}$ | $\frac{k_{1} x_{3}}{\left(k_{2}+x_{3}\right)\left(1+\frac{x_{5}}{k_{3}}\right)}$ | $\frac{k_{1} x_{3}}{\left(k_{2}+x_{3}\right)\left(1+\frac{x_{6}}{k_{3}}\right)}$ | $\frac{k_{1} x_{3}}{\left(k_{2}+x_{3}\right)\left(1+\frac{x_{7}}{k_{3}}\right)}$ |

Table 2: List of all possible reactions of variable 3 in the problem metabol2

```
g has defaultLowerBound = -4.
g_1_1 has lowerBound = 0.
g_2_2 has lowerBound = 0.
g_3_3 has lowerBound = 0.
g has defaultUpperBound = 4.
g_1_1 has upperBound = 0.
g_2_2 has upperBound = 0.
g_3_3 has upperBound = 0.
h has defaultLowerBound = -4.
h_1_1 has lowerBound = 1.E-15
h_2_2 has lowerBound = 1.E-15
h_3_3 has lowerBound = 1.E-15
h has defaultUpperBound = 4.
```

The keywords 'defaultLowerBound' and 'defaultUpperBound' can be used to assign one value to all elements in a vector or matrix. Naturally, subsequent assignments of specific elements overwrites the default value.

Besides, one of the benchmark problems include an additional constraint of type $\left\{g_{i, j} \in[-3,3], g_{i, j} \neq 0\right\}$. This means that there is an interaction between variable
$i$ and $j$ but the direction is unknown. We use the following syntax to constrain the value to non-zero:

```
g_2_1 is nonZero
h_5_5 is nonZero
```


### 2.7 Error function

The error function is defined by the keyword 'errorFunction'. For identification of both structure and parameters we have used:

```
errorFunction
has type = minusLogLikelihoodPlusLambdaK
has equation = -L+lambda*K
has lambda = 1.
```

Hence, we have chosen to consider the error function

$$
-L(\hat{X} \mid \mathbf{k})+\lambda K
$$

The first term is the negative log-likelihood of the experimental data, and the second term is a term that penalizes structural complexity of the model.
In detail, $L$ is the log-likelihood, $\hat{X}$ denotes experimental data, $\mathbf{k}$ is a vector of parameters, $\lambda$ is a constant, and $K$ is the number of parameters. By assuming independent and normally distributed measurement errors and disregarding constant terms we can express the log-likelihood for one time series as

$$
L\left(\hat{X}_{j} \mid \mathbf{k}\right)=-\frac{1}{2} \sum_{i}\left(\frac{X_{j}\left(t_{i}\right)-\hat{X}_{j}\left(t_{i}\right)}{\sigma_{j}\left(t_{i}\right)}\right)^{2}
$$

where $i$ indexes the measurement points, and where $X_{j}, \hat{X}_{j}$ and $\sigma_{j}$ denotes simulated data, experimental data and standard deviation for variable $j$, respectively. The total log-likelihood $L(\hat{X} \mid \mathbf{k})$ is defined by summing over all variables and all experiments.

For models based on chemical rate equations the number of parameters, $K$, is simply the total number of parameters on the right-hand side of the ODEs. For S-systems, it is natural to define $K$ as the total number of non-zero elements in $g$ and $h$ plus the parameters in $\alpha$ and $\beta$.

For identification of parameters (fixed structure) one can use:

```
errorFunction
has type = minusLogLikelihood
has equation = -L
```


### 2.8 Experiments

General information about the experiments are given in the following form.

```
experiment 1 has name = exp1
experiment_2 has name = exp2
experiment_3 has name = exp3
experiment_4 has name = exp4
```

Each experiment has a number and a name. For perfect data (no noise), 'has perfectData' can be added.

```
experiment_1 has name = exp1 has perfectData
experiment_2 has name = exp2 has perfectData
experiment_3 has name = exp3 has perfectData
experiment_4 has name = exp4 has perfectData
```

Then, details about each experiment are given.

```
sample_1 of experiment_1
has time = 0.0E+00
has variable_ = 0.200E+01 0.300E+02 0.1202588848674883E+01 ...
has sdev of variable_ = 0.0E+00 0.0E+00 0.53781408E-01 ...
sample_2 of experiment_1
has time = 0.75000000E+01
has variable_ = 0.200E+01 0.300E+02 0.9256634735714073E+01 ...
has sdev of variable_ = 0.0E+00 0.0E+00 0.92566347E+00 ...
21 of experiment_1
has time = 0.15000000E+03
has variable_ = 0.200E+01 0.300E+02 0.7581719037437853E+01 ...
has sdev of variable_ = 0.0E+00 0.0E+00 0.75817190E+00 ...
```

The keyword 'sample_' followed by an integer begins description of one sample. The rest of the line 'of experiment_1' states from which experiment the sample is taken. Each sample has a time-point, a vector of variables, and a vector of standard deviations. The vectors have the same length as the number of variables.

This compact form is useful when we have fully observed variables. In general, the sampled variables can be given individually as

```
sample_1 of experiment_1
has time = 0.0E+00
has variable_1 = 0.200E+01
has variable_2 = 0.300E+02
has variable_3 = 0.1202588848674883E+01
has sdev of variable_1 = 0.0E+00
has sdev of variable_2 = 0.0E+00
has sdev of variable_3 = 0.53781408E-01
```


### 2.9 Initial bounds

Initial bounds are given for each dependent variable in each experiments. The keywords 'variable_' and 'experiment_' followed by integers specify which variable and experiment to consider.

```
variable_3 of experiment_1
has lowerInitialBound = 0.1091E+01
has upperInitialBound = 0.1314E+01
variable_4 of experiment_1
has lowerInitialBound = 0.4505E+02
has upperInitialBound = 0.5388E+02
variable_5 of experiment_1
has lowerInitialBound = 0.4428E+02
has upperInitialBound = 0.5311E+02
variable_6 of experiment_1
has lowerInitialBound = 0.9109E+02
has upperInitialBound = 0.1087E+03
variable_7 of experiment_1
has lowerInitialBound = 0.1283E+01
has upperInitialBound = 0.1527E+01
variable_3 of experiment_2
has lowerInitialBound = 0.1139E+01
has upperInitialBound = 0.1363E+01
```

Note that information about initial bounds is unnecessary for perfect data.

### 2.10 Initial solution

The right-hand sides of all ODEs are by default assigned zero.
The initial solution specify a potential starting model other than zero. The syntax is similar to the one used to describe the model space. Instead of 'possibleReaction' we now write 'reaction', and instead of 'spaceOfVariable' we now write 'variable'. Here is an example for the case when the true structure is known for variable 3 of the problem 'metabol2'.

```
reaction_1 of variable_3
has type = michaelisMentenNonCompInhib
has variable X1 = variable_3
has variable X2 = variable_2
has rangeOfParameter k1 = range_2
has rangeOfParameter k2 = range_3
has rangeOfParameter k3 = range_3
reaction_2 of variable_3
has type = michaelisMentenNonCompInhib
```

```
has variable X1 = variable_3
has variable X2 = variable_1
has rangeOfParameter k1 = range_2
has rangeOfParameter k2 = range_3
has rangeOfParameter k3 = range_3
reaction_3 of variable_3
has type = michaelisMenten
has variable X1 = variable_4
has rangeOfParameter k1 = range_1
has rangeOfParameter k2 = range_3
reaction_4 of variable_3
has type = michaelisMenten
has variable X1 = variable_5
has rangeOfParameter k1 = range_1
has rangeOfParameter k2 = range_3
```

For S-systems, an initial solution is easily defined with similar syntax as used to define the model space. The keyword 'initialValue' is used to assign a specific element. The keyword 'defaultInitialValue' is used to assign all elements in a vector or matrix.

```
alpha has defaultInitialValue = 1
beta has defaultInitialValue = 1
beta_2 has initialValue = 0.
g has defaultInitialValue = 0
g_2_3 has initialValue = 2.
h has defaultInitialValue = 0
h_1_1 has initialValue = 1.
h_2_2 has initialValue = 1.
h_3_3 has initialValue = 1.
```

For a problem with 3 dependent variables this gives:

$$
\begin{aligned}
& \alpha=\left[\begin{array}{lll}
1 & 1 & 1
\end{array}\right] \\
& \beta=\left[\begin{array}{lll}
1 & 0 & 1
\end{array}\right] \\
& g=\left[\begin{array}{lll}
0 & 0 & 0 \\
0 & 0 & 2 \\
0 & 0 & 0
\end{array}\right] \\
& h=\left[\begin{array}{lll}
1 & 0 & 0 \\
0 & 1 & 0 \\
0 & 0 & 1
\end{array}\right] .
\end{aligned}
$$

### 2.11 End of problem

The problem ends in the following way:
end problem metabol2

