

Location Leakage in Distance Bounding: Why Location Privacy does not Work

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Abstract

In many cases, we can only have access to a service by proving we are sufficiently close to a particular location (e.g., in automobile or building access control). In these cases, proximity can be guaranteed through signal attenuation. However, by using additional transmitters an attacker can relay signals between the prover and the verifier. Distance-bounding protocols are the main countermeasure against such attacks; however, such protocols may leak information regarding the location of the prover and/or the verifier who run the distance-bounding protocol.

In this paper, we consider a formal model for location privacy in the context of distance-bounding. In particular, our contributions are threefold: we first define a security game for location privacy in distance bounding; secondly, we define an adversarial model for this game, with two adversary classes; finally, we assess the feasibility of attaining location privacy for distance-bounding protocols. Concretely, we prove that for protocols with a beginning or a termination, it is theoretically impossible to achieve location privacy for either of the two adversary classes, in the sense that there always exists a polynomially-bounded adversary winning the security game. However, for so-called limited adversaries, who cannot see the location of arbitrary provers, carefully chosen parameters do, in practice, enable computational location privacy.

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5 *Keywords:* location privacy, distance-bounding, authentication.
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7 8 **1. Introduction** 9

10 Often, our location is critical in order to gain access to places and/or
11 services. For instance, in applications such as automobile access control
12 the key (prover) needs to be close enough to the car lock (verifier) in order
13 to unlock it [17]. In some cases, unlocking the car may in fact also start
14 the car (in passive keyless entry and start (PKES) systems [18]). If the
15 proximity check is performed through signal attenuation, an adversary may
16 easily perform man-in-the-middle attacks by relaying messages between the
17 communicating parties (provers and verifiers), while these parties are situated
18 far from each other. Thus, in the automobile example, an adversary may
19 unlock the car even if the car key (the prover) is located very far. This type
20 of attack (called mafia fraud [11]) can also be mounted against bankcards [13],
21 mobile phones [19], proximity cards [20], and wireless ad-hoc networks [21,
22 27].

23 Distance-bounding (DB) protocols are meant to counteract man-in-the-
24 middle relay attacks in authentication schemes. They are challenge-response
25 authentication protocols, that allow the verifier, by measuring the time-of-
26 flight of the messages exchanged, to calculate an upper bound on the prover's
27 distance (as well as checking the validity of the responses which usually en-
28 sure authentication). DB protocols were first introduced by Brands and
29 Chaum [6] to preclude relay attacks in ATM systems. Subsequently, numer-
30 ous DB protocols were proposed [22, 30, 9] and many attacks against them
31 have been published [2, 3, 15]. DB protocols have also been analysed for
32 the case of noisy channels [23] and the optimal setting of security param-
33 eters [12, 25]. To the best of our knowledge [4, 5] describes the latest most
34 secure distance-bounding protocol against all known attack modes. Another
35 provably-secure protocol attaining quite strong terrorist-fraud resistance re-
36 quirements has been recently published in [16].

37 Location privacy was introduced in the context of distance bounding by
38 Rasmussen and Čapkun [28], who noted that distance-bounding protocols
39 may leak further location-related information than just the fact that the
40 prover is within the maximum allowed distance from the verifier. This infor-
41 mation leakage follows from the measurement of the messages' arrival times.

42 To combat this, Rasmussen and Čapkun [28] proposed a privacy-preserving
43 distance-bounding protocol (denoted here as the RČ protocol). Though the
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5 protocol in [28] claims to preserve location privacy, we note that location
6 privacy has never been formalized in the literature. Additionally, the RC
7 protocol has been shown to be susceptible to a non-polynomial dictionary
8 attack which may reveal the prover's and verifier's locations [1] as well as to a
9 *mafia fraud* attack [24]. Mitrokotsa *et al.* [24] have proposed a new distance-
10 bounding protocol called *Location-Private Distance Bounding* (LPDB) that
11 improves the basic construction of the RC protocol and renders it secure
12 against the latter attack.
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15 Distance bounding can also be extended to location verification [32] (also
16 known as secure positioning [31]), where multiple verifiers interact with a sin-
17 gle prover. In that case the location of the prover can be determined using the
18 intersection of the bounding spheres surrounding each verifier. This approach
19 is also taken under consideration in the recent work regarding position-based
20 cryptography [10]. Our approach here is different as we consider a single
21 verifier and many provers, and we thus only achieve distance bounding, and
22 not secure positioning. Moreover, in position-based cryptography all the ad-
23 versaries have the same knowledge as the prover, including the secret key.
24 However, in our model, we do not allow the adversary knowledge of the secret
25 key, as that would allow it to trivially distinguish between the two provers
26 in the location privacy game, without actually requiring any location data.
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30 We also mention the recent work on localisation privacy by Burmester
31 [7, 8], where location is used in a steganographic sense (such that provers
32 are convinced that verifier-generated challenges are honest, and they do not
33 reveal their presence to adversaries). However, very notably the constructions
34 in [8] require provers to be aware of their position/location, which is a strong
35 assumption in generic authentication/distance-bounding scenarios. In this
36 case, location is used as a part of the verifier's challenge, and the prover
37 verifies that the location is sufficiently close to its own location.
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40 **Contributions:** In this paper, we address precisely the topics of location
41 privacy in distance-bounding. Our contributions are threefold:
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- 44 1. We first define a classical left-or-right *indistinguishability* game for lo-
45 cation privacy in distance-bounding protocols. In this game, the ad-
46 versary knows its distance to the verifier \mathcal{V} and can create provers \mathcal{P}
47 at arbitrary distances from itself and \mathcal{V} .
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- 49 2. For this location privacy game, we consider two main adversarial classes:
50 *omniscient* and *limited* adversaries. *Omniscient* adversaries capture an
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adversary that can measure the signal strength of the transmitted messages and is aware, for all transmissions along the timed channel, when the message is sent and when it arrives at its own interface. Unsurprisingly, no location privacy is feasible for omniscient adversaries. *Limited* adversaries, on the other hand, are only aware of the time at which they receive messages from other participants.

3. Finally, we show that achieving location privacy with respect to limited adversaries is impossible for protocols with a beginning or a termination, and which run in polynomial time. We prove that location privacy against limited adversaries minimally requires the prover and the verifier to introduce exponential delays between receiving and sending messages, and we give a lower bound for these delays. Since the transmission speed is high (e.g. the speed of light in the case of RFID transmissions), the delay can be implemented in practice. Finally, we show how to specify these delays in the LPDB protocol proposed in [24].

Organization: This paper is organized as follows. We begin by defining distance-bounding protocols and location privacy in Section 2, outlining also our adversarial classes. We then assess the feasibility of achieving location privacy for distance-bounding protocols in Section 3, for both *omniscient* and *limited* adversaries, giving a lower bound for the delays that each party must have between receiving a message and sending a response message. We apply our results and the obtained bound in Section 4, in order to modify the LPDB protocol [24] to attain location privacy with respect to limited adversaries.

2. Preliminaries

2.1. Communication Model

Our distance-bounding scenario resembles that of Dürholz *et al.* [14], but we consider multiple provers. Concretely, there is a single verifier \mathcal{V} , but many provers $\mathcal{P}_1, \dots, \mathcal{P}_n$, such that \mathcal{V} and \mathcal{P}_i for every i share a secret key K_i output by a key generation algorithm Kg . We also assume that when it is initialised, the verifier \mathcal{V} is also equipped with an upper bound on the maximum allowed communication time (or time distance) t_{\max} between itself and the prover.

The communication model considered by [14] is round-based. However, e.g. the RČ [28] and the LPDB [24] distance-bounding protocols are *not*

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5 round-based. Therefore, we consider a more generalised model, where the
6 two parties \mathcal{P} and \mathcal{V} interact with no round-based restriction, via *two* types
7 of channels: a *timeless* and a *timed* channel. Parties \mathcal{P} and \mathcal{V} may send
8 messages m along each of the two channels (i.e., they are duplex channels).
9 In order to make the model more realistic we consider the transmissions along
10 the *timed* channel to be bit-by-bit.

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12 More formally, the *timed* channel is associated with the global clock, such
13 that each bit of an input message m will be associated with a time \mathbf{ts} at which
14 the sending party has *sent* the bit. The corresponding output bit of message
15 m is associated with a time \mathbf{tr} , which is the time at which the receiving party
16 has *received* the bit. The bit-by-bit treatment of the transmission time is
17 compulsory, as in practice, each bit of the message is transmitted sequentially
18 or in smaller packets. However, for practical purposes we will often associate
19 (in our proofs) the sending time of a message with the sending time of the first
20 bit of this message, since this particular value is enough to leak significant
21 information regarding the position of the honest protocol participants (prover
22 and/or verifier). We discuss the soundness and the limitations of our model
23 in Section 5.

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25 For the sake of completeness, however, we associate in our model a message
26 m with an $|m|$ -dimensional vector of sending times $\bar{\mathbf{ts}}$ and an $|m|$ -
27 dimensional vector of transmission times $\bar{\mathbf{tr}}$. We also require that the values
28 in $\bar{\mathbf{ts}}$ and those in $\bar{\mathbf{tr}}$ are monotone non-decreasing, i.e. for any message m
29 and any $1 \leq i < j \leq m$, it holds that $\mathbf{ts}_i \leq \mathbf{ts}_j$ and $\mathbf{tr}_i \leq \mathbf{tr}_j$. Furthermore,
30 if we consider the communication between two parties A and B and that
31 a message m is sent from the party A to the party B at time $\bar{\mathbf{ts}}$ then the
32 reception time $\bar{\mathbf{tr}}$ of the message m at the party B will satisfy the following
33 equation for every $i = \{1, \dots, |m|\}$ ¹:

$$34 \quad \mathbf{tr}_i = \mathbf{ts}_i + t_{AB},$$

35 where t_{AB} denotes the *time distance* between the parties A and B . More
36 precisely, t_{AB} denotes the time (measured in time units TU) that every bit
37 of a message m takes to travel between A and B .

38 Moreover, if the message m leaks off this channel to an adversary \mathcal{A} , each
39 bit of the leaked message is associated with an $|m|$ -dimensional timestamp

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50 ¹In particular, we assume a perfect reliability of the transmission channel. We discuss
51 the strength of this assumption in Section 5.

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$\bar{\text{tr}}_{\mathcal{A}}$. Note that this information alone may not suffice to learn the *sending* time of the message, as the adversary does not necessarily know the distance between it and the sending party.

Both channels allow the prover \mathcal{P} and the verifier \mathcal{V} to interact concurrently, i.e. it is possible that both the prover \mathcal{P} and the verifier \mathcal{V} transmit at the same time across the duplex channel. This is indeed the case for the RČ protocol [28].

We now define communication in distance-bounding protocols as being *slow* (or *lazy*) if it takes place on the timeless communication channel and *fast* (or *time-critical*) if it takes place on the timed communication channel. Note that it is possible to alternate fast and slow communication arbitrarily. We note that this approach is perfectly in-tune with the similar communication model of [14], but it is also compatible with protocols that are not round-based.

Definition 1. *We say that $\mathcal{DB} = (\mathcal{V}, \mathcal{P}, \text{Kg})$ is a distance-bounding protocol with parameters (t_{\max}, ϵ) where t_{\max} denotes the upper bound on transmission time in the fast phase and ϵ denotes the tolerance level for honest \mathcal{P} - \mathcal{V} authentication failures if and only if:*

KEY GENERATION: Kg generates a secret key $K \leftarrow \text{Kg}(1^\ell)$ for any $\ell \in \mathbb{N}$.

DISTANCE-BOUNDING AUTHENTICATION: *The joint execution of the prover and verifier algorithms \mathcal{V} and \mathcal{P} for parameters (t_{\max}, ϵ) ends with a verifier-generated distance-bounding authentication bit $b \in \{0, 1\}$.*

We require ϵ -completeness, i.e., the interaction of an honest prover \mathcal{P} and an honest, fixed verifier \mathcal{V} for parameters (t_{\max}, ϵ) is accepted by the verifier with probability at least $1 - \epsilon$ if $t_{\mathcal{V}\mathcal{P}} \leq t_{\max}$.

2.2. Adversarial Models

In our framework, the goal of the adversary is to break location privacy as defined below. In this section, we first show how adversaries interact with the communication channels and with the honest parties during an attack. Then, we define two adversarial classes depending on the strength of the adversary. Finally, we show the location privacy game.

We consider adversaries \mathcal{A} that interact with the distance-bounding system as follows: (1) \mathcal{A} may eavesdrop on the communication (across both the *timed* and the *timeless* channel) of an honest prover \mathcal{P} and an honest verifier \mathcal{V} ; and (2) \mathcal{A} may interact with honest provers in prover-adversary sessions and with honest verifiers in adversary-verifier sessions. Note that

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5 this behavior implies that an adversary can mount a full man-in-the-middle
6 attack by simply opening concurrent prover-adversary and adversary-verifier
7 sessions. This is again in agreement with the treatment given by Dürholz *et*
8 *al.*; we refer to that paper for the more formal notions of session identifiers.
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10 In view of [33, 26], we consider that frequency hopping (i.e. implementing
11 a protocol such that the sender and the receiver hop from one frequency to
12 another during the transmission) is not an effective countermeasure against
13 eavesdropping adversaries. In particular, by simply eavesdropping all possi-
14 ble frequencies (in practice the prover and the verifier are unable to use too
15 many different frequencies), the adversary can successfully “piece together”
16 the communication.
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18 We consider two types of adversaries: the *limited* and the *omniscient*
19 adversaries, which are described as follows:
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21 **LIMITED ADVERSARIES:** These adversaries may eavesdrop on honest
22 prover-verifier sessions or communicate with provers and verifiers in prover-
23 adversary and respectively adversary-verifier sessions. On eavesdropping the
24 timed channel in honest prover-verifier sessions, limited adversaries learn the
25 transmitted message m and the bit-by-bit time the message is received at,
26 $\bar{t}r_{\mathcal{A}} = \bar{t}s + \bar{t}t_{P,\mathcal{A}}$, where P is the party that sent the message m and $\bar{t}t_{P,\mathcal{A}}$ is an
27 $|m|$ -dimensional vector with entries equaling the time distance $t_{P,\mathcal{A}}$ between
28 P and the adversary \mathcal{A} . Note that the adversary \mathcal{A} is able to choose its loca-
29 tion and knows $t_{\mathcal{A}\mathcal{V}}$ (i.e. its time distance from the verifier \mathcal{V}); consequently,
30 \mathcal{A} learns the sending times at which the verifier sends its messages.
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32 **OMNISCIENT ADVERSARIES:** These adversaries can also eavesdrop on
33 honest prover-verifier sessions or communicate with provers and verifiers as
34 above. Additionally, an omniscient adversary can measure the signal strength
35 of the transmitted messages and is aware, for all transmissions along the
36 timed channel, when the message is sent and when it arrives at its interface.
37 More precisely, on eavesdropping on the timed channel during an honest
38 prover-verifier session, omniscient adversaries learn the message m , the bit-
39 by-bit time the message is received, $\bar{t}r_{\mathcal{A}} = \bar{t}s + \bar{t}t_{P,\mathcal{A}}$, and the bit-by-bit sending
40 time $\bar{t}s$. Thus, strong adversaries can trivially learn the distance between
41 them and the party P that sent the message.
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43 To justify that an omniscient adversary can also learn the sending time
44 of messages, we could model this by distributed, *limited* adversaries, i.e.
45 $\mathcal{A} = (\mathcal{A}_1, \mathcal{A}_2)$. The composite adversary \mathcal{A} chooses the *locations* of \mathcal{A}_1 and
46 \mathcal{A}_2 and can do triangulation of signals. This definition also extends to a
47 *moving* adversary (i.e. an adversary that is able to change its location) as
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discussed in Section 3.1.

We consider only polynomial adversaries, (i.e. having polynomial run-time and running polynomially many sessions with the provers and the verifier). The adversary's goal is to break the location privacy of the distance-bounding protocol, which we define by means of a left-or-right *indistinguishability* game as described below.

PHASE 1: In this phase, a limited adversary is given the security parameter (in unary) 1^λ . The adversary may now initialise provers \mathcal{P}_i and the verifier \mathcal{V} at arbitrary locations with respect to itself and the verifier, and may interact arbitrarily with the provers and the verifier. At the end of this phase, the adversary outputs two indices i, j such that $t_{\mathcal{P}_i\mathcal{V}}$ and $t_{\mathcal{P}_j\mathcal{V}}$ are both smaller than the threshold t_{\max} ; the two indices are then forwarded to a challenger.

PHASE 2: The challenger checks that the two provers are both within the maximum distance t_{\max} , then closes all sessions that are open for these provers. The challenger flips a bit b and assigns the handle $\mathcal{P}_{\text{Chal}}$ as follows: $\mathcal{P}_{\text{Chal}} = \mathcal{P}_i$ if $b = 0$ and $\mathcal{P}_{\text{Chal}} = \mathcal{P}_j$ if $b = 1$.

PHASE 3: Finally, by interacting with the challenge prover $\mathcal{P}_{\text{Chal}}$, as well as all other provers with the exception of \mathcal{P}_i and \mathcal{P}_j , the adversary must produce a decision bit d . Let $\text{Exp}_{\mathcal{DB}}^{\text{LocPriv}}(\mathcal{A}, 1^\lambda)$ be the output of a single run of the location privacy game. We say that the adversary *wins* if $d = b$, and we write it as $\text{Exp}_{\mathcal{DB}}^{\text{LocPriv}}(\mathcal{A}, 1^\lambda) = 1$. The adversary can be considered as a hypothesis test for the following hypotheses:

\mathcal{H}_0 : the response sent from the prover $\mathcal{P}_{\text{Chal}}$ to \mathcal{V} 's challenge is actually from the prover \mathcal{P}_0 .

and

\mathcal{H}_1 : the response sent from the prover $\mathcal{P}_{\text{Chal}}$ to \mathcal{V} 's challenge is actually from the prover \mathcal{P}_1 .

We define the advantage of the adversary in this game as:

$$\text{Adv}_{\mathcal{DB}}^{\text{LocPriv}} \mathcal{A} = |2\mathbb{P} [\text{Exp}_{\mathcal{DB}}^{\text{LocPriv}}(\mathcal{A}, 1^\lambda) = 1] - 1|$$

Definition 2. We say that distance-bounding protocols provide location privacy if $\forall \text{loc}_{\mathcal{P}_0}, \text{loc}_{\mathcal{P}_1}, \forall \text{loc}_{\mathcal{V}}, \forall \mathcal{A}$ it holds:

$$\text{Adv}_{\mathcal{DB}}^{\text{LocPriv}} \mathcal{A} = \text{negl}(1^\lambda),$$

where $\text{negl}(1^\lambda)$ denotes a negligible function in the security parameters.

We should note here that an adversary would select the location of the participants in such a way as to maximize his advantage. Thus, an adversary \mathcal{A} would not select \mathcal{P}_0 and \mathcal{P}_1 at the same location or at equal distance to \mathcal{A} and \mathcal{V} .

3. Why Location Privacy does not Work

In this section we first argue that *location privacy* cannot be achieved with respect to an *omniscient* adversary. Then, we show that *location privacy* can only be achieved with respect to *limited* adversaries if the honest parties running the protocol introduce (minimally) a delay in their transmissions; we furthermore give a lower bound on this delay.

3.1. Omniscient Adversary

It is trivial to see that no location privacy can be attained with respect to an omniscient adversary. Indeed, consider an omniscient adversary placed arbitrarily with respect to the verifier. Let this adversary \mathcal{A} create two provers \mathcal{P}_0 and \mathcal{P}_1 such that the distance between this adversary and the provers is different i.e. $t_{\mathcal{P}_0\mathcal{A}} \neq t_{\mathcal{P}_1\mathcal{A}}^2$.

The adversary forwards $\mathcal{P}_0, \mathcal{P}_1$ to the challenger, receiving the handle $\mathcal{P}_{\text{Chal}}$, which is either \mathcal{P}_0 or \mathcal{P}_1 . Now, the adversary eavesdrops on a session between $\mathcal{P}_{\text{Chal}}$ and \mathcal{V} , thus learning the sending time of the messages and the time the attacker receives them. The adversary thus calculates the time distance between itself and the two parties communicating and, since the distances are all different, it can identify the parties with probability 1.

A single, but *moving* adversary (i.e., an adversary that can change its position during the attack) could also infer some information about the location of the prover by standing between \mathcal{P}_0 and \mathcal{P}_1 and moving toward \mathcal{P}_0 due to the Doppler effect. If bits arrive with a higher frequency, they must be sent by \mathcal{P}_0 instead of \mathcal{P}_1 .

²Obviously an adversary \mathcal{A} would choose its location in order to maximise its advantage. Thus, choosing provers at equal distance to it would not be a good choice.

3.2. Limited Adversary

By eavesdropping on the duplex timed channel between the challenged prover and the verifier, the adversary will receive $\text{tr}_{\mathcal{A}}^i$, the timestamp when \mathcal{A} receives the first bit of message m_i . The adversary \mathcal{A} also observes:

- $t_{\mathcal{V}} = \text{tr}_{\mathcal{A}}^1$: the time \mathcal{A} receives the first message bit from \mathcal{V} .
- $t_{\mathcal{P}} = \text{tr}_{\mathcal{A}}^2$: the time \mathcal{A} receives the first message bit from \mathcal{P} .

In what follows we show that the very first bit sent through the timed channel leaks. To be able to prove that, we make the following reasonable assumptions regarding how the sending time of this first bit is decided during the protocol. Note that similar observations hold for the final bit sent. For simplicity, we only treat the first one.

Assumption 1. *We assume that the distance-bounding phase of a distance-bounding protocol may have one of the following constructions:*

- **Case 1:** *The verifier \mathcal{V} starts the distance-bounding phase after a reference time t_0 and a random delay, possibly equal to 0, which we denote $\text{delay}_{\mathcal{V}}$, while the prover \mathcal{P}_b where $b \in \{0, 1\}$ starts after receiving the first message from the verifier \mathcal{V} and a random delay $\text{delay}_{\mathcal{P}_b}$.*
- **Case 2:** *The prover \mathcal{P}_b starts the distance-bounding phase after a reference time t_0 and a random delay $\text{delay}_{\mathcal{P}_b}$, while the verifier \mathcal{V} starts after receiving the first message from the prover \mathcal{P}_b and a random delay $\text{delay}_{\mathcal{V}}$.*
- **Case 3:** *The prover \mathcal{P}_b and the verifier \mathcal{V} start sending messages independently. More precisely, the prover \mathcal{P}_b starts sending messages after a reference time $T_{\mathcal{P}_b}$ and a random delay $\text{delay}_{\mathcal{P}_b}$, while the verifier \mathcal{V} starts sending messages after a reference time $T_{\mathcal{V}}$ and a random delay $\text{delay}_{\mathcal{V}}$.*

We should note here that when we mention “random delay” we mean a delay of arbitrary distribution.

Assumption 2. *We also assume that \mathcal{A} knows the times $T_{\mathcal{P}_b}$ (where $b \in \{0, 1\}$) and $T_{\mathcal{V}}$; the latter value is defined only for Case 3 of Assumption 1.*

In Figure 1 are depicted the above described cases. Without loss of generality in Figure 1 the adversary \mathcal{A} is located between the verifier \mathcal{V} and the prover \mathcal{P} .

It is easy to see that in our model a limited adversary \mathcal{A} knows and can even choose the locations of $\mathcal{P}_0, \mathcal{P}_1$ with respect to itself and the verifier \mathcal{V} , i.e. the values $t_{\mathcal{A}\mathcal{P}_0}, t_{\mathcal{A}\mathcal{P}_1}, t_{\mathcal{V}\mathcal{P}_0}, t_{\mathcal{V}\mathcal{P}_1}$. Also, \mathcal{A} knows the distance $t_{\mathcal{A}\mathcal{V}}$ to \mathcal{V} . We will show how an adversary intercepting the values above can distinguish between the two hypotheses $\mathcal{H}_0, \mathcal{H}_1$ with non-negligible probability.

Lemma 1. *Under Assumptions 1 and 2 we assume that there exists ϵ and a bound B such that:*

$$\mathbb{P}[\text{delay} \leq B] = 1 - \epsilon,$$

where *delay* might represent the delays of the provers $\text{delay}_{\mathcal{P}_0}, \text{delay}_{\mathcal{P}_1}$, or the delay ($\text{delay}_{\mathcal{V}}$) of the verifier as defined in Assumption 1. Then there exists an adversary \mathcal{A} against location indistinguishability which achieves a distinguishing advantage:

$$\text{Adv}_{\mathcal{A}} \geq \left\lceil \frac{t_{\max}}{4B} \right\rceil (1 - 2\epsilon),$$

where t_{\max} is the maximum allowed transmission time between a legitimate prover \mathcal{P} and a verifier \mathcal{V} .

Moreover, this adversary does not need to take part in the actual protocol; the attack relies exclusively on eavesdropping. Assuming that the protocol is complete and polynomially bounded, there is a negligible ϵ such that B exists and is polynomially bounded. So, the advantage $\text{Adv}_{\mathcal{A}}$ is not negligible. Consequently, a distance-bounding protocol as defined in Definition 1 does not provide *location privacy* as per Definition 2.

PROOF. Based on Assumption 1 we have three cases.

Case 1: *The verifier \mathcal{V} starts the distance bounding phase after a reference time t_0 and a random delay (denoted as $\text{delay}_{\mathcal{V}}$), whereas the prover \mathcal{P}_b starts after receiving the first message from the verifier \mathcal{V} and a random delay (denoted as $\text{delay}_{\mathcal{P}_b}$).*

This case is depicted in figure 1 (a). More precisely, we consider that the following events take place:

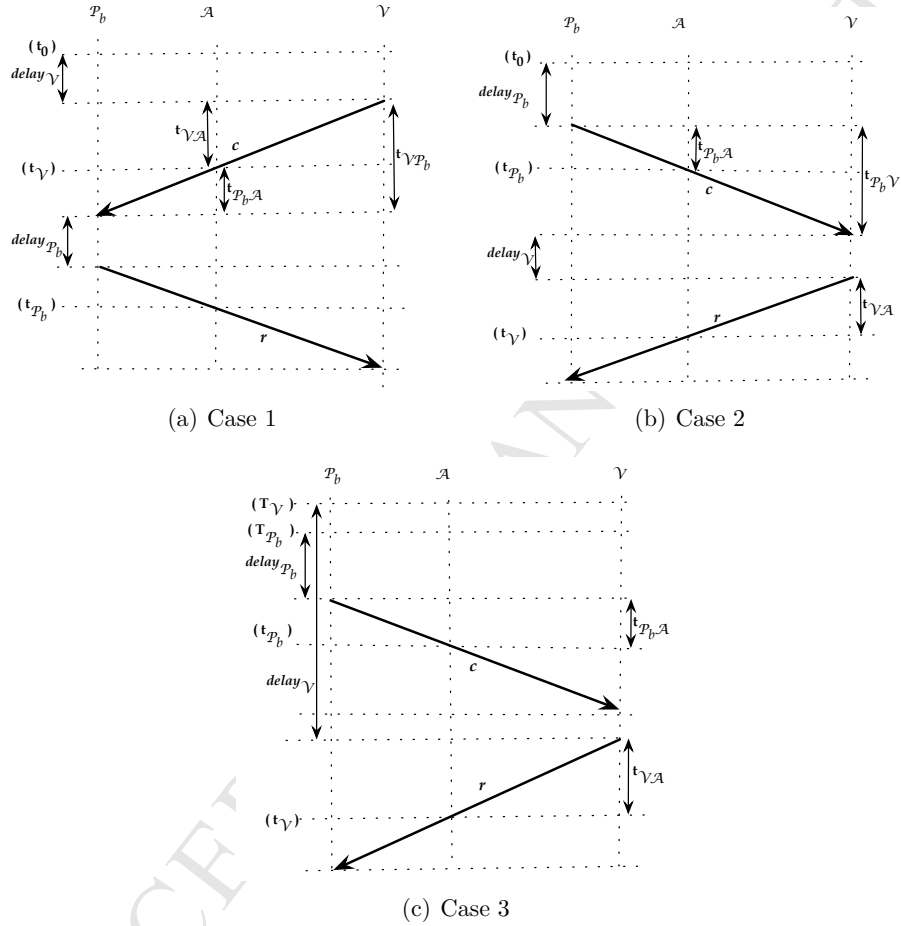


Figure 1: Transmission of messages between the verifier and the prover for the three different cases of the construction of a distance-bounding protocol.

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5 1. After some time reference t_0 and a $delay_{\mathcal{V}}$ the verifier \mathcal{V} sends a message
6 c to the prover \mathcal{P}_b where $b \in \{0, 1\}$. The first bit of this message will
7 arrive at the adversary \mathcal{A} at time $t_{\mathcal{V}}$ such that:
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$$9 \quad t_{\mathcal{V}} = t_0 + delay_{\mathcal{V}} + t_{\mathcal{V}\mathcal{A}}, \quad (1)$$

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11 where $t_{\mathcal{V}\mathcal{A}}$ denotes the time of flight for one bit from the verifier \mathcal{V} to
12 the adversary \mathcal{A} .
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- 15 2. The prover \mathcal{P}_b with $b \in \{0, 1\}$ responds to the verifier \mathcal{V} with a message
16 r , after some delay ($delay_{\mathcal{P}_b}$). The first bit of r arrives at \mathcal{A} at time $t_{\mathcal{P}_b}$
17 such that:
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$$20 \quad t_{\mathcal{P}_b} = t_0 + delay_{\mathcal{V}} + t_{\mathcal{V}\mathcal{P}_b} + delay_{\mathcal{P}_b} + t_{\mathcal{P}_b\mathcal{A}}, \quad (2)$$

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22 where $t_{\mathcal{V}\mathcal{P}_b}$ denotes the time-of-flight for one bit from \mathcal{V} to \mathcal{P}_b , and $t_{\mathcal{P}_b\mathcal{A}}$
23 denotes the time-of-flight for one bit from \mathcal{P}_b to \mathcal{A} .
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26 From equations (1) and (2) it is easy to see that:
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$$28 \quad t_{\mathcal{P}_b} - t_{\mathcal{V}} = t_{\mathcal{V}\mathcal{P}_b} - t_{\mathcal{V}\mathcal{A}} + delay_{\mathcal{P}_b} + t_{\mathcal{P}_b\mathcal{A}}.$$

29
30 We let d_b be the probability density function (pdf) of $delay_{\mathcal{P}_b}$, i.e. we consider
31 the delay to be a random variable distributed according to d_b . If hypothesis
32 \mathcal{H}_0 holds, then $t_{\mathcal{P}} = t_{\mathcal{P}_0}$, while if hypothesis \mathcal{H}_1 holds, then $t_{\mathcal{P}} = t_{\mathcal{P}_1}$. Since $t_{\mathcal{P}}$
33 and $t_{\mathcal{V}}$ depend on random delays, they can be perceived as random variables.
34 Let:
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$$37 \quad T = t_{\mathcal{P}} - t_{\mathcal{V}} - t_{\mathcal{V}\mathcal{P}_0} + t_{\mathcal{V}\mathcal{A}} - t_{\mathcal{P}_0\mathcal{A}} \quad \text{and}$$

$$38 \quad \Delta = t_{\mathcal{V}\mathcal{P}_1} + t_{\mathcal{P}_1\mathcal{A}} - t_{\mathcal{V}\mathcal{P}_0} - t_{\mathcal{P}_0\mathcal{A}}.$$

39
40 Note that whereas the value Δ is fixed and even chosen by the adversary,
41 T is a random variable, depending on the delays. Indeed, if hypothesis
42 \mathcal{H}_0 holds then $T = delay_{\mathcal{P}_0}$ has pdf d_0 , while if hypothesis \mathcal{H}_1 holds, then
43 $T = delay_{\mathcal{P}_1} + \Delta$ and we write $\mathbb{P}[T = t] = d_1(t - \Delta)$, i.e. T has a distribution
44 equivalent to d_1 , shifted by a fixed value Δ .
45
46

47 In the following, we often condition success probabilities on hypotheses
48 \mathcal{H}_0 and \mathcal{H}_1 and use the notation $\mathbb{P}_{\mathcal{H}_b}[\text{event}]$ for $\mathbb{P}[\text{event} \mid \mathcal{H}_b \text{ holds}]$, i.e. the
49 probability that *event* holds, conditioned on the fact that \mathcal{H}_b holds.
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We consider that \mathcal{A} is implementing a best distinguisher based on the likelihood that $\mathbb{P}_{\mathcal{H}_0}[T = t] > \mathbb{P}_{\mathcal{H}_1}[T = t]$ for observed value t . If this holds, then \mathcal{A} outputs 0, else it outputs 1. So \mathcal{A} outputs 0 iff the observed value of $T = t_{\mathcal{P}} - t_{\mathcal{V}} - t_{\mathcal{V}\mathcal{P}_0} + t_{\mathcal{V}\mathcal{A}} - t_{\mathcal{P}_0\mathcal{A}}$ is $T = t$ such that:

$$\mathbb{P}[t = \text{delay}_{\mathcal{P}_0}] > \mathbb{P}[t = \text{delay}_{\mathcal{P}_1} + \Delta].$$

Then, it holds:

$$\begin{aligned} \text{Adv} &= \mathbb{P}_{\mathcal{H}_0}[\mathcal{A} \rightarrow 0] - \mathbb{P}_{\mathcal{H}_1}[\mathcal{A} \rightarrow 0] \\ &= \frac{1}{2} \int_{-\infty}^{+\infty} |d_0(t) - d_1(t - \Delta)| dt, \end{aligned} \quad (3)$$

where d_0 and d_1 make $[0, B]$ have density at least $1 - \epsilon$. When $t_{\mathcal{P}_0\mathcal{V}} = t_{\mathcal{P}_1\mathcal{V}} = t_{\max}$, \mathcal{P}_0 , \mathcal{V} and \mathcal{P}_1 are aligned in this order, and the adversary \mathcal{A} overlaps with the location of \mathcal{P}_0 , then $\Delta = 2t_{\max}$.

Case 2: *The prover \mathcal{P}_b starts the distance-bounding phase after a reference time t_0 and a random delay (denoted as $\text{delay}_{\mathcal{P}_b}$). While the verifier \mathcal{V} starts after receiving the first message from the prover \mathcal{P}_b and a random delay (denoted as $\text{delay}_{\mathcal{V}}$).*

This case is depicted in figure 1 (b). Now, we have:

$$\begin{aligned} t_{\mathcal{P}_b} &= t_0 + \text{delay}_{\mathcal{P}_b} + t_{\mathcal{P}_b\mathcal{A}} \\ t_{\mathcal{V}} &= t_0 + \text{delay}_{\mathcal{P}_b} + t_{\mathcal{P}_b\mathcal{V}} + \text{delay}_{\mathcal{V}} + t_{\mathcal{V}\mathcal{A}} \\ t_{\mathcal{V}} - t_{\mathcal{P}_b} &= t_{\mathcal{P}_b\mathcal{V}} + \text{delay}_{\mathcal{V}} + t_{\mathcal{V}\mathcal{A}} - t_{\mathcal{P}_b\mathcal{A}}. \end{aligned}$$

We let:

$$\begin{aligned} T &= t_{\mathcal{V}} - t_{\mathcal{P}} - t_{\mathcal{P}_0\mathcal{V}} - t_{\mathcal{V}\mathcal{A}} + t_{\mathcal{P}_0\mathcal{A}} \quad \text{and} \\ \Delta &= t_{\mathcal{P}_1\mathcal{V}} - t_{\mathcal{P}_1\mathcal{A}} - t_{\mathcal{P}_0\mathcal{V}} + t_{\mathcal{P}_0\mathcal{A}}. \end{aligned}$$

Similarly, if the adversary \mathcal{A} is implementing a distinguisher for the two provers \mathcal{P}_0 and \mathcal{P}_1 then its advantage is given by:

$$\begin{aligned} \text{Adv} &= \mathbb{P}_{\mathcal{H}_0}[\mathcal{A} \rightarrow 0] - \mathbb{P}_{\mathcal{H}_1}[\mathcal{A} \rightarrow 0] \\ &= \frac{1}{2} \int_{-\infty}^{+\infty} |d(t) - d(t - \Delta)| dt, \end{aligned} \quad (4)$$

where d denotes the pdf of the random variable $\text{delay}_{\mathcal{V}}$, such that $[0, B]$ has density at least $1 - \epsilon$. When $t_{\mathcal{P}_0\mathcal{V}} = t_{\mathcal{P}_1\mathcal{V}} = t_{\max}$, \mathcal{P}_0 , \mathcal{V} and \mathcal{P}_1 are aligned

and the location of the adversary \mathcal{A} overlaps with the location of the prover \mathcal{P}_1 , then $\Delta = 2t_{\max}$. Thus, from equations (3) and (4) we derive that in both cases it holds:

$$\text{Adv} = \frac{1}{2} \int_{-\infty}^{+\infty} |q_0(t) - q_1(t - \Delta)| dt$$

for some functions q_0 and q_1 that make $[0, B]$ have density at least $1 - \epsilon$. We further have a case where $\Delta = 2t_{\max}$. Let:

$$x_{b,i} = \int_{(i-1)|\Delta}^{i|\Delta} q_b(t) dt \quad \text{and} \quad n = \left\lceil \frac{B}{|\Delta|} \right\rceil.$$

We have $x_{b,0} = 0$, $x_{b,n+1} = 0$, $x_{b,i} \geq 0$ and $x_{b,1} + \dots + x_{b,n} \geq 1 - \epsilon$. Given $I \subseteq \{0, \dots, n\}$ we let $T_I = \bigcup_{i \in I} [(i-1)|\Delta, i|\Delta]$. For $\Delta > 0$, we have:

$$\text{Adv}_{T_I, \Delta} = \sum_{i \in I} (x_{0,i} - x_{1,i-1}) \quad \text{and} \quad (5)$$

$$\text{Adv}_{T_I, -\Delta} = \sum_{i \in I} (x_{0,i} - x_{1,i+1}).$$

Let:

$$\text{Adv}_{\Delta} = \max_I \text{Adv}_{T_I, \Delta} = \frac{1}{2} \sum_{i=0}^n |x_{0,i} - x_{1,i-1}|$$

$$\text{Adv}_{-\Delta} = \max_I \text{Adv}_{T_I, -\Delta} = \frac{1}{2} \sum_{i=0}^n |x_{0,i} - x_{1,i+1}|.$$

We have:

$$\begin{aligned} \text{Adv}_{\Delta} + \text{Adv}_{-\Delta} &= \frac{1}{2} \sum_{i=0}^n (|x_{0,i} - x_{1,i-1}| + |x_{0,i} - x_{1,i+1}|) \\ &\geq \frac{1}{2} \sum_{i=0}^n |x_{1,i+1} - x_{1,i-1}|. \end{aligned} \quad (6)$$

Since $x_{1,i} \geq 0$ and $x_{1,1} + \dots + x_{1,n} \geq 1 - \epsilon$, there exists some index j such that: $x_{1,j} \geq \frac{1-\epsilon}{n}$. Thus:

$$\begin{aligned} \text{Adv}_{\Delta} + \text{Adv}_{-\Delta} &\geq \frac{1}{2} (|x_{1,j} - x_{1,j-2}| + |x_{1,j-2} - x_{1,j-4}| + \dots) \\ &\geq \frac{x_{1,j}}{2} \geq \frac{1-\epsilon}{2n}. \end{aligned} \quad (7)$$

Thus,

$$\max(\text{Adv}_\Delta, \text{Adv}_{-\Delta}) \geq \frac{1 - \epsilon}{4n}.$$

So, there exists Δ such that:

$$\text{Adv}_\Delta \geq \left\lceil \frac{|\Delta|}{4B} \right\rceil (1 - \epsilon).$$

For $\Delta = 2t_{\max}$ there exists an adversary \mathcal{A} such that:

$$\text{Adv}_\mathcal{A} \geq \left\lceil \frac{t_{\max}}{2B} \right\rceil (1 - \epsilon).$$

Case 3: *The prover \mathcal{P}_b and the verifier \mathcal{V} send messages independently. More precisely, the prover \mathcal{P}_b starts sending messages after a reference time $T_{\mathcal{P}_b}$ and a random delay ($\text{delay}_{\mathcal{P}_b}$) while the verifier \mathcal{V} starts sending messages after a reference time $T_{\mathcal{V}}$ and a random delay ($\text{delay}_{\mathcal{V}}$). We assume that for this case the adversary \mathcal{A} knows the values $T_{\mathcal{P}_b} - T_{\mathcal{V}}$.*

This case is depicted in Figure 1 (c). We now have:

$$\begin{aligned} t_{\mathcal{V}} &= T_{\mathcal{V}} + \text{delay}_{\mathcal{V}} + t_{\mathcal{V}\mathcal{A}} \\ t_{\mathcal{P}_b} &= T_{\mathcal{P}_b} + \text{delay}_{\mathcal{P}_b} + t_{\mathcal{P}_b\mathcal{A}} \\ t_{\mathcal{P}_b} - t_{\mathcal{V}} &= \text{delay}_{\mathcal{P}_b} - \text{delay}_{\mathcal{V}} + T_{\mathcal{P}_b} + t_{\mathcal{P}_b\mathcal{A}} - T_{\mathcal{V}} - t_{\mathcal{V}\mathcal{A}}. \end{aligned}$$

We let:

$$T = t_{\mathcal{P}} - t_{\mathcal{V}} - T_{\mathcal{P}_1} - t_{\mathcal{P}_1\mathcal{A}} + T_{\mathcal{V}} + t_{\mathcal{V}\mathcal{A}} \text{ and} \quad (8)$$

$$\Delta = T_{\mathcal{P}_1} + t_{\mathcal{P}_1\mathcal{A}} - T_{\mathcal{P}_0} - t_{\mathcal{P}_0\mathcal{A}}. \quad (9)$$

We consider that the adversary \mathcal{A} is implementing a best distinguisher based on the likelihood if $\mathbb{P}_{\mathcal{H}_0}[t_{\mathcal{P}} - t_{\mathcal{V}}] > \mathbb{P}_{\mathcal{H}_1}[t_{\mathcal{P}} - t_{\mathcal{V}}]$ then \mathcal{A} outputs 0; otherwise it outputs 1. So, \mathcal{A} outputs 0 iff $t_{\mathcal{P}} - t_{\mathcal{V}} - T_{\mathcal{P}_1} - t_{\mathcal{P}_1\mathcal{A}} + T_{\mathcal{V}} + t_{\mathcal{V}\mathcal{A}} = T = t$ such that:

$$\mathcal{P}[t = \text{delay}_{\mathcal{P}_0} - \text{delay}_{\mathcal{V}}] > \mathcal{P}[t = \text{delay}_{\mathcal{P}_1} - \text{delay}_{\mathcal{V}} + \Delta].$$

Then, it holds:

$$\begin{aligned} \text{Adv} &= \mathbb{P}_{\mathcal{H}_0}[\mathcal{A} \rightarrow 0] - \mathbb{P}_{\mathcal{H}_1}[\mathcal{A} \rightarrow 0] \\ &= \frac{1}{2} \int_{-\infty}^{+\infty} |q_0(t) - q_1(t - \Delta)| dt, \end{aligned} \quad (10)$$

where q_b for $b \in \{0, 1\}$ denotes the pdf of the random variable $\text{delay}_{\mathcal{P}_b} - \text{delay}_{\mathcal{V}}$ and the support of q_0 and q_1 make $[-B, B]$ have density at least $1 - 2\epsilon$. When $t_{\mathcal{P}_0\mathcal{V}} = t_{\mathcal{P}_1\mathcal{V}} = t_{\max}$, \mathcal{P}_0 , \mathcal{V} and \mathcal{P}_1 are aligned in this order and if $T_{\mathcal{P}_1} \geq T_{\mathcal{P}_0}$ the location of the adversary \mathcal{A} overlaps with the location of \mathcal{P}_0 while if $T_{\mathcal{P}_1} < T_{\mathcal{P}_0}$ the location of the adversary \mathcal{A} overlaps with the location of the prover \mathcal{P}_1 . Thus, in both of these cases it holds that $|\Delta| \geq 2t_{\max}$. Let:

$$x_{b,i} = \int_{(i-1)|\Delta}^{i|\Delta} q_b(t) dt \quad \text{and} \quad n = \left\lceil \frac{B}{|\Delta|} \right\rceil.$$

We have $x_{b,0} = 0$, $x_{b,n+1} = 0$, $x_{b,i} \geq 0$, $x_{b,-n+1} + \dots + x_{b,n} \geq 1 - 2\epsilon$ and:

$$\begin{aligned} \text{Adv}_{\Delta} + \text{Adv}_{-\Delta} &= \frac{1}{2} \sum_{i=-n}^n (|x_{0,i} - x_{1,i-1}| + |x_{0,i} - x_{1,i+1}|) \\ &\geq \frac{1}{2} \sum_{i=0}^{-n} |x_{1,i+1} - x_{1,i-1}|. \end{aligned}$$

Since $x_{1,i} \geq 0$ and $x_{1,-n+1} + \dots + x_{1,n} \geq 1 - 2\epsilon$, there exists some index j such that: $x_{1,j} \geq \frac{1-2\epsilon}{2n}$. Thus:

$$\begin{aligned} \text{Adv}_{\Delta} + \text{Adv}_{-\Delta} &\geq \frac{1}{2} (|x_{1,j} - x_{1,j-2}| + |x_{1,j-2} - x_{1,j-4}| + \dots) \\ &\geq \frac{x_{1,j}}{2} \geq \frac{1-2\epsilon}{4n}. \end{aligned}$$

Thus,

$$\max(\text{Adv}_{\Delta}, \text{Adv}_{-\Delta}) \geq \frac{1-2\epsilon}{8n}.$$

So, there exists Δ such that:

$$\text{Adv} \geq \left\lceil \frac{|\Delta|}{8B} \right\rceil \geq \frac{t_{\max}}{4B} (1-2\epsilon).$$

□

Lemma 2. *If Assumption 1 holds and d_b follows the uniform distribution in the range $[0, B]$ and denotes the pdf of the $\text{delay}_{\mathcal{P}_b}$ while $\text{delay}_{\mathcal{V}}$ is always equal to 0 then the best distinguisher based on $t_{\mathcal{P}} - t_{\mathcal{V}}$ and the locations satisfies:*

$$\text{Adv}_{\mathcal{A}} = \frac{2t_{\max}}{B},$$

where t_{\max} denotes the maximum allowed transmission time between a legitimate prover \mathcal{P} and a verifier \mathcal{V} .

PROOF. Following the proof of the Lemma 1 on page 11 the best distinguisher based on $t_{\mathcal{P}} - t_{\mathcal{V}}$ and the locations (of the provers and the verifier) follows equations (3), (4) or (10). So, it satisfies:

$$\text{Adv} = \frac{1}{2} \int_{-\infty}^{+\infty} |d_0(t) - d_1(-\Delta + t)| dt$$

since $\text{delay}_{\mathcal{V}} = 0$. Since d_b follows the uniform distribution in the range $[0, B]$, it holds:

$$\text{Adv}_{\mathcal{A}} = \frac{1}{2} \int_0^{\Delta} \frac{dt}{B} + \frac{1}{2} \int_B^{B+\Delta} \frac{dt}{B} = \frac{\Delta}{B}$$

and Δ is bounded by $2t_{\max}$ in all three cases.

□

Practical Consequences. Although the attack is polynomial, we can still live with it in practice thanks to the very high celerity of light, since the time it takes to cover 10 m is 2^{-25} sec. Indeed, let:

$$h = \log_2 \frac{B}{2t_{\max}}$$

The best advantage is comparable to guessing h bits correctly. To have a privacy level of h bits (i.e., a best advantage of 2^{-h}), we shall thus have:

$$B \geq 2^{h+1} t_{\max} \quad (11)$$

For instance, when t_{\max} is the time light takes to go through the distance of 10 m and $h = 20$ bits (i.e., an adversary cannot distinguish two provers, accept with one chance out of a million), we have $B \geq 0.07$ sec, which is still a reasonable delay, though not polynomially bounded due to equation (11).

However, note that adding such a delay does not immediately guarantee location privacy against arbitrary attackers. This delay only prevents the generic attack we showed, and can be extended to any passive attacker, but it is not trivial to know whether it also automatically prevents active limited-adversary attacks. This issue is left for future work.

4. Location Private Construction

In this section we apply our results from the previous section to achieve a location private distance-bounding protocol for limited adversaries. The proposed protocol is based on the LPDB protocol [24]. We assume that the verifier \mathcal{V} and the prover \mathcal{P} share a secret key K . As in the LPDB protocol, we have two phases: the *initialisation phase* and the *distance-bounding phase*.

- **Initialisation Phase:** The prover \mathcal{P} generates a random nonce $N_{\mathcal{P}}$ and sends it to the verifier \mathcal{V} . The verifier \mathcal{V} generates a random nonce $N_{\mathcal{V}}$ and sends it to the prover \mathcal{P} . Both the prover and the verifier use as input the concatenation of the nonces $N_{\mathcal{P}}$ and $N_{\mathcal{V}}$ as input to a keyed pseudorandom function (f_K) and divide the output of the PRF into two parts, i.e.:

$$M \parallel R_{\mathcal{P}} \rightarrow f_K(N_{\mathcal{P}} \parallel N_{\mathcal{V}}).$$

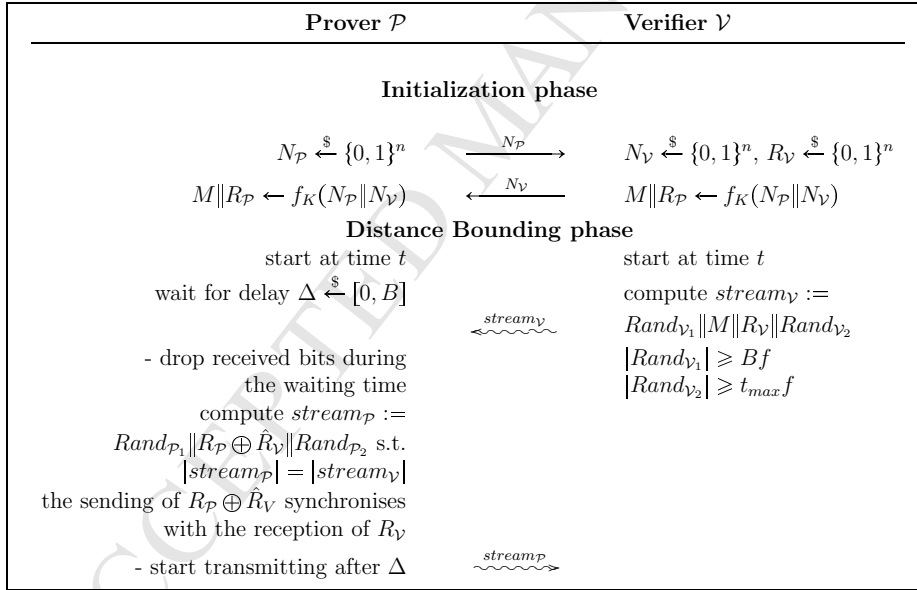


Figure 2: Proposed location-private distance-bounding protocol, secure against limited adversaries. Here $\xleftarrow{\$}$ denotes sampling uniformly at random, \leftarrow denotes a simple message transmission, and \rightsquigarrow denotes a continuous stream transmission at maximal bit rate.

Furthermore, \mathcal{V} generates another random value $R_{\mathcal{V}}$ of length n .

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- **Distance Bounding Phase:** Both the prover \mathcal{P} and the verifier \mathcal{V} start their actions at a commonly agreed time t . More precisely, at time t the verifier \mathcal{V} starts transmitting the stream of bits $stream_{\mathcal{V}}$ such that: $stream_{\mathcal{V}} := Rand_{\mathcal{V}_1} \| M \| R_{\mathcal{V}} \| Rand_{\mathcal{V}_2}$. At time t the prover \mathcal{P} starts waiting for a delay Δ that follows the uniform distribution with range $[0, B]$, where B satisfies the following condition as explained in section 3.2:

$$B \geq 2^{h+1} t_{max}$$

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The prover \mathcal{P} drops any bits received during the waiting time Δ . After this delay, the prover \mathcal{P} starts transmitting the stream of bits $stream_{\mathcal{P}}$ such that:

$$stream_{\mathcal{P}} := Rand_{\mathcal{P}_1} \| R_{\mathcal{P}} \oplus \hat{R}_{\mathcal{V}} \| Rand_{\mathcal{P}_2}$$

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where $\hat{R}_{\mathcal{V}}$ denotes the received value of $R_{\mathcal{V}}$ from the prover \mathcal{P} . The transmission of $R_{\mathcal{P}} \oplus \hat{R}_{\mathcal{V}}$ must start as soon as \mathcal{P} starts receiving the bits of $R_{\mathcal{V}}$.

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We note here that $Rand_{\mathcal{P}_1}$, $Rand_{\mathcal{P}_2}$, $Rand_{\mathcal{V}_1}$, $Rand_{\mathcal{V}_2}$ denote random values generated by the prover \mathcal{P} and the verifier \mathcal{V} respectively. Compared to the LPDB protocol [24], we further require that:

$$|stream_{\mathcal{V}}| = |stream_{\mathcal{P}}| \text{ and } |Rand_{\mathcal{V}_1}| \geq Bf \text{ and } |Rand_{\mathcal{V}_2}| \geq t_{max}f.$$

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The verifier \mathcal{V} could freely select the length of $Rand_{\mathcal{V}_1}$ and $Rand_{\mathcal{V}_2}$ satisfying these inequalities. It is easy to see that it holds:

$$|Rand_{\mathcal{P}_1}| = |Rand_{\mathcal{V}_1}| + |M| + (t_{\mathcal{P}\mathcal{V}} - \Delta)f,$$

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which is positive and

$$|Rand_{\mathcal{P}_2}| = |Rand_{\mathcal{V}_2}| - (t_{\mathcal{P}\mathcal{V}} - \Delta)f$$

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which is also positive.

4.1. Security of the Location Private Construction

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We briefly sketch here the security proof for our new protocol.

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Theorem 1. *For a passive limited adversary, if f is a PRF then:*

$$Adv_{\mathcal{DB}}^{\text{LocPriv}}(\mathcal{A}) \leq 2^{-h} + \text{negl}$$

PROOF. Note that the maximal delay B is exponential in h due to equation (11). For a passive limited adversary \mathcal{A} , f_K can be replaced by a random function, then M and $R_{\mathcal{P}}$ can be assumed to be random. Then, the distribution of the view of the adversary $View_{\mathcal{A}}$ consists of $N_{\mathcal{P}}$, $N_{\mathcal{V}}$, $stream_{\mathcal{V}}$, $stream_{\mathcal{P}}$ and the time of reception of the two streams. The reception times of the first bits are $t_{\mathcal{V}}$ and $t_{\mathcal{P}}$. Since the streams have equal length, all other reception times can be obtained from $t_{\mathcal{V}}$ and $t_{\mathcal{P}}$.

We reduce the `LocPriv` game to a similar one where the PRF f is replaced by a random function. The difference between $\text{Adv}_{DB}^{\text{LocPriv}}(\mathcal{A})$ and the new advantage Adv is negligible, thanks to the PRF property. Clearly, the messages are uniformly distributed.

The protocol belongs to Case 3 of assumption 2. Based on Lemma 5, we have:

$$\text{Adv} \leq \frac{2t_{max}}{B} \leq 2^{-h}.$$

□

We should mention here that the security of the proposed protocol conforms with the bound given in Theorem 2 as already been proven for the LPDB protocol [24].

Theorem 2. *Assuming that f is a PRF, that $R_{\mathcal{V}}$ is uniformly distributed in a set of exponential size, that $R_{\mathcal{P}}$ is in a set of exponential size, the LPDB protocol [24] is a distance bounding protocol which provides resistance to distance fraud, and resistance to mafia fraud.*

5. Conclusions and Discussion

In this paper, we investigate the problem of location privacy in distance-bounding protocols. More precisely, we define a security game for location privacy in distance-bounding protocols and an adversarial model, composed of two classes of adversaries, an omniscient and a limited adversary. We prove that location privacy is information-theoretically impossible for any adversary of the two classes. In particular, a generic passive adversary can break the location privacy of any polynomial-time protocol. Nevertheless, we show that for limited adversaries, carefully chosen parameters enable computational, provable location privacy in practice. For those parameters we

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5 propose a location private distance-bounding protocol based on the LPDB
6 distance-bounding protocol [24].

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8 We prove our results with respect to our game-based notion of location
9 privacy, in which the communication between provers and verifiers takes place
10 across a channel equipped with a timer. Adversaries may run man-in-the-
11 middle attacks. They know their distance to the verifier, but not necessarily
12 their distance to the prover. However, for each message of the protocol, the
13 adversary learns the arrival time of the message, in a bitwise fashion. The
14 goal of the adversary is to distinguish between two possible provers, which
15 are within the proximity (associated with a bound t_{\max}) of the verifier.
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18 In our model, we make two related, but distinct assumptions. The *first*
19 is that the adversary is able to learn the (exact) time of arrival of mes-
20 sages at its interface. This is a reasonable assumption considering that in
21 distance-bounding scenarios, the verifier has a clock that allows it to pre-
22 cisely measure the roundtrip transmission time (with a good granularity).
23 In fact [29] describes an implementation of distance bounding, wherein the
24 verifier pinpoints the location of a prover with a maximal distance error of
25 15 cm. An adversary has at least as much granularity in measuring the time
26 of arrival as the verifier. Note that the more precise the adversary's clock is,
27 the finer it can distinguish between two very close provers.
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30 Our *second* assumption is that the transmission speed is constant and
31 transmissions are (practically) collision-free. We equate transmission
32 times with physical distances and assume that all bits sent by one party
33 arrive at the others. Indeed, it is not unrealistic to model our attack in
34 this way; an adversary can use the bits it *does* receive to correct any de-
35 lays or errors. Once again, a reliable transmission only translates in a more
36 fine-grained distinction for the adversary. The quality of the signal and the
37 reliability of the channel depends on the hardware on which the protocol
38 is deployed. Since most classical NFC and RFID hardware support reliable
39 light speed transmission and run at very close proximity, our assumption
40 accurately covers these scenarios.
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43 The *omniscient* adversary model is very strong. We assume that the
44 adversary may in fact represent a collusion of attackers, which can in fact
45 triangulate signals. It is realistic to assume that such adversaries exist (e.g.
46 governmental agencies and law enforcement institutions). Wireless transmis-
47 sions are particularly vulnerable to triangulation. In this sense, our impos-
48 sibility results state that one cannot stay off the radar and at the same time
49 benefit from services requiring transmissions. However, it is still reassuring to
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5 know that adding a large delay may at least prevent curious *limited* attackers
6 from learning the sender's location.

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8 Finally, we briefly comment on intermediate adversarial models. As men-
9 tioned in Section 2.2, an *omniscient* adversary can be realized either by a
10 collusion of adversaries or by a single one who is able to move. Whereas it
11 could make sense to consider intermediate adversary strengths, our results
12 point out that location privacy is impossible to achieve in polynomial time
13 even in the presence of the weakest adversaries we can define, i.e. *limited*
14 ones.
15

16 17 18 **Acknowledgment**

19
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25

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