# Formal Methods for Software Development

**Verification with Spin** 

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#### **Spin: Previous Lecture vs. This Lecture**

**Previous lecture** 

SPIN appeared as a PROMELA simulator

This lecture

Intro to SPIN as a model checker

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⇒ Finding no counter example proves stated correctness properties.

exhaustive search

=

resolving non-determinism in all possible ways

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two kinds of non-determinism to be resolved:

explicit, local: if/do statements

:: guardX -> ...

:: guardY -> ...

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For model checking Promela code,

two kinds of non-determinism to be resolved:

explicit, local: if/do statements

```
:: guardX -> ...
:: guardY -> ...
```

implicit, global: scheduling of concurrent processes (see next lecture)

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- generating a verifier

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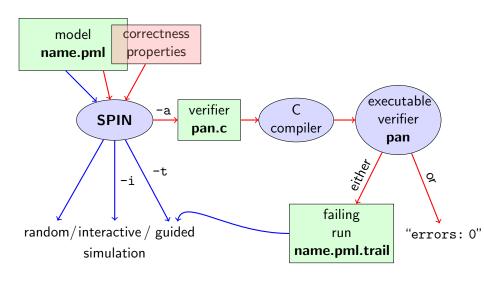
Main functionality of Spin:

- simulating a model (randomly/interactively/guided)
- generating a verifier

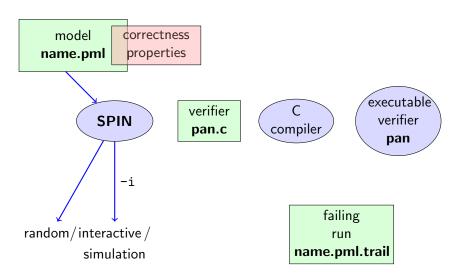
Verifier generated by SPIN is a C program performing model checking:

- exhaustively checks PROMELA model against correctness properties
- ▶ in case the check is negative: generates a failing run of the model, to be simulated by SPIN

## **SPIN Workflow: Overview**



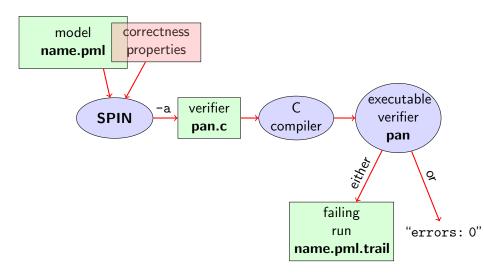
## **Plain Simulation with SPIN**

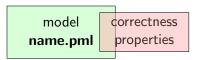


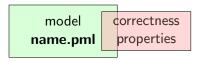
### Rehearsal: Simulation Demo

run example, random and interactive zero.pml

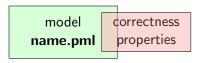
# Model Checking with Spin







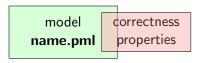
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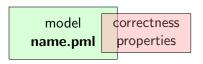
assertion statements



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### stating properties within model, using

- assertion statements
- meta labels
  - end labels
  - accept labels
  - progress labels



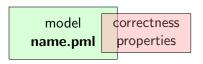
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- never claims
- ► temporal logic formulas



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- meta labels
  - end labels (today)
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### **Definition (Assertion Statements)**

were *expr* is any Prometa expression.

Assertion statements in Prometa are statements of the form assert(expr)

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stmt2;
...
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```
...
stmt1;
assert(max == a);
stmt2;
...
if
:: b1 -> stmt3;
assert(x < y)
:: b2 -> stmt4
```

# Meaning of **Boolean** Assertion Statements

#### assert(expr)

- ▶ has no effect if *expr* evaluates to true
- ▶ triggers an error message if *expr* evaluates to false

This holds in both, simulation and model checking mode.

## Meaning of General Assertion Statements

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This holds in both, simulation and model checking mode.

#### Recall:

bool true false is syntactic sugar for bit 1 0

 $\Rightarrow$  general case covers Boolean case

## Instead of using 'printf's for Debugging ...

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#### **Command Line Execution**

```
(simulate, inject fault, simulate again)
```

> spin [-i] max.pml

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```
/* after choosing a,b from {1,2,3} */
if
    :: a >= b -> max = a
    :: a <= b -> max = b
fi;
assert( max == (a>b -> a : b) )
```

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Now, we have a first example with a formulated correctness property.

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We can do model checking, for the first time!

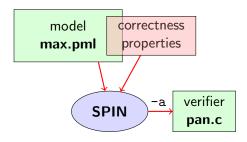
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We can do model checking, for the first time!

(Historic moment in the course.)

#### Generate Verifier in C



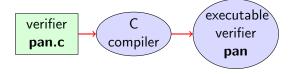
#### **Command Line Execution**

Generate Verifier in C

> spin -a max2.pml

SPIN generates Verifier in C, called pan.c (plus helper files)

## **Compile To Executable Verifier**

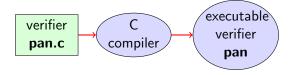


#### **Command Line Execution**

compile to executable verifier

> qcc -o pan pan.c

## **Compile To Executable Verifier**



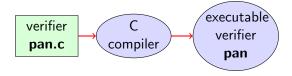
#### **Command Line Execution**

compile to executable verifier

> gcc -o pan pan.c

C compiler generates executable verifier pan

# **Compile To Executable Verifier**



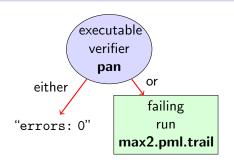
#### **Command Line Execution**

compile to executable verifier

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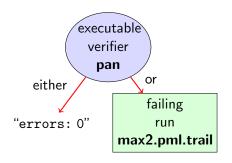
C compiler generates executable verifier pan

pan: historically "protocol analyzer", now "process analyzer"



#### **Command Line Execution**

$$>$$
 ./ $pan$  or  $>$   $pan$ 

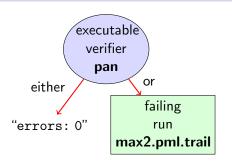


#### **Command Line Execution**

run verifier pan

$$>$$
 ./pan or  $>$  pan

▶ prints "errors: 0"

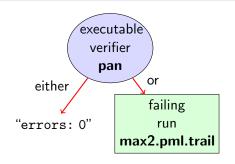


```
Command Line Execution run verifier pan
```

> ./pan or > pan

▶ prints "errors: 0" ⇒ Correctness Property verified!

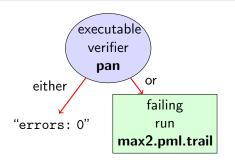
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#### **Command Line Execution**

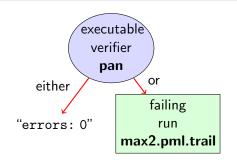
```
> ./pan or > pan
```

- prints "errors: 0", or
- $\triangleright$  prints "errors: n" (n > 0)



#### **Command Line Execution**

- > ./pan or > pan
  - prints "errors: 0", or
  - ▶ prints "errors: n" (n > 0)  $\Rightarrow$  counter example found!

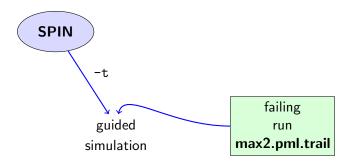


#### **Command Line Execution**

- > ./pan or > pan
  - prints "errors: 0", or
  - ▶ prints "errors: n" (n > 0)  $\Rightarrow$  counter example found! records failing run in max2.pml.trail

#### **Guided Simulation**

To examine failing run: employ simulation mode, "guided" by trail file.



#### **Command Line Execution**

inject a fault, re-run verification, and then:

$$> spin - t - p - l max2.pml$$

can look like:

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assignments in the run

can look like:

assignments in the run values of variables whenever updated

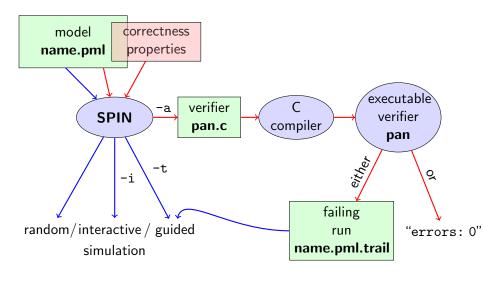
can look like:

assignments in the run values of variables whenever updated

(If output doesn't mention max variable, re-verify with ./pan -E)

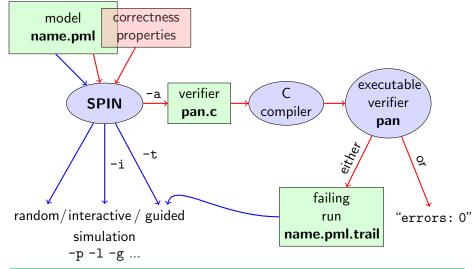
#### What did we do so far?

following whole cycle (most primitive example, assertions only)



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```
int dividend = 15;
int divisor = 4:
int quotient, remainder;
quotient = 0;
remainder = dividend;
do
  :: remainder > divisor ->
     quotient++;
     remainder = remainder - divisor
  :: else ->
     break
od;
printf("%d_divided_by_d%d_=d_d,d_remainder_=d_kd), remainder_d=d_kd
       dividend, divisor, quotient, remainder)
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       break
  od;
  printf("%d_divided_by_d%d_=d_d,d_remainder_=d_kd), remainder_d=d_kd
          dividend, divisor, quotient, remainder)
simulate, add assertion, ...
```

## Further Examples: Greatest Common Divisor

greatest common divisor of x and y

```
int a, b;
a = x; b = y;
do
    :: a > b -> a = a - b
    :: b > a -> b = b - a
    :: a == b -> break
od;
printf("The_GCD_of_%d_and_%d_=_%d\n", x, y, a)
```

greatest common divisor of x and y

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full functional specification w. assertion not possible (why?)

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   a = x; b = y;
   do
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      :: b > a -> b = b - a
      :: a == b -> break
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```

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greatest common divisor of x and y
   int a, b;
  a = x; b = y;
  do
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  od:
   printf("The_{\sqcup}GCD_{\sqcup}of_{\sqcup}%d_{\sqcup}and_{\sqcup}%d_{\sqcup}=_{\sqcup}%d\backslash n", x, v. a)
full functional specification w. assertion not possible (why?)
still, assertions can perform sanity check
⇒ typical for model checking
```

typical command line sequences:

random simulation

spin name.pml

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random simulation

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interactive simulation

spin -i name.pml

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typical command line sequences:
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#### random simulation

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#### model checking

spin -a name.pml
gcc -o pan pan.c
./pan

```
typical command line sequences:
```

# random simulation spin name.pml interactive simulation spin -i name.pml

#### model checking

```
spin -a name.pml
gcc -o pan pan.c
./pan
and in case of error
spin -t -p -l -g name.pml
```

#### **Spin Reference Card**

#### Ben-Ari produced Spin Reference Card, summarizing

- typical command line sequences
- options for
  - ► Spin
  - gcc
  - pan
- ► Promela
  - datatypes
  - operators
  - statements
  - guarded commands
  - processes
  - channels
- temporal logic syntax

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- temporal logic syntax
- ⇒ available from course page (see 'Links, Papers, and Software')

# Why Spin?

- ➤ SPIN targets software, instead of hardware verification ("Formal Methods for *Software* Development")
- ▶ 2001 ACM Software Systems Award (other winning systems include: Unix, TCP/IP, WWW, Tcl/Tk, Java, GCC, TEX, Coq)
- used for safety critical applications
- distributed freely as research tool, well-documented, actively maintained, large user-base in academia and in industry
- ▶ annual Spin user workshops series held since 1995
- lacktriangle based on standard theory of  $(\omega ext{--})$ automata and linear temporal logic

# Why Spin? (Cont'd)

- ▶ PROMELA and SPIN are rather simple to use
- good to understand a few systems really well, rather than many systems poorly
- availability of good course book (Ben-Ari)
- availability of front end JSPIN (also Ben-Ari)

# Why Spin? (Cont'd)

- ▶ PROMELA and SPIN are rather simple to use
- good to understand a few systems really well, rather than many systems poorly
- availability of good course book (Ben-Ari)
- availability of front end JSPIN (also Ben-Ari)
- and: availability of our own web interface

### What is JSPIN?

- ▶ graphical user interface for SPIN
- developed for pedagogical purposes
- written in JAVA
- simple user interface
- ► Spin options automatically supplied
- fully configurable
- supports graphics output of transition system

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- supports graphics output of transition system
- makes back-end calls transparent

### $\operatorname{JSPIN}$ Demo

#### **Command Line Execution**

calling JSPIN

> java -jar /usr/local/jSpin/jSpin.jar
(with path adjusted to your setting)

or use shell script:

> jspin

#### **Command Line Execution**

```
calling JSPIN
```

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play around with similar examples ...

Given Promela model M, and correctness properties  $C_1, \ldots, C_n$ .

 $\triangleright$  Be  $R_M$  the set of all possible runs of M.

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- ▶ *M* is correct wrt.  $C_1, \ldots, C_n$  iff  $R_M \subseteq (R_{M,C_1} \cap \ldots \cap R_{M,C_n})$ .
- ▶ If M is not correct wrt.  $C_1, \ldots, C_n$ , then each  $r \in (R_M \setminus (R_{M,C_1} \cap \ldots \cap R_{M,C_n}))$  is a counter example.

quoting from file max3.pml:

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generate and execute pan

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Note: no assert in max3.pml.

```
Further inspection of pan output:
...
pan: invalid end state (at depth 1)
pan: wrote max3.pml.trail
```

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In max3.pml, there exists a blocking run where no process can take over.

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(Fix error)

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#### **Definition (End Location)**

End locations of a process P are:

P's textual end

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Can get SPIN to ignore 'invalid end state' error: ./pan -E

#### Literature for this Lecture

Ben-Ari Chapter 2, Sections 4.7.1, 4.7.2