

# Formal Methods for Software Development

## Introduction

Wolfgang Ahrendt

Department of Computer Science and Engineering  
Chalmers University of Technology  
and  
University of Gothenburg

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## Teachers

- ▶ Wolfgang Ahrendt (WA)    **examiner, lecturer**
- ▶ Oskar Abrahamsson (OA)    **teaching assistant**
- ▶ Andreas Lööv (AL)    **teaching assistant**

course assistant activities include:

- ▶ giving exercise classes
- ▶ correcting lab hand-ins
- ▶ student support via:
  - ▶ e-mail
  - ▶ meetings on e-mail request
    - ▶ Oskar, room 5453
    - ▶ Andreas, room 5461

## Course Home Page

On Canvas, via Chalmers and GU.

Also used for online news and discussions.

# Course Structure

## Course Structure

Topic	# Lectures	# Exercises	Lab
Intro	1	✗	✗
Modeling & Model Checking with <i>PROMELA &amp; SPIN</i>	6	3	✓
Specification & Verification with <i>JML &amp; KeY</i>	6 (+1?)	3	✓

*PROMELA & SPIN* abstract programs, model checking, automated

*JML & KeY* concrete Java, deductive verification, semi-automated

... more on this later!

## Lectures

- ▶ Please ask questions during lectures
- ▶ Please respond to my questions; 'wrong' answers highly welcome
- ▶ Slides appear online shortly *after* each lecture

## Exercises

- ▶ One exercise web page (almost) each week (6 in total)
- ▶ Discussed in next exercise class
- ▶ Play around with the exercises before coming to the class
- ▶ Exercises **highly** recommended
- ▶ Bring laptops if you have  
(ideally w. installed tools or browser interfaces working)

# Passing Criteria

- ▶ Oral examination in exam week
- ▶ Two lab hand-ins
- ▶ (No written end-exam)
- ▶ Oral exam and labs can be passed separately

# Oral Exam

- ▶ individual, oral examination
- ▶ 30 min per student
- ▶ slots between 28 October and 1 November
- ▶ see course page for more information



## Labs

- ▶ 2 Lab handins: PROMELA/SPIN 04 Oct, JML/KeY 28 Oct
  - ▶ 2 Lab Questions Sessions
  - ▶ Submission via **Fire**, linked from course home page
  - ▶ If submission is returned, roughly one week for correction
  - ▶ You work in groups of **two**. No exception!<sup>a</sup>  
You pair up by either:
    1. talk to people
    2. post request via Canvas
    3. participate in pairing at first exercise session
- In case all that is **not** sufficient, contact Oskar by e-mail.

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<sup>a</sup>Only PhD students have to work alone.

- ▶ Canvas
- ▶ Web Pages (linked from Canvas)
- ▶ Fire System (for lab submissions)

(inspect course schedule)

# Course Evaluation

1. course evaluation group:
  - ▶ student representatives
    - ▶ randomly selected (Chalmers)
    - ▶ volunteers (GU)
  - ▶ one meeting during the course, one after
2. web questionnaire after the course

Randomly selected Chalmers students:

- ▶ Anna Brunzell
- ▶ David Hagerman Olzon
- ▶ Gabriel Lindeby
- ▶ Ramkumar Venkatesh
- ▶ Yonca Yunatci

GU students: please consider volunteering

- ▶ In part I, we partly use:

**Ben-Ari** Mordechai Ben-Ari

*Principles of the Spin Model Checker*

Springer, 2008

*Ben-Ari received ACM award for outstanding contributions to CS education. Recommended by G. Holzmann. Excellent student text book.*

(E-book at [link.springer.com](http://link.springer.com))

- ▶ Relevant for part II:

**KeYbook** W. Ahrendt, B. Beckert, R. Bubel, R. Hähnle, P. Schmitt, M. Ulbrich, editors.

*Deductive Software Verification - The KeY Book*

Vol 10001 of *LNCS*, Springer, 2016

(E-book at [link.springer.com](http://link.springer.com))

# Additional Literature

**Holzmann** Gerard J. Holzmann  
**The Spin Model Checker**  
Addison Wesley, 2004

**BayerKatoen** Christel Baier, Joost-Pieter Katoen  
**Principles of Model Checking**  
MIT Press, 2008

# Connection to other Courses

## Prerequisites

- ▶ Skills in first-order logic and temporal logic, e.g., from
  - ▶ Logic in Computer Science, or
  - ▶ Discrete Event Systems
- ▶ Skills in object-oriented programming (like Java)

## Related courses (not assumed!)

- ▶ Concurrent Programming
- ▶ Finite Automata
- ▶ Testing, Debugging, and Verification

if you took any of those: nice

if not: don't worry, we introduce everything we use here

# Motivation:

## Software Defects cause BIG Failures

Tiny faults in technical systems can have catastrophic consequences

### In particular, this goes for software systems

- ▶ Ariane 5
- ▶ Mars Climate Orbiter
- ▶ London Ambulance Dispatch System
- ▶ NEDAP Voting Computer Attack
- ▶ ...

# Motivation:

## Software Defects cause OMNIPRESENT Failures

Ubiquitous Computing results in Ubiquitous Failures

### Software is almost everywhere:

- ▶ Mobiles
- ▶ Clouds
- ▶ Smart cards
- ▶ Smart devices
- ▶ Cars
- ▶ Blockchains
- ▶ ...

software/specification quality is a growing commercial and legal issue



# Achieving Reliability in Engineering

## Well-known strategies from mechanical and civil engineering

- ▶ Precise calculations (or accurate estimations) of forces, stress, etc.
- ▶ Redundancy (“make it a bit stronger than necessary”)
- ▶ Robust design (single fault not catastrophic)
- ▶ Clear separation of subsystems
- ▶ Design follows patterns that are proven to work

# Why is this So Difficult for Software?

- ▶ Software systems compute **non-continuous** functions.  
Single bit-flip may change behaviour completely.
- ▶ Redundancy as replication does not help against **bugs**.  
Redundant SW development only viable in special cases.
- ▶ Insufficient **separation** of subsystems.  
Seemingly correct sub-systems may together behave incorrectly.
- ▶ Software designs have very high logical **complexity**.
- ▶ Most SW engineers **untrained** to address correctness.
- ▶ Cost efficiency favoured over reliability.
- ▶ Design practise for reliable software in **immature** state  
for complex (e.g., distributed) systems.

# How to Ensure Software Correctness/Compliance?

A central strategy: [testing](#)

(others: SW processes, reviews, libraries, ...)

## Testing against internal SW errors (“bugs”)

- ▶ find (hopefully) representative test configurations
- ▶ check intentional system behaviour on those

## Testing against external faults

- ▶ inject faults (memory, communication) by simulation or radiation
- ▶ trace fault propagation

# Limitations of Testing

- ▶ Testing shows presence of errors, not their absence  
(exhaustive testing viable only for trivial systems)
- ▶ Representativeness of test cases/injected faults subjective  
How to test for the unexpected? Rare cases?
- ▶ Testing is labour intensive, hence expensive

# What **are** Formal Methods

- ▶ Rigorous methods for system design/development/analysis
- ▶ Mathematics and symbolic logic  $\Rightarrow$  **formal**
- ▶ Increase confidence in a system
- ▶ Two aspects:
  - ▶ System **requirements**
  - ▶ System **implementation**
- ▶ Formalise both
- ▶ Use **tools** for
  - ▶ **exhaustive** search for failing scenario, or
  - ▶ mechanical **proof** that implementation satisfies requirements

# What are Formal Methods **for**

- ▶ Complement other analysis and design methods
- ▶ Increase confidence in system correctness
- ▶ Good at finding bugs  
(in code **and** specification)
- ▶ **Ensure** certain properties of the system (model)
- ▶ Should ideally be as automated as possible

and

- ▶ **Training in Formal Methods increases high quality development skills**

# Specification — What a System **Should** Do

- ▶ Simple properties
  - ▶ Safety properties  
Something bad will never happen (e.g., green light mutual exclusion)
  - ▶ Liveness properties  
Something good will happen eventually
- ▶ General properties of concurrent/distributed systems
  - ▶ deadlock-free, no starvation, fairness, ...
- ▶ Non-functional properties
  - ▶ Execution time, memory, usability, ...
- ▶ Full behavioural specification
  - ▶ Code functionality described by **contracts**
  - ▶ Data consistency, system **invariants**  
(in particular for efficient, i.e., redundant, data representations)
  - ▶ Modularity, encapsulation
  - ▶ Refinement relation

# The Main Point of Formal Methods is **Not**

- ▶ to show correctness of entire systems
- ▶ to replace testing
- ▶ to replace good design practises

There is no silver bullet!

- ▶ No correct system w/o clear requirements & good design



# But ...

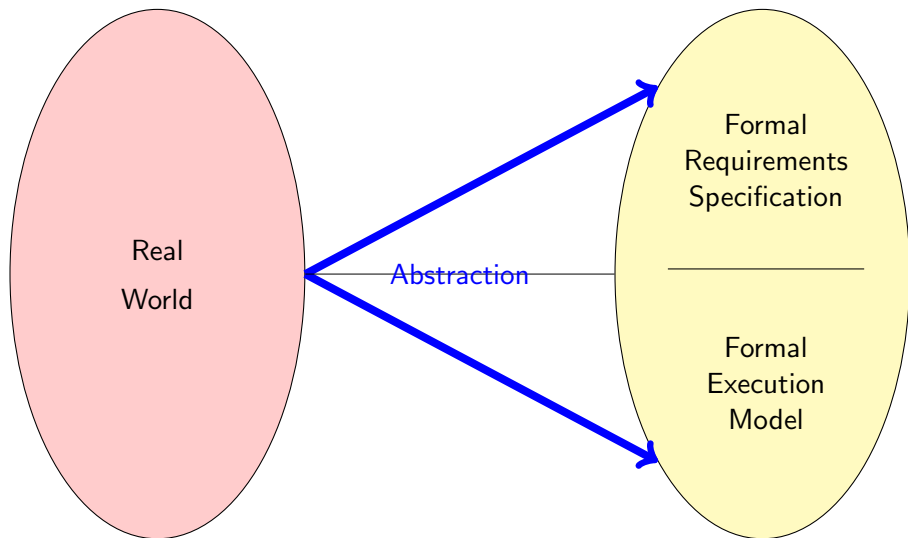
- ▶ Formal proof can replace (infinitely) many test cases
- ▶ Formal methods improve the quality of specs (even without formal verification)
- ▶ Formal methods **guarantee** specific properties of system (model)

# A Fundamental Fact

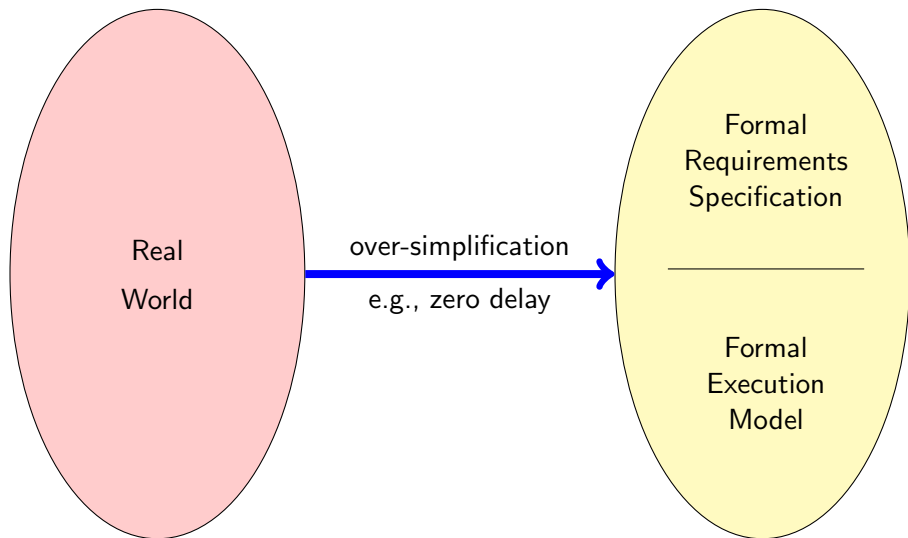
Formalisation of system requirements is hard

Let's see why ...

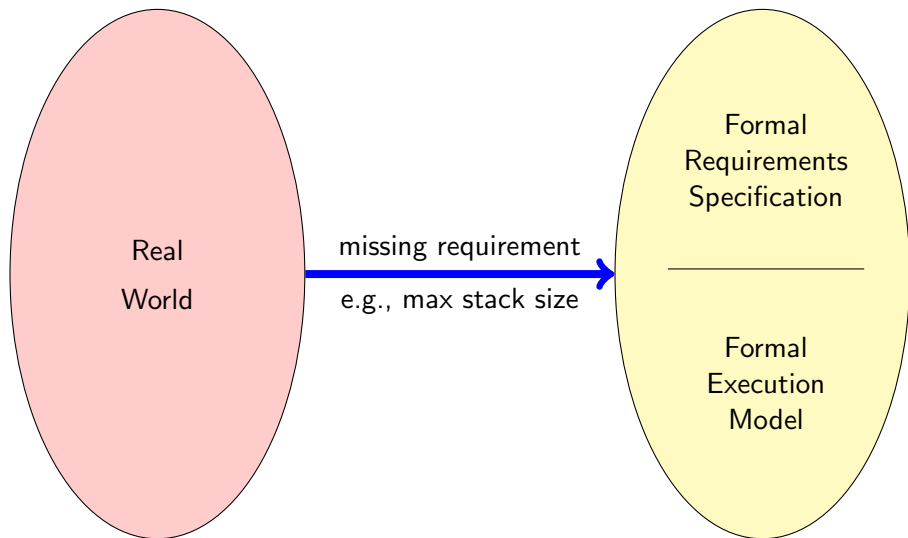
# Difficulties in Creating Formal Models



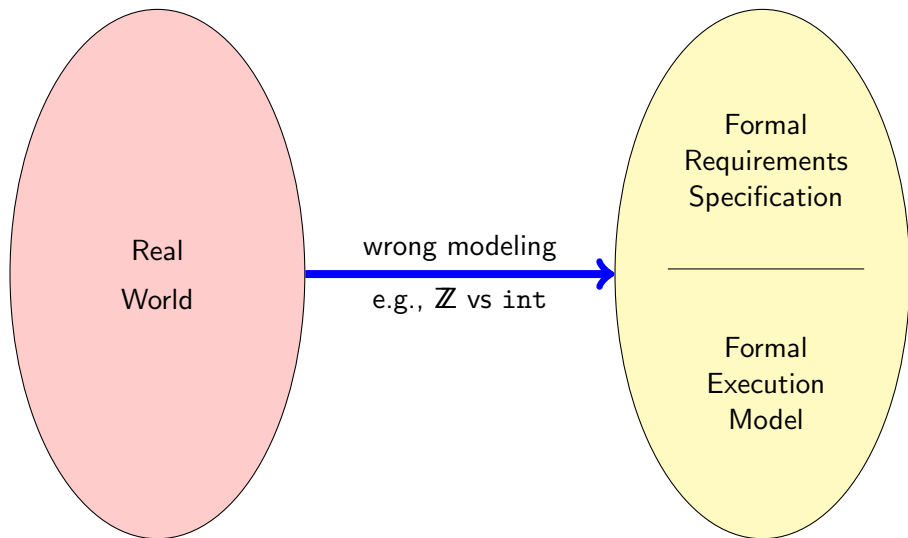
# Difficulties in Creating Formal Models



# Difficulties in Creating Formal Models



# Difficulties in Creating Formal Models



# Formalization Helps to Find Bugs in Specs

Errors in specifications are as common as errors in code, but their discovery gives deep insights in (mis)conceptions of the system.

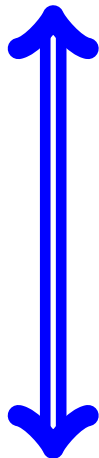
- ▶ Wellformedness and consistency of formal specs partly machine-checkable
- ▶ Declared signature (symbols) helps to spot incomplete specs
- ▶ Failed verification of implementation against spec gives feedback on erroneous formalization

# Another Fundamental Fact

Proving properties of systems can be hard



# Level of System (Implementation) Description



- ▶ **Abstract level**

- ▶ Finitely many states (bounded size datatypes)
- ▶ Simplification, unfaithful modeling inevitable
- ▶ Automated proofs are (in principle) possible

- ▶ **Concrete level**

- ▶ Unbounded size datatypes  
(pointer chains, dynamic containers, streams)
- ▶ Complex datatypes and control structures
- ▶ Realistic programming model (e.g., Java)
- ▶ Automated proofs hard or impossible!

# Expressiveness of Specification



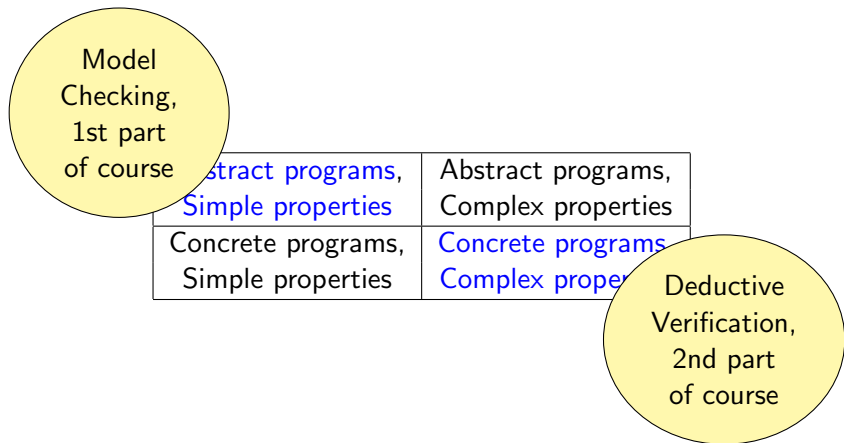
## ▶ Simple

- ▶ Simple or general properties
- ▶ Finitely many case distinctions
- ▶ Approximation, low precision
- ▶ Automated proofs are (in principle) possible

## ▶ Complex

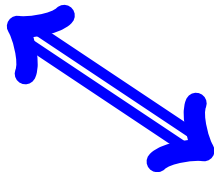
- ▶ Full behavioural specification
- ▶ Quantification over infinite or large domains
- ▶ High precision, tight modeling
- ▶ Automated proofs hard or impossible!

# Main Approaches



# Proof Automation

- ▶ “Automated” Proof  
 (“batch-mode”)
  - ▶ No interaction (or lemmas) necessary
  - ▶ Tuning of tool parameters necessary
  - ▶ Formal specification still “by hand”
  
- ▶ “Semi-Automated” Proof  
 (“interactive”)
  - ▶ Interaction (or lemmas) may be required
  - ▶ Need certain knowledge of tool internals  
Intermediate inspection can help
  - ▶ User steps are checked by tool



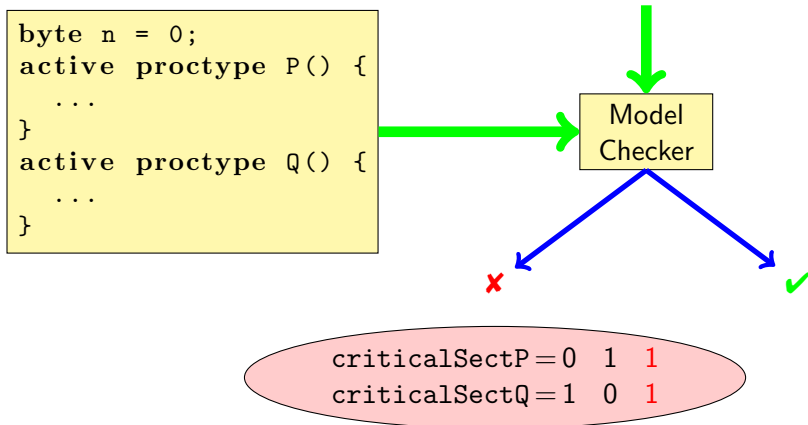
# Model Checking with SPIN

## System Model

```
byte n = 0;  
active proctype P() {  
  ...  
}  
active proctype Q() {  
  ...  
}
```

## System Property

`[]!(criticalSectP && criticalSectQ)`



# Model Checking in Industry—Examples

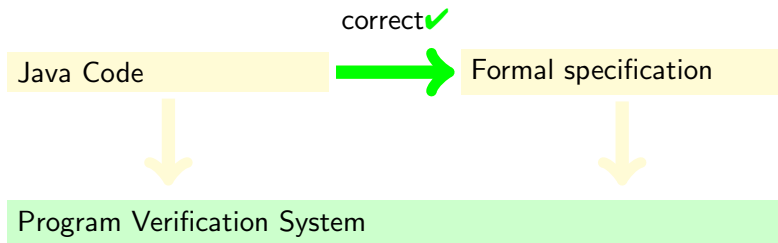
- ▶ Hardware verification
  - ▶ Good match between limitations of methods and application
  - ▶ Intel, Motorola, AMD, . . .
- ▶ Software verification
  - ▶ Specialized software: control systems, protocols
  - ▶ Typically no direct checking of executable system, but of abstractions
  - ▶ Bell Labs, Microsoft

# A Major Case Study with SPIN

## Checking feature interaction for telephone call processing software

- ▶ Software for PathStar<sup>©</sup> server from Lucent Technologies
- ▶ Automated abstraction of unchanged C code into PROMELA
- ▶ Web interface, with SPIN as back-end, to:
  - ▶ determine properties (ca. 20 temporal formulas)
  - ▶ invoke verification runs
  - ▶ report error traces
- ▶ Finds error trace, reported as C execution trace
- ▶ Work farmed out to 16 computers, daily, overnight runs
- ▶ 18 months, 300 versions of system model, 75 bugs found
- ▶ Strength: detection of undesired feature interactions (difficult with traditional testing)
- ▶ Main challenge: defining meaningful properties

# Deductive Verification with KeY



Proof rules establish relation “implementation conforms to specs”



# Deductive Verification in Industry—Examples

- ▶ Hardware verification
  - ▶ For complex systems, mostly floating-point processors
  - ▶ Intel, Motorola, AMD, ...
- ▶ Software verification
  - ▶ Safety critical systems:
    - ▶ Paris driver-less metro (Meteor)
    - ▶ Emergency closing system in North Sea
  - ▶ Libraries
  - ▶ Implementations of Protocols

## Java Card 2.2.1 API Reference Implementation

- ▶ Reference implementation and full functional specification
- ▶ All Java Card 2.2.1 API classes and methods
  - ▶ 60 classes; ca. 5,000 LoC (250kB) source code
  - ▶ specification ca. 10,000 LoC
- ▶ Conformant to implementation on actual smart cards
- ▶ All methods fully verified against their spec
  - ▶ 293 proofs; 5–85,000 nodes
- ▶ Total effort several person months
- ▶ Most proofs fully automatic
- ▶ Main challenge: [getting specs right](#)

# Major Case Studies with KeY: Timsort

## Timsort

Hybrid sorting algorithm (insertion sort + merge sort) optimized for partially sorted arrays (typical for real-world data).

## Facts

- ▶ Designed by Tim Peters (for Python)
- ▶ Since Java 1.7 default algorithm for non-primitive arrays/collections

## Timsort is used in

- ▶ Java (standard libraries OpenJDK, Oracle)
- ▶ Python (standard library), used by Google
- ▶ Android (standard library), used by Google
- ▶ ... and many more languages / frameworks!

# Timsort: People



- ▶ Tim Peters
- ▶ Sorting Algorithm Designer
- ▶ Python Guru



- ▶ Stijn de Gouw
- ▶ Assistant Professor
- ▶ Formerly postman in the NL
- ▶ Interested in sorting for professional reasons

# Timsort: People

The screenshot shows a WhatsApp chat interface. At the top left is a profile card for Stijn de Gouw, marked as 'Away'. On the right are icons for video call, voice call, and a group of people. The chat history shows a message from Stijn: "are you ready for the meeting?" dated 20 Oct 2014. A reply from Richard says: "Hi Stijn, yes, I have time until 14:00 (or a bit longer)" at 13:35. Stijn replies: "ok great" at 13:35, followed by "I've been working a bit on timsort (though less than I intended to do)". A date separator for 27 Oct 2014 is shown. Richard's message starts with "morning richard" at 08:52, followed by a long message: "don't want to keep this from you, but please keep it to yourself for now... as you know I was working on proving correctness of timsort (the soring algorithm used in the jdk) I figured that the jdk was probably pretty thoroughly tested so went right ahead with specifying rather than debugging the algorithm ... but I actually discovered a bug 😊". The phrase "but I actually discovered a bug" is highlighted with a red box. A reply from Stijn says "Cool 😊" at 09:07, followed by "Good morning!".

Stijn de Gouw  
Away

are you ready for the meeting? 20 Oct 2014

Hi Stijn, yes, I have time until 14:00 (or a bit longer) 13:35

ok great 13:35

I've been working a bit on timsort (though less than I intended to do)

27 Oct 2014

morning richard 08:52

don't want to keep this from you, but please keep it to yourself for now... as you know I was working on proving correctness of timsort (the soring algorithm used in the jdk)

I figured that the jdk was probably pretty thoroughly tested so went right ahead with specifying rather than debugging the algorithm ... but I actually discovered a bug 😊

Cool 😊 09:07

Good morning!

professional reasons

# Major Case Studies with KeY

## Found Bug in Java Libraries' main Sorting Method using KeY

- ▶ `java.util.Collections.sort` and `java.util.Arrays.sort` implement **Timsort**
- ▶ KeY verification of **OpenJDK** implementation revealed *bug*.
- ▶ **Same bug** present in **Android** SDK, **Phyton** library, **Haskell** library

## Verified Fix using KeY

- ▶ Fixing the implementation
- ▶ Verified new version with KeY

# Major Case Studies with KeY

## Found Bug in Java Libraries' main Sort Method using KeY

- ▶ `java.util.Collections.sort` implements `util.Arrays.sort` using `Timsort`
- ▶ KeY verification revealed *bug*.
- ▶ Same bug in Haskell library

Some researchers found an error in the logic of `merge_collapse`, explained here, and with corrected code shown in

## Verified

- ▶ Fixing
- ▶ Verified with KeY

It should be fixed anyway, and their suggested fix looks good to me.  
**Tim Peters via Python-Bugtracker**

# Major Case Studies with KeY

## Found Bug in Java Libraries' main Sort Method using KeY

- ▶ `java.util.Collections.sort` and `java.util.Arrays.sort` implemented using TimSort
- ▶ KeY verified an error in the implementation explained here, [revealed bug](#).
- ▶ Same error was also found in Haskell library

Congratulations to Stijn de Gouw et al. for finding and fixing a bug in TimSort using formal methods!

Some of the authors of their suggestion: **Joshua Bloch** via **Twitter** and **Tim Peters** via **Google**

## Verified

- ▶ Fixing
- ▶ Verified with KeY



# Tool Support is Essential

## Some Reasons for Using Tools

- ▶ Automate repetitive tasks
- ▶ Avoid typos, etc.
- ▶ Cope with large/complex programs
- ▶ Make verification certifiable

## Tools used in this course:

**SPIN** to verify PROMELA programs against Temporal Logic specs

**SPIN web interface** developed for this course!

**JSPIN** front-end for SPIN

**KeY** to verify Java programs against contracts in JML

All are free and run on Windows/Unixes/Mac.

**Install first SPIN and JSPIN on your computer,  
or make sure the SPIN web interface works.**

# You will gain experience in ...

- ▶ Modelling, and modelling languages
- ▶ Specification, and specification languages
- ▶ In depth analysis of possible system behaviour
- ▶ Typical types of errors
- ▶ Reasoning about system (mis)behaviour
- ▶ ...

# Learning Outcomes—Knowledge and Understanding

- ▶ Explain the potential and limitations of using logic based verification methods for assessing and improving software correctness
- ▶ Identify what can and what cannot be expressed by certain specification/modeling formalisms
- ▶ Identify what can and cannot be analyzed with certain logics and proof methods

# Learning Outcomes—Skills and Abilities

- ▶ Express safety and liveness properties of (concurrent) programs in a formal way
- ▶ Describe the basics of verifying safety and liveness properties via model checking
- ▶ Successfully employ tools which prove or disprove temporal properties
- ▶ Write formal specifications of object-oriented system units, using the concepts of method contracts and class invariants
- ▶ Describe how the connection between programs and formal specifications can be represented in a program logic
- ▶ Verify functional properties of simple Java programs with a verification tool

# Learning Outcomes—Judgment and Approach

- ▶ Judge and communicate the significance of correctness for software development
- ▶ Employ abstraction, modelling, and rigorous reasoning when approaching the development of correctly functioning software

# Literature for this Lecture

- FM in SE** B. Beckert, R. Hähnle, T. Hoare, D. Smith, C. Green, S. Ranise, C. Tinelli, T. Ball, and S. K. Rajamani: *Intelligent Systems and Formal Methods in Software Engineering*. IEEE Intelligent Systems, 21(6):71–81, 2006  
(Access to e-version via Chalmers Library)
- KeY** R. Hähnle: *Quo Vadis Formal Verification*. In: W. Ahrendt, B. Beckert, R. Bubel, R. Hähnle, P. Schmitt, M. Ulbrich editors. Vol 10001 of *LNCS*, Springer, 2016  
(E-book at [link.springer.com](http://link.springer.com))
- SPIN** Gerard J. Holzmann: *A Verification Model of a Telephone Switch*. In: *The Spin Model Checker*, Chapter 14, Addison Wesley, 2004