

# Formal Methods for Software Development

## Introduction

Wolfgang Ahrendt

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Chalmers University of Technology  
and  
University of Gothenburg

03 September 2019

## Teachers

- ▶ Wolfgang Ahrendt (WA)    examiner, lecturer
- ▶ Oskar Abrahamsson (OA)    teaching assistant
- ▶ Andreas Lööv (AL)    teaching assistant

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- ▶ Oskar Abrahamsson (OA)    **teaching assistant**
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course assistant activities include:

- ▶ giving exercise classes
- ▶ correcting lab hand-ins
- ▶ student support via:
  - ▶ e-mail
  - ▶ meetings on e-mail request
    - ▶ Oskar, room 5453
    - ▶ Andreas, room 5461

## Course Home Page

On Canvas, via Chalmers and GU.

Also used for online news and discussions.

# Course Structure

## Course Structure

| Topic   | # Lectures | # Exercises | Lab |
|---|------------|-------------|-----|
| Intro   | 1          | ✗           | ✗   |
| Modeling & Model Checking with<br><i>PROMELA &amp; SPIN</i> | 6          | 3           | ✓   |
| Specification & Verification with<br><i>JML &amp; KeY</i>   | 6 (+1?)    | 3           | ✓   |

*PROMELA & SPIN* abstract programs, model checking, automated

*JML & KeY* concrete Java, deductive verification, semi-automated

... more on this later!

## Lectures

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- ▶ Please respond to my questions

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- ▶ Please respond to my questions
- ▶ Slides appear online shortly *after* each lecture



## Exercises

- ▶ One exercise web page (almost) each week (6 in total)
- ▶ Discussed in next exercise class
- ▶ Play around with the exercises before coming to the class
- ▶ Exercises **highly** recommended
- ▶ Bring laptops if you have  
(ideally w. installed tools or browser interfaces working)

# Passing Criteria

- ▶ Oral examination in exam week
- ▶ Two lab hand-ins
- ▶ (No written end-exam)
- ▶ Oral exam and labs can be passed separately

- ▶ individual, oral examination

# Oral Exam

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  - ▶ Submission via **Fire**, linked from course home page
  - ▶ If submission is returned, roughly one week for correction
  - ▶ You work in groups of **two**. No exception!<sup>a</sup>  
You pair up by either:
    1. talk to people
    2. post request via Canvas
    3. participate in pairing at first exercise session
- In case all that is **not** sufficient, contact Oskar by e-mail.

---

<sup>a</sup>Only PhD students have to work alone.



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- ▶ Web Pages (linked from Canvas)
- ▶ Fire System (for lab submissions)

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(inspect course schedule)

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1. course evaluation group:
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    - ▶ randomly selected (Chalmers)
    - ▶ volunteers (GU)
  - ▶ one meeting during the course, one after
2. web questionnaire after the course

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- ▶ Ramkumar Venkatesh
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GU students: please consider volunteering

- ▶ In part I, we partly use:

**Ben-Ari** Mordechai Ben-Ari

*Principles of the Spin Model Checker*

Springer, 2008

*Ben-Ari received ACM award for outstanding contributions to CS education. Recommended by G. Holzmann. Excellent student text book.*

(E-book at [link.springer.com](http://link.springer.com))

- ▶ Relevant for part II:

**KeYbook** W. Ahrendt, B. Beckert, R. Bubel, R. Hähnle, P. Schmitt, M. Ulbrich, editors.

*Deductive Software Verification - The KeY Book*

Vol 10001 of LNCS, Springer, 2016

(E-book at [link.springer.com](http://link.springer.com))

# Additional Literature

**Holzmann** Gerard J. Holzmann  
**The Spin Model Checker**  
Addison Wesley, 2004

**BayerKatoen** Christel Baier, Joost-Pieter Katoen  
**Principles of Model Checking**  
MIT Press, 2008

# Connection to other Courses

## Prerequisites

- ▶ Skills in first-order logic and temporal logic, e.g., from
  - ▶ Logic in Computer Science, or
  - ▶ Discrete Event Systems
- ▶ Skills in object-oriented programming (like Java)

## Related courses (not assumed!)

- ▶ Concurrent Programming
- ▶ Finite Automata
- ▶ Testing, Debugging, and Verification



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if not: don't worry, we introduce everything we use here

# Motivation:

## Software Defects cause BIG Failures

Tiny faults in technical systems can have catastrophic consequences

### In particular, this goes for software systems

- ▶ Ariane 5
- ▶ Mars Climate Orbiter
- ▶ London Ambulance Dispatch System
- ▶ NEDAP Voting Computer Attack
- ▶ ...

# Motivation:

## Software Defects cause OMNIPRESENT Failures

Ubiquitous Computing results in Ubiquitous Failures

### Software is almost everywhere:

- ▶ Mobiles
- ▶ Clouds
- ▶ Smart cards
- ▶ Smart devices
- ▶ Cars
- ▶ Blockchains
- ▶ ...

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software/specification quality is a growing commercial and legal issue

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- ▶ Clear separation of subsystems
- ▶ Design follows patterns that are proven to work

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- ▶ Cost efficiency favoured over reliability.
- ▶ Design practise for reliable software in **immature** state  
for complex (e.g., distributed) systems.

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A central strategy: **testing**

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**Testing against internal SW errors (“bugs”)**

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## Testing against external faults

- ▶ inject faults (memory, communication) by simulation or radiation
- ▶ trace fault propagation

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- ▶ Representativeness of test cases/injected faults subjective  
How to test for the unexpected? Rare cases?
- ▶ Testing is labour intensive, hence expensive

# What **are** Formal Methods

- ▶ Rigorous methods for system design/development/analysis
- ▶ Mathematics and symbolic logic  $\Rightarrow$  **formal**
- ▶ Increase confidence in a system
- ▶ Two aspects:
  - ▶ System **requirements**
  - ▶ System **implementation**
- ▶ Formalise both
- ▶ Use **tools** for
  - ▶ **exhaustive** search for failing scenario, or
  - ▶ mechanical **proof** that implementation satisfies requirements



# What are Formal Methods **for**

- ▶ Complement other analysis and design methods
- ▶ Increase confidence in system correctness
- ▶ Good at finding bugs  
(in code **and** specification)
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- ▶ Should ideally be as automated as possible

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and

- ▶ **Training in Formal Methods increases high quality development skills**

# Specification — What a System **Should** Do

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(in particular for efficient, i.e., redundant, data representations)
  - ▶ Modularity, encapsulation
  - ▶ Refinement relation

# The Main Point of Formal Methods is **Not**

- ▶ to show correctness of entire systems
- ▶ to replace testing
- ▶ to replace good design practises

There is no silver bullet!

- ▶ No correct system w/o clear requirements & good design

# But ...

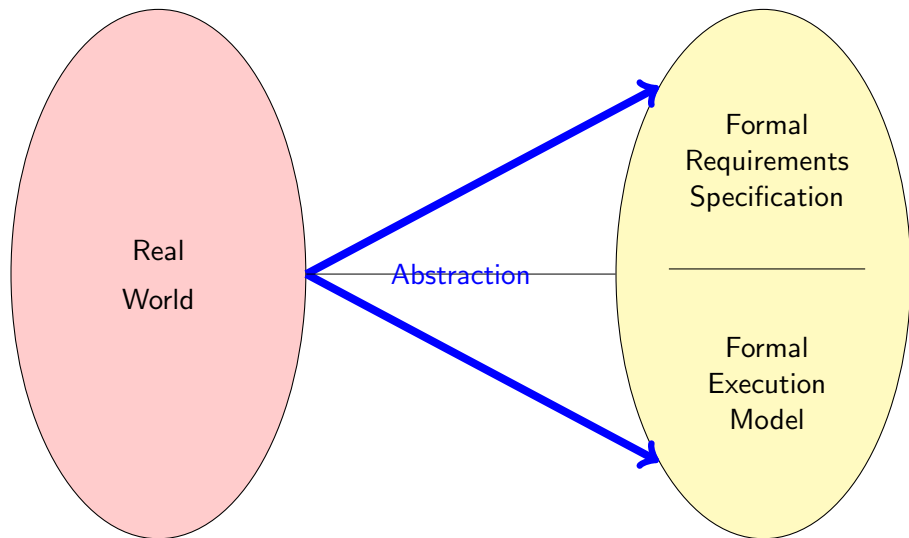
- ▶ Formal proof can replace (infinitely) many test cases
- ▶ Formal methods improve the quality of specs (even without formal verification)
- ▶ Formal methods **guarantee** specific properties of system (model)

# A Fundamental Fact

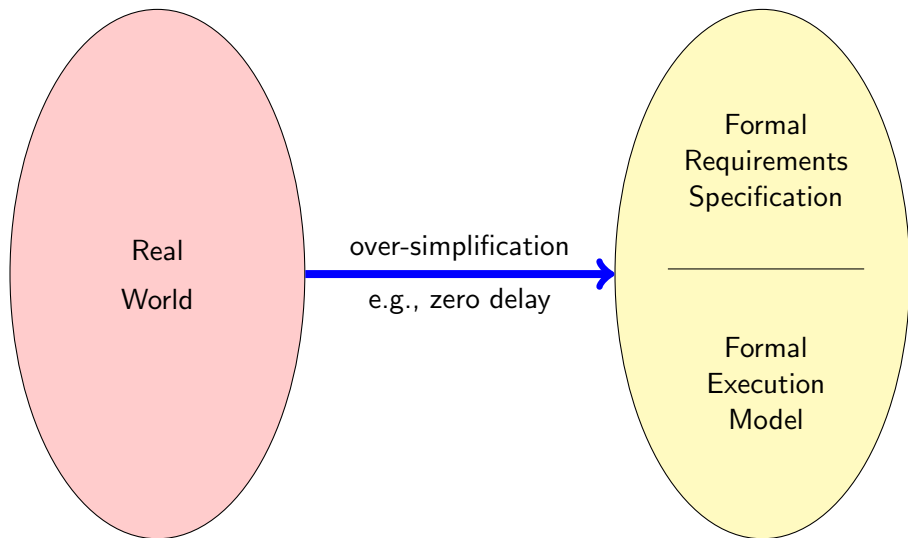
Formalisation of system requirements is hard

Let's see why ...

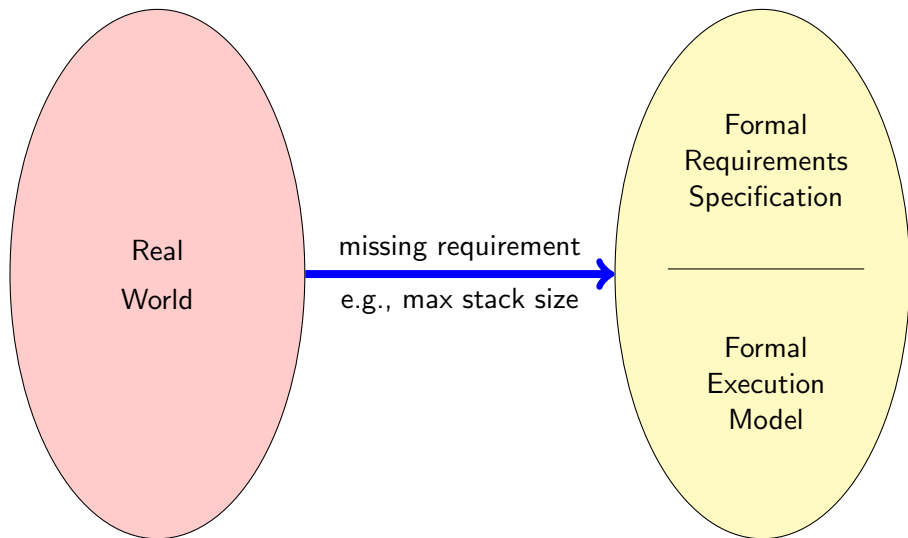
# Difficulties in Creating Formal Models



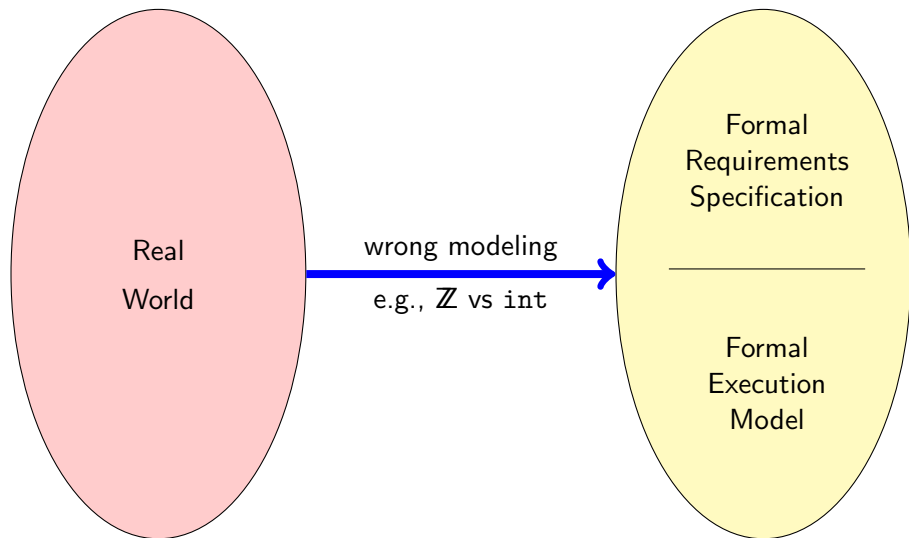
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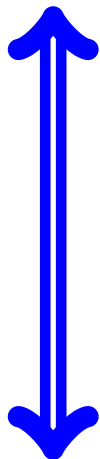
Errors in specifications are as common as errors in code, but their discovery gives deep insights in (mis)conceptions of the system.

- ▶ Wellformedness and consistency of formal specs partly machine-checkable
- ▶ Declared signature (symbols) helps to spot incomplete specs
- ▶ Failed verification of implementation against spec gives feedback on erroneous formalization

# Another Fundamental Fact

Proving properties of systems can be hard

# Level of System (Implementation) Description



- ▶ **Abstract level**

- ▶ Finitely many states (bounded size datatypes)
- ▶ Simplification, unfaithful modeling inevitable
- ▶ Automated proofs are (in principle) possible

- ▶ **Concrete level**

- ▶ Unbounded size datatypes  
(pointer chains, dynamic containers, streams)
- ▶ Complex datatypes and control structures
- ▶ Realistic programming model (e.g., Java)
- ▶ Automated proofs hard or impossible!

# Expressiveness of Specification



## ▶ Simple

- ▶ Simple or general properties
- ▶ Finitely many case distinctions
- ▶ Approximation, low precision
- ▶ Automated proofs are (in principle) possible

## ▶ Complex

- ▶ Full behavioural specification
- ▶ Quantification over infinite or large domains
- ▶ High precision, tight modeling
- ▶ Automated proofs hard or impossible!



# Main Approaches

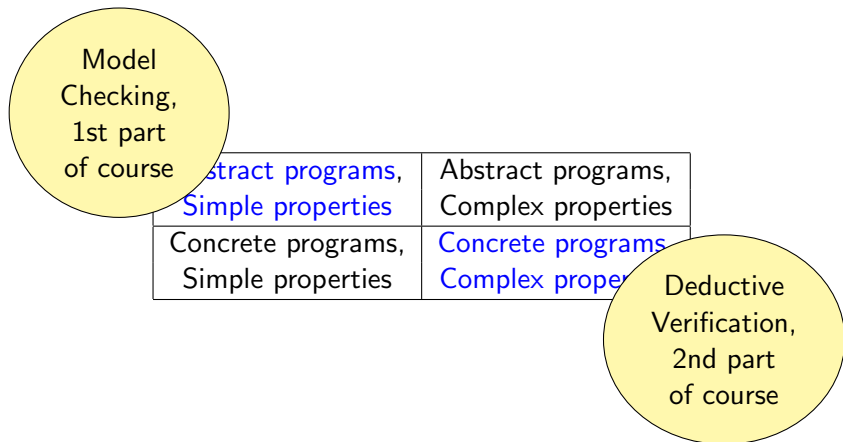
|   |  |
|---|--|
| Abstract programs,<br>Simple properties | Abstract programs,<br>Complex properties |
| Concrete programs,<br>Simple properties | Concrete programs,<br>Complex properties |

# Main Approaches

Model  
Checking,  
1st part  
of course

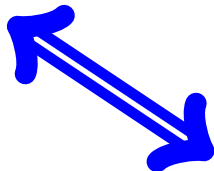
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# Main Approaches



# Proof Automation

- ▶ “Automated” Proof  
(“batch-mode”)
  - ▶ No interaction (or lemmas) necessary
  - ▶ Tuning of tool parameters necessary
  - ▶ Formal specification still “by hand”
  
- ▶ “Semi-Automated” Proof  
(“interactive”)
  - ▶ Interaction (or lemmas) may be required
  - ▶ Need certain knowledge of tool internals  
Intermediate inspection can help
  - ▶ User steps are checked by tool



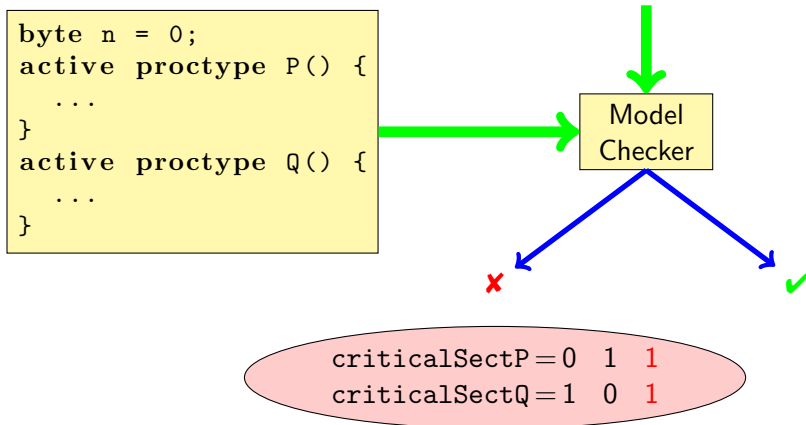
# Model Checking with SPIN

## System Model

```
byte n = 0;  
active proctype P() {  
  ...  
}  
active proctype Q() {  
  ...  
}
```

## System Property

`[]!(criticalSectP && criticalSectQ)`



# Model Checking in Industry—Examples

- ▶ Hardware verification
  - ▶ Good match between limitations of methods and application
  - ▶ Intel, Motorola, AMD, . . .
- ▶ Software verification
  - ▶ Specialized software: control systems, protocols
  - ▶ Typically no direct checking of executable system, but of abstractions
  - ▶ Bell Labs, Microsoft

# A Major Case Study with SPIN

## Checking feature interaction for telephone call processing software

- ▶ Software for PathStar<sup>©</sup> server from Lucent Technologies
- ▶ Automated abstraction of unchanged C code into PROMELA
- ▶ Web interface, with SPIN as back-end, to:
  - ▶ determine properties (ca. 20 temporal formulas)
  - ▶ invoke verification runs
  - ▶ report error traces
- ▶ Finds error trace, reported as C execution trace
- ▶ Work farmed out to 16 computers, daily, overnight runs
- ▶ 18 months, 300 versions of system model, 75 bugs found
- ▶ Strength: detection of undesired feature interactions (difficult with traditional testing)
- ▶ Main challenge: defining meaningful properties

# Deductive Verification with KeY

Java Code

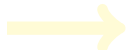
Formal specification



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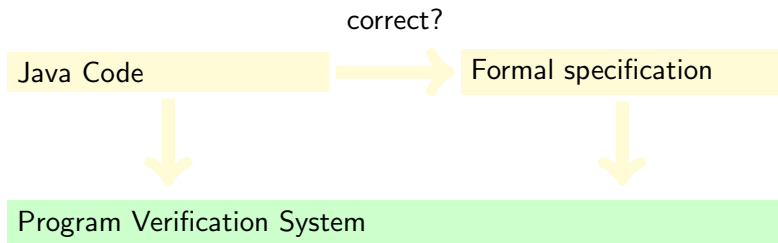
correct?

Java Code

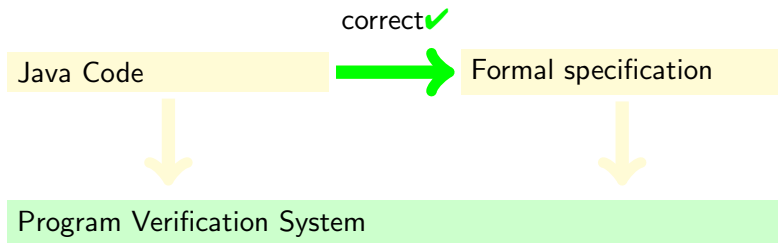


Formal specification

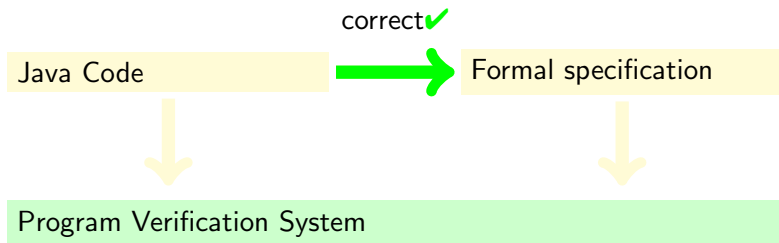
# Deductive Verification with KeY



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# Deductive Verification with KeY



Proof rules establish relation “implementation conforms to specs”

# Deductive Verification in Industry—Examples

- ▶ Hardware verification
  - ▶ For complex systems, mostly floating-point processors
  - ▶ Intel, Motorola, AMD, ...
- ▶ Software verification
  - ▶ Safety critical systems:
    - ▶ Paris driver-less metro (Meteor)
    - ▶ Emergency closing system in North Sea
  - ▶ Libraries
  - ▶ Implementations of Protocols

## Java Card 2.2.1 API Reference Implementation

- ▶ Reference implementation and full functional specification
- ▶ All Java Card 2.2.1 API classes and methods
  - ▶ 60 classes; ca. 5,000 LoC (250kB) source code
  - ▶ specification ca. 10,000 LoC
- ▶ Conformant to implementation on actual smart cards
- ▶ All methods fully verified against their spec
  - ▶ 293 proofs; 5–85,000 nodes
- ▶ Total effort several person months
- ▶ Most proofs fully automatic
- ▶ Main challenge: [getting specs right](#)

# Major Case Studies with KeY: Timsort

## Timsort

Hybrid sorting algorithm (insertion sort + merge sort) optimized for partially sorted arrays (typical for real-world data).

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## Facts

- ▶ Designed by Tim Peters (for Python)
- ▶ Since Java 1.7 default algorithm for non-primitive arrays/collections



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## Facts

- ▶ Designed by Tim Peters (for Python)
- ▶ Since Java 1.7 default algorithm for non-primitive arrays/collections

## Timsort is used in

- ▶ Java (standard libraries OpenJDK, Oracle)
- ▶ Python (standard library), used by Google
- ▶ Android (standard library), used by Google
- ▶ ... and many more languages / frameworks!

# Timsort: People



▶ Tim Peters

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- ▶ Tim Peters
- ▶ Sorting Algorithm Designer

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- ▶ Stijn de Gouw
- ▶ Assistant Professor
- ▶ Formerly postman in the NL

# Timsort: People



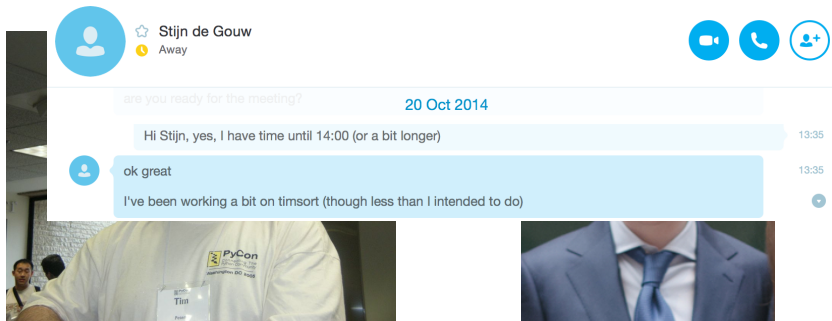
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- ▶ Assistant Professor
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- ▶ Interested in sorting for professional reasons



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# Timsort: People

The screenshot shows a WhatsApp chat interface. At the top left is a profile card for Stijn de Gouw, marked as 'Away'. On the right are icons for video call, voice call, and a group of people. The chat history shows a message from Stijn: "are you ready for the meeting?" dated 20 Oct 2014. A reply from Richard says: "Hi Stijn, yes, I have time until 14:00 (or a bit longer)" at 13:35. Stijn replies: "ok great" at 13:35. Richard then says: "I've been working a bit on timsort (though less than I intended to do)". A date separator for 27 Oct 2014 is shown. Richard sends a long message at 08:52: "morning richard", "don't want to keep this from you, but please keep it to yourself for now... as you know I was working on proving correctness of timsort (the soring algorithm used in the jdk)", and "I figured that the jdk was probably pretty thoroughly tested so went right ahead with specifying rather than debugging the algorithm... but I actually discovered a bug 😊". Stijn replies at 09:07: "Cool 😊" and "Good morning!".

Stijn de Gouw  
Away

are you ready for the meeting? 20 Oct 2014

Hi Stijn, yes, I have time until 14:00 (or a bit longer) 13:35

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27 Oct 2014

morning richard 08:52

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Cool 😊 09:07

Good morning!

professional reasons

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## Found Bug in Java Libraries' main Sorting Method using KeY

- ▶ `java.util.Collections.sort` and `java.util.Arrays.sort` implement **Timsort**
- ▶ KeY verification of **OpenJDK** implementation revealed *bug*.
- ▶ **Same bug** present in **Android** SDK, **Phyton** library, **Haskell** library

# Major Case Studies with KeY

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## Verified Fix using KeY

- ▶ Fixing the implementation
- ▶ Verified new version with KeY

# Major Case Studies with KeY

## Found Bug in Java Libraries' main Sort Method using KeY

- ▶ `java.util.Collections.sort` implements `util.Arrays.sort` using `Timsort`
- ▶ KeY verification revealed *bug*.
- ▶ Same bug was found in Haskell library

Some researchers found an error in the logic of `merge_collapse`, explained here, and with corrected code shown in

## Verified

- ▶ Fixing
- ▶ Verified with KeY

It should be fixed anyway, and their suggested fix looks good to me.  
**Tim Peters via Python-Bugtracker**

# Major Case Studies with KeY

## Found Bug in Java Libraries' main Sort Method using KeY

- ▶ `java.util.Collections.sort` and `java.util.Arrays.sort` implemented using TimSort
- ▶ KeY verified an error in the implementation explained here, [revealed bug](#).
- ▶ Same error was also found in Haskell library

Congratulations to Stijn de Gouw et al. for finding and fixing a bug in TimSort using formal methods!

Some of the authors of their suggestion: **Joshua Bloch** via **Twitter**

It should be fixed in **Tim Peters** via **Twitter**

gusted fix looks good

## Verified

- ▶ Fixing
- ▶ Verified with KeY

# Tool Support is Essential

## Some Reasons for Using Tools

- ▶ Automate repetitive tasks
- ▶ Avoid typos, etc.
- ▶ Cope with large/complex programs
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## Tools used in this course:

**SPIN** to verify PROMELA programs against Temporal Logic specs

**SPIN web interface** developed for this course!

**JSPIN** front-end for SPIN

**KeY** to verify Java programs against contracts in JML

All are free and run on Windows/Unices/Mac.

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**Install first SPIN and JSPIN on your computer,  
or make sure the SPIN web interface works.**

# You will gain experience in ...

- ▶ Modelling, and modelling languages

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- ▶ ...



# Learning Outcomes—Knowledge and Understanding

- ▶ Explain the potential and limitations of using logic based verification methods for assessing and improving software correctness
- ▶ Identify what can and what cannot be expressed by certain specification/modeling formalisms
- ▶ Identify what can and cannot be analyzed with certain logics and proof methods

# Learning Outcomes—Skills and Abilities

- ▶ Express safety and liveness properties of (concurrent) programs in a formal way
- ▶ Describe the basics of verifying safety and liveness properties via model checking
- ▶ Successfully employ tools which prove or disprove temporal properties
- ▶ Write formal specifications of object-oriented system units, using the concepts of method contracts and class invariants
- ▶ Describe how the connection between programs and formal specifications can be represented in a program logic
- ▶ Verify functional properties of simple Java programs with a verification tool

# Learning Outcomes—Judgment and Approach

- ▶ Judge and communicate the significance of correctness for software development
- ▶ Employ abstraction, modelling, and rigorous reasoning when approaching the development of correctly functioning software

# Literature for this Lecture

- FM in SE** B. Beckert, R. Hähnle, T. Hoare, D. Smith, C. Green, S. Ranise, C. Tinelli, T. Ball, and S. K. Rajamani: *Intelligent Systems and Formal Methods in Software Engineering*. IEEE Intelligent Systems, 21(6):71–81, 2006  
(Access to e-version via Chalmers Library)
- KeY** R. Hähnle: *Quo Vadis Formal Verification*. In: W. Ahrendt, B. Beckert, R. Bubel, R. Hähnle, P. Schmitt, M. Ulbrich editors. Vol 10001 of *LNCS*, Springer, 2016  
(E-book at [link.springer.com](http://link.springer.com))
- SPIN** Gerard J. Holzmann: *A Verification Model of a Telephone Switch*. In: *The Spin Model Checker*, Chapter 14, Addison Wesley, 2004