

# Parallelizing computations

Lecture 9 of TDA384/DIT391 (Principles of Concurrent Programming)

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Fork/join parallelism

Pools and work stealing

Concurrent programming introduces:

- + the potential for parallel execution (faster, better resource usage)
- the risk of race conditions (incorrect, unpredictable computations)

The main challenge of concurrent programming is thus introducing parallelism without affecting correctness.

My concurrent program will be so fast, there will be no time to check the answer!



- Scott West, circa 2010

In this class, we explore several general approaches to parallelizing computations in multi-processor systems.

A task  $\langle F, D \rangle$  consists in computing the result F(D) of applying function F to input data D.

A parallelization of  $\langle F, D \rangle$  is a collection  $\langle F_1, D_1 \rangle, \langle F_2, D_2 \rangle, \dots$  of tasks such that F(D) equals the composition of  $F_1(D_1), F_2(D_2), \dots$ 

We first cast the problems and solutions using Erlang's notation and models – message-passing between processes – since it is easier to prototype implementations of the solutions.

Then, we will apply the same concepts and techniques to shared-memory models such as Java threads.

## Challenges to parallelization

A strategy to parallelize a task  $\langle F, D \rangle$  should be:

- correct: the overall result of the parallelization is F(D)
- efficient: the total resources (time and memory) used to compute the parallelization are less than those necessary to compute (*F*, *D*) sequentially

A number of factors challenge designing correct and efficient parallelizations:

- sequential dependencies
- synchronization costs
- spawning costs
- · error proneness and composability

Some steps in a task computation depend on the result of other steps; this creates sequential dependencies where one task must wait for another task to run. Sequential dependencies limit the amount of parallelism that can be achieved.

For example, to compute the sum  $1 + 2 + \cdots + 8$  we could split into:

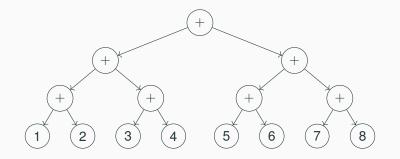
- a. computing 1 + 2, 3 + 4, 5 + 6, 7 + 8
- b. computing (1 + 2) + (3 + 4) and (5 + 6) + (7 + 8)
- c. computing ((1 + 2) + (3 + 4)) + ((5 + 6) + (7 + 8))

The computations in each group depend on the computations in the previous group, and hence the corresponding tasks must execute after the latter have completed.

The synchronization problems (producer-consumer, dining philosophers, etc.) we discussed in various classes capture kinds of <u>sequential dependencies</u> that may occur when parallelizing.

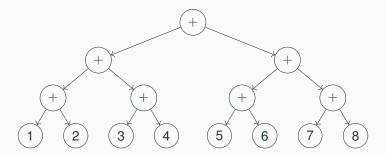
Some steps in a task computation depends on the result of other steps; this creates sequential dependencies where one task must wait for another task to run.

We represent tasks as the nodes in a graph, with arrows connecting a task to the ones it depends on. The graph must be acyclic for the decomposition to be executable.



### **Dependency graph**

We represent tasks as the nodes in a graph, with arrows connecting a task to the ones it depends on. The graph must be acyclic for the decomposition to be executable.



The time to compute a node is the maximum of the times to compute its children, plus the time computing the node itself. Assuming all operations take a similar time, the longest path from the root to a leaf is proportional to the optimal running time with parallelization (ignoring overheads and assuming all processes can run in parallel). Synchronization is required to preserve correctness, but it also introduces overheads that add to the overall cost of parallelization.

In shared-memory concurrency:

- synchronization is based on locking
- locking synchronizes data from cache to main memory, which may involve a 100x overhead
- other costs associated with locking may include context switching (wait/signal) and system calls (mutual exclusion primitives)

In message-passing concurrency:

- synchronization is based on messages
- exchanging small messages is efficient, but sending around large data is quite expensive (still goes through main memory)
- other costs associated with message passing may include extra acknowledgment messages and mailbox management (removing unprocessed messages)

Creating a new process is generally expensive compared to sequential function calls within the same process, since it involves:

- reserving memory
- · registering the new process with runtime system
- setting up the process's local memory (stack and mailbox)

Even if process creation is increasingly optimized, the cost of spawning should be weighted against the speed up that can be obtained by additional parallelism. In particular, when the processes become way more than the available processors, there will be <u>diminishing returns</u> with more spawning. Synchronization is prone to errors such as <u>data races</u>, <u>deadlocks</u>, and <u>starvation</u>. Message-based synchronization may improve the situation, but it is far for being straightforward and problem free. Synchronization is prone to errors such as <u>data races</u>, <u>deadlocks</u>, and <u>starvation</u>. Message-based synchronization may improve the situation, but it is far for being straightforward and problem free.

From the point of view of software construction, the lack of composability is a challenge that prevents us from developing parallelization strategies that are generally applicable.

Consider an Account class with methods deposit and withdraw that execute atomically. What happens if we combine the two methods to implement a transfer operation?

```
class Account {
   synchronized void
   deposit(int amount)
   { balance += amount; }
   synchronized void
   withdraw(int amount)
   { balance -= amount; }
}
```

Consider an Account class with methods deposit and withdraw that execute atomically. What happens if we combine the two methods to implement a transfer operation?

#### class Account { synchronized void

}

```
deposit(int amount)
 $ balance += amount; } void transfer(int amount, Account other)
synchronized void
 withdraw(int amount)
   balance -= amount; }
                       }
```

#### class TransferAccount

```
extends Account {
// transfer from 'this' to 'other'
```

```
{ this.withdraw(amount);
```

```
other.deposit(amount); }
```

#### execute atomically

Method transfer does not execute atomically: other threads can execute between the call to withdraw and the call to deposit, possibly preventing the transfer from succeeding (for example, account other may be closed; or the total balance temporarily looks lower than it is!).

### Composability

```
class Account {
   void // thread unsafe!
   deposit(int amount)
   { balance += amount; }
   void // thread unsafe!
   withdraw(int amount)
   { balance -= amount; }
}
```

```
class TransferAccount
    extends Account {
    // transfer from 'this' to 'other'
    synchronized void
    transfer(int amount, Account other)
    { this.withdraw(amount);
        other.deposit(amount); }
}
```

None of the natural solutions to composing is fully satisfactory:

- let clients of Account do the locking where needed error proneness, revealing implementation details, scalability
- recursive locking risk of deadlock, performance overhead

Even if there is no locking with message passing, we still encounter similar problems – synchronizing the effects of messaging two independent processes.

### Sequential dependencies and spawning costs

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In the rest of this class, we present:

- fork/join parallelism techniques, which help naturally capture sequential dependencies
- pools, which help curb the spawning costs

In future classes we will address the remaining problems of reducing synchronization costs and achieving composability.

# Fork/join parallelism

### **Parallel servers**

A server's event loop offers clear opportunities for parallelism:

- · each request sent to the server is independent of the others
- instead of serving requests sequentially, a server spawns a new process for every request
- a child processes computes, sends response to the client, and terminates

```
loop(State, Operation) ->
                                 ploop(State, Operation) ->
receive
                                  receive
  {request, From, Ref, Data} ->
                                    {request, From, Ref, Data} ->
     From ! {reply, Ref,
                                     spawn(fun ()->
             Operation(Data)},
                                      Result = Operation(Data),
     loop(new_state(State));
                                      From ! {reply, Ref, Result}
  % other operations...
                                           end),
                                      loop(new_state(State));
end.
                                    % other operations...
                                  end.
```

The structure of recursive functions lends itself to parallelization according to the structure of recursion.

Recursion is easier to parallelize when it is expressed in a mostly side-effect free language like sequential Erlang:

- spawn a process for every recursive call
- no side effects means no hidden dependencies a process's results only depends on its explicit input

```
merge_sort(List)
 when length(List) =< 1 ->
   List:
merge_sort(List) ->
  Mid = length(List) div 2,
   % split in two halves
  {L, R} = lists:split(Mid, List),
    % recursively sort each half
  SL = merge_sort(L),
  SR = merge_sort(R),
    % merge sorted halves
  merge(SL, SR).
   cannot be computed inside closure
```

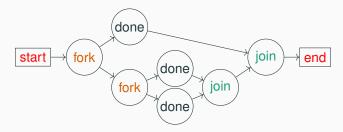
in spawn: must be the parent's pid

```
pmerge_sort(List)
 when length(List) =< 1 ->
    List:
pmerge_sort(List) ->
 Mid = length(List) div 2,
  {L, R} = lists:split(Mid, List),
 Pid = self(),
 spawn(fun ()-> Pid !
    {sl, pmerge_sort(L)} end),
  spawn(fun ()-> Pid !
     {sr, pmerge_sort(R)} end),
  receive {sl, SL} -> sl end,
  receive {sr, SR} -> sr end,
 merge(SL, SR).
```

## Fork/join parallelism

This recursive subdivision of a task that assigns new processes to smaller tasks is called fork/join parallelism:

- forking: spawning child processes and assigning them smaller tasks
- joining: waiting for the child processes to complete and combining their results



The order in which we wait at a join node for forked children does not affect the total waiting time: if we wait for a slower process first, we won't wait for the others later.

Function map's recursive structure lends itself to parallelization.

```
% apply F to all
% elements of list
map(_, []) -> [];
map(F, [H|T]) ->
[F(H)|map(F,T)].
```

% wait for all Children % and collect results in order gather(Children, Ref) -> [receive {Child, Ref, Res} -> Res end || Child <- Children].</pre> % parallel map  $pmap(F, L) \rightarrow$ Me = self(), % my pid Ref = make\_ref(), % for every E in L: Children =  $map(fun(E) \rightarrow$ % spawn a process spawn(fun() -> % sending Me result of F(E) Me ! {self(), Ref, F(E)} end) end, L),

% collect and return results
gather(Children, Ref).

list comprehension ensures results are collected in order

#### **Parallel reduce**

The parallel version of reduce (also called foldr) uses a halving strategy similar to merge sort.

reduce(\_, A, []) -> A;

reduce(F, A, [H|T]) ->

F(H, reduce(F, A, T)).

```
preduce(F, A, L) equals
reduce(F, A, L) if:
```

- F is associative (preduce does not apply F right-to-left)
- for every list element E:
   F(E, A) = F(A, E) = E
   (preduce reduces A in every base case, not just once)

 $preduce(\_, A, []) \rightarrow A;$  $preduce(F, A, [E]) \rightarrow F(A, E);$ preduce(F, A, List) -> Mid = length(List) div 2, {L, R} = lists:split(Mid, List), Me = self(), % L ++ R =:= ListnLp = spawn(fun() -> % on left half Me ! {self(), preduce(F, A, L)} end), Rp = spawn(fun() -> % on right half Me ! {self(), preduce(F, A, R)} end), % combine results of left, right half F(receive {Lp, Lr} -> Lr end, receive {Rp, Rr} -> Rr end).

MapReduce is a programming model based on parallel distributed variants of the primitive operations map and reduce. MapReduce is a somewhat more general model, since it may produce a list of values from a list of key/value pairs, but the underlying ideas are the same.

MapReduce implementations typically work on very large, highly-parallel, distributed databases or filesystems.

- The original MapReduce implementation was proprietary developed at Google
- Apache Hadoop offers a widely-used open-source Java implementation of MapReduce

Java package java.util.concurrent includes a library for fork/join parallelism. To implement a method T m() using fork/join parallelism:

If m is a procedure (T is **void**):

- create a class that inherits from RecursiveAction
- override **void** compute() with m's computation

If m is a function:

- create a class that inherits from RecursiveTask<T>
- override T compute() with m's computation

RecursiveAction and RecursiveTask<T> provide methods:

- fork(): schedule for asynchronous parallel execution
- T join(): wait for termination, and return result if T != void
- T invoke(): arrange synchronous parallel execution (fork and join), and return result if T != void
- invokeAll(Collection<T> tasks) invoke all tasks in collection (fork all and join all), and return collection of results

#### Parallel merge sort using fork/join

#### public class PMergeSort extends RecursiveAction {

private Integer[] data; // values to be sorted
private int low, high; // to be sorted: data[low..high)

#### @Override

}

```
protected void compute() {
```

if (high - low <= 1) return; // size <= 1: sorted already
int mid = low + (high - low)/2; // mid point</pre>

#### // left and right halves

PMergeSort left = new PMergeSort(data, low, mid); PMergeSort right = new PMergeSort(data, mid, high); left.fork(); // fork thread working on left right.fork(); // fork thread working on right left.join(); // wait for sorted left half right.join(); // wait for sorted right half merge(mid); // merge halves The top computation of a fork/join task is started by a pool object:

```
// to sort array 'numbers' using PMergeSort:
RecursiveAction sorter = new PMergeSort(numbers, 0, numbers.length);
// schedule 'sorter' for execution, and wait for computation to finish
ForkJoinPool.commonPool().invoke(sorter);
// now 'numbers' is sorted
```

The pool takes care of efficiently dispatching work to threads, as we describe in the rest of this class.

The framework introduces a layer of abstraction between computational tasks and actual running threads that execute the tasks. This way, the fork/join model simplifies parallelizing computations, since we can focus on how to split data among tasks in a way that avoids data races.

}

There are a number of things that should be improved in the parallel merge sort example: granularity too small!

protected void compute() { if (high - low <= 1) **Freturn**; // size <= 1: sorted already int mid = low + (high - low)/2; // mid point // left and right halves PMergeSort left = new PMergeSort(data, low, mid); PMergeSort right = new PMergeSort(data, mid, high); left.fork(); // fork thread working on left right.fork(); // fork thread working on right left.join(); // wait for sorted left half right.join(); // wait for sorted right half // merge halves merge(mid);

the forking thread is idle!

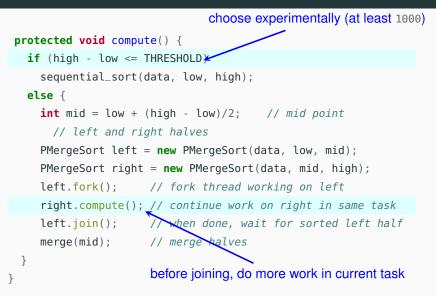
## Fork/join good practices

In order to obtain good performance using fork/join parallelism:

- After forking children tasks, keep some work for the parent task before it joins the children
- For the same reason, use invoke and invokeAll only at the top level as a norm
- Perform small enough tasks sequentially in the parent task, and fork children tasks only when there is a substantial chunk of work left; Java's fork/join framework recommends that each task be assigned between 100 and 10'000 basic computational steps
- Make sure different tasks can proceed independently minimize data dependencies

The advantages of parallelism may only be visible with several physical processors, and on very large inputs. (The Java runtime may even need to warm up before it optimizes the parallel code more aggressively.)

### Revisited parallel merge sort using fork/join



# Pools and work stealing

Parallelizing by following the recursive structure of a task is simple and appealing. However, the potential performance gains should be weighted against the overhead of creating and running many processes. Parallelizing by following the recursive structure of a task is simple and appealing. However, the potential performance gains should be weighted against the overhead of creating and running many processes.

Process creation in Erlang is lightweight: 1 GiB of memory fits about 432'000 processes, so <u>one</u> <u>million processes</u> is quite feasible.



Parallelizing by following the recursive structure of a task is simple and appealing. However, the potential performance gains should be weighted against the overhead of creating and running many processes.

There are still limits to how many processes fit in memory. Besides, even if we have enough memory, more processes do not improve performance if their number greatly exceeds the number of available physical processors.



Process pools are a technique to address the problem of using an appropriate number of processes.

A pool creates a number of worker processes upon initialization. The number of workers is chosen according to the actual resources that are available to run them in parallel – a detail which pool users need not know about.

- As long as more work is available, the pool deals a work assignment to a worker that is available
- The pool collects the results of the workers' computations
- When all work is completed, the pool terminates and returns the overall result

This kind of pool is called a dealing pool because it actively deals work to workers.

# Workers

Workers are servers that run as long as the pool that created them does. A worker can be in one of two states:

- · idle: waiting for work assignments from the pool
- busy: computing a work assignment

As soon as a worker completes a work assignments, it sends the result to the pool and goes back to being idle.

```
% create worker for 'Pool' computing 'Function'
init_worker(Pool, Function) ->
spawn(fun ()-> worker(Pool, Function) end).
```

```
worker(Pool, Function) ->
receive {Pool, Data} -> % assignment from pool
Result = Function(Data), % compute work
Pool ! {self(), Result}, % send result to pool
worker(Pool, Function) % back to idle
end.
```

# Pool state

A pool keeps track of:

- the remaining work not assigned yet
- · the busy workers
- the idle workers

-record(pool, {work, busy, idle}).

The pool also stores:

- · a split function, used to extract a single work item
- a join function, used to combine partial results
- · the overall result of the computation that is underway

```
pool(Pool#pool, Split, Join, Result) -> todo.

    state of record type pool
```

The pool terminates and returns the result of the computation when there are no pending work items, and all workers are busy (thus all work has been done).

```
% work completed, no busy workers: return result
pool(#pool{work = [], busy = []},
    __Split, _Join, Result) ->
    Result;
```

As long as there is some pending work and some idle workers, the pool deals work to some of those idle workers.

```
% work pending, some idle workers: assign work
pool(Pool = #pool{work = Work = [_]_], % matches if Work not empty
                 busy = Busy,
                 idle = [Worker|Idle]},
    Split, Join, Result) ->
    {Chunk, Remaining} = Split(Work), % split pending work
                              % send chunk to worker
   Worker ! {self(), Chunk},
   pool(Pool#pool{work = Remaining,
                   busy = [Worker|Busy],
                  idle = Idle},
        Split, Join, Result);
```

Using a function Split provides flexibility in splitting work into chunks.

When there are no pending work items or all workers are busy, the pool can only wait for workers to send back results.

Note that the condition "no pending work or all workers busy" is implicit because this clause comes last in the definition of pool.

Initializing a pool requires a function to be computed, a workload, split and join functions, and a number of worker threads.

```
init_pool(Function, Work, Split, Join, Initial, N) ->
Pool = self(),
    % spawn N workers for the same pool
Workers = [init_worker(Pool, Function) || _ <- lists:seq(1, N)],
[link(W) || W <- Workers], % link workers to pool
    % initially all work is pending, all workers are idle
pool(#pool{work = Work, busy = [], idle = Workers},
    Split, Join, Initial).</pre>
```

Function link ensures that the worker processes are terminated as soon as the process running the pool does.

In practice we would set N to an optimal number based on the available resources, and export init\_pool working with that number.

We can define a parallel version of map using a pool:

```
pmap(F, L, N) -> init_pool(F, % function to be mapped
L, % work: list to be mapped
fun ([H|T]) -> {H, T} end, % split: take first element
fun (R,Res) -> [R|Res] end, % join: cons with list
[], N).
```

Note that the order of the results may change from run to run. It is possible to restore the original order by using a more complex join function.

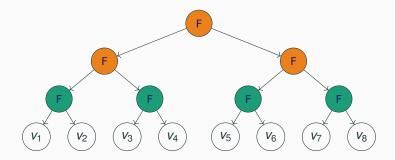
We can define a parallel version of reduce using a pool:

```
preduce(F, I, L, N) ->
    init_pool(fun ({X,Y}) -> F(X,Y) end, % so that a chunk is a pair
    L, % split: take first two elements
    fun (W) -> chunk_two(I, W) end,
    F, % join: folding function!
    I, N).
```

This works correctly under the same conditions as the direct recursive version of preduce shown before: F should be associative, and I should be a neutral element under F.

The syntax is a bit cumbersome, but the basic idea is that preduce assigns to each worker the reduction of two consecutive input elements.

In our version of preduce using a dealing pool, a lot of reduction work is actually done by the pool process when executing join for each result. In the dependency graph, the bottom level is computed by the workers; the upper levels are computed by the pool while joining.



# **Recursive dealing pools**

More generally, the dealing process pool we have designed works well if joining is a lightweight operation compared to computing the work function.

A more flexible solution subdivides work in tasks. Each task consists of a function to be applied to a list of data.

-record(task, {function, data}).

- The split function extracts a smaller task from a bigger one
- The join function creates a task consisting of computing the join

With this approach, the pool can delegate joining to the workers or do it directly if it is little work. By creating suitable join and split functions we can make a better usage of workers and achieve a better parallelization.

We call this kind of pool recursive (dealing) pool, because it may recursively generate new work while combining intermediate results.

Dealing pools work well if:

- the workload can be split it even chunks, and
- the workload does not change over time (for example if users send new tasks or cancel tasks dynamically)

Under these conditions, the workload is <u>balanced evenly</u> between workers, so as to maximize the amount of parallel computation.

In realistic applications, however, these conditions are not met:

- it may be hard to predict reliably which tasks take more time to compute
- the workload is highly dynamic

Stealing pools use a different approach to allocating tasks to workers that better addresses these challenging conditions.

A stealing pool associates a queue to every worker process. The pool offloads new tasks by adding them a worker's queue.

When a worker becomes idle:

- first, it gets the next task from the its queue
- if its queue is empty, it can directly steal tasks from the queue of another worker that is currently busy

With this approach, workers adjust <u>dynamically</u> to the current working conditions without requiring a supervisor that can reliably predict the workload required by each task. With stealing, the pool may even send all tasks to <u>one default thread</u>, letting other idle threads steal directly from it, <u>simplifying</u> the pool and reducing the <u>synchronization</u> <u>costs</u> it incurs.

# Work stealing algorithm

This is an outline of the algorithm for work stealing. It assumes that the queue array queue can be accessed by concurrent threads without race conditions.

#### public class WorkStealingThread

```
{ Queue [] queue; // queues of all worker threads
 public void run() {
  { int me = ThreadID.get(); // my thread id
   while (true) {
     for (Task task: queue[me]) // run all tasks in my queue
       task.run():
     // now my queue is empty: select another random thread
     int victim = random.nextInt(queue.length);
     // try to take a task out of the victim's queue
     Task stolen = queue[victim].pop();
     // if the victim's queue was not empty, run the stolen task
     if (stolen != null) stolen.run();
```

Java offers efficient implementations of thread pools in package java.util.concurrent.

The interface ExecutorService provides:

- void execute(Runnable thread): schedule thread for execution
- Future submit(Runnable thread): schedule thread for execution, and return a Future object (to cancel the execution, or wait for termination)

Implementations of ExecutorService with different characteristics can also be obtained by factory methods of **class Executors**:

- CachedThreadPool: thread pool of dynamically variable size
- WorkStealingPool: thread pool using work stealing
- ForkJoinPool: work-stealing pool for running fork/join tasks

Without thread pools:

```
Counter counter = new Counter();
```

// threads t and u

Thread t = new Thread(counter);

Thread u = new Thread(counter);

t.start(); // increment once

u.start(); // increment twice

try { // wait for termination

t.join(); u.join(); }

catch (InterruptedException e)

```
{ System.out.println("Int!"); }
```

#### With thread pools:

Counter counter = **new** Counter(); // threads t and u Thread t = new Thread(counter); Thread u = **new** Thread(counter): ExecutorService pool = Executors.newWorkStealingPool(); // schedule t and u for execution Future<?> ft = pool.submit(t); Future<?> fu = pool.submit(u); try { // wait for termination ft.get(); fu.get(); } catch (InterruptedException ExecutionException e) { System.out.println("Int!"); }

Erlang provides some load distribution services in the system module pool. These are aimed at distributing the load between different nodes, each a full-fledged collection of processes.

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