

# Formal Methods for Software Development

## Introduction

Wolfgang Ahrendt

Department of Computer Science and Engineering  
Chalmers University of Technology  
and  
University of Gothenburg

04 September 2018

## Teachers

- ▶ Wolfgang Ahrendt (WA)    **examiner, lecturer**
- ▶ Oskar Abrahamsson (OA)    **teaching assistant**
- ▶ Andreas Lööv (AL)    **teaching assistant**

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course assistant activities include:

- ▶ giving exercise classes
- ▶ correcting lab hand-ins
- ▶ student support via:
  - ▶ e-mail
  - ▶ meetings on e-mail request
    - ▶ Oskar, room 5461
    - ▶ Andreas, room 5461

## Course Home Page

Linked from Chalmers and GU course portals

## Google News Group

- ▶ Sign up via course home page (see [News Group](#))
- ▶ Changes, updates, questions, discussions (don't post solutions)

# Course Structure

## Course Structure

Topic	# Lectures	# Exercises	Lab
Intro	1	✗	✗
Modeling & Model Checking with <i>PROMELA &amp; SPIN</i>	6	3	✓
Specification & Verification with <i>JML &amp; KeY</i>	7	3	✓

*PROMELA & SPIN* abstract programs, model checking, automated

*JML & KeY* concrete Java, deductive verification, semi-automated

... more on this later!

## Lectures

- ▶ Please ask questions during lectures
- ▶ Please respond to my questions

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- ▶ Please respond to my questions
- ▶ Slides appear online shortly *after* each lecture



## Exercises

- ▶ One exercise web page (almost) each week (6 in total)
- ▶ Discussed in next exercise class
- ▶ Play around with the exercises before coming to the class
- ▶ Exercises **highly** recommended
- ▶ Bring laptops if you have  
(ideally w. installed tools or browser interfaces working)

# Passing Criteria

- ▶ Oral examination in exam week
- ▶ Two lab hand-ins
- ▶ (No written end-exam)
- ▶ Oral exam and labs can be passed separately

- ▶ individual, oral examination

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- ▶ 2 Lab Questions Sessions
- ▶ Submission via **Fire**, linked from course home page
- ▶ If submission is returned, roughly one week for correction
- ▶ You work in groups of **two**. No exception!<sup>a</sup>  
You pair up by either:
  1. talk to people
  2. post to the Google group
  3. participate in pairing at first exercise session

In case all that is **not** sufficient, contact Oskar by e-mail.

---

<sup>a</sup>Only PhD students have to work alone.



# Schedule

see course homepage

# Course Evaluation

1. course evaluation group:
  - ▶ student representatives
    - ▶ randomly selected (Chalmers)
    - ▶ volunteers (GU)
  - ▶ one meeting during the course, one after
2. web questionnaire after the course

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- ▶ Erik Hermansson
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GU students: please consider volunteering

- ▶ In part I, we partly use:

**Ben-Ari** Mordechai Ben-Ari

*Principles of the Spin Model Checker*

Springer, 2008

*Ben-Ari received ACM award for outstanding contributions to CS education. Recommended by G. Holzmann. Excellent student text book.*

(E-book at [link.springer.com](http://link.springer.com))

- ▶ Relevant for part II:

**KeYbook** W. Ahrendt, B. Beckert, R. Bubel, R. Hähnle, P. Schmitt, M. Ulbrich, editors.

*Deductive Software Verification - The KeY Book*

Vol 10001 of *LNCS*, Springer, 2016

(E-book at [link.springer.com](http://link.springer.com))

# Additional Literature

**Holzmann** Gerard J. Holzmann  
**The Spin Model Checker**  
Addison Wesley, 2004

**BayerKatoen** Christel Baier, Joost-Pieter Katoen  
**Principles of Model Checking**  
MIT Press, 2008

# Connection to other Courses

## Prerequisites

- ▶ Skills in first-order logic and temporal logic, e.g., from
  - ▶ Logic in Computer Science, or
  - ▶ Discrete Event Systems
- ▶ Skills in object-oriented programming (like Java)

## Related courses (not assumed!)

- ▶ Concurrent Programming
- ▶ Finite Automata
- ▶ Testing, Debugging, and Verification

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if not: don't worry, we introduce everything we use here

# Motivation:

## Software Defects cause BIG Failures

Tiny faults in technical systems can have catastrophic consequences

### In particular, this goes for software systems

- ▶ Ariane 5
- ▶ Mars Climate Orbiter
- ▶ London Ambulance Dispatch System
- ▶ NEDAP Voting Computer Attack
- ▶ ...

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## Software Defects cause OMNIPRESENT Failures

Ubiquitous Computing results in Ubiquitous Failures

### Software is almost everywhere:

- ▶ Mobiles
- ▶ Clouds
- ▶ Smart cards
- ▶ Smart devices
- ▶ Cars
- ▶ ...

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software/specification quality is a growing commercial and legal issue

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## Well-known strategies from mechanical and civil engineering

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- ▶ Robust design (single fault not catastrophic)
- ▶ Clear separation of subsystems
- ▶ Design follows patterns that are proven to work

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- ▶ Design practise for reliable software in **immature** state  
for complex (e.g., distributed) systems.



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A central strategy: [testing](#)

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## Testing against external faults

- ▶ inject faults (memory, communication) by simulation or radiation
- ▶ trace fault propagation

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How to test for the unexpected? Rare cases?
- ▶ Testing is labour intensive, hence expensive

# What **are** Formal Methods

- ▶ Rigorous methods for system design/development/analysis
- ▶ Mathematics and symbolic logic  $\Rightarrow$  **formal**
- ▶ Increase confidence in a system
- ▶ Two aspects:
  - ▶ System **requirements**
  - ▶ System **implementation**
- ▶ Formalise both
- ▶ Use **tools** for
  - ▶ **exhaustive** search for failing scenario, or
  - ▶ mechanical **proof** that implementation satisfies requirements

# What are Formal Methods **for**

- ▶ Complement other analysis and design methods
- ▶ Increase confidence in system correctness
- ▶ Good at finding bugs  
(in code **and** specification)
- ▶ **Ensure** certain properties of the system (model)
- ▶ Should ideally be as automated as possible



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and

- ▶ **Training in Formal Methods increases high quality development skills**

# Specification — What a System **Should** Do

- ▶ Simple properties
  - ▶ Safety properties  
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(in particular for efficient, i.e., redundant, data representations)
  - ▶ Modularity, encapsulation
  - ▶ Refinement relation



# The Main Point of Formal Methods is **Not**

- ▶ to show correctness of entire systems
- ▶ to replace testing
- ▶ to replace good design practises

There is no silver bullet!

- ▶ No correct system w/o clear requirements & good design

# But ...

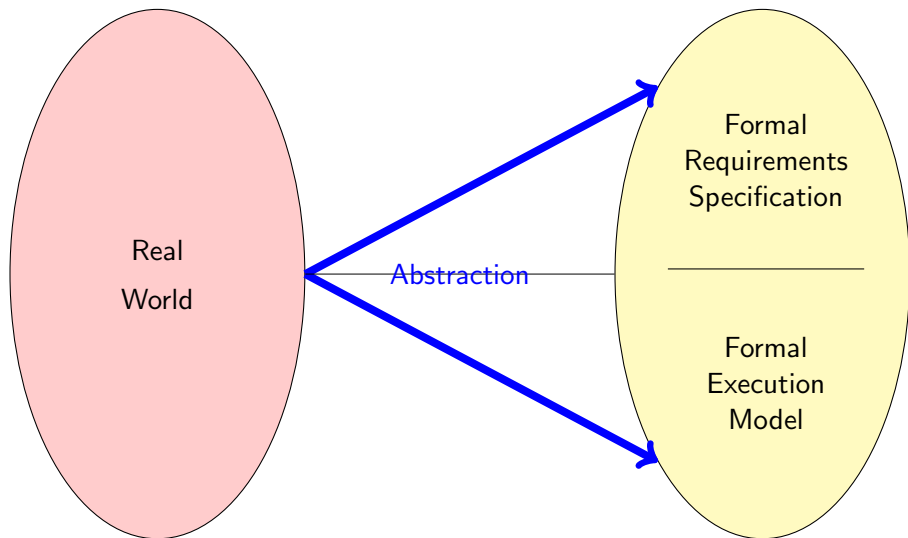
- ▶ Formal proof can replace (infinitely) many test cases
- ▶ Formal methods improve the quality of specs (even without formal verification)
- ▶ Formal methods guarantee specific properties of system (model)

# A Fundamental Fact

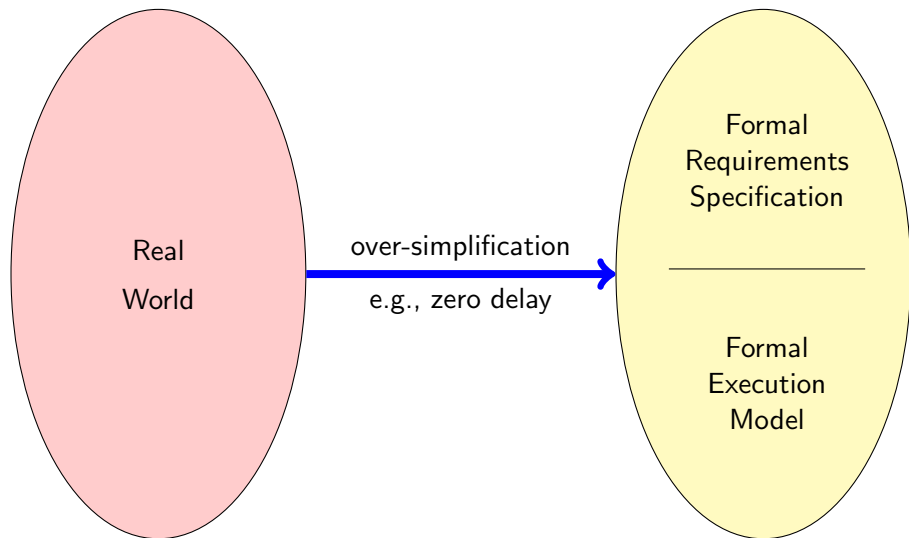
Formalisation of system requirements is hard

Let's see why ...

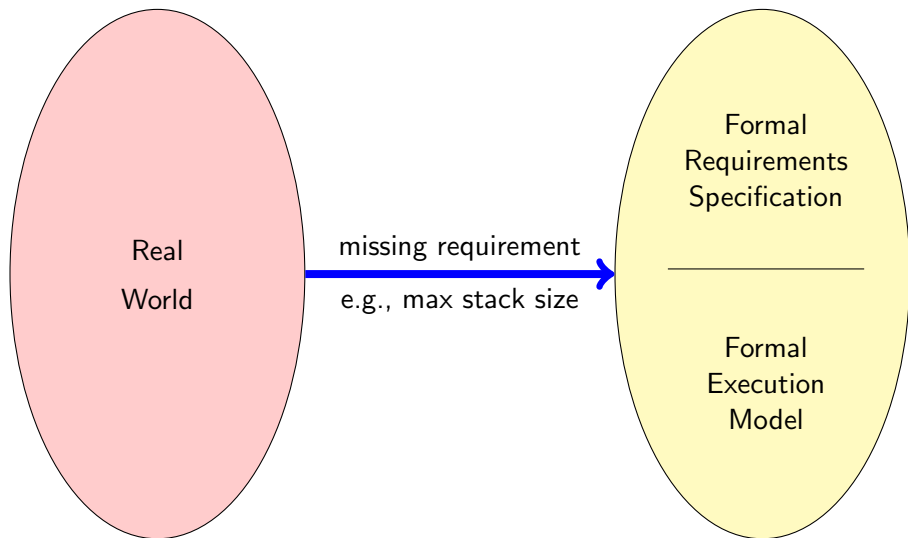
# Difficulties in Creating Formal Models



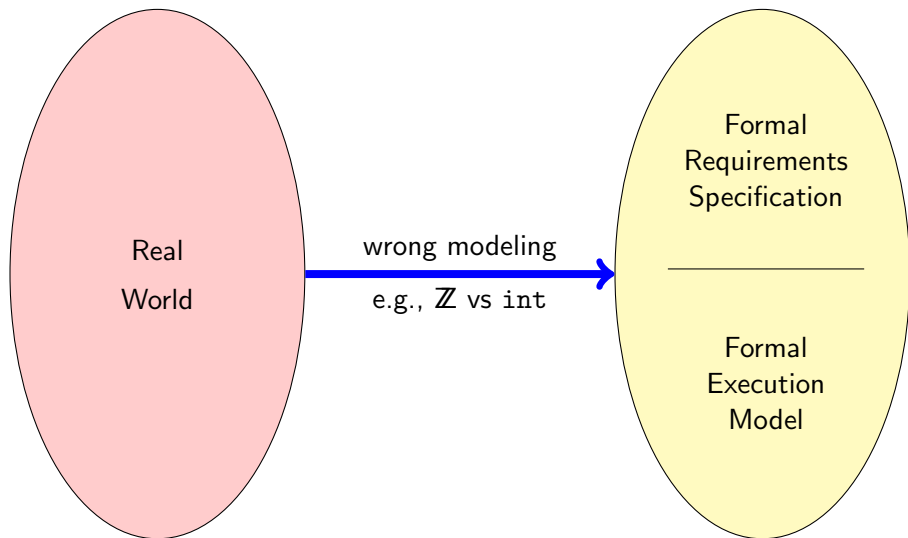
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# Formalization Helps to Find Bugs in Specs

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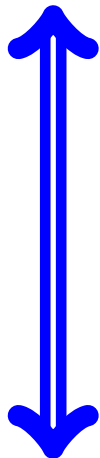
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- ▶ Wellformedness and consistency of formal specs partly machine-checkable
- ▶ Declared signature (symbols) helps to spot incomplete specs
- ▶ Failed verification of implementation against spec gives feedback on erroneous formalization

# Another Fundamental Fact

Proving properties of systems can be hard

# Level of System (Implementation) Description



- ▶ **Abstract level**

- ▶ Finitely many states (bounded size datatypes)
- ▶ Automated proofs are (in principle) possible
- ▶ Simplification, unfaithful modeling inevitable

- ▶ **Concrete level**

- ▶ Unbounded size datatypes  
(pointer chains, dynamic containers, streams)
- ▶ Complex datatypes and control structures
- ▶ Realistic programming model (e.g., Java)
- ▶ Automated proofs hard or impossible!

# Expressiveness of Specification



## ▶ Simple

- ▶ Simple or general properties
- ▶ Finitely many case distinctions
- ▶ Approximation, low precision
- ▶ Automated proofs are (in principle) possible

## ▶ Complex

- ▶ Full behavioural specification
- ▶ Quantification over infinite or large domains
- ▶ High precision, tight modeling
- ▶ Automated proofs hard or impossible!

# Main Approaches

Abstract programs, Simple properties	Abstract programs, Complex properties
Concrete programs, Simple properties	Concrete programs, Complex properties



# Main Approaches

SPIN  
1st part  
of course

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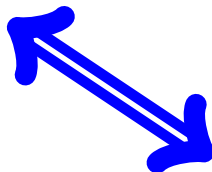
SPIN  
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Abstract programs, Simple properties	Abstract programs, Complex properties
Concrete programs, Simple properties	Concrete programs, Complex properties

KeY  
2nd part  
of course

# Proof Automation

- ▶ “Automated” Proof  
(“batch-mode”)
  - ▶ No interaction (or lemmas) necessary
  - ▶ Proof may fail or result inconclusive  
Tuning of tool parameters necessary
  - ▶ Formal specification still “by hand”
  
- ▶ “Semi-Automated” Proof  
(“interactive”)
  - ▶ Interaction (or lemmas) may be required
  - ▶ Need certain knowledge of tool internals  
Intermediate inspection can help
  - ▶ User steps are checked by tool



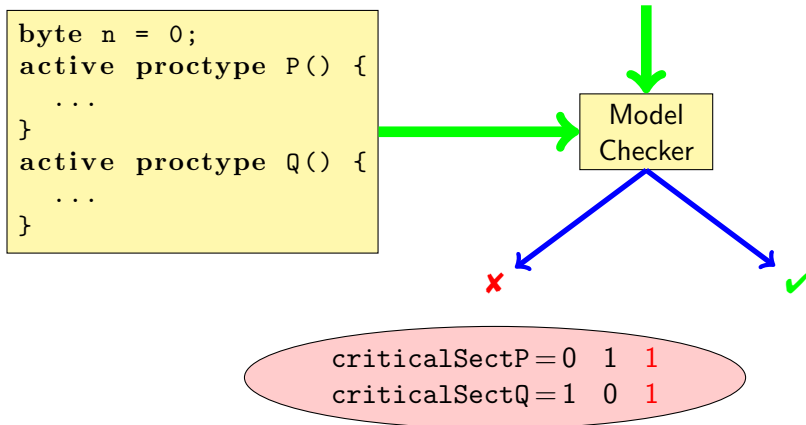
# Model Checking with SPIN

## System Model

```
byte n = 0;  
active proctype P() {  
  ...  
}  
active proctype Q() {  
  ...  
}
```

## System Property

$[\ ] ! (\text{criticalSectP} \ \&\& \ \text{criticalSectQ})$



# Model Checking in Industry—Examples

- ▶ Hardware verification
  - ▶ Good match between limitations of methods and application
  - ▶ Intel, Motorola, AMD, . . .
- ▶ Software verification
  - ▶ Specialized software: control systems, protocols
  - ▶ Typically no direct checking of executable system, but of abstractions
  - ▶ Bell Labs, Microsoft

# A Major Case Study with SPIN

## Checking feature interaction for telephone call processing software

- ▶ Software for PathStar<sup>©</sup> server from Lucent Technologies
- ▶ Automated abstraction of unchanged C code into PROMELA
- ▶ Web interface, with SPIN as back-end, to:
  - ▶ determine properties (ca. 20 temporal formulas)
  - ▶ invoke verification runs
  - ▶ report error traces
- ▶ Finds error trace, reported as C execution trace
- ▶ Work farmed out to 16 computers, daily, overnight runs
- ▶ 18 months, 300 versions of system model, 75 bugs found
- ▶ Strength: detection of undesired feature interactions (difficult with traditional testing)
- ▶ Main challenge: defining meaningful properties

# Deductive Verification with KeY

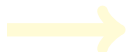
Java Code

Formal specification

# Deductive Verification with KeY

correct?

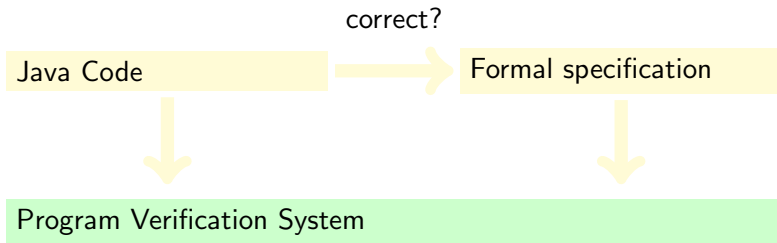
Java Code



Formal specification



# Deductive Verification with KeY



# Deductive Verification with KeY

correct ✓

Java Code

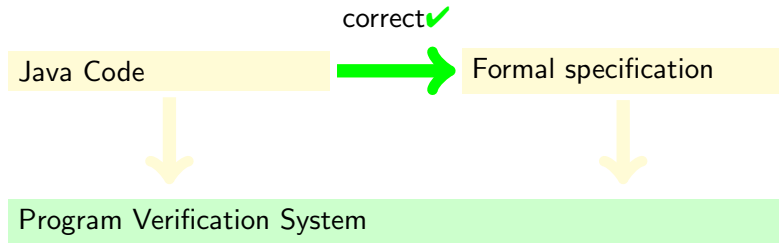


Formal specification



Program Verification System

# Deductive Verification with KeY



Proof rules establish relation “implementation conforms to specs”

**Computer support essential for verification of real programs**

`synchronized StringBuffer append(char c)`

- ▶ ca. 15.000 proof steps
- ▶ ca. 200 case distinctions
- ▶ Two human interactions, ca. 1 minute computing time

# Deductive Verification in Industry—Examples

- ▶ Hardware verification
  - ▶ For complex systems, mostly floating-point processors
  - ▶ Intel, Motorola, AMD, ...
- ▶ Software verification
  - ▶ Safety critical systems:
    - ▶ Paris driver-less metro (Meteor)
    - ▶ Emergency closing system in North Sea
  - ▶ Libraries
  - ▶ Implementations of Protocols

## Java Card 2.2.1 API Reference Implementation

- ▶ Reference implementation and full functional specification
- ▶ All Java Card 2.2.1 API classes and methods
  - ▶ 60 classes; ca. 5,000 LoC (250kB) source code
  - ▶ specification ca. 10,000 LoC
- ▶ Conformant to implementation on actual smart cards
- ▶ All methods fully verified against their spec
  - ▶ 293 proofs; 5–85,000 nodes
- ▶ Total effort several person months
- ▶ Most proofs fully automatic
- ▶ Main challenge: [getting specs right](#)

# Major Case Studies with KeY: Timsort

## Timsort

Hybrid sorting algorithm (insertion sort + merge sort) optimized for partially sorted arrays (typical for real-world data).

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## Timsort is used in

- ▶ Java (standard libraries OpenJDK, Oracle)
- ▶ Python (standard library), used by Google
- ▶ Android (standard library), used by Google
- ▶ ... and many more languages / frameworks!



# Timsort: People



▶ Tim Peters

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- ▶ Sorting Algorithm Designer

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- ▶ Sorting Algorithm Designer
- ▶ Python Guru

# Timsort: People



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- ▶ Stijn de Gouw

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- ▶ Formerly postman in the NL

# Timsort: People

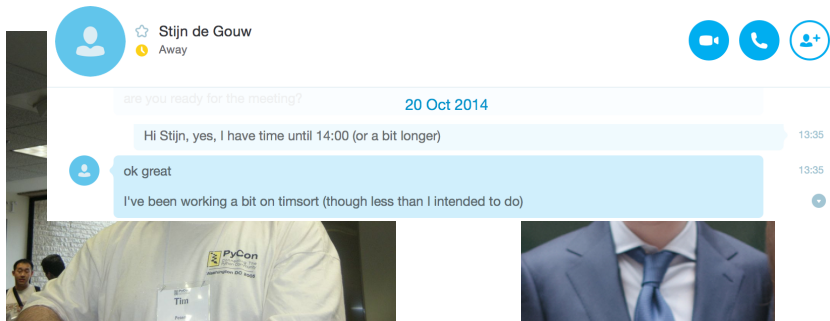


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- ▶ Stijn de Gouw
- ▶ Assistant Professor
- ▶ Formerly postman in the NL
- ▶ Interested in sorting for professional reasons

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# Timsort: People

The screenshot shows a WhatsApp chat interface. At the top left is a profile card for Stijn de Gouw, marked as 'Away'. On the right are icons for video call, voice call, and a contact list. The chat history shows a message from Stijn: "are you ready for the meeting?" dated 20 Oct 2014. A response from Richard follows: "Hi Stijn, yes, I have time until 14:00 (or a bit longer)" at 13:35. Richard then says "ok great" and "I've been working a bit on timsort (though less than I intended to do)" at 13:35. A date separator for 27 Oct 2014 is shown. Richard's message continues: "morning richard" at 08:52, followed by a long message: "don't want to keep this from you, but please keep it to yourself for now... as you know I was working on proving correctness of timsort (the soring algorithm used in the jdk) I figured that the jdk was probably pretty thoroughly tested so went right ahead with specifying rather than debugging the algorithm... but I actually discovered a bug 😊". A response from Stijn says "Cool 😊" at 09:07, followed by "Good morning!".

Stijn de Gouw  
Away

are you ready for the meeting? 20 Oct 2014

Hi Stijn, yes, I have time until 14:00 (or a bit longer) 13:35

ok great 13:35

I've been working a bit on timsort (though less than I intended to do)

27 Oct 2014

morning richard 08:52

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I figured that the jdk was probably pretty thoroughly tested so went right ahead with specifying rather than debugging the algorithm... but I actually discovered a bug 😊

Cool 😊 09:07

Good morning!

professional reasons

# Timsort: People

The screenshot shows a WhatsApp chat interface. At the top left is a profile card for 'Stijn de Gouw' with a star icon and 'Away' status. On the right are icons for video call, voice call, and a group of people. The chat history shows a message from Stijn: 'are you ready for the meeting?' dated '20 Oct 2014'. A reply from the other person says: 'Hi Stijn, yes, I have time until 14:00 (or a bit longer)' at 13:35. Another reply says: 'ok great' at 13:35. A third message says: 'I've been working a bit on timsort (though less than I intended to do)'. A date separator '27 Oct 2014' is shown. A long message from the other person says: 'morning richard' at 08:52, followed by 'don't want to keep this from you, but please keep it to yourself for now... as you know I was working on proving correctness of timsort (the soring algorithm used in the jdk)'. The next line says: 'I figured that the jdk was probably pretty thoroughly tested so went right ahead with specifying rather than debugging the algorithr ... but I actually discovered a bug 😊'. The phrase 'but I actually discovered a bug' is highlighted with a red box. A final reply says: 'Cool 😊' at 09:07, followed by 'Good morning!'. At the bottom, the text 'professional reasons' is written.

Stijn de Gouw  
☆  
🟡 Away

are you ready for the meeting?  
20 Oct 2014

Hi Stijn, yes, I have time until 14:00 (or a bit longer) 13:35

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professional reasons

## Found Bug in Java Libraries' main Sorting Method using KeY

- ▶ `java.util.Collections.sort` and `java.util.Arrays.sort` implement **Timsort**
- ▶ KeY verification of **OpenJDK** implementation revealed *bug*.
- ▶ **Same bug** present in **Android** SDK, **Oracle's** JDK, **Phyton** library, **Haskell** library

# Major Case Studies with KeY

## Found Bug in Java Libraries' main Sorting Method using KeY

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- ▶ **Same bug** present in **Android** SDK, **Oracle's** JDK, **Phyton** library, **Haskell** library

## Verified Fix using KeY

- ▶ Fixing the implementation
- ▶ Verified new version with KeY

# Major Case Studies with KeY

## Found Bug in Java Libraries' main Sorting Method using KeY

- ▶ `java.util.Collections.sort` and `java.util.Arrays.sort` implement **Timsort**
- ▶ KeY verification of `Arrays.sort` revealed *bug*.
- ▶ **Same bug** previously found by researchers in Haskell, `Python` library,

Some researchers found an error in the logic of merge\_collapse, explained here, and with corrected code shown in

## Verified

- ▶ Fixing
- ▶ Verified

It should be fixed anyway, and their suggested fix looks good to me.

**Tim Peters via Python-Bugtracker**

# Major Case Studies with KeY

## Found Bug in Java Libraries' main Sorting Method using KeY

- ▶ `java.util.Collections.sort` and `java.util.Arrays.sort` implemented `TimSort`
- ▶ KeY verified an error in the implementation, *revealed bug.*
- ▶ Same error was shown in `Python` library, `Haskell`

Congratulations to Stijn de Gouw et al. for finding and fixing a bug in TimSort using formal methods!

Some of the authors of their suggestion: **Joshua Bloch** via **Twitter**

It should be fixed. Suggested fix looks good. **Tim Peters** via **Twitter**

## Verified

- ▶ Fixing
- ▶ Verified with KeY

# Tool Support is Essential

## Some Reasons for Using Tools

- ▶ Automate repetitive tasks
- ▶ Avoid typos, etc.
- ▶ Cope with large/complex programs
- ▶ Make verification certifiable

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## Tools used in this course:

**SPIN** to verify PROMELA programs against Temporal Logic specs

**SPIN web interface** developed for this course!

**JSPIN** front-end for SPIN

**KeY** to verify Java programs against contracts in JML

All are free and run on Windows/Unixes/Mac.



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All are free and run on Windows/Unixes/Mac.

**Install first SPIN and JSPIN on your computer,  
or make sure the SPIN web interface works.**

# You will gain experience in ...

- ▶ Modelling, and modelling languages

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- ▶ Modelling, and modelling languages
- ▶ Specification, and specification languages

# You will gain experience in ...

- ▶ Modelling, and modelling languages
- ▶ Specification, and specification languages
- ▶ In depth analysis of possible system behaviour

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- ▶ Reasoning about system (mis)behaviour
- ▶ ...

# Learning Outcomes—Knowledge and Understanding

- ▶ Explain the potential and limitations of using logic based verification methods for assessing and improving software correctness
- ▶ Identify what can and what cannot be expressed by certain specification/modeling formalisms
- ▶ Identify what can and cannot be analyzed with certain logics and proof methods



# Learning Outcomes—Skills and Abilities

- ▶ Express safety and liveness properties of (concurrent) programs in a formal way
- ▶ Describe the basics of verifying safety and liveness properties via model checking
- ▶ Successfully employ tools which prove or disprove temporal properties
- ▶ Write formal specifications of object-oriented system units, using the concepts of method contracts and class invariants
- ▶ Describe how the connection between programs and formal specifications can be represented in a program logic
- ▶ Verify functional properties of simple Java programs with a verification tool

# Learning Outcomes—Judgment and Approach

- ▶ Judge and communicate the significance of correctness for software development
- ▶ Employ abstraction, modelling, and rigorous reasoning when approaching the development of correctly functioning software

# Literature for this Lecture

- FM in SE** B. Beckert, R. Hähnle, T. Hoare, D. Smith, C. Green, S. Ranise, C. Tinelli, T. Ball, and S. K. Rajamani: *Intelligent Systems and Formal Methods in Software Engineering*. IEEE Intelligent Systems, 21(6):71–81, 2006  
(Access to e-version via Chalmers Library)
- KeY** R. Hähnle: *Quo Vadis Formal Verification*. In: W. Ahrendt, B. Beckert, R. Bubel, R. Hähnle, P. Schmitt, M. Ulbrich editors. Vol 10001 of *LNCS*, Springer, 2016  
(E-book at [link.springer.com](http://link.springer.com))
- SPIN** Gerard J. Holzmann: *A Verification Model of a Telephone Switch*. In: *The Spin Model Checker*, Chapter 14, Addison Wesley, 2004