

# Formal Methods for Software Development

## Modeling Concurrency

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# Concurrent Systems – The Big Picture

Concurrency: different processes trying not to run into each others' way

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Shared resource = crossing, bikers = processes,  
and a (data) race in progress, approaching a disaster.

Solutions to this must be carefully **designed** and **verified**, otherwise. . .

# Concurrent Systems – The Big Picture



# Focus of this Lecture

Aim of SPIN-style model checking methodology:

exhibit

flaws in

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Focus of next lecture:

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  - ▶ reliability of communication media

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- ▶ lack of reproducibility  
⇒ even if failures appear in test phase,  
often impossible to analyze/debug defect
- ▶ lack of time  
exhaustive testing exhausts the testers long before it exhausts  
behavior of the system...



# Mission of SPIN-style Model Checking

offer an efficient methodology to

- ▶ improve the design
- ▶ exhibit defects

of concurrent and distributed systems

# Activities in SPIN-style Model Checking

1. model (critical aspects of) concurrent/distributed system with PROMELA
2. state crucial properties with assertions, temporal logic, ...
3. use SPIN to check all possible runs of the model
4. analyze result, possibly re-work 1. and 2.

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Separate concerns of model vs. property! Check the property you want the model to have, not the one it happens to have.

# Main Challenges of Modeling

## expressiveness

Model must be expressive enough to 'embrace' defects the real system could have

## simplicity

Model must be simple enough to be 'model checkable', theoretically and practically

# Modeling Concurrent Systems in Promela

In the SPIN approach,  
the cornerstone of modeling concurrent/distributed systems are

PROMELA processes.

# Initializing Processes

Can be instantiated *implicitly* using 'active'.

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Can be instantiated *implicitly* using 'active'.

Can be instantiated *explicitly* with key word 'init'

```
init {  
    printf("Hello_world\n")  
}
```

`init` is used to start other processes with `run` statement.

# Starting Processes

Processes can be started *explicitly* using `run`

```
proctype P() {  
    byte x;  
    ...  
}
```

```
init {  
    run P();  
    run P()  
}
```

Each `run` operator starts copy of process (with copy of local variables)



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Each `run` operator starts copy of process (with copy of local variables)

`run P()` does *not* wait for P to finish

(PROMELA's `run` corresponds to JAVA's `start`, *not* to JAVA's `run`)

# Atomic Start of Multiple Processes

By convention, run operators enclosed in atomic block

```
proctype P() {  
    byte x;  
    ...  
}
```

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init {  
    atomic {  
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Effect: processes only start executing once all are created

(More on `atomic` later)

# Joining Processes

*joining*: waiting for all other processes to finish

```
byte result;
```

```
proctype P() {  
    ...  
}
```

```
init {  
    atomic {  
        run P();  
        run P()  
    }  
    (_nr_pr == 1); /*blocks until join*/  
    printf("result_□=%d", result)  
}
```

# Joining Processes

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byte result;
```

```
proctype P() {
```

```
    ...
```

```
}
```

```
init {
```

```
    atomic {
```

```
        run P();
```

```
        run P();
```

```
    }
```

```
    (_nr_pr == 1); /*blocks until join*/
```

```
    printf("result_□=%d", result)
```

```
}
```

`_nr_pr` built-in variable holding number of running processes

`_nr_pr == 1` only 'this' process (init) is (still) running

# Process Parameters

Processes may have formal parameters, instantiated by `run`:

```
proctype P(byte id; byte incr) {  
    ...  
}  
  
init {  
    run P(7, 10);  
    run P(8, 15)  
}
```



# Active (Sets of) Processes

init can be made **implicit** by using the active modifier:

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active proctype P() {  
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```
active [n] proctype P() {  
    ...  
}
```

Implicit init will run **n copies** of P

# Local and Global Data

Variables declared **outside** of the processes are **global** to all processes.

Variables declared **inside** a process are **local** to that processes.

```
byte n;
```

```
proctype P(byte id; byte incr) {  
    byte t;  
    ...  
}
```

n is **global**

t is **local**

# Modeling with Global Data

Pragmatics of modeling with global data:

**Shared memory** of concurrent systems often modeled by global variables of numeric (or array) type

**Status of shared resources** (printer, traffic light, ...) often modeled by global variables of Boolean or enumeration type (`bool/mtype`).

**Communication mediums** of distributed systems often modeled by global variables of channel type (`chan`). (next lecture)

# Interference on Global Data

```
byte n = 0;

active proctype P() {
    n = 1;
    printf("Proc P, n=%d\n", n)
}
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How many outputs possible?

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How many outputs possible?

Different processes can interfere on global data



# Examples

1. `interleave0.pml`  
SPIN simulation, SPINSPIDER automata + transition system
2. `interleave1.pml`  
SPIN simulation, adding assertion, fine-grained execution model, model checking
3. `interleave5.pml`  
SPIN simulation, SPIN model checking, trail inspection

# Synchronization on Global Data

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Executability addresses many issues in the interplay of processes.

Most synchronization primitives (test & set, compare & swap, semaphores, ...) can be modeled w. *executability and atomicity*.

# Executability

Each statement has the notion of executability.

Executability of **basic statements**:

<i>statement type</i>	<i>executable</i>
assignment	always
assertion	always
print statement	always
<i>expression statement</i>	
send/receive statement	

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send/receive statement	(next lecture)

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(Inspect end.pml)

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# Executability and Blocking

## Definition (Blocking)

A **statement blocks** iff it is *not* executable.

A **process blocks** iff its location counter points to a blocking statement.

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Executability, resp. blocking are the key to PROMELA-style modeling of solutions to synchronization problems.

## Definition (Deadlock (simplified))

Let  $CRP$  be the set of currently running processes.

A **deadlock** is a point in the execution where

- ▶  $CRP \neq \emptyset$
- ▶ all  $p \in CRP$  are blocking

(Verify end.pml)

## Definition (End Location)

End locations of a process P are:

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- ▶ P's textual end
- ▶ each location marked with an end label: "endxxx:"

## Definition (Deadlock (full version))

Let  $CRP$  be the set of currently running processes.

Let  $NEL \subseteq CRP$  be the set of (currently running) processes which are *not* at a valid end location.

A **deadlock** is a point in the execution where

- ▶  $NEL \neq \emptyset$
- ▶ all  $p \in NEL$  are blocking

# Deadlock Detection

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(Fix `end.pml`)

# Atomicity

limit the possibility of sequences being interrupted by other processes

## weakly atomic sequence

can *only* be interrupted when a statement blocks

## strongly atomic sequence

cannot be interrupted at all

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## weakly atomic sequence

can *only* be interrupted when a statement blocks  
defined in PROMELA by `atomic{list_of_statements}`

## strongly atomic sequence

cannot be interrupted at all  
defined in PROMELA by `d_step{list_of_statements}`

## Executability (Cont'd)

atomic resp. `d_step` statement is executable  
iff  
guard (i.e., the first inner statement) is executable

# Deterministic Sequences

`d_step`:

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# Deterministic Sequences

`d_step`:

- ▶ strongly atomic
- ▶ deterministic (like a single `step`)
- ▶ choices resolved in fixed way (always take the first possible option)  
⇒ avoid choices in `d_step`
- ▶ it is an error if any statement within `d_step`,  
*other than the first one* (called '*guard*'), blocks

```
d_step {  
    stmt1; ← guard  
    stmt2;  
    stmt3  
}
```

If `stmt1` blocks, `d_step` is **not entered**, and blocks as a whole.

It is an **error** if `stmt2` or `stmt3` block.



# (Weakly) Atomic Sequences

**atomic:**

- ▶ weakly atomic
- ▶ can be non-deterministic

```
atomic {  
    stmt1; ← guard  
    stmt2;  
    stmt3  
}
```

If *guard* blocks, **atomic** is **not entered**, and blocks as a whole.

Once **atomic** is entered, control is kept until a statement blocks, and **only in this case** passed to another process.

# The Critical Section Problem

Archetypal problem of concurrent systems

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Given a number of looping processes, each containing a **critical section**, design an algorithm such that:

**Mutual Exclusion** At most one process is executing its critical section at any time.

**Absence of Deadlock** If *some* processes are trying to enter their critical sections, then *one* of them must eventually succeed.

**Absence of (individual) Starvation** If *any* process tries to enter its critical section, then *that* process must eventually succeed.

# Critical Section Pattern

For demonstration and simplicity:

Noncritical and critical sections only `printf` statements here

```
active proctype P() {
  do :: printf("P_non-critical_actions\n");
      /* begin critical section */
      printf("P_uses_shared_resources\n")
      /* end critical section */
od
}
```

```
active proctype Q() {
  do :: printf("Q_non-critical_actions\n");
      /* begin critical section */
      printf("Q_uses_shared_resources\n")
      /* end critical section */
od
}
```



# No Mutual Exclusion Yet

More infrastructure to achieve ME.

Adding two Boolean flags:

```
bool P_in_CS = false;
bool Q_in_CS = false;

active proctype P() {
    do :: printf("P_non-critical_actions\n");
        P_in_CS = true;
        /* begin critical section */
        printf("P_uses_shared_resources\n");
        /* end critical section */
        P_in_CS = false
    od
}

active proctype Q() {
    ...correspondingly...
}
```

## Show Mutual Exclusion VIOLATION with SPIN

adding assertions

```
bool P_in_CS = false;
bool Q_in_CS = false;

active proctype P() {
    do :: printf("P non-critical actions\n");
        P_in_CS = true;
        /* begin critical section */
        printf("P uses shared resources\n");
        assert(!Q_in_CS);
        /* end critical section */
        P_in_CS = false
    od
}

active proctype Q() {
    .....assert(!P_in_CS);.....
}
```

# Mutual Exclusion by Busy Waiting

```
bool P_in_CS = false;
bool Q_in_CS = false;

active proctype P() {
    do :: printf("P_in_non-critical_actions\n");
        P_in_CS = true;
        do :: !Q_in_CS -> break
            :: else -> skip
        od;
        /* begin critical section */
        printf("P_in_uses_shared_resources\n");
        assert(!Q_in_CS);
        /* end critical section */
        P_in_CS = false
    od
}

active proctype Q() { ...correspondingly... }
```

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Instead of Busy Waiting, process should

1. yield control,
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Instead of Busy Waiting, process should

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We use **expression statement** `!Q_in_CS`  
to let process P **block** where it should not proceed!

# Mutual Exclusion by Blocking

```
active proctype P() {
  do :: printf("P_\u00a0non-critical_\u00a0actions\n");
      P_in_CS = true;
      !Q_in_CS;
      /* begin critical section */
      printf("P_\u00a0uses_\u00a0shared_\u00a0resources\n");
      assert(!Q_in_CS);
      /* end critical section */
      P_in_CS = false
od
}
```

  

```
active proctype Q() {
  ...correspondingly...
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# Verify Mutual Exclusion of this

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SPIN error (invalid end state)

⇒ deadlock



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can make pan ignore the deadlock: `./pan -E`

SPIN still reports assertion violation(!)

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In this example:

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In this example:

- ▶ mutual exclusion (ME) cannot be shown by SPIN
- ▶  $P/Q\_in\_CS$  sufficient for *achieving* ME
- ▶  $P/Q\_in\_CS$  *not* sufficient for *proving* ME

# Proving Mutual Exclusion

In this example:

- ▶ mutual exclusion (ME) cannot be shown by SPIN
- ▶  $P/Q\_in\_CS$  sufficient for *achieving* ME
- ▶  $P/Q\_in\_CS$  *not* sufficient for *proving* ME

Need more infrastructure.

**Ghost variables:** variables for verification, not for modeling

# Show Mutual Exclusion with Ghost Variable

```
int critical = 0;

active proctype P() {
  do :: printf("P_\u25a1non-critical_\u25a1actions\n");
      P_in_CS = true;
      !Q_in_CS;
      /* begin critical section */
      critical++;
      printf("P_\u25a1uses_\u25a1shared_\u25a1resources\n");
      assert(critical < 2);
      critical--;
      /* end critical section */
      P_in_CS = false
    od
}

active proctype Q() {
  ...correspondingly...
}
```

# Verify Mutual Exclusion of this

SPIN (./pan -E) shows no assertion is violated  
⇒ mutual exclusion is verified



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Still SPIN (without -E) reports (invalid end state)

⇒ deadlock

# Deadlock Hunting

## Invalid End State:

- ▶ A process does not finish at its end
- ▶ OK if it is not crucial to continue – add end labels (see `end.pml`)
- ▶ If it is crucial to continue:  
Real **deadlock**

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Real **deadlock**

## Address Deadlock with SPIN:

- ▶ Verify to produce a failing run trail
- ▶ Simulate to see how the processes get to the interlock
- ▶ Fix the code (not using the end labels nor `-E` option)

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checking and setting the flag in one atomic step

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atomic {  
    !Q_in_CS;  
    P_in_CS = true  
}
```

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- ▶ ... and many more

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Using `atomic` and `d_step` too heavily, for too large blocks, can result in well-behaved models, while modeling the wrong system.