

# Parallel Functional Programming

## Lecture 3

Mary Sheeran

with thanks to Simon Marlow for use of slides  
and to Koen Claessen for the guest appearance

<http://www.cse.chalmers.se/edu/course/pfp>

# par and pseq

MUST

Pass an unevaluated computation to par

It must be somewhat expensive

Make sure the result is not needed for a bit

Make sure the result is shared by the rest of the program

# par and pseq

MUST

Pass an unevaluated computation to par

It must be somewhat expensive

Make sure the result is not needed for a bit

Make sure the result is shared by most of the program

Demands an operational understanding of program execution

# Eval monad plus Strategies

Eval monad enables expressing ordering between instances of `par` and `pseq`

Strategies separate algorithm from parallelisation

Provide useful higher level abstractions

But still demand an understanding of laziness

## A monad for deterministic parallelism

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### Abstract

We present a new programming model for deterministic parallel computation in a pure functional language. The model is monadic and has explicit granularity, but allows dynamic construction of dataflow networks that are scheduled at runtime, while remaining deterministic and pure. The implementation is based on monadic concurrency, which has until now only been used to simulate concurrency in functional languages, rather than to provide parallelism. We present the API with its semantics, and argue that parallel execution is deterministic. Furthermore, we present a complete work-stealing scheduler implemented as a Haskell library, and we show that it performs at least as well as the existing parallel programming models in Haskell.

pure interface, while allowing a parallel implementation. We give a formal operational semantics for the new interface.

Our programming model is closely related to a number of others; a detailed comparison can be found in Section 8. Probably the closest relative is *parH* (Nikhil 2001), a variant of Haskell that also has *I*-structures; the principal difference with our model is that the monad allows us to retain referential transparency, which was lost in *parH* with the introduction of *I*-structures. The target domain of our programming model is large-grained irregular parallelism, rather than fine-grained regular data parallelism (for the latter Data Parallel Haskell (Chakravarty et al. 2007) is more appropriate).

Our implementation is based on *monadic concurrency* (Scholz 1995), a technique that has previously been used to good effect to simulate concurrency in a sequential functional language (Claessen

# Builds on Koen's paper

## FUNCTIONAL PEARLS

### *A Poor Man's Concurrency Monad*

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#### Abstract

Without adding any primitives to the language, we define a concurrency monad transformer in Haskell. This allows us to add a limited form of concurrency to any existing monad. The atomic actions of the new monad are lifted actions of the underlying monad. Some extra operations, such as `fork`, to initiate new processes, are provided. We discuss the implementation, and use some examples to illustrate the usefulness of this construction.

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# the Par Monad

Our goal with this work is to find a parallel programming model that is expressive enough to subsume Strategies, robust enough to reliably express parallelism, and accessible enough that non-expert programmers can achieve parallelism with little effort.

# The **Par** Monad

```
data Par
instance Monad Par
```

Par is a monad for parallel computation

```
runPar :: Par a -> a
```

Parallel computations are pure (and hence deterministic)

```
fork :: Par () -> Par ()
```

forking is *explicit*

```
data IVar
```

```
new :: Par (IVar a)
```

```
get :: IVar a -> Par a
```

```
put :: NFData a => IVar a -> a -> Par ()
```

results are communicated through IVars

# IVar

a write-once mutable reference cell

supports two operations: `put` and `get`

`put` assigns a value to the IVar, and may only be executed once per IVar

Subsequent puts are an error

`get` waits until the IVar has been assigned a value, and then returns the value

# the Par Monad

Implemented as a Haskell library

surprisingly little code!

includes a work stealing scheduler

You get to roll your own schedulers!

Programmer has more control than with Strategies

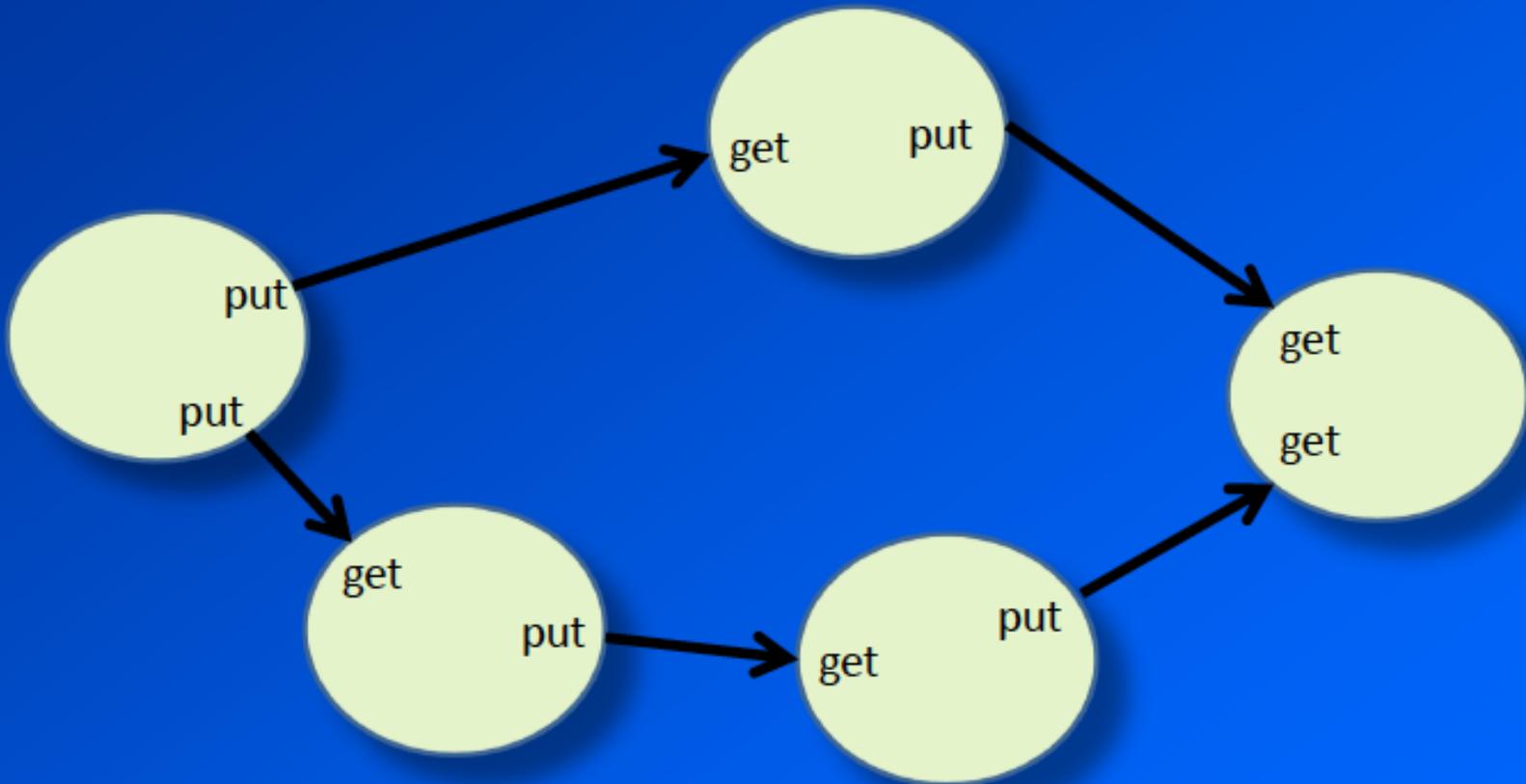
=> less error prone?

Good performance (comparable to Strategies)

particularly if granularity is not too small

# Par expresses dynamic dataflow

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```
runPar $ do
```

```
  i <- new
```

```
  j <- new
```

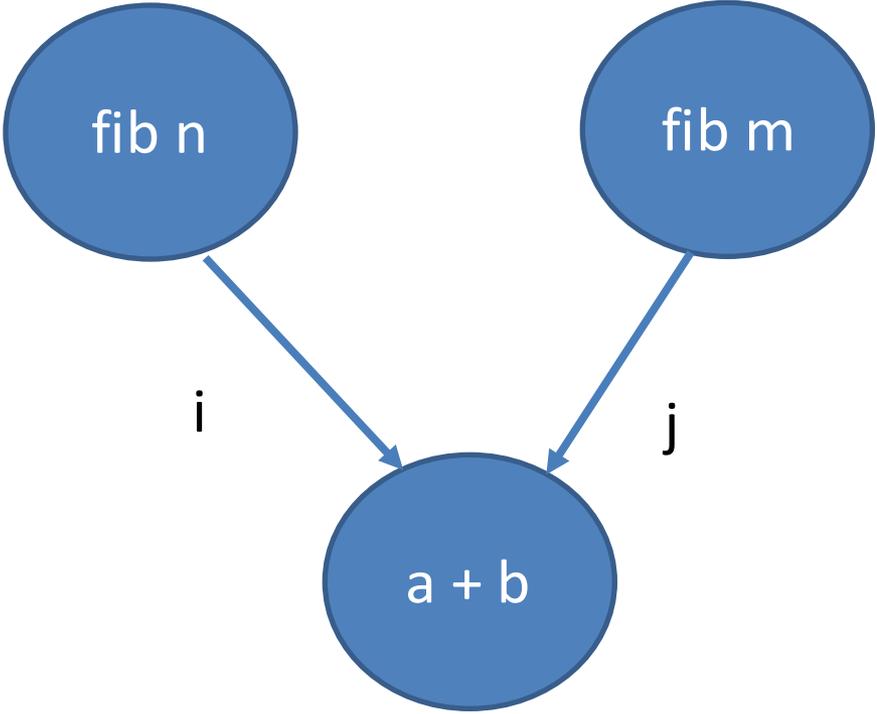
```
  fork (put i (fib n))
```

```
  fork (put j (fib m))
```

```
  a <- get i
```

```
  b <- get j
```

```
  return (a+b)
```



```
spawn :: NFData a => Par a -> Par (IVar a)
spawn p = do
    i <- new
    fork (do x <- p; put i x)
    return i
```

```
parMapM :: NFData b => (a -> Par b) -> [a] -> Par [b]
parMapM f as = do
  ibs <- mapM (spawn . f) as
  mapM get ibs
```

```
search :: ( partial -> Maybe solution )  
        -> ( partial -> [ partial ] )  
        -> partial  
        -> [solution]
```

See PCPH ch. 4

```
search :: ( partial -> Maybe solution )
        -> ( partial -> [ partial ] )
        -> partial
        -> [solution]
search finished refine emptysoln = generate emptysoln
  where generate partial
        | Just soln <- finished partial = [soln]
        | otherwise = concat (map generate (refine partial))
```

```
parsesearch :: NFData solution
    => ( partial -> Maybe solution )
    -> ( partial -> [ partial ] )
    -> partial
    -> [solution]
parsesearch finished refine emptysoln
= runPar $ generate emptysoln
where
    generate partial
    | Just soln <- finished partial = return [soln]
    | otherwise = do
        solnss <- parMapM generate (refine partial)
        return (concat solnss)
```

# needs granularity control

```
parsesearch :: NFData solution
            => Int
            -> ( partial -> Maybe solution ) -- finished?
            -> ( partial -> [ partial ] ) -- refine a solution
            -> partial -- initial solution
            -> [solution]

parsesearch maxdepth finished refine emptysoln
= runPar $ generate 0 emptysoln
where
  generate d partial | d >= maxdepth
    = return (search finished refine partial)
  generate d partial
    | Just soln <- finished partial = return [soln]
    | otherwise = do
      solnss <- parMapM (generate (d+1)) (refine partial)
      return (concat solnss)
```

# Dataflow problems

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- Par really shines when the problem is easily expressed as a dataflow graph, particularly an irregular or dynamic graph (e.g. shape depends on the program input)
- Identify the nodes and edges of the graph
  - each node is created by fork
  - each edge is an IVar

# Implementation

---

- Starting point: A Poor Man's Concurrency Monad (Claessen JFP'99)
- PMC was used to *simulate* concurrency in a sequential Haskell implementation. We are using it as a way to implement very lightweight non-preemptive threads, with a parallel scheduler.
- Following PMC, the implementation is divided into two:
  - **Par** computations produce a lazy **Trace**
  - A scheduler consumes the Traces, and switches between multiple threads

# Trace

```
data Trace = forall a . Get (IVar a) (a -> Trace)
           | forall a . Put (IVar a) a Trace
           | forall a . New (IVarContents a) (IVar a -> Trace)
           | Fork Trace Trace
           | Done
           | Yield Trace
           | forall a . LiftIO (IO a) (a -> Trace)
```

# The Par monad

---

- Par is a CPS monad:

```
newtype Par a = Par {
  runCont :: (a -> Trace) -> Trace
}

instance Monad Par where
  return a = Par $ \c -> c a
  m >>= k = Par $ \c -> runCont m $
    \a -> runCont (k a) c
```

# Operations

---

```
fork :: Par () -> Par ()
fork p = Par $ \c ->
    Fork (runCont p (\_ -> Done)) (c ())

new :: Par (IVar a)
new = Par $ \c -> New c

get :: IVar a -> Par a
get v = Par $ \c -> Get v c

put :: NFData a => IVar a -> a -> Par ()
put v a = deepseq a (Par $ \c -> Put v a (c ()))
```

e.g.

---

- This code:

```
do
  x <- new
  fork (put x 3)
  r <- get x
  return (r+1)
```

- will produce a trace like this:

```
New (\x ->
  Fork (Put x 3 $ Done)
      (Get x (\r ->
        c (r + 1))))
```

# The scheduler

- First, a sequential scheduler.

```
sched :: SchedState -> Trace -> IO ()  
type SchedState = [Trace]
```

The currently running thread

The work pool,  
“runnable threads”

Why IO?  
Because we’re going  
to extend it to be a  
parallel scheduler in a  
moment.

# Representation of IVar

```
newtype IVar a = IVar (IORef (IVarContents a))
```

# Representation of IVar

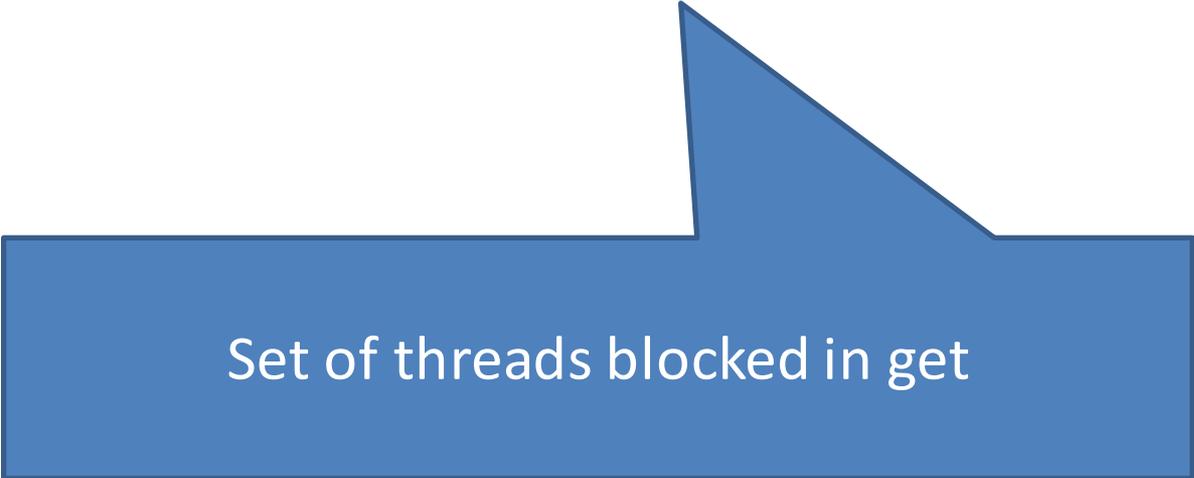
```
newtype IVar a = IVar (IORef (IVarContents a))
```

```
data IVarContents a = Full a | Empty | Blocked [a -> Trace]
```

# Representation of IVar

```
newtype IVar a = IVar (IORef (IVarContents a))
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```
data IVarContents a = Full a | Empty | Blocked [a -> Trace]
```



Set of threads blocked in get

```
reschedule :: SchedState -> IO ()
reschedule [] = return ()
reschedule (t:ts) = sched ts t
```

**sched state done = reschedule state**

```
sched state (Fork child parent)
  = sched (child:state) parent
```

# New and Get

---

```
sched state (New f) = do
  r <- newIORef (Blocked [])
  sched state (f (IVar r))
```

```
sched state (Get (IVar v) c) = do
  e <- readIORef v
  case e of
    Full a -> sched state (c a)
    Blocked cs -> do
      writeIORef v (Blocked (c:cs))
      reschedule state
```

# Put

```
sched state (Put (IVar v) a t) = do
  cs <- modifyIORef v $ \e -> case e of
    Empty -> (Full a, [])
    Full _ -> error "multiple put"
    Blocked ds -> (Full a, ds)
  let state' = map ($ a) cs ++ state
  sched state' t
```

```
modifyIORef :: IORef a -> (a -> (a,b)) -> IO b
```

# Put

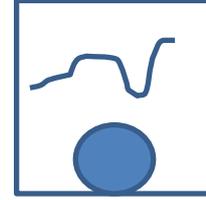
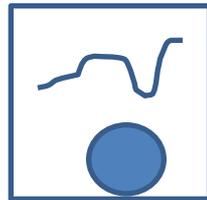
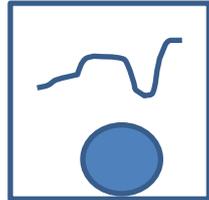
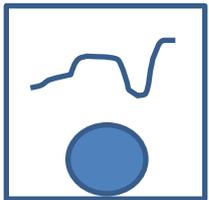
```
sched state (Put (IVar v) a t) = do
  cs <- modifyIORef v $ \e -> case e of
    Empty -> (Full a, [])
    Full _ -> error "multiple put"
    Blocked ds -> (Full a, ds)
  let state' = map ($ a) cs ++ state
  sched state' t
```

Wake up blocked threads  
Add them to work pool

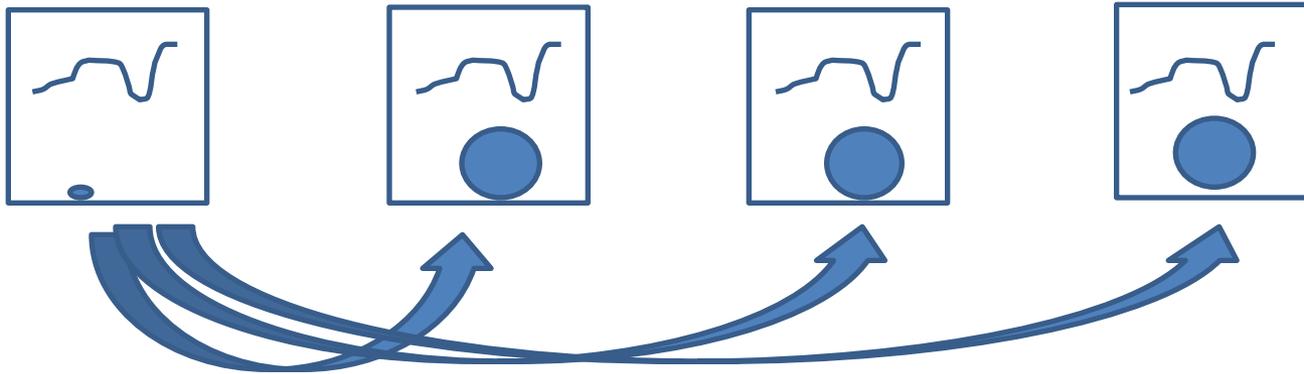
```
modifyIORef :: IORef a -> (a -> (a,b)) -> IO b
```

# Parallel scheduler

One scheduler thread per core, each with a work pool

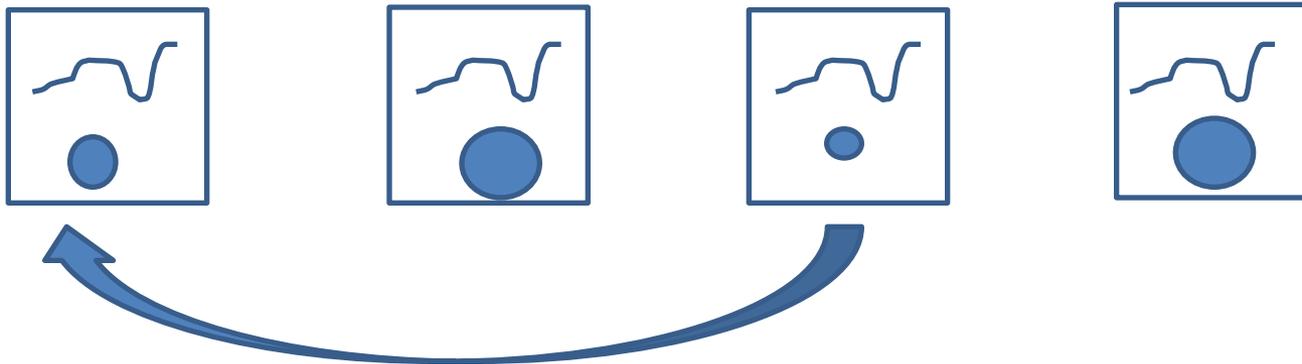


When work pool dries up attempts to steal from other work pools



# success

When work pool dries up attempts to steal from other work pools



If no work to be found, worker thread becomes idle (and is added to shared list of idle workers)

A worker thread that creates a new work item wakes up one of these idle workers

When all work pools are empty, computation is complete and **runPar** returns

# The code is readable!

```

sched :: Sched -> Trace -> IO ()
sched queue t = loop t
  where
    loop t = case t of
      New a f -> do
        r <- newIORef a
        loop (f (IVar r))
      Get (IVar v) c -> do
        e <- readIORef v
        case e of
          Full a -> loop (c a)
          _other -> do
            r <- atomicModifyIORef v $ \e -> case e of
              Empty -> (Blocked [c], reschedule queue)
              Full a -> (Full a, loop (c a))
              Blocked cs ->
                (Blocked (c:cs), reschedule queue) r

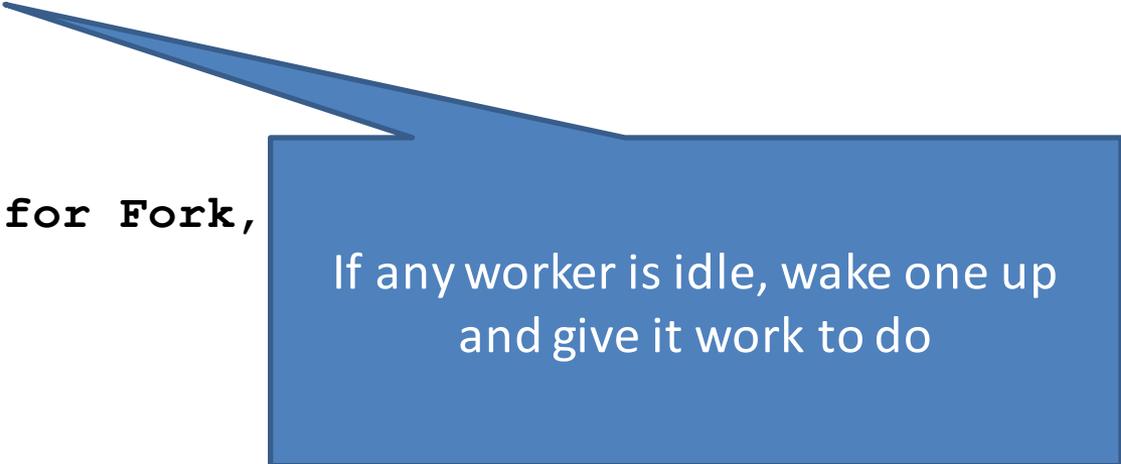
```

```
Put (IVar v) a t -> do
  cs <- atomicModifyIORef v $ \e -> case e of
    Empty -> (Full a, [])
    Full _ -> error "multiple put"
    Blocked cs -> (Full a, cs)
  mapM_ (pushWork queue. ($a)) cs
  loop t
```

```
. . .      -- Cases for Fork, Done, Yield, LiftIO
```

```
Put (IVar v) a t -> do
  cs <- atomicModifyIORef v $ \e -> case e of
    Empty -> (Full a, [])
    Full _ -> error "multiple put"
    Blocked cs -> (Full a, cs)
  mapM_ (pushWork queue. ($a)) cs
  loop t
```

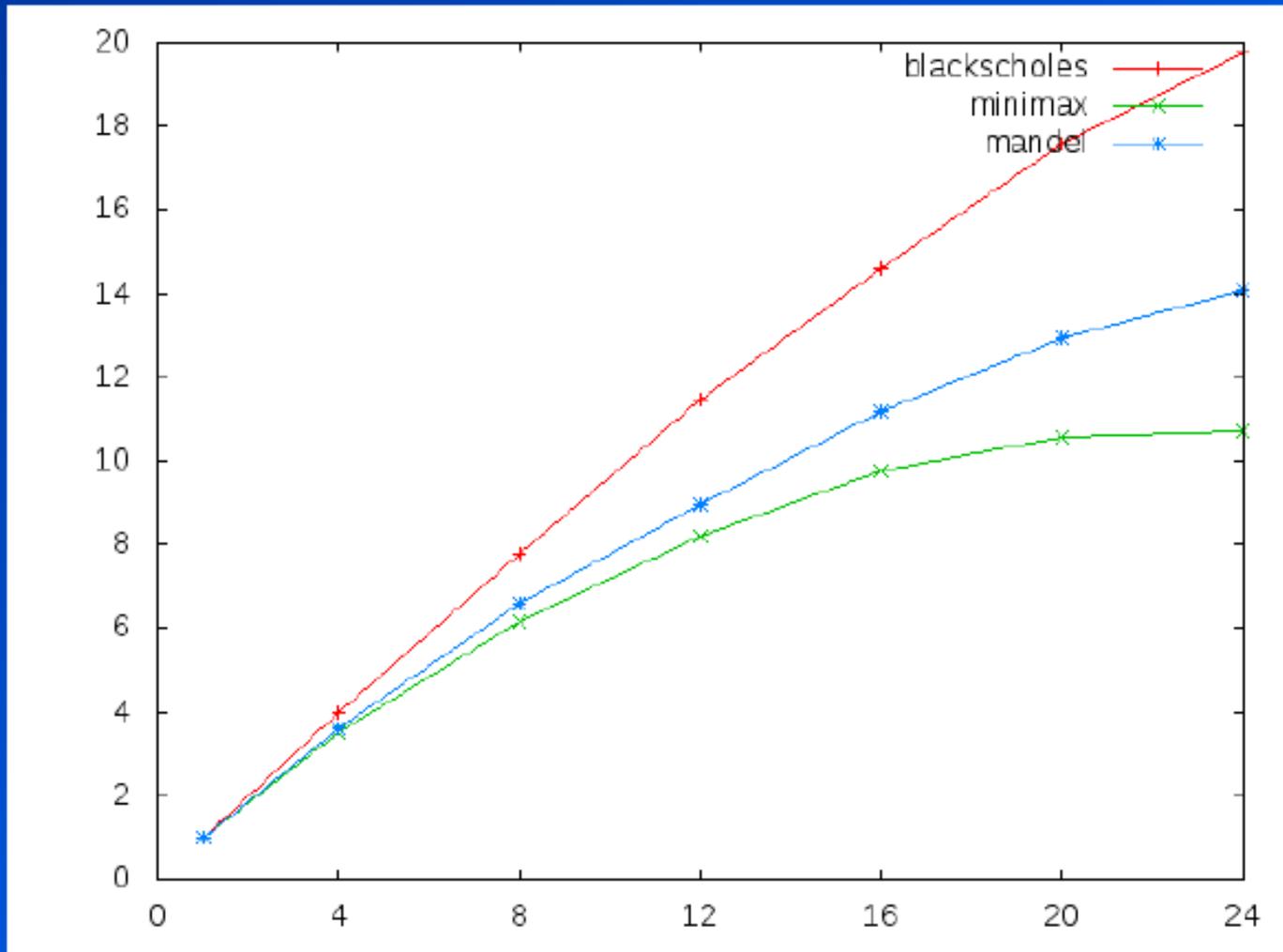
```
. . . -- Cases for Fork,
```



If any worker is idle, wake one up  
and give it work to do

# Results

speedup



cores

99%

95%

50%

# Modularity

---

- Key property of Strategies is modularity

```
parMap f xs = map f xs `using` parList rwhnf
```

- Relies on lazy evaluation
  - fragile
  - not always convenient to build a lazy data structure
- Par takes a different approach to modularity:
  - the Par monad is for *coordination* only
  - the application code is written separately as pure Haskell functions
  - The “parallelism guru” writes the coordination code
  - **Par** performance is not critical, as long as the grain size is not too small

# Par monad

Builds on old ideas of dataflow machines (hot topic in the 70s and 80s, reappearing in companies like [Maxeler](#))

Express parallelism by expressing data dependencies or using common patterns (like `parMapM`)

Very good match with skeletons!

Large grained, irregular parallelism is target

# Par monad compared to Strategies

Separation of function and parallelisation done differently

Eval monad and Strategies are advisory

Eval monad well integrated with Threadscope

Par monad and Strategies tend to achieve similar performance

But remember

runPar is expensive and runEval is free!

# Par monad compared to Strategies

Par monad does not support speculative parallelism as Strategies do

Par monad supports stream processing pipelines well

Strategies appropriate if you are producing a lazy data structure

Note: Par monad and Strategies can be combined...

# Par Monad easier to use than par?

fork creates **one parallel task**

Dependencies between tasks represented by Ivars

No need to reason about laziness

put is hyperstrict by default

Final suggestion in Par Monad paper is that maybe par is suitable for **automatic parallelisation**

# From PCPH

Unfortunately, right now there's no way to generate a visual representation of the dataflow graph from some Par monad code, but hopefully in the future someone will write a tool to do that.