Recursive Datatypes and Lists

data Suit = Spades | Hearts | Diamonds | Clubs

Interpretation:

"Here is a new type Suit. This type has four possible values: Spades, Hearts, Diamonds and Clubs."

data Suit = Spades | Hearts | Diamonds | Clubs

- This definition introduces five things:
 - The type Suit
 - The constructors

Spades	:: Suit
Hearts	:: Suit
Diamonds	:: Suit
Clubs	:: Suit

data Rank = Numeric Integer | Jack | Queen | King | Ace

Interpretation:

"Here is a new type Rank. Values of this type have five possible possible forms: Numeric n, Jack, Queen, King or Ace, where n is a value of type Integer"

data Rank = Numeric Integer | Jack | Queen | King | Ace

This definition introduces six things:

- The type Rank
- The constructors

Numeric	::???
Jack	:: ???
Queen	:: ???
King	:: ???
Ace	:: ???

data Rank = Numeric Integer | Jack | Queen | King | Ace

This definition introduces six things:

- The type Rank
- The constructors
 - Numeric:: Integer \rightarrow RankJack:: ???Queen:: ???King:: ???Ace:: ???

data Rank = Numeric Integer | Jack | Queen | King | Ace

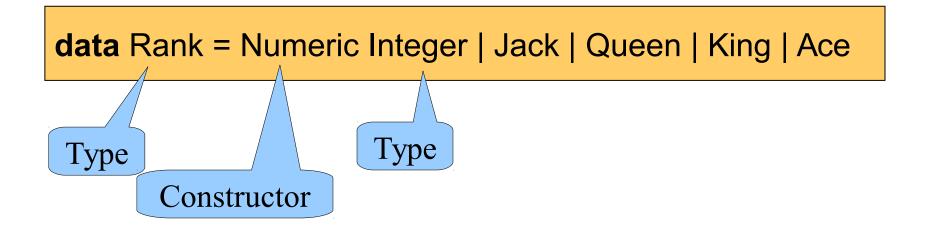
This definition introduces six things:

- The type Rank
- The constructors
 - Numeric Jack
 - Queen

King

Ace

- :: Integer → Rank :: Rank
- :: Rank
- :: Rank
- :: Rank



data Card = Card Rank Suit

Interpretation:

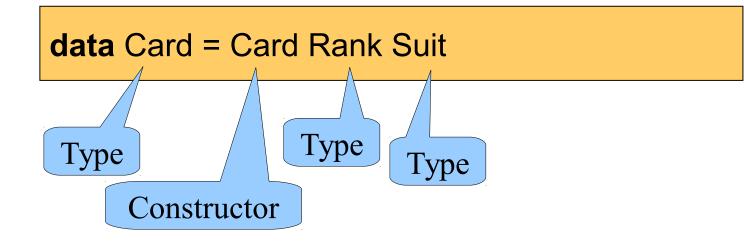
"Here is a new type Card. Values of this type have the form Card r s, where r and s are values of type Rank and Suit respectively."

data Card = Card Rank Suit

This definition introduces two things:
The type Card
The constructor Card :: ???

data Card = Card Rank Suit

This definition introduces two things:
– The type Card
– The constructor
Card :: Rank → Suit → Card



data Hand = Empty | Add Card Hand

Interpretation:

"Here is a new type Hand. Values of this type have two possible forms: Empty or Add c h where c and h are of type Card and Hand respectively."

data Hand = Empty | Add Card Hand

Alternative interpretation:

"A hand is either empty or consists of a card on top of a smaller hand."

data Hand = Empty | Add Card Hand

This definition introduces three things: - The type Hand - The constructors Empty :: ??? Add :: ???

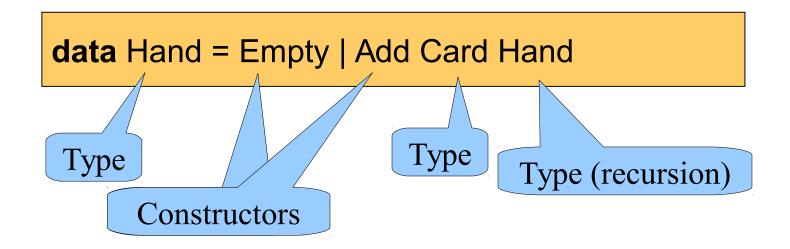
data Hand = Empty | Add Card Hand

This definition introduces three things: – The type Hand – The constructors Empty :: Hand Add :: ???

data Hand = Empty | Add Card Hand

This definition introduces three things:The type HandThe constructors

Empty :: Hand Add :: Card \rightarrow Hand \rightarrow Hand



Define functions by stating their results for all possible forms of the input

size :: Hand \rightarrow Integer

Define functions by stating their results for all possible forms of the input

size :: Hand \rightarrow Integersize Empty= 0size (Add card hand)= 1 + size hand

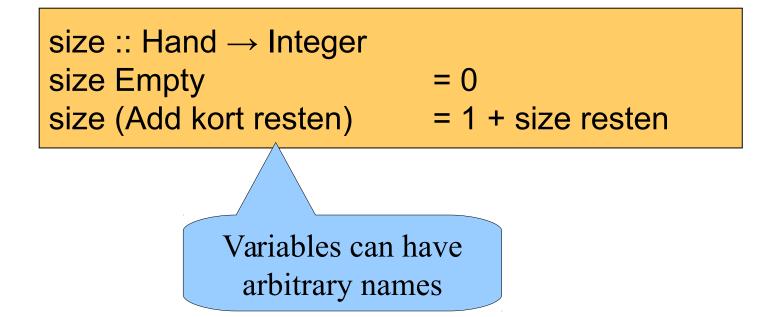
Interpretation:

"If the argument is Empty, then the result is 0. If the argument consists of a card card on top of a hand hand, then the result is 1 + the size of the rest of the hand."

size :: Hand \rightarrow Integersize Empty= 0size (Add card hand)= 1 + size hand

Patterns have two purposes:

- 1. Distinguish between forms of the input (e.g. Empty and Add)
- 2. Give names to parts of the input (In the definition of size, card is the first card in the argument, and hand is the rest of the hand.)



Construction/destruction

When used in an expression (RHS), Add *constructs* a hand:

aHand :: Hand aHand = Add c1 (Add c2 Empty)

When used in a pattern (LHS), Add *destructs* a hand:

size (Add card hand) = ...

Lists – how they work

data List = Empty | Add ?? List

- Can we generalize the Hand type to lists with elements of arbitrary type?
- What to put on the place of the ??

data List a = Empty | Add a (List a)

A parameterized type

Constructors: Empty :: ??? Add :: ???

data List a = Empty | Add a (List a)

A parameterized type

Constructors: Empty :: List a Add :: ???

data List a = Empty | Add a (List a)

A parameterized type

Constructors: Empty :: List a Add :: $a \rightarrow List a \rightarrow List a$

Constructing lists

• List containing the numbers 1, 2 and 3:

myList1 :: List Integer myList1 = Add 1 (Add 2 (Add 3 Empty))

• List containing the strings "apa", "hund":

myList2 :: List String myList2 = Add "apa" (Add "hund" Empty)

Constructing lists

• Cannot mix elements of different types:

myList3 = Add True (Add "bil" Empty)

Error: Couldn't match expected type 'Bool' with actual type '[Char]'

data List a = Empty | Add a (List a)

A parameterized type

Constructors: Empty :: List a Add :: $a \rightarrow List a \rightarrow List a$

Built-in lists

The List type is just for demonstration, Haskell has an <u>equivalent</u> built-in list type that should be used instead:

List a ≈ [a]

Built-in lists

data [a] = [] | (:) a [a]

Not a legal definition, but the built-in lists are *conceptually* defined like this

Constructors:

 $\begin{array}{ll} [] & \vdots & [a] \\ (\vdots) & \vdots & a \rightarrow & [a] \rightarrow & [a] \end{array}$

Built-in lists

```
Instead of
   Add 1 (Add 2 (Add 3 Empty))
we can use built-in lists and write
   (:) 1 ((:) 2 ((:) 3 []))
or, equivalently
   1:2:3:[]
or, equivalently
                              Special syntax for the
   [1,2,3]
                                  built-in lists
```

Some list operations

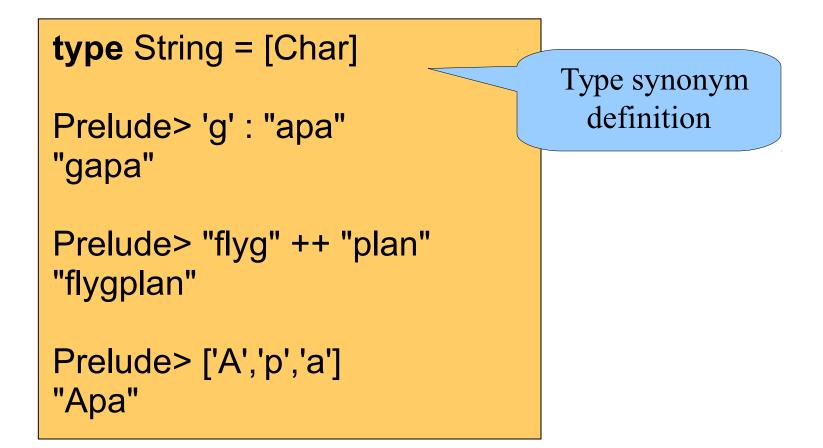
• From the Data.List module (also in the Prelude):

```
reverse :: [a] -> [a]
 -- reverse a list
take :: Int -> [a] -> [a]
 -- (take n) picks the first n elements
(++) :: [a] -> [a] -> [a]
 -- append a list after another
replicate :: Int -> a -> [a]
 -- make a list by replicating an element
```

Some list operations

```
*Main> reverse [1,2,3]
[3,2,1]
*Main> take 4 [1..10]
[1,2,3,4]
*Main> [1,2,3] ++ [4,5,6]
[1,2,3,4,5,6]
*Main> replicate 5 2
[2,2,2,2,2]
```

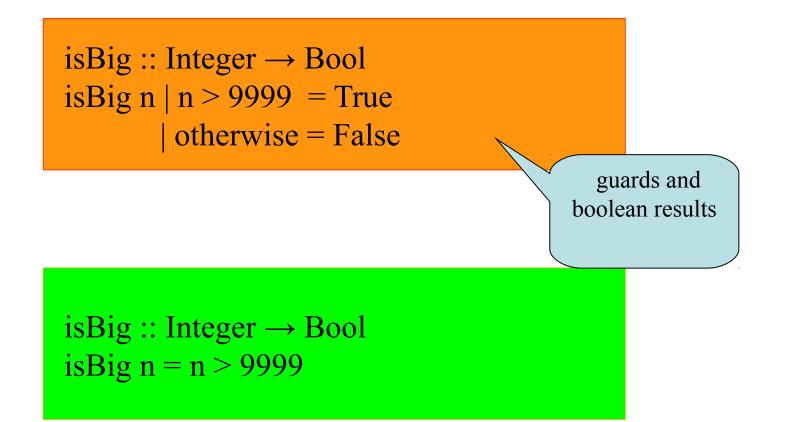
Strings are lists of characters



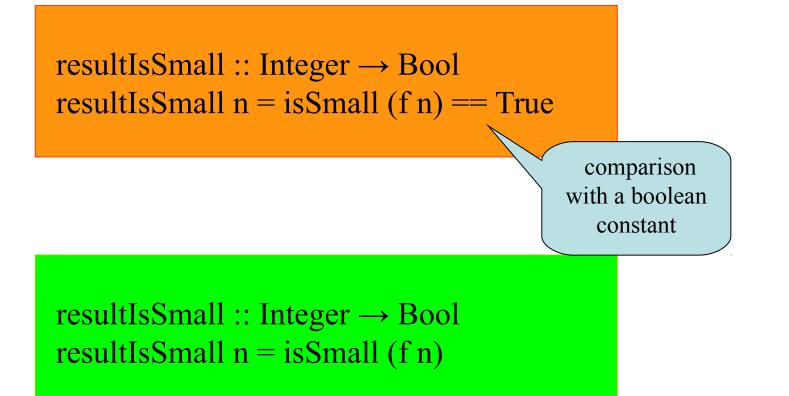
More on Types

- Functions can have "general" types:
 - polymorphism
 - reverse :: [a] \rightarrow [a]
 - -(:) :: $a \rightarrow [a] \rightarrow [a]$
- Sometimes, these types can be restricted
 - Ord a \Rightarrow ... for comparisons (<, <=, >, >=, ...)
 - Eq a => ... for equality (==, \neq)
 - Num a => ... for numeric operations (+, -, *, ...)

Do's and Don'ts



Do's and Don'ts



Do's and Don'ts



comparison with a boolean constant

resultIsBig :: Integer \rightarrow Bool resultIsBig n = not (isSmall (f n))

