Formal Methods for Software Development Modeling Distributed Systems

Wolfgang Ahrendt

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This Lecture

You know you have a distributed system when the crash of a computer you've never heard of stops you from getting any work done.—Leslie Lamport

Using Prometa channels for modeling distributed systems

Modeling Distributed Systems

Distributed systems consist of

- nodes.
- interacting via communication channels,
- protocols dictate how nodes communicate with each other.

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Distributed systems consist of

- nodes,
- interacting via communication channels,
- protocols dictate how nodes communicate with each other.

Distributed systems are very complex.

Models of distributed systems abstract away from details of networks/protocols/nodes.

In Promela:

- ▶ nodes modeled by PROMELA processes
- communication channels modeled by PROMELA channels
- protocols modeled by algorithm distributed over processes

Channels in Promela

In Promela, channels are first class citizens.

Data type chan with two operations for sending and receiving

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A variable of channel type is declared by initializer:

```
chan name = [capacity] \text{ of } \{type_1, ..., type_n\}
```

name name of channel variable

capacity non-negative integer constant

type; PROMELA data types

Channels in Promela

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Data type chan with two operations for sending and receiving

A variable of channel type is declared by initializer:

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chan name = [capacity] of \{type_1, ..., type_n\}

name name of channel variable capacity non-negative integer constant type_i PROMELA data types
```

Example:

```
chan ch = [2] of { mtype, byte, bool }
```

```
chan name = [capacity] of \{type_1, ..., type_n\}
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Creates channel, stored in variable name

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Can buffer up to *capacity* messages, if *capacity* ≥ 1 \Rightarrow "buffered channel"

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```

Creates channel, stored in variable name

Messages communicated via channel are n-tuples $\in type_1 \times ... \times type_n$

Can buffer up to $\emph{capacity}$ messages, if $\emph{capacity} \geq 1$

⇒ "buffered channel"

The channel has *no* buffer if capacity = 0

⇒ "rendezvous channel"

Example:

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Creates channel, stored in variable ch

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Messages communicated via ch are 3-tuples $\in \mathbf{mtype} \times \mathbf{byte} \times \mathbf{bool}$

Example:

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chan ch = [2] of { mtype, byte, bool }
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```
Given, e.g., mtype = {red, yellow, green}, an example message on ch can be:
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 ${\sf Messages} \ {\sf communicated} \ {\sf via} \ {\sf ch} \ {\sf are} \ 3{\sf -tuples} \in {\bf mtype} \times {\bf byte} \times {\bf bool}$

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Given, e.g., mtype = {red, yellow, green}, an example message on ch can be: green, 20, false
```

Example:

```
chan ch = [2] of { mtype, byte, bool }

Creates channel, stored in variable ch

Messages communicated via ch are 3-tuples ∈ mtype × byte × bool

Given, e.g., mtype = {red, yellow, green},
an example message on ch can be: green, 20, false

ch is a buffered channel, buffering up to 2 messages
```

send statement has the form:

name! $expr_1, \dots, expr_n$

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▶ name: channel variable

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- ightharpoonup assigns values of message to var_1, \dots, var_n

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- name: channel variable
- var₁, ..., var_n: sequence of variables, where number and types match message type
- assigns values of message to var₁, ..., var_n
- ▶ example: ch ? color, time, flash

```
chan request = [0] of { byte };
active proctype Client0() {
  request ! 0
}
active proctype Client1() {
  request ! 1
}
```

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ClientO and Client1 send messages O resp. 1 to channel request

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chan request = [0] of { byte };
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...
```

ClientO and Client1 send messages O resp. 1 to channel request Order of sending is nondeterministic

```
chan request = [0] of { byte };
...
active proctype Server() {
  byte num;
  do
    :: request ? num;
      printf("servinguclientu%d\n", num)
  od
}
```

```
chan request = [0] of { byte };
. . .
active proctype Server() {
  byte num;
  do
    :: request ? num;
       printf("serving client %d\n", num)
  od
Server loops on
```

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chan request = [0] of { byte };
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active proctype Server() {
  byte num;
  do
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}
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Server loops on

receiving first message from request,

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chan request = [0] of { byte };
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receiving first message from request, storing value in num

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chan request = [0] of { byte };
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active proctype Server() {
  byte num;
  do
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}
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Server loops on

- receiving first message from request, storing value in num
- printing

Demo

rendezvous1 random simulation

Executability of receive Statement (non-buffered)

request ? num

executable only when another process offers send on channel request

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 \Rightarrow receive statement frequently used as guard in if/do-statements

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do

:: request ? num ->
    printf("servinguclientu%d\n", num)
od
```

Executability of receive Statement (non-buffered)

```
request ? num
 executable only when another process offers send on channel request
  \Rightarrow receive statement frequently used as guard in if/do-statements
  do
     :: request ? num ->
         printf("serving client \%d\n", num)
  od
("->" equivalent to ";")
```

Demo

rendezvous1 interactive simulation

Rendezvous Channels

```
chan ch = [0] of { byte, byte };
/* global only to make visible in SpinSpider */
byte hour, minute;
active proctype Sender() {
  printf("ready\n");
  ch! 11, 45;
  printf("Sent\n")
active proctype Receiver() {
  printf("steady\n");
  ch ? hour, minute;
  printf("Received\n")
```

Rendezvous Channels

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/* global only to make visible in SpinSpider */
byte hour, minute;
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  printf("Received\n")
```

Which interleavings can occur?

Rendezvous Channels

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/* global only to make visible in SpinSpider */
byte hour, minute:
active proctype Sender() {
  printf("ready\n");
  ch! 11, 45;
  printf("Sent\n")
active proctype Receiver() {
  printf("steady\n");
  ch ? hour, minute;
  printf("Received\n")
```

Which interleavings can occur? \Rightarrow ask SpinSpider

Demo

through $\rm JSPIN\colon$ $\rm SPINSPIDER$ on ReadySteady.pml

On a rendezvous channel:

Transfer of message from sender to receiver is synchronous, i.e., one single operation.

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```
Sender Receiver
\vdots \qquad \qquad \vdots
(11,45) \longrightarrow (hour,minute)
\vdots \qquad \qquad \vdots
```

Either:

1. Location counter of sender process at send ("!"): "offer to engage in rendezvous"

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In both case, the next step is:

Location counter of both processes is incremented at once.

Either:

- Location counter of sender process at send ("!"): "offer to engage in rendezvous"
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- Location counter of receiver process at receive ("?"): "offer to engage in rendezvous"
- 2. Location counter of sender process at send ("!"): "rendezvous can be accepted"

In both case, the next step is:

Location counter of both processes is incremented at once.

 ${\it Only}$ place where ${\it Promela}$ processes execute synchronously

Reconsider Client Server

```
chan request = [0] of { byte };
active proctype Server() {
  byte num;
  do :: request ? num ->
        printf("serving_client_%d\n", num)
  od
active proctype Client0() {
  request ! 0
}
active proctype Client1() {
  request ! 1
```

Reconsider Client Server

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chan request = [0] of { byte };
active proctype Server() {
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active proctype Client0() {
  request ! 0
}
active proctype Client1() {
  request ! 1
```

So far no reply to clients

Reply Channels

```
chan request = [0] of { byte };
chan ack = [0] of { bool }:
active proctype Server() {
 byte num;
 do :: request ? num ->
        printf("serving client \%d\n", num);
        ack! true
 od
active proctype Client0() {
  request ! 0; ack ? _; printf("acknowledged\n")
}
active proctype Client1() {
  request ! 1; ack ? _; printf("acknowledged\n")
}
```

Reply Channels

```
chan request = [0] of { byte };
chan ack = [0] of { bool }:
active proctype Server() {
  byte num;
  do :: request ? num ->
        printf("serving client \%d\n", num);
        ack! true
 od
active proctype Client0() {
  request ! 0; ack ? _; printf("acknowledged\n")
active proctype Client1() {
  request ! 1; ack ? _; printf("acknowledged\n")
}
(Anonymous variable "_": data from channel no stored anywhere)
```

```
mtype = { nice, rude };
chan request = [0] of { mtype };
chan reply = [0] of { mtype };
active proctype Server() {
  mtype msg;
  do :: request ? msg; reply ! msg
  od
}
active proctype NiceClient() {
  mtype msg;
  request ! nice; reply ? msg;
}
active proctype RudeClient() {
  mtype msg;
  request ! rude; reply ? msg
}
```

```
mtype = { nice, rude };
chan request = [0] of { mtype };
chan reply = [0] of { mtype };
active proctype Server() {
  mtype msg;
  do :: request ? msg; reply ! msg
  od
}
active proctype NiceClient() {
  mtype msg;
  request ! nice; reply ? msg;
  assert(msg == nice)
active proctype RudeClient() {
  mtype msg;
  request ! rude; reply ? msg
}
```

```
mtype = { nice, rude };
chan request = [0] of { mtype };
chan reply = [0] of { mtype };
active proctype Server() {
  mtype msg;
  do :: request ? msg; reply ! msg
  od
}
active proctype NiceClient() {
  mtype msg;
  request ! nice; reply ? msg;
  assert(msg == nice)
                                  Is the assertion valid?
active proctype RudeClient() {
  mtype msg;
  request ! rude; reply ? msg
}
```

```
mtype = { nice, rude };
chan request = [0] of { mtype };
chan reply = [0] of { mtype };
active proctype Server() {
  mtype msg;
  do :: request ? msg; reply ! msg
  od
}
active proctype NiceClient() {
  mtype msg;
  request ! nice; reply ? msg;
  assert(msg == nice)
                                  Is the assertion valid? Ask Spin.
active proctype RudeClient() {
  mtype msg;
  request ! rude; reply ? msg
}
```

More realistic with several servers:

```
active [2] proctype Server() {
 mtype msg;
 do :: request ? msg; reply ! msg
  od
}
active proctype NiceClient() {
  mtype msg;
  request ! nice; reply ? msg;
active proctype RudeClient() {
 mtype msg;
  request ! rude; reply ? msg
}
```

More realistic with several servers:

```
active [2] proctype Server() {
 mtype msg;
 do :: request ? msg; reply ! msg
  od
}
active proctype NiceClient() {
  mtype msg;
  request ! nice; reply ? msg;
  assert(msg == nice)
active proctype RudeClient() {
  mtype msg;
  request ! rude; reply ? msg
}
```

More realistic with several servers:

active [2] proctype Serve

```
active [2] proctype Server() {
 mtype msg;
 do :: request ? msg; reply ! msg
  od
}
active proctype NiceClient() {
  mtype msg;
  request ! nice; reply ? msg;
                                  And here?
  assert(msg == nice)
active proctype RudeClient() {
  mtype msg;
  request ! rude; reply ? msg
}
```

More realistic with several servers: active [2] proctype Server() { mtype msg; do :: request ? msg; reply ! msg od } active proctype NiceClient() { mtype msg; request ! nice; reply ? msg; assert(msg == nice) And here? Analyse with Spin. active proctype RudeClient() { mtype msg; request ! rude; reply ? msg }

To fix the protocol:

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clients declare local reply channel + send it to server

```
mtype = { nice, rude };
chan request = [0] of { mtype, chan };
active [2] proctype Server() {
 mtype msg; chan ch;
 do :: request ? msg, ch;
        ch! msg
 od
active proctype NiceClient() {
  chan reply = [0] of { mtype }; mtype msg;
  request ! nice, reply; reply ? msg;
  assert ( msg == nice )
}
active proctype RudeClient() {
  chan reply = [0] of { mtype }; mtype msg;
  request ! rude, reply; reply ? msg
}
```

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mtype = { nice, rude };
chan request = [0] of { mtype, chan };
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 mtype msg; chan ch;
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        ch! msg
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active proctype NiceClient() {
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  request ! nice, reply; reply ? msg;
  assert( msg == nice )
}
active proctype RudeClient() {
  chan reply = [0] of { mtype }; mtype msg;
  request ! rude, reply; reply ? msg
}
      verify with Spin
```

Scope of Channels

Global channel

▶ All processes can send and/or receive messages

Local channel

- Dies with its process
- ► Can model 'private' communication & security issues
- ► Example: Local channel can be passed through a global channel

Sending Process IDs

Used fixed constants used for identification (here nice, rude)

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Processes send their own, unique process ID, _pid, as part of message

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Experiment with rendezvous3.pml

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Processes send their own, unique process ID, _pid, as part of message

Experiment with rendezvous3.pml

Example, clients code:

```
chan reply = [0] of { byte, byte };
request ! _pid, reply;
reply ? serverID, serversClient;
```

Sending Process IDs

Used fixed constants used for identification (here nice, rude)

- inflexible
- doesn't scale

Alternative:

Processes send their own, unique process ID, _pid, as part of message

Experiment with rendezvous3.pml

Example, clients code:

```
chan reply = [0] of { byte, byte };
request ! _pid, reply;
reply ? serverID, serversClient;
assert( serversClient == _pid )
```

Limitations of Rendezvous Channels

- Rendezvous too restrictive for many applications
- Servers and clients block each other too much
- ▶ Difficult to manage uneven workload (online shop: dozens of webservers serve thousands of clients)

Buffered channels queue messages.
Requests/services no not immediately block clients/servers.

Example:

```
chan ch = [3] of { mtype, byte, bool }
```

Buffered channels, with capacity cap

► Can hold up to *cap* messages

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- ► (Normal) receive statement reads and removes message

Buffered channels, with capacity cap

- Can hold up to cap messages
- Are a FIFO (first-in-first-out) data structure: always the 'oldest' message in channel is retrieved by a receive
- ► (Normal) receive statement reads and removes message
- Sending and receiving to/from buffered channels is asynchronous, i.e. interleaved

Executability of Buffered Channel operations

Given channel ch, with capacity cap, currently containing n messages

receive statement ch ? msg is executable iff ch is not empty, i.e., n>0

send statement ch ! msg is executable iff there is still 'space' in the message queue, i.e., n < cap

A non-executable receive or send statement will block until it is executable again

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A non-executable receive or send statement will block until it is executable again

(With option -m, SPIN has a different send semantics: Attempt to send to full channel doesn't block, but message gets lost.)

Checking Channel for Full/Empty

This can prevent unnecessary blocking:

Given channel ch:

full(ch) checks whether ch is full
nfull(ch) checks whether ch is not full
empty(ch) checks whether ch is empty
nempty(ch) checks whether ch is not empty

Illegal to negate those.

Avoid combining with else.

Copy Message without Removing

Assume ch to be a buffered channel.

```
ch ? color, time, flash
```

- ► Assigns values from the message to color, time, flash
- ▶ Removes message from ch

Copy Message without Removing

Assume ch to be a buffered channel.

```
ch ? color, time, flash
```

- ► Assigns values from the message to color, time, flash
- ▶ Removes message from ch

```
ch ? <color, time, flash>
```

- ► Assign values from the message to color, time, flash
- Leaves message in ch

Recurring task: Dispatch action depending on message

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```
mtype = {hi, bye};
chan ch = [0] of \{mtype\};
active proctype Server () {
  mtype msg;
read:
  ch ? msg;
 do
    :: msg == hi -> printf("Hello.\n"); goto read
    :: msg == bye -> printf("See,you.\n"); break
  od
```

. . .

```
Recurring task: Dispatch action depending on message
mtype = {hi, bye};
chan ch = [0] of \{mtype\};
active proctype Server () {
   mtype msg;
read:
  ch ? msg;
  do
    :: msg == hi -> printf("Hello.\n"); goto read
    :: msg == bye -> printf("See,you.\n"); break
  od
```

There is a better way!

. . .

Recurring task: Dispatch action depending on message type.

```
mtype = {hi, bye};
chan ch = [0] of {mtype};

active proctype Server () {
   do
     :: ch ? hi -> printf("Hello.\n")
     :: ch ? bye -> printf("See_you.\n"); break
   od
}
...
```

hi and bye are values, not variables!

Pattern Matching

Receive statement allows also non-variable expressions as arguments:

$$ch ? exp_1, \ldots, exp_n$$

- $ightharpoonup exp_1, \dots, exp_n$ any(!) expressions of correct type
- ► Receive statement is executable, iff
 - 1. either
 - ch is buffered channel and not empty, or
 - ch is rendezvous channel and some process ready to send to ch
 - 2. message msg_1, \ldots, msg_n in channel ch matches exp_1, \ldots, exp_n
- msg_i matches exp_i iff
 - $ightharpoonup exp_i$ is a variable and msg_i a value (of correct type)
 - exp_i is not a variable and exp_i == msg_i

Assume

```
chan ch = [0] of {int, int};
int id = 5;
```

Assume

```
chan ch = [0] of {int, int};
int id = 5;
```

Does ch ? 0, id match message

▶ [0, 5]?

Assume

```
chan ch = [0] of {int, int};
int id = 5;
```

Does ch ? 0, id match message

▶ [0, 5] ?

Assume

```
chan ch = [0] of {int, int};
int id = 5;
```

```
▶ [0, 5] ? ✓ [0, 7] ?
```

```
Assume
```

```
chan ch = [0] of {int, int};
int id = 5;
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```
▶ [0, 5] ? ✓ [0, 7] ? ✓
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Assume
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Does ch ? 0, id match message

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To match the value stored in a variable var use eval(var)

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FMSD: Modeling Distributed Systems

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Dispatching Messages Revisited

Random receive ?? (for buffered channels)

- Executable if matching message exists in channel.
- ▶ If executed, first matching message removed from channel.

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Nicer Message Formatting

 $\ensuremath{\mathrm{P}\mathrm{R}\mathrm{O}\mathrm{M}\mathrm{E}\mathrm{L}\mathrm{A}}$ provides an alternative, but equivalent syntax for

ch ! exp1, exp2, exp3

Nicer Message Formatting

PROMELA provides an alternative, but equivalent syntax for

namely

Increases readability for certain applications, e.g. protocol modelling:

```
ch!send(msg,id) vs. ch!send,msg,id
ch!ack(id) vs. ch!ack,id
```

And finally

Buffered channels are part of the state!

State space gets much bigger using buffered channels

Use with care (and with small buffers).