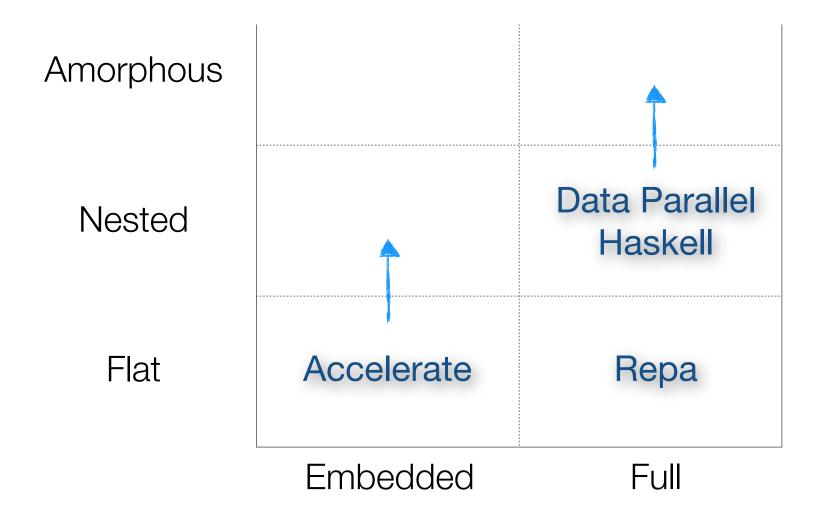
Parallel Functional Programming Repa and wrap up

Mary Sheeran

http://www.cse.chalmers.se/edu/course/pfp



DPH

Parallel arrays

[: e :]

(which can contain arrays)

DPH

Parallel arrays [: e:] (which can contain arrays)

Expressing parallelism = applying collective operations to parallel arrays

Note: demand for any element in a parallel array results in eval of all elements

DPH array operations

```
(!:) :: [:a:] -> Int -> a
sliceP :: [:a:] -> (Int,Int) -> [:a:]
replicateP :: Int -> a -> [:a:]
mapP :: (a->b) -> [:a:] -> [:b:]
zipP :: [:a:] -> [:b:] -> [:(a,b):]
zipWithP :: (a->b->c) -> [:a:] -> [:b:] -> [:c:]
filterP :: (a->Bool) -> [:a:] -> [:a:]
concatP :: [:[:a:]:] -> [:a:]
concatMapP :: (a -> [:b:]) -> [:a:] -> [:b:]
unconcatP :: [:[:a:]:] -> [:b:] -> [:[:b:]:]
transposeP :: [:[:a:]:] -> [:[:a:]:]
expandP :: [:[:a:]:] -> [:b:] -> [:b:]
combineP :: [:Bool:] -> [:a:] -> [:a:]
splitP :: [:Bool:] -> [:a:] -> ([:a:], [:a:])
```

Examples

```
svMul :: [:(Int,Float):] -> [:Float:] -> Float
svMul sv v = sumP [: f*(v !: i) | (i,f) <- sv :]</pre>
```

```
smMul :: [:[:(Int,Float):]:] -> [:Float:] -> [:Float:]
smMul sm v = [: svMul row v | row <- sm :]</pre>
```

Nested data parallelism
Parallel op (svMul) on each row

Data parallelism

Perform same computation on a collection of differing data values

examples: HPF (High Performance Fortran)

CUDA

Both support only flat data parallelism

Flat: each of the individual computations on (array) elements is sequential

those computations don't need to communicate parallel computations don't spark further parallel computations

Regular, Shape-polymorphic, Parallel Arrays in Haskell

Gabriele Keller[†] Manuel M. T. Chakravarty[†] Roman Leshchinskiy[†]
Simon Peyton Jones[‡] Ben Lippmeier[†]

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API for purely functional, collective operations over dense, rectangular, multi-dimensional arrays supporting shape polymorphism

Ideas

Purely functional array interface using collective (whole array) operations like map, fold and permutations can

- combine efficiency and clarity
- focus attention on structure of algorithm, away from low level details

Influenced by work on algorithmic skeletons based on Bird Meertens formalism

Provides shape polymorphism not in a standalone specialist compiler like SAC, but using the Haskell type system

terminology

Regular arrays

dense, rectangular, most elements non-zero

shape polymorphic

functions work over arrays of arbitrary dimension

terminology

Regular arrays

dense, rectan

shape polym

functions wo

note: the arrays are purely functional and immutable

All elements of an array are demanded at once -> parallelism

P processing elements, n array elements => n/P consecutive elements on each proc. element

But things moved on!

Repa from ICFP 2010 had ONE type of array (that could be either delayed or manifest, like in many EDSLs)

A paper from Haskell'11 showed efficient parallel stencil convolution

http://www.cse.unsw.edu.au/~keller/Papers/stencil.pdf

Fancier array type

```
data Array sh a
                { arrayExtent :: sh
  = Array
                , arrayRegions :: [Region sh a] }
data Region sh a
                { regionRange :: Range sh
   = Region
                               :: Generator sh a }
                 , regionGen
data Range sh
  = RangeAll
  | RangeRects { rangeMatch
                               :: sh -> Bool
                               :: [Rect sh] }
                , rangeRects
data Rect sh
  = Rect sh sh
data Generator sh a
  = GenManifest { genVector :: Vector a }
   | forall cursor.
    GenCursored { genMake
                              :: sh -> cursor
                , genShift
                              :: sh -> cursor -> cursor
                 , genLoad
                              :: cursor -> a }
```

Figure 5. New Repa Array Types

Fancier array type

```
data Array sh a
                 { arrayExtent :: sh
  = Array
                 , arrayRegions :: [Region sh a] }
data Region sh a
                { regionRange :: Range sh
   = Region
                                :: Generator sh a }
                 , regionGen
data Range sh
  = RangeAll
  | RangeRects { rangeMatch
                 , rangeRects
                                :: [R
data Rect sh
  = Rect sh sh
data Generator sh a
  = GenManifest { genVector
   | forall cursor.
     GenCursored { genMake
```

But you need to be a guru to get good performance!

Put Array representation into the type!

The fundamental problem with Repa 1 & 2 is the following: at an particular point in the code, the programmer typically has a clear idea of the array representation they desire. For example, it may consist of three regions, left edge, middle, right edge, each of which is a delayed array. Although this knowledge is statically known to the the programmer, it is invisible in the types and only exposed to the compiler if very aggressive value inlining is used. Moreover, the programmer's typeless reasoning can easily fail, leading to massive performance degradation.

The solution is to expose static information about array representation to Haskell's main static reasoning system; its type system.

Repa 3 (Haskell'12)

Guiding Parallel Array Fusion with Indexed Types

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[‡]Microsoft Research Ltd Cambridge, England {simonpj}@microsoft.com

Abstract

We present a refined approach to parallel array fusion that uses indexed types to specify the internal representation of each array. Our approach aids the client programmer in reasoning about the performance of their program in terms of the source code. It also makes the intermediate code easier to transform at compile-time, resulting in faster compilation and more reliable runtimes. We demonstrate how our new approach improves both the clarity and performance of several end-user written programs, including a fluid flow solver and an interpolator for volumetric data.

Categories and Subject Descriptors D.3.3 [Programming Lan-

This second version of doubleZip runs as fast as a hand-written imperative loop. Unfortunately, it is cluttered with explicit pattern matching, bang patterns, and use of the force function. This clutter is needed to guide the compiler towards efficient code, but it obscures the algorithmic meaning of the source program. It also demands a deeper understanding of the compilation method than most users will have, and in the next section, we will see that these changes add an implicit precondition that is not captured in the function signature. The second major version of the library, Repa 2, added support for efficient parallel stencil convolution, but at the same time also increased the level of clutter needed to achieve efficient code [8].

http://www.youtube.com/watch?v=YmZtP11mBho

quote on previous slide was from this paper

version

I use a recent Repa (3.4.0.1) (which works with the GHC that you get with the current Haskell platform)

cabal update cabal install repa

http://repa.ouroborus.net/

(I don't have llvm installed. Using GHC's llvm backend speeds things up significantly, apparently.)

Repa Arrays

Repa arrays are wrappers around a linear structure that holds the element data.

The representation tag determines what structure holds the data.

Delayed Representations (functions that compute elements)

D -- Functions from indices to elements.

C -- Cursor functions.

Manifest Representations (real data)

U -- Adaptive unboxed vectors.

V -- Boxed vectors.

B -- Strict ByteStrings.

F -- Foreign memory buffers.

Meta Representations

- P -- Arrays that are partitioned into several representations.
- S -- Hints that computing this array is a small amount of work, so computation should be sequential rather than parallel to avoid scheduling overheads.
- I -- Hints that computing this array will be an unbalanced workload, so computation of successive elements should be interleaved between the processors
- X -- Arrays whose elements are all undefined.

10 Array representations!

- D Delayed arrays (delayed) §3.1
- C Cursored arrays (delayed) §4.4
- U Adaptive unboxed vectors (manifest) §3.1
- V Boxed vectors (manifest) §4.1
- B Strict byte arrays (manifest) §4.1
- F Foreign memory buffers (manifest) §4.1
- P Partitioned arrays (meta) §4.2
- S Smallness hints (meta) §5.1.1
- I Interleave hints (meta) §5.2.1
- X Undefined arrays (meta) §4.2

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- X Undefined arrays (meta) §4.2

But the 18 minute presentation at Haskell'12 makes it all make sense!! Watch it!

http://www.youtube.com/watch?v=YmZtP11mBho

Type Indexing

data family Array rep sh e

type index giving representation

Type Indexing

data family Array rep sh e

shape

Type Indexing

element type

map

```
map
:: (Shape sh, Source r a) =>
    (a -> b) -> Array r sh a -> Array D sh b
```

map

```
map
:: (Shape sh, Source r a) =>
    (a -> b) -> Array r sh a -> Array D sh b

map f arr = case delay arr of ADelayed sh g ->
    ADelayed sh (f . g)
```

Fusion

Delayed (and cursored) arrays enable fusion that avoids intermediate arrays

User-defined worker functions can be fused

This is what gives tight loops in the final code

Parallel computation of array elements

example

import Data.Array.Repa as R

transpose2P :: Monad m => Array U DIM2 Double -> m (Array U DIM2 Double)

example

import Data.Array.Repa as R

index type

SHAPE

EXTENT

example

import Data.Array.Repa as R

transpose2P :: Monad m => Array U DIM2 Double -> m (Array U DIM2 Double)

DIM0 = Z (scalar)

DIM1 = DIM0 :. Int

DIM2 = DIM1 :. Int

snoc lists

Haskell lists are cons lists

1:2:3:[] is the same as [1,2,3]

Repa uses snoc lists at type level for shape types and at value level for shapes

DIM2 = Z :. Int :. Int is a shape type

Z:.i:.j read as (i,j) is an index into a two dim. array

transpose 2D array in parallel

more general transpose (on inner two dimensions)

```
transpose
:: (Shape sh, Source r e) =>
   Array r ((sh :. Int) :. Int) e
   -> Array D ((sh :. Int) :. Int) e
```

more general transpose (on inner two dimensions) is provided

```
transpose
  :: (Shape sh, Source r e) =>
    Array r ((sh :. Int) :. Int) e
    -> Array D ((sh :. Int) :. Int) e
```

This type says an array with at least 2 dimensions. The function is shape polymorphic

more general transpose (on inner two dimensions) is provided

```
transpose
  :: (Shape sh, Source r e) =>
    Array r ((sh :. Int) :. Int) e
    -> Array D ((sh :. Int) :. Int) e
```

Functions with at-least constraints become a parallel map over the unspecified dimensions (called rank generalisation)

Important way to express parallel patterns

Remember

Arrays of type (Array D sh a) or (Array C sh a) are *not real arrays*. They are represented as functions that compute each element on demand. You need to use <u>computeS</u>, <u>computeP</u>, <u>computeUnboxedP</u> and so on to actually evaluate the elements.

(quote from

http://hackage.haskell.org/package/repa-3.4.0.1/docs/Data-Array-Repa.html which has lots more good advice, including about compiler flags)

Example: sorting

Batcher's bitonic sort (see lecture from Monday)

"hardware-like" data-independent

http://www.cs.kent.edu/~batcher/sort.pdf

bitonic sequence

```
inc (not decreasing)
then
dec (not increasing)
```

or a cyclic shift of such a sequence

1 9

1 2 9 10

1 2 3 4 9 10 8 6

1 2 3 4 5 6 7 8 9 10 8 6 4 2 1 0 1 2 3 4 4 9 10 8 6 5

Swap!

1 2 3 4 4 2 9 10 8 6 5 6

- 1 2 3 4 5 6 7 8 9 10 8 6 4 2 1 0
- 1 2 3 4 4 2 1 0 9 10 8 6 5 6 7 8

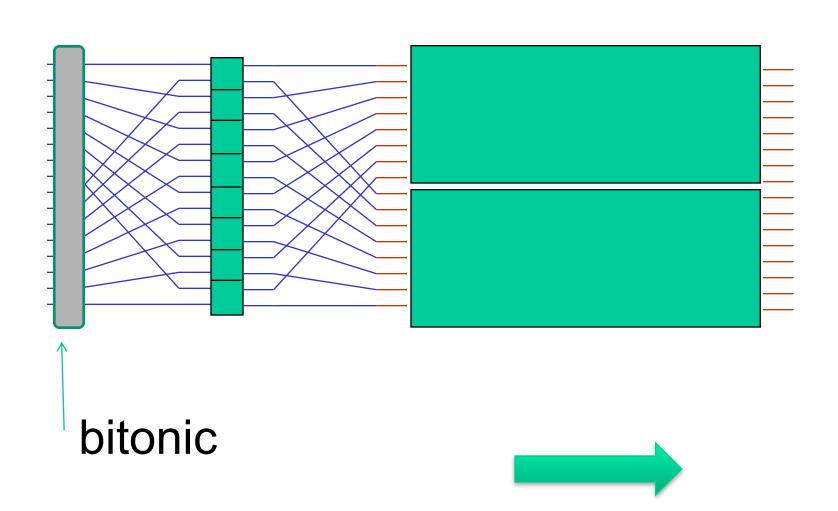
1 2 3 4 4 2 1 0 9 10 8 6 5 6 7 8

bitonic

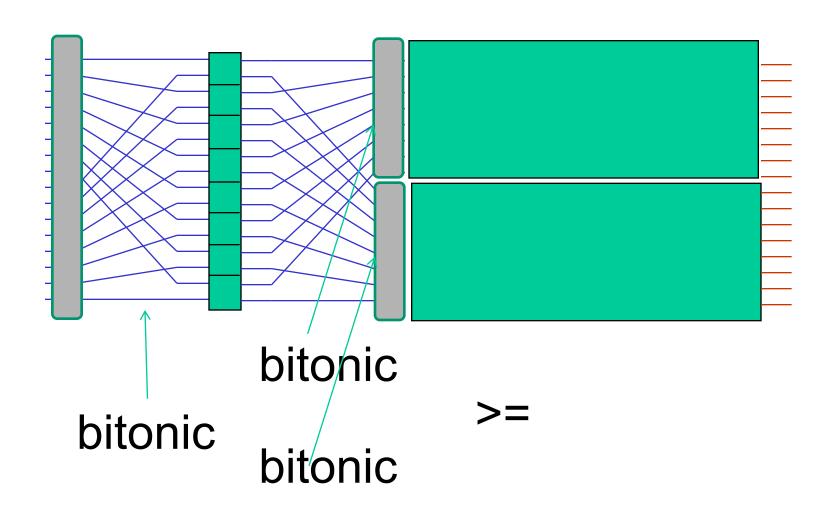
 \leq

bitonic

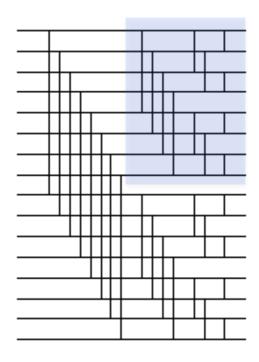
Butterfly



Butterfly



bitonic merger



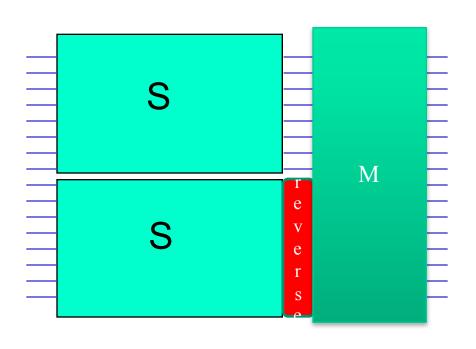
Question

What are the work and depth (or span) of bitonic merger?

Making a recursive sorter (D&C)

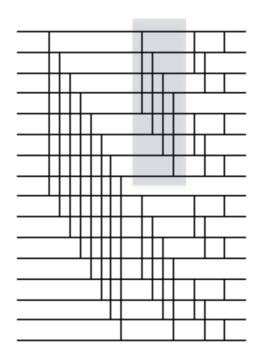
Make a bitonic sequence using two half-size sorters

Batcher's sorter (bitonic)

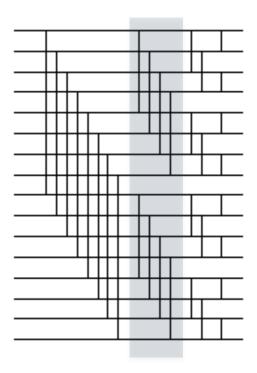


Let's try to write this sorter down in Repa

bitonic merger



bitonic merger



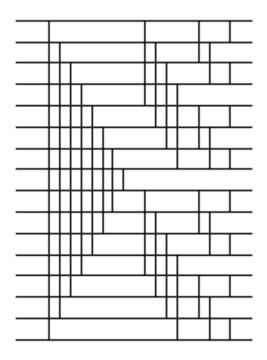
dee for diamond

assume input array has length a power of 2, s > 0 in this and later functions

dee for diamond

```
bitonicMerge n = compose [dee min max (n-i) | i <- [1..n]]
```

tmerge



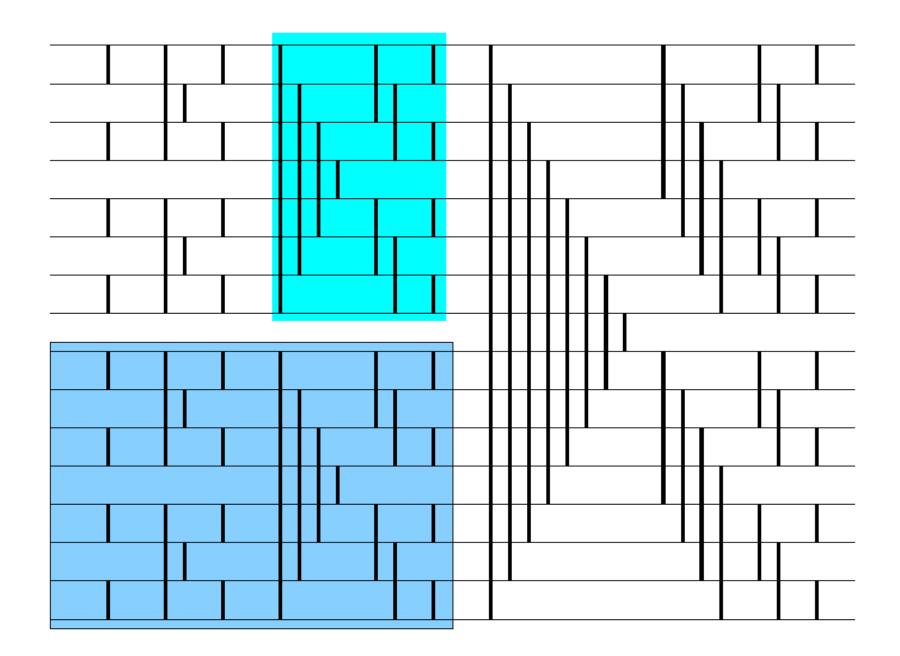
vee

vee

```
vee f g 3 out(0) -> f a(0) a(7) 101111
out(7) -> g a(7) a(0)
out(1) -> f a(1) a(6)
out(6) -> g a(6) a(1)
```

tmerge

tmerge n = compose \$ vee min max (n-1) : [dee min max (n-i) | i <- [2..n]]



tsort n = compose [tmerge i | i <- [1..n]]</pre>

Question

What are work and depth of this sorter??

Performance is decent!

Initial benchmarking for 2^20 Ints

Around 800ms on 4 cores on this laptop

Compares to around 1.6 seconds for Data.List.sort (which is sequential)

Still slower than Persson's non-entry from the sorting competition in the 2012 course (which was at 400ms) -- a factor of a bit under 2, which is about what you would expect when comparing Batcher's bitonic sort to quicksort

Comments

Should be very scalable

Can probably be sped up! Need to add sequentialness ©

Similar approach might greatly speed up the FFT in repa-examples (and I found a guy running an FFT in Haskell competition)

Note that this approach turned a nested algorithm into a flat one

Idiomatic Repa (written by experts) is about 3 times slower. Genericity costs here!

Message: map, fold and scan are not enough. We need to think more about higher order functions on arrays (e.g. with binary operators)

Repa's real strength

Stencil computations!

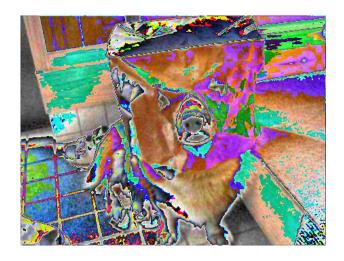
```
[stencil2| 0 1 0
1 0 1
0 1 0 |]
```

```
do
  (r, g, b) <- liftM (either (error . show) R.unzip3) readImageFromBMP "in.bmp"
  [r', g', b'] <- mapM (applyStencil simpleStencil) [r, g, b]
  writeImageToBMP "out.bmp" (U.zip3 r' g' b')</pre>
```

Repa's real strength

http://www.cse.chalmers.se/edu/year/2015/course/DAT280_Parallel_Functional_Programming/Papers/RepaTutorial13.pdf





Nice success story at NYT

Haskell in the Newsroom

Haskell in Industry

stackoverflow

is your friend

See for example

http://stackoverflow.com/questions/14082158/idiomatic-option-pricing-and-risk-using-repa-parallel-arrays?rq=1

Conclusions

Based on DPH technology

Good speedups!

Neat programs

Good control of Parallelism

BUT CACHE AWARENESS needs to be tackled

Array representations for parallel functional programming is an important, fun and frustrating research topic ©

Questions to think about

What is the right set of whole array operations?

(remember Backus from the first lecture)

par and pseq
Parallel strategies
Par monad

Skeletons

par and pseq
Parallel strategies
Par monad

Skeletons

DPH

Repa

Accelerate

par and pseq

Parallel strategies

Par monad

Skeletons

Haxl

DPH SaC

Repa

Accelerate

par and pseq

Parallel strategies

Par monad

Skeletons



Backus
Bird Meertens

DPH SaC

Haxl

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Haxl

Repa

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par and pseq

Parallel strategies

Par monad

Skeletons





DPH SaC

Haxl

Repa

Accelerate

Find out more

Haskell Symposium

Array Workshop (PLDI)

Functional High Performance Computing (ICFP)

• • • •

FP group talks

Internships / meetups / developer conferences

Books e.g. http://www.parallel-algorithms-book.com/

Crux

Abstract, beautiful, elegant, simple

Real, physical, large scale, users, complicated

"It has long been my personal view that the separation of practical and theoretical work is artificial and injurious. Much of the practical work done in computing, both in software and in hardware design, is unsound and clumsy because the people who do it have not any clear understanding of the fundamental design principles of their work. Most of the abstract mathematical and theoretical work is sterile because it has no point of contact with real computing. One of the central aims of the Programming Research Group as a teaching and research group has been to set up an atmosphere in which this separation cannot happen."

Christoper Strachey

Best masters thesis topics

you dream up yourself!

Future

Heterogeneous

Huge Scale! Exascale

embedded

DSLs

Exam

No fundmental change will not insist on correct syntax

Guest lectures are also fair game