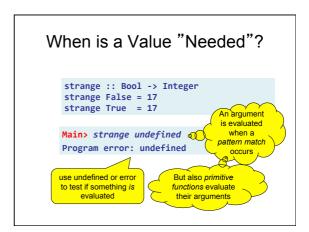


Laziness • Haskell is a lazy language - A particular function argument is only evaluated when it is needed, and - if it is needed then it is evaluated just once (\x -> x + x) (9 + 12) A computation model called graph reduction (9 + 12) (9 + 12) (1) needs its arguments



Lazy Programming Style

- Separate
 - Where the computation of a value is defined
 - Where the computation of a value happens



Backtracking

- · E.g. the Suduko lab
- Write an expression which represents all valid solutions to a problem and pick the first one.
- Laziness ensures that we do not generate more than we need

```
At Most Once?

apa :: Integer -> Integer
apa x = (f x)^2 + f x + 1

Main> apa (6^2)

bepa :: Integer -> Integer -> Integer
bepa x y = f 17 + x + y

Main> bepa 1 2 + bepa 3 4

"
Quiz: How to avoid recomputation?
```

Infinite Lists

- Because of laziness, values in Haskell can be infinite
- Do not compute them completely!
 Instead, only use parts of them take n [3..]
 xs `zip` [1..]

Examples

· Uses of infinite lists

```
iterate
iterate :: (a -> a) -> a -> [a]
iterate f x = x : iterate f (f x)

Main> iterate (*2) 1
[1,2,4,8,16,32,64,128,256,512,1024,...
```

Other Handy Functions

```
repeat :: a -> [a]
repeat x = x : repeat x

cycle :: [a] -> [a]
cycle xs = xs ++ cycle xs

Quiz: How to
define these
with iterate?
```

Alternative Definitions

```
repeat :: a -> [a]
repeat x = iterate id x

cycle :: [a] -> [a]
cycle xs = concat (repeat xs)
```

Replicate

```
replicate :: Int -> a -> [a]
replicate n x = take n (repeat x)

Main> replicate 5 'a'
"aaaaa"
```

Problem: Grouping List Elements

```
group :: Int -> [a] -> [[a]]
group = ?

Main> group 3 "apabepacepa!"
["apa","bep","ace","pa!"]
```

Problem: Grouping List Elements

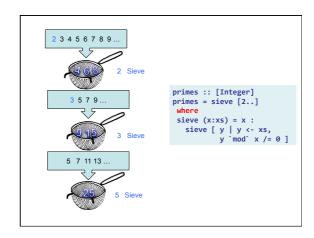
```
group :: Int -> [a] -> [[a]]
group n = takeWhile (not . null)
. map (take n)
. iterate (drop n)

. connects "stages"
-- like Unix pipe
symbol |
```

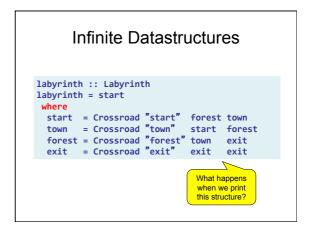
Problem: Prime Numbers

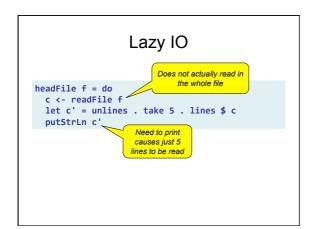
```
primes :: [Integer]
primes = ?

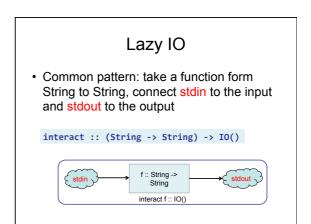
Main> take 4 primes
[2,3,5,7]
```

Infinite Datastructures data Labyrinth = Crossroad { what :: String , left :: Labyrinth , right :: Labyrinth } How to make an interesting labyrinth?







Lazy IO

import Network.HTTP.Base(urlEncode)

encodeLines = interact \$
 unlines . map urlEncode . lines

Main> encodelines hello world hello%20world 2+3=5 2%2B3%3D5

...

Other IO Variants

String is a list of Char, each element is thus allocated individually. IO using String has very poor performance

- Data.ByteString provides an alternative non-lazy array-like representation ByteString
- Data.ByteString.Lazy provides a hybrid version which works like a list of max 64KB chunks

Controlling Laziness

- Haskell includes some features to reduce the amount of laziness allowing us to decide when something gets evaluated
- Used for performance tuning, particularly for controlling space usage
- Not recommended that you mess with this unless you have to – hard to get right in general



Example

· Sum of a list of numbers

million :: Integer million = 1000000

Main sum [1..million]
** Exception: Stack overflow **

Example

• sum of a list of numbers

sum':: [Integer] -> Integer
sum' [] = 0
sum' (x:xs) = x + sum' xs

million = 1000000 :: Integer

Main sum' [1..million]

** Exception: Stack overflow **

Not a problem of lazy evaluation! All languages will have problems with this

1 + (2 + (3 + (4 + ...

Tail Recursion

- Important concept in non-lazy functional programming for efficient recursion
- Also useful in Haskell for recursive functions which compute a basic typed result (Integer, Double, Int, ...)

results which cannot be computed lazily (bit-by-bit)

Tail Recursion

 A function is tail recursive if the recursive call itself produces the result

Example

```
last :: [a] -> a
last [x] = x
last (x:xs) = last xs

The recursive call is the whole result
```

Tail recursion uses no stack space. Can be compiled to an unconditional jump

Tail Recursive Sum

```
sum':: [Integer] -> Integer
sum' = s 0
    where s acc [] = acc
    s acc (x:xs) = s (acc+x) xs
```

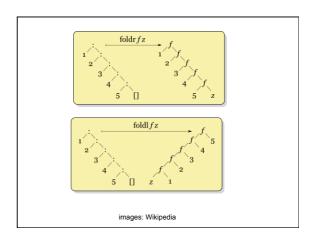
 Not typically used with lazy data (e.g. lists) since it stops us producing any of the result list until the last step of the recursion

The Tail Recursive Pattern: foldl

```
fold1 :: (a -> b -> a) -> a -> [b] -> a
fold1 f v [] = v
fold1 f v (x:xs) = fold1 f (f v x) xs

fold1 f v ( a : b : c : ...)
gives (...(v `f` a) `f` b) `f` c ) `f` ...

sum = fold1 (+) 0
```



Problem solved?

· Lazy evaluation is too lazy!

```
sum' [1..million]
== s 0 [1..million]
== s (0+1) [2..million]
== s (0+1+2) [3..million]
...

Not computed until needed.
i.e., at the millionth recursive call!
```

Controlling lazyness: seq

Haskell includes a primitive function

which forces it's first argument to be evaluated (typically before evaluating the second).

The prelude also defines a strict application operation:

```
($!) :: (a -> b ) -> a -> b

f $! x = x `seq` f x
```

Strictness

 The compiler looks for arguments which will eventually be needed and will insert seg in appropriate places. E.g.

```
sum':: [Integer] -> Integer
sum' = s 0
where s acc [] = acc
s acc (x:xs) = acc `seq` s (acc+x) xs

force acc to be simplified on each recursive call
```

Strict Tail Recursion: foldl'

Example

Space Leak

- This problem is often called a space leak
 - sum forces us to build the whole of [1..million]
 - lazyness ("at most once") requires us to keep the list in memory since it is going to be used by length
 - if we only computed sum then the garbage collector would collect it as we go along.

Solution

 Make average use tail recursion by computing sum and length at the same time:

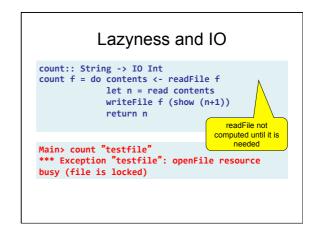
Gotcha: seq is still quite lazy!

seq forces evaluation of first argument, but only as far as the outermost constructor

This is called "evaluation to weak head-normal form (whnf)". Examples of whnfs:

```
- undefined : undefined
- (undefined, undefined)
- Just undefined
> undefined:undefined `seq` 3
3
```

Example: sumlength sumlength = foldl' f (0,0) where f (s,1) a = (s+a,1+1) sumlength = foldl' f (0,0) where f (s,1) a = let (s',1') = (s+a,1+1) in s' `seq` l' `seq` (s',1') force the evaluation of the components before the pair is constructed



Lazyness and IO

```
count:: String -> IO Int
count f = do contents <- readFile f
    let n = read contents
    n `seq` writeFile f (show (n+1))
    return n</pre>
```

- · Often lazy IO is "just the right thing"
- · Need to control it sometimes
 - Usually solve this by working at the level of file handles. See e.g. System.IO

Conclusion

- Laziness
 - Evaluate "at most once"
 - programming style
- · Do not have to use it
 - But powerful tool!
- · Can make programs more "modular"
- · Performance issues tricky
 - evaluation can be controlled using e.g. tail recursion and strictness. Best avoided unless necessary

Next time: Controlling Evaluation for Parallelism

- In theory a compiler should be able to automatically compile pure functional programs to use multiple cores
 - purity ⇒ computations can be freely reordered without changing the result
- In practice this is hard. We need to give hints as to which strategy to use
 - but no synchronisation/deadlock issues need to be considered!

par and pseq

ghc -threaded uses a threaded runtime system. To make use of it we need to add some parallelism hints to the code

Control.Parallel provides

```
pseq , par :: a -> b -> b
```

- pseq seq but with a stronger promise of left-to-right evaluation order
- par maybe evaluate left argument (to whnf) possibly in parallel with its right arg.