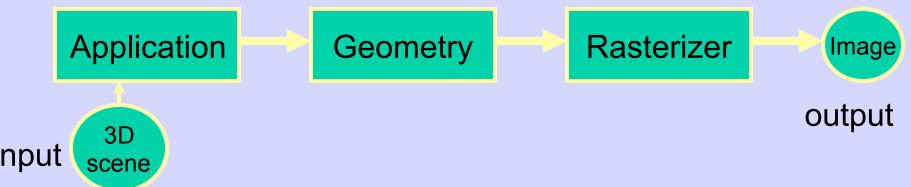
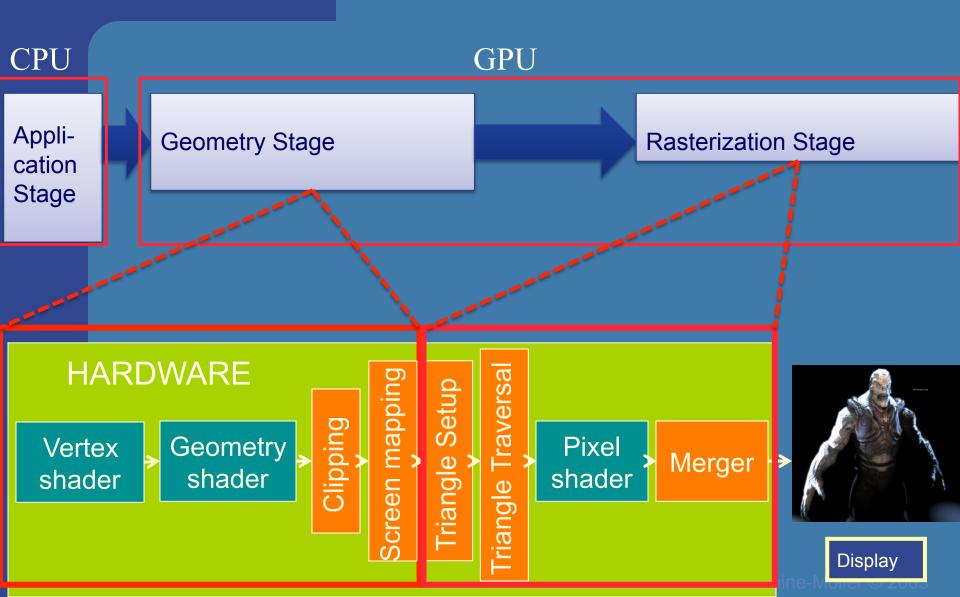
Full-time wrapup

Lecture 1: Real-time Rendering The Graphics Rendering Pipeline

- Three conceptual stages of the pipeline:
 - Application (executed on the CPU)
 - logic, speed-up techniques, animation, etc...
 - Geometry
 - Executing vertex and geometry shader
 - Vertex shader:
 - lighting computations per triangle vertex
 - Project onto screen (3D to 2D)
 - Rasterizer
 - Executing fragment shader
 - Interpolation of parameters (colors, texcoords etc) over triangle
 - Z-buffering, fragment merge (i.e., blending), stencil tests...



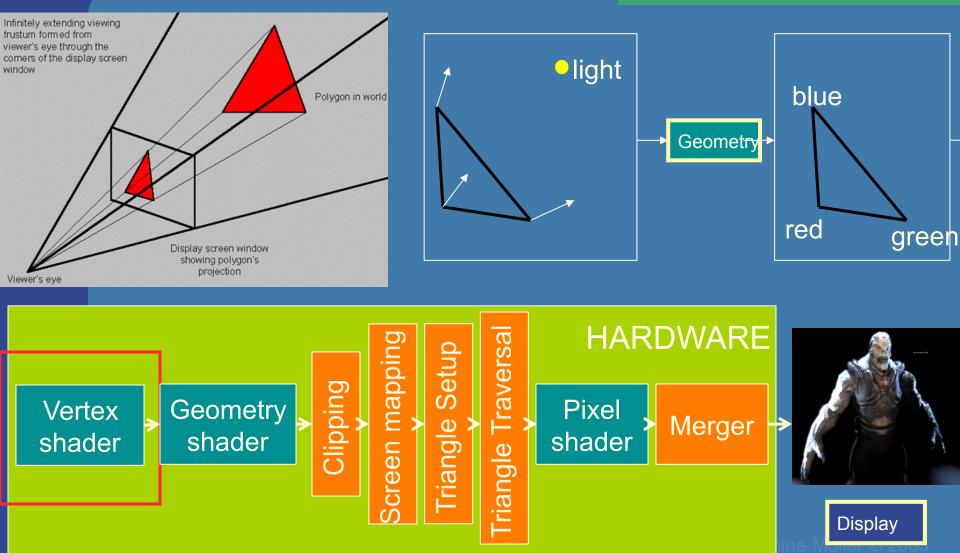
Rendering Pipeline and Hardware



Geometry Stage

Vertex shader:

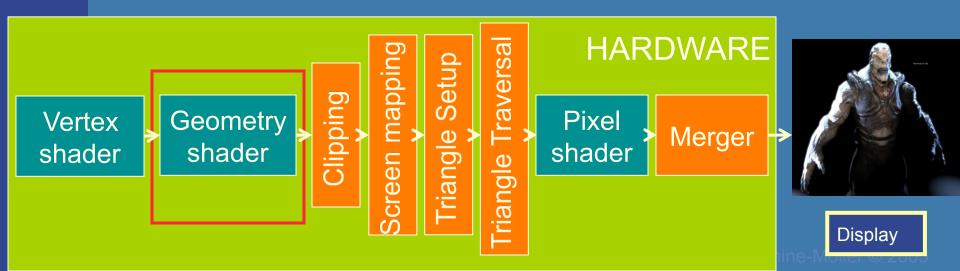
- •Lighting (colors)
- •Screen space positions



Geometry Stage

Geometry shader:

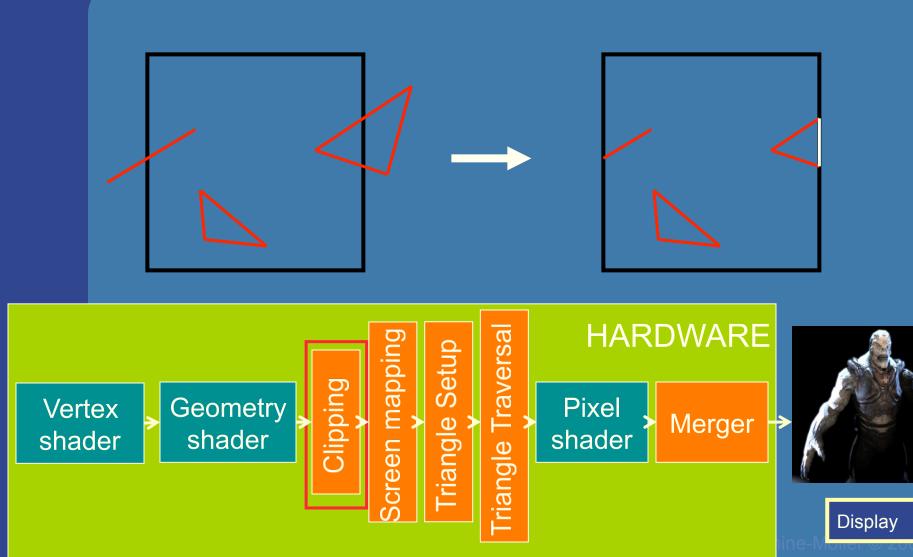
- •One input primitive
- •Many output primitives



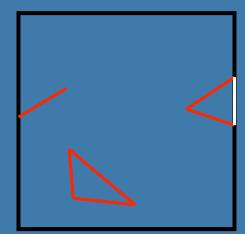
or

Geometry Stage

Clips triangles against the unit cube (i.e., "screen borders")



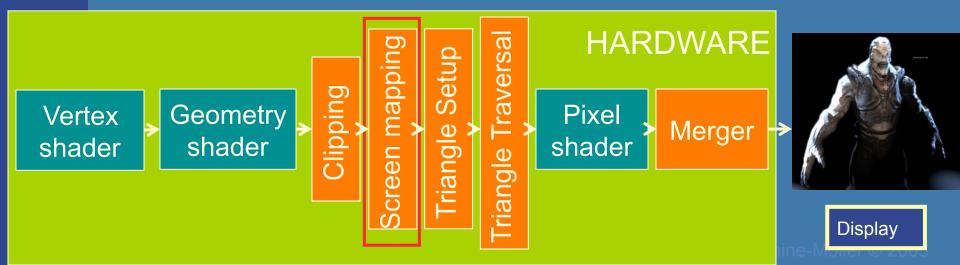
Rasterizer Stage



Maps window size to unit cube

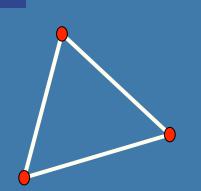
Geometry stage always operates inside a unit cube [-1,-1,-1]-[1,1,1] Next, the rasterization is made against a draw area corresponding to window dimensions.

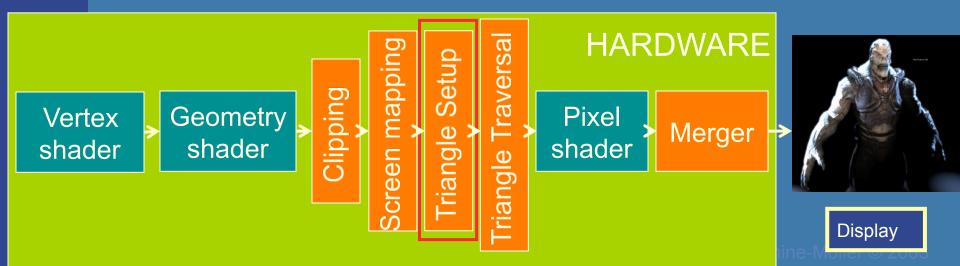




Rasterizer Stage

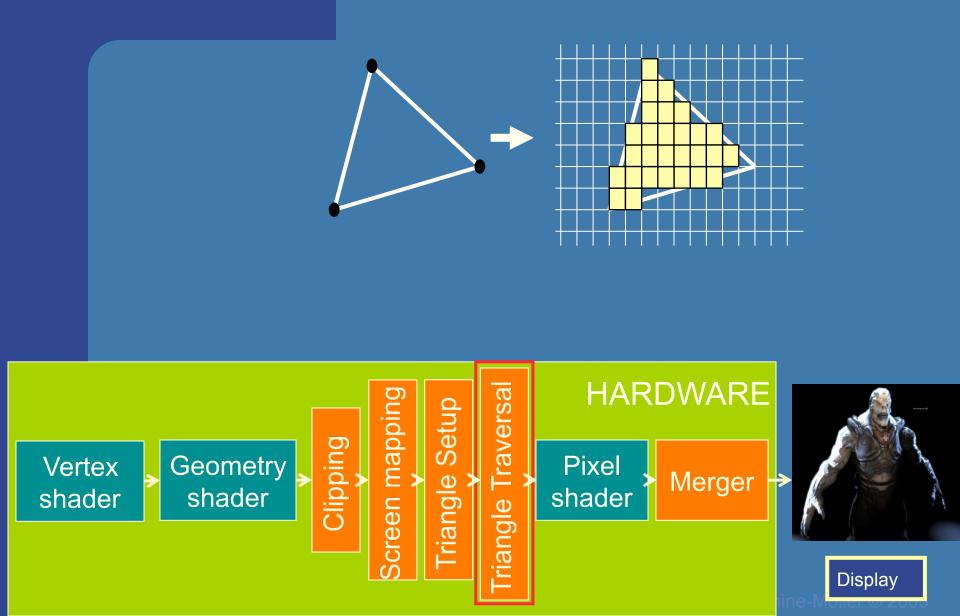
Collects three vertices into one triangle





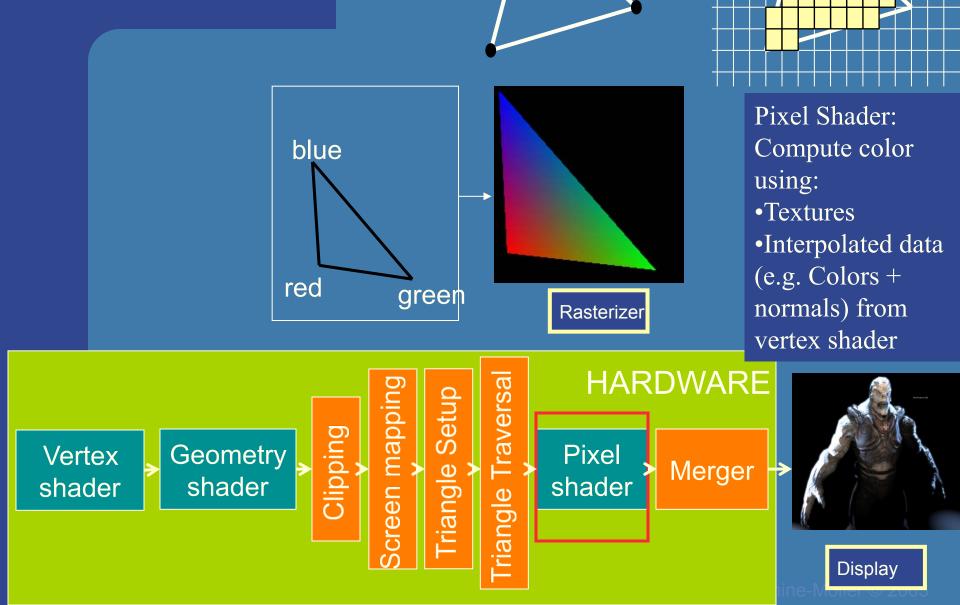
Rasterizer Stage

Creates the fragments/ pixels for the triangle





Rasterizer Stage



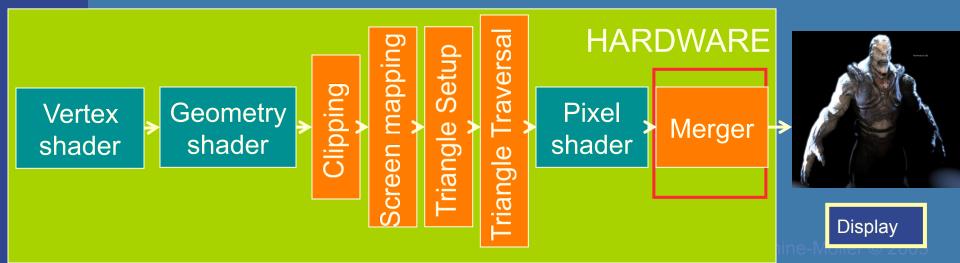
Rasterizer Stage

The merge units update the frame buffer with the pixel's color



Frame buffer:

- Color buffers
- Depth buffer
- Stencil buffer



z-Buffer Algorithm

- Use a buffer called the z or depth buffer to store the depth of the closest object at each pixel found so far
- As we render each polygon, compare the depth of each pixel to depth in z buffer
- If less, place shade of pixel in color buffer and update z buffer

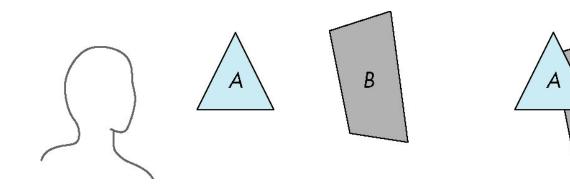
Also know double buffering!

Screen Tearing



Painter's Algorithm

 Render polygons a back to front order so that polygons behind others are simply painted over



B behind A as seen by viewer

Fill B then A

B

•Requires ordering of polygons first

–O(n log n) calculation for ordering
–Not every polygon is either in front or behind all other polygons

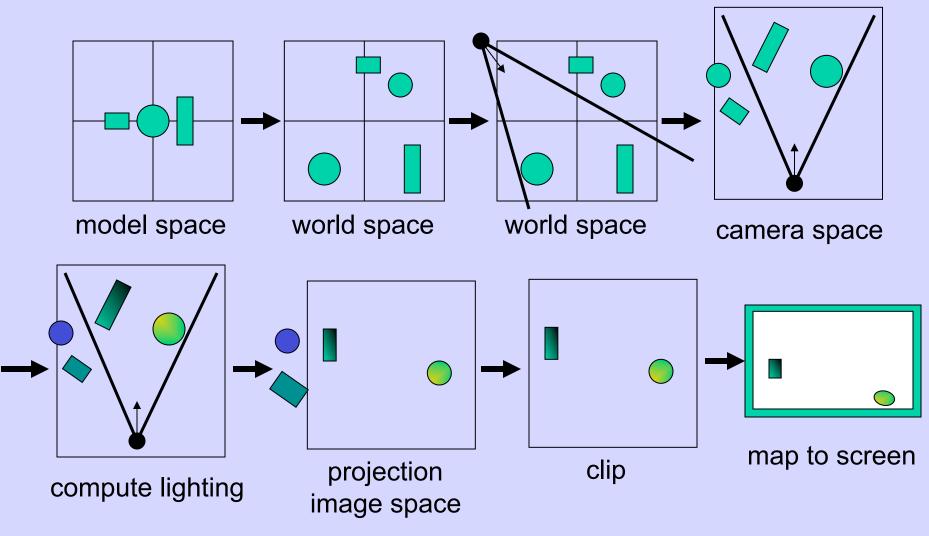
I.e., : Sort all triangles and render them back-to-front.

GEOMETRY – transformation summary

Application

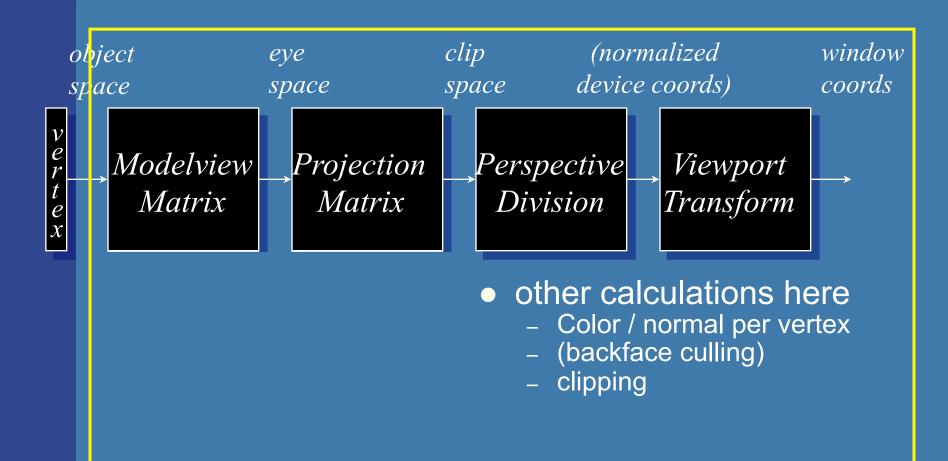
Geometry

Rasterizer



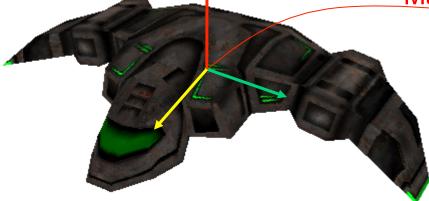
Lecture 2:

Transformation Pipeline



OpenGL | Geometry stage | done on GPU

Model to World Matrix



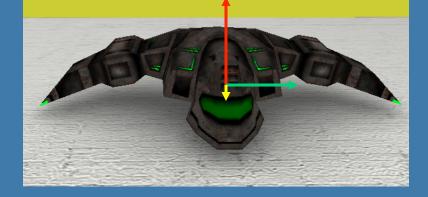
Model space

World space

World to View Matrix

camera

ModelViewMtx = Model to View Matrix



View space

Lecture 2: Transforms

Scaling, rotations, translations

• Cannot use same matrix to transform normals

Use:
$$\mathbf{N} = \left(\mathbf{M}^{-1}\right)^T$$
 instead of \mathbf{M}

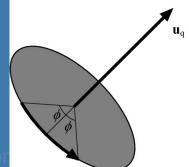
Homogeneous notation

- Projections
- Quaternions $\hat{\mathbf{q}} = (\sin \phi \mathbf{u}_q, \cos \phi)$

Know what they are good for. Not knowing the mathematical rules.



 ...represents a rotation of 2φ radians around axis uq of point p



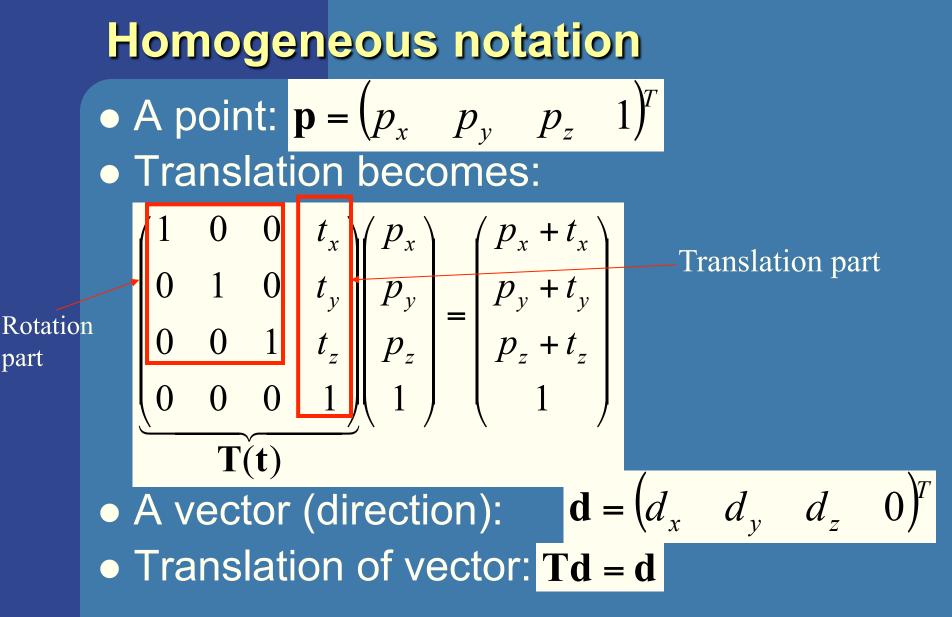
 $(M^{-1})^{T} = M$

transform

if rigid-

body

02. Vectors and Transforms



Change of Frames
• How to get the M_{model-to-world} matrix:
$$P=(0,5,0,1)$$
 (M_{model-to-world} =
$$\begin{bmatrix} a_x & b_x & c_x & o_x \\ a_y & b_y & c_y & o_y \\ a_z & b_z & c_z & o_z \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 \\ 5 \\ 0 \\ 1 \end{bmatrix} \mathbf{y}$$

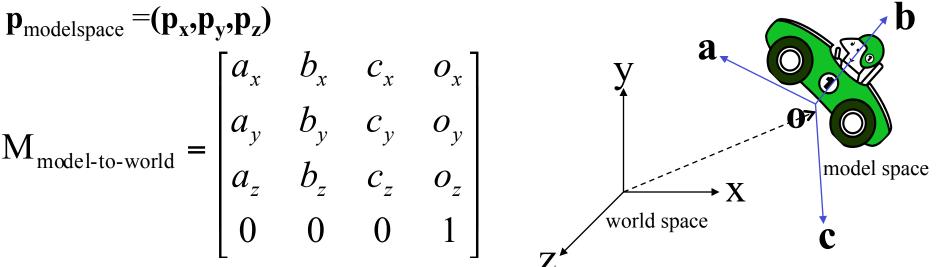
The basis vectors **a,b,c**

are expressed in the world coordinate system (Both coordinate systems are right-handed)

E.g.:
$$\mathbf{p}_{\text{world}} = \mathbf{M}_{\text{m}\to\text{w}} \mathbf{p}_{\text{model}} = \mathbf{M}_{\text{m}\to\text{w}} (0,5,0,1)^{\text{T}} = 5 \mathbf{b} (+ \mathbf{o})$$

Same example, just explained differently:

Change of Frames



Let's initially disregard the translation **o**. I.e., $\mathbf{o}=[0,0,0]^{\mathbb{Z}}$ X: One step along **a** results in \mathbf{a}_x steps along world space axis x. One step along **b** results in \mathbf{b}_x steps along world space axis x.

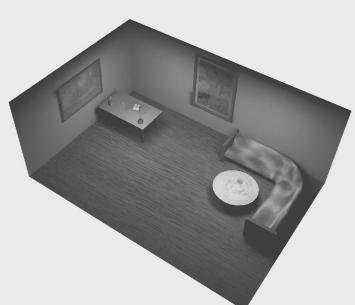
One step along **c** results in \mathbf{c}_x steps along world space axis x.

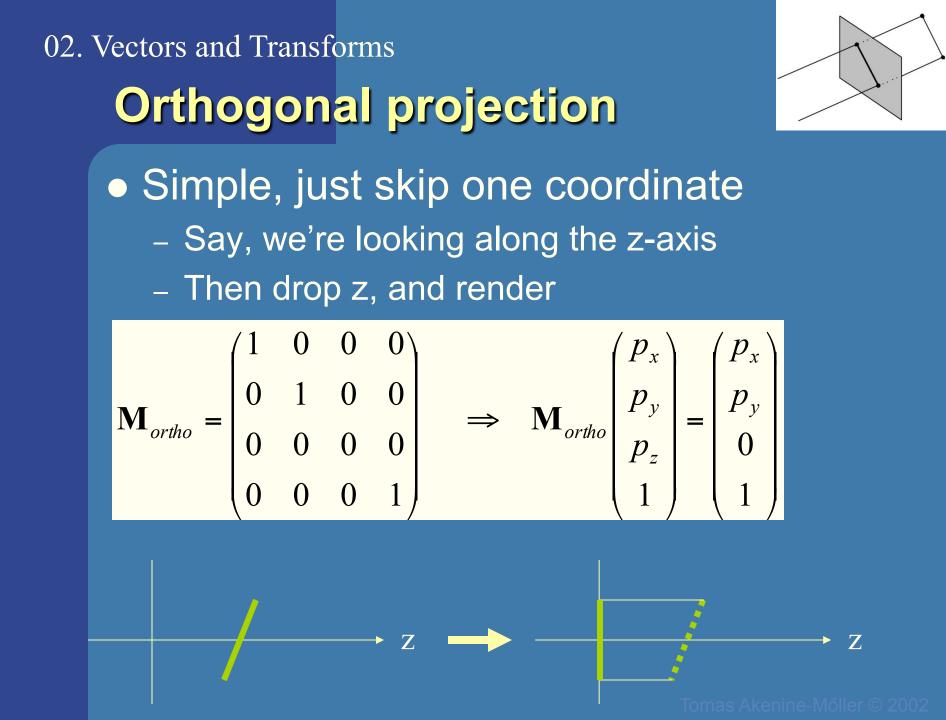
The x-coord for **p** in *world space* (instead of modelspace) is thus $[a_x b_x c_x]\mathbf{p}$. The y-coord for **p** in world space is thus $[a_y b_y c_y]\mathbf{p}$. The z-coord for **p** in world space is thus $[a_z b_z c_z]\mathbf{p}$.

With the translation **o** we get $\mathbf{p}_{\text{worldspace}} = M_{\text{model-to-world}} \mathbf{p}_{\text{modelspace}}$

02. Vectors and Transforms **Projections** Orthogonal (parallel) and Perspective



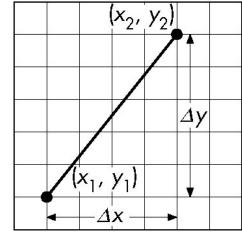




02. Rasterization, Depth Sorting and Culling:

DDA Algorithm

<u>Digital Differential Analyzer</u>



–DDA was a mechanical device for numerical solution of differential equations

-Line y=kx+ m satisfies differential equation dy/dx = k = $\Delta y/\Delta x = y_2-y_1/x_2-x_1$

• Along scan line $\Delta x = 1$

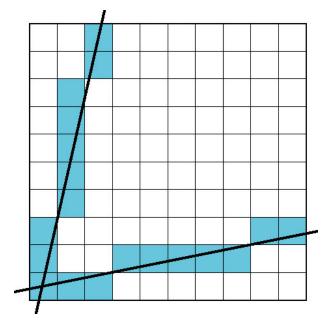
```
y=y1;
For(x=x1; x<=x2,ix++) {
   write_pixel(x, round(y), line_color)
   y+=k;
}
```

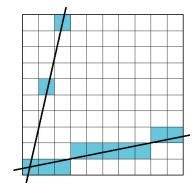
02. Rasterization, Depth Sorting and Culling:

Using Symmetry

- Use for $1 \ge k \ge 0$
- For k > 1, swap role of x and y

-For each y, plot closest x





Otherwise we get problem for steep slopes 02. Rasterization, Depth Sorting and Culling:

- Very Important!

- The problem with DDA is that it uses floats which was slow in the old days
- Bresenhams algorithm only uses integers

You do not need to know Bresenham's algorithm by heart. It is enough that you **understand** it if you see it.

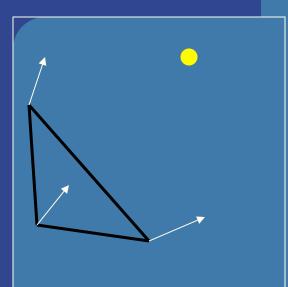
LightingLecture 3: Shading $i=i_{amb}+i_{diff}+i_{spec}+i_{emission}$



Know how to compute components. Also, Blinns and Phongs highlight model

Ulf Assarsson © 2004

Lighting



Material:

•Ambient (r,g,b,a)

- •Diffuse (r,g,b,a)
- •Specular (r,g,b,a)
- •Emission (r,g,b,a) ="självlysande färg"

Light:

•Ambient (r,g,b,a)

•Diffuse (r,g,b,a)

•Specular (r,g,b,a)

DIFFUSE	Base color
SPECULAR	Highlight Color
AMBIENT	Low-light Color
EMISSION	Glow Color
SHININESS	Surface Smoothness

3. Shading:
Lighting

$$i=i_{amb}+i_{diff}+i_{spec}+i_{emission}$$

I.e.:
 $i=i_{amb}+i_{diff}+i_{spec}+i_{emission}$
 $i_{amb} = \mathbf{m}_{amb} \otimes \mathbf{s}_{amb}$
 $i_{diff} = (\mathbf{n}\cdot\mathbf{l})\mathbf{m}_{diff} \otimes \mathbf{s}_{diff}$
(($\mathbf{n}\cdot\mathbf{l}$) < 0) $\Rightarrow \mathbf{i}_{spec / diff} = 0$
Phong's reflection model:
 $\mathbf{i}_{spec} = \max(0, (\mathbf{r}\cdot\mathbf{v}))^{m_{shi}} \mathbf{m}_{spec} \otimes \mathbf{s}_{spec}$
Blinn's reflection model:
 $\mathbf{i}_{spec} = \max(0, (\mathbf{h}\cdot\mathbf{n}))^{m_{shi}} \mathbf{m}_{spec} \otimes \mathbf{s}_{spec}$

$$\mathbf{i}_{emission} = \mathbf{m}_{emission}$$

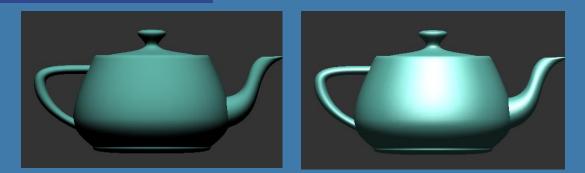
0

Tomas Akenine-Mőller © 2002

03. Shading:

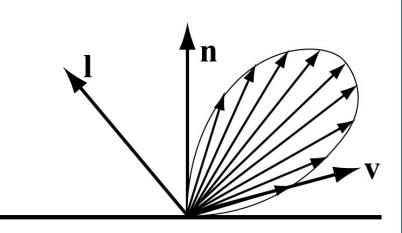
Diffuse component : idiff • = amb+ diff+ spec+ emission • Diffuse is Lambert's law: $i_{diff} = \mathbf{n} \cdot \mathbf{l} = \cos \phi$ Photons are scattered equally in all directions (Note that **n** and **l** need to be $\mathbf{i}_{diff} = (\mathbf{n} \cdot \mathbf{l})\mathbf{m}_{diff} \otimes \mathbf{s}_{diff}$ normalized) \bigcirc light source φ $l/\cos\phi$

03. Shading: Lighting Specular component : ispec



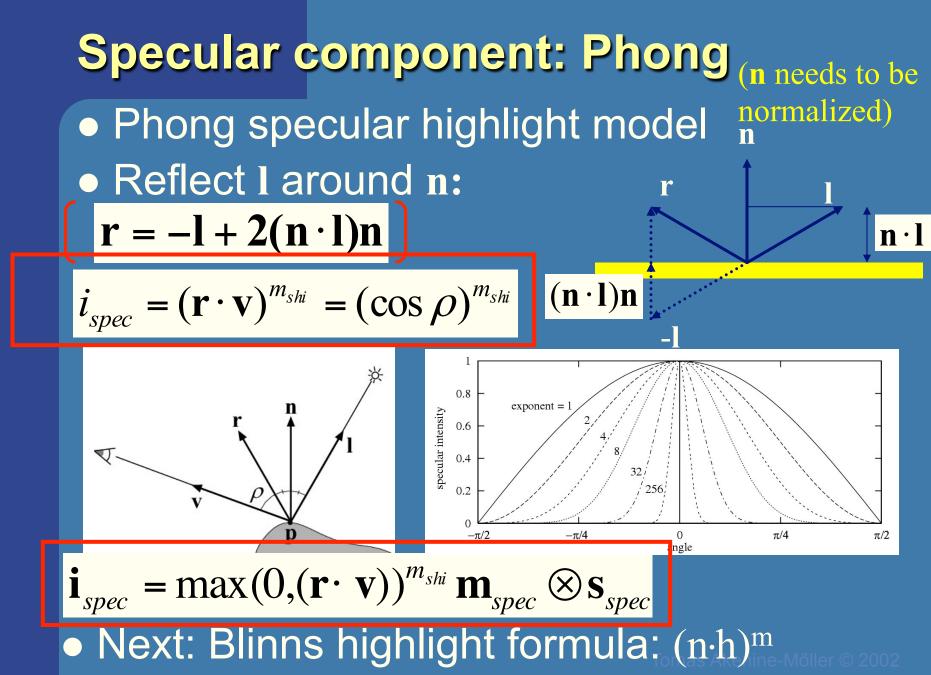
Diffuse is dull (left)Specular: simulates a highlight

 \bigcirc light source



Tomas Akenine-Mőller © 2002

03. Shading:





Halfway Vector

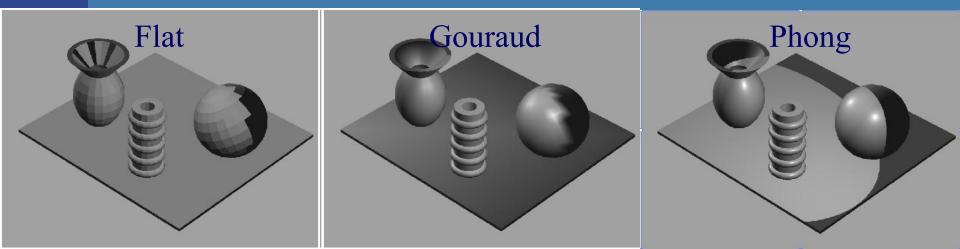
The University of New Mexico

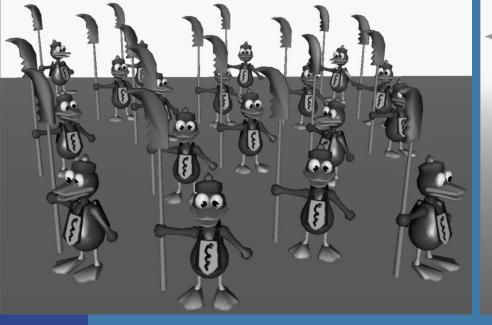
Blinn proposed replacing **v**·**r** by **n**·**h** where h = (I+v)/|I + v| $(\mathbf{I}+\mathbf{v})/2$ is halfway between **I** and **v** n If **n**, **I**, and **v** are coplanar: w $\psi = \phi/2$ Must then adjust exponent so that $(\mathbf{n} \cdot \mathbf{h})^{e'} \approx (\mathbf{r} \cdot \mathbf{v})^{e}$ $(e' \approx 4e)$ $= \max(0, (\mathbf{h} \cdot \mathbf{n})^{m_{shi}})\mathbf{m}_{snec}$

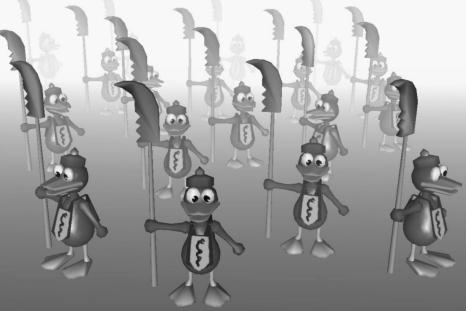
03. Shading:

Shading

- Three common types of shading:
 - Flat, Goraud, and Phong
- In standard Gouraud shading the lighting is computed per triangle vertex and for each pixel, the <u>color is interpolated</u> from the colors at the vertices.
- In Phong Shading the lighting is <u>not</u> computed per vertex. Instead the <u>normal is interpolated</u> per pixel from the normals defined at the vertices and <u>full lighting is computed per pixel</u> using this normal. This is of course more expensive but looks better.







• Color of fog: \mathbf{c}_f color of surface: \mathbf{c}_s $\mathbf{c}_p = f\mathbf{c}_s + (1 - f)\mathbf{c}_f$ $f \in [0,1]$

• How to compute *f*?

• E.g., linearly:

$$f = \frac{Z_{end} - Z_p}{Z_{end} - Z_{start}}$$

Tomas Akenine-Mőller © 2002

03. Shading:

Transparency and alpha

• Transparency

- Very simple in real-time contexts
- The tool: alpha blending (mix two colors)
- Alpha (α) is another component in the frame buffer, or on triangle
 - Represents the opacity
 - 1.0 is totally opaque
 - 0.0 is totally transparent

• The over operator: (Blending) $\mathbf{c}_{o} = \alpha \mathbf{c}_{s} + (1 - \alpha) \mathbf{c}_{d}$

Rendered object

Tomas Akenine-Mőller © 2002

03. Shading:

Transparency

Need to sort the transparent objects

- First, render all non-transparent triangles as usual.
- Then, sort all transparent triangles and render back-to-front with blending enabled. (and using standard depth test)

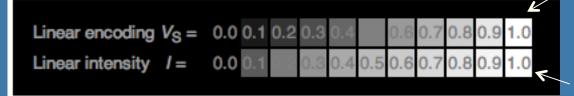
 The reason is to avoid problems with the depth test and because the blending operation (i.e., over operator) is order dependent.

$$c = c_i^{(1/\gamma)}$$

Gamma correction

monitor/intensity relation gamma correction corrected signal * gamma corrected level 0.8 0.8 0.8 output signal 0.4 intensity 0.6 0.6 = 04 0.4 0.2 0.2 0.2 0.4 0.6 0.8 0.2 0.4 0.6 0.8 0 0.2 0.4 0.6 0.8 0 0 electron gun voltage computed light intensity

- (Standard is 2.2)
- 1. Screen has non-linear color intensity
 - 1. We often want linear output (e.g. antialiasing)
- 2. Also happens to give more efficient color space when compressing intensity from 32-bit floats to 8-bits. Thus, often desired when storing textures.



better distribution for humans Gamma of 2.2 Truth

On most displays (those with gamma of about 2.2), one can observe that the linear intensity output (bottom) has a large jump in perceived brightness between the intensity values 0.0 and 0.1, while the steps at the higher end of the scale are hardly perceptible. A linear input that has a nonlinearly-increasing intensity (upper), will show much more even steps in perceived brightness.

Tomas Akenine-Mőller © 2002

Leture 3.2: Sampling, filtrering, and Antialiasing

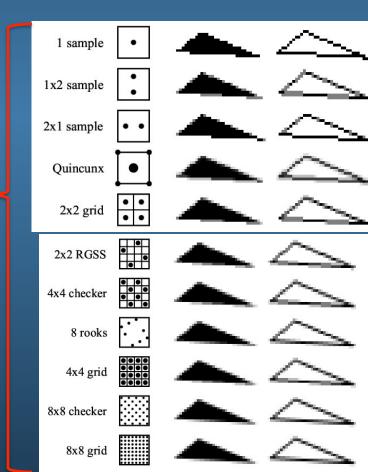
When does it occur?

In 1) pixels, 2) time, 3) texturing

Supersampling schemes

Jittered sampling
Why is it good?

•	•	•	• •	•	•
	•	• •	•		•
•	•	•	•	•	



04. Texturing

Most important:

- Texturing
 - Mipmapping: bi/tri-linear filtering, anisotropic filtering
- Environment mapping
 - Cube mapping
- Bump mapping
- 3D-textures,
- Particle systems
- Sprites and billboards

Filtering

FILTERING:

For magnification: Nearest or Linear (box vs Tent filter)

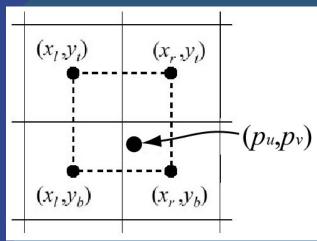


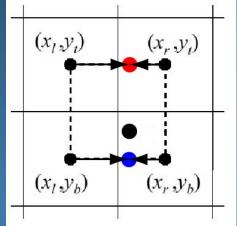
• For minification: nearest, linear and...

- Bilinear using mipmapping
- Trilinear using mipmapping
- Anisotropic up to 16 mipmap lookups along line of anisotropy

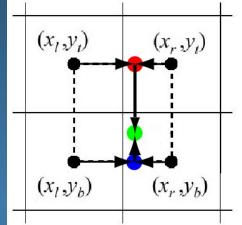
Interpolation

Magnification

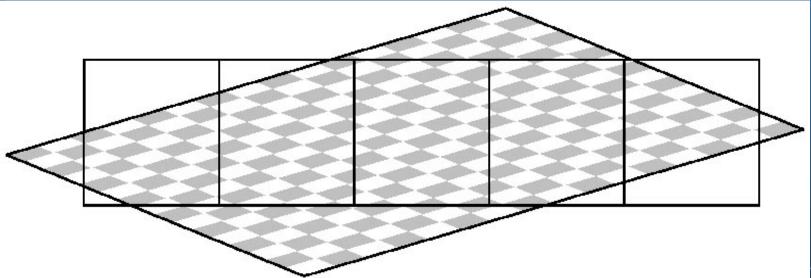




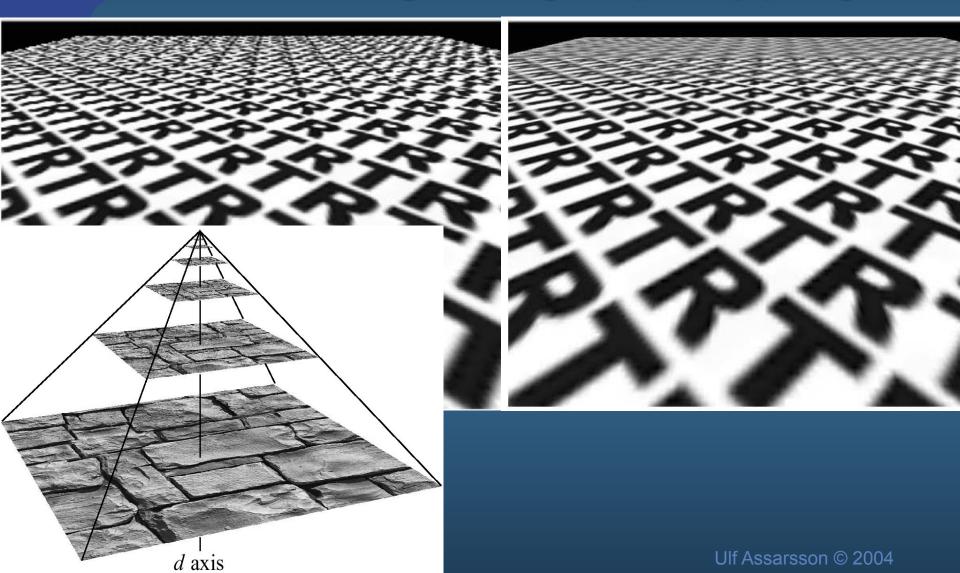




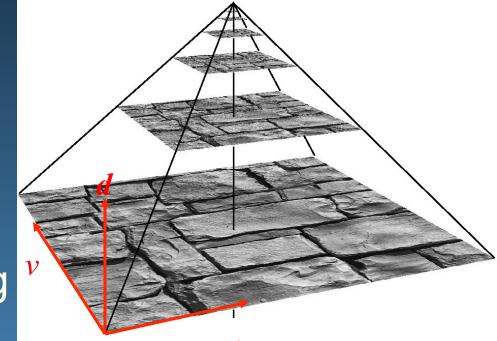
Minification



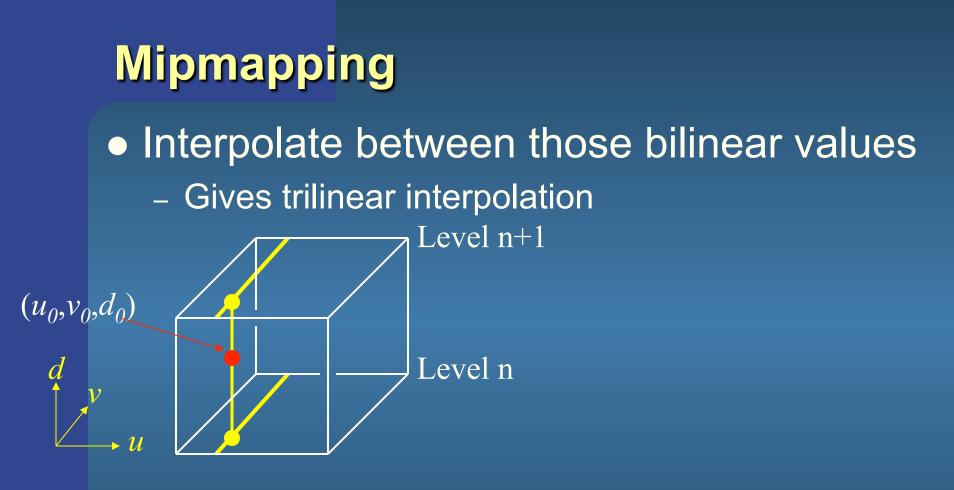
Bilinear filtering using Mipmapping



Mipmapping Image pyramid Half width and height when going upwards

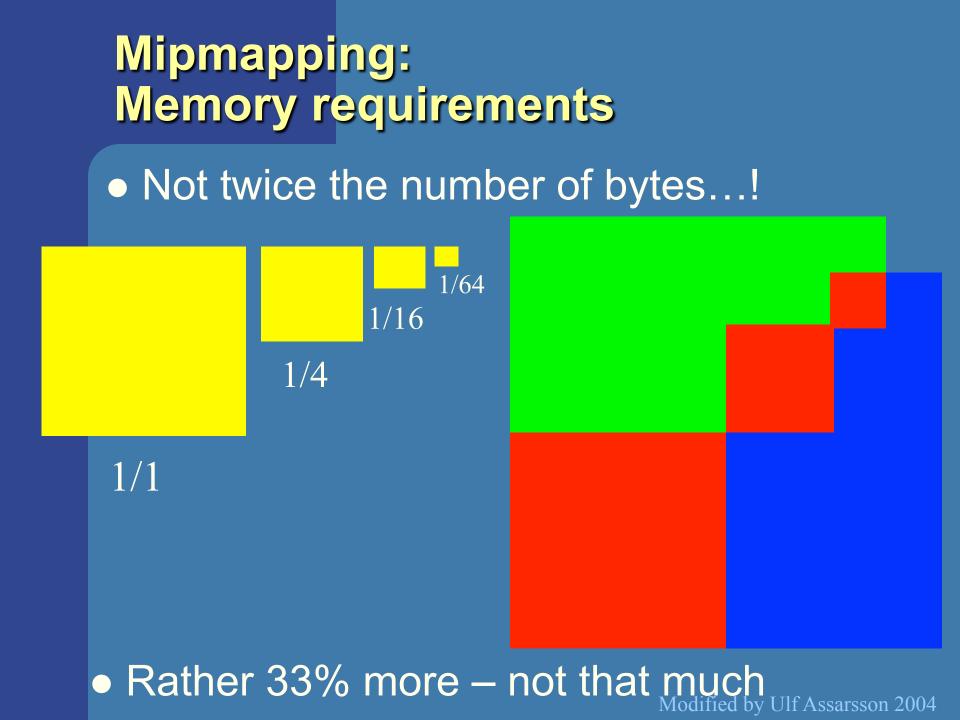


- Average over 4 "parent texels" to form "child texel"
- Depending on amount of minification, determine which image to fetch from
- Compute *d* first, gives two images
 - Bilinear interpolation in each

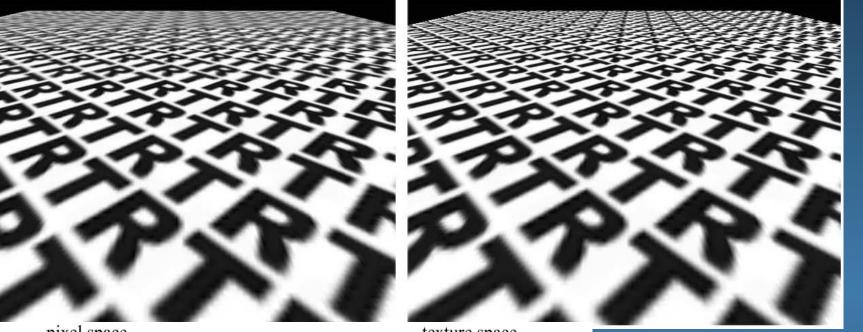


• Constant time filtering: 8 texel accesses

Tomas Akenine-Mőller © 2002

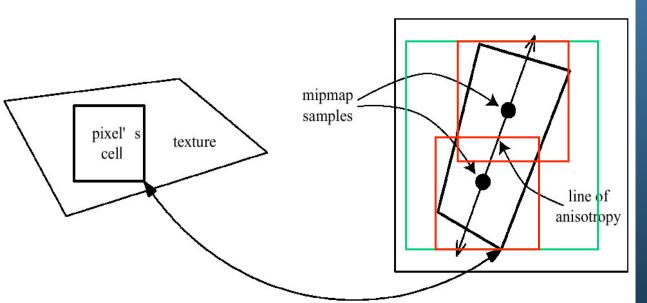


Anisotropic texture filtering



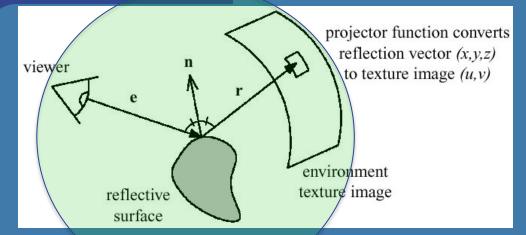
pixel space

texture space



See page 168-169

Environment mapping

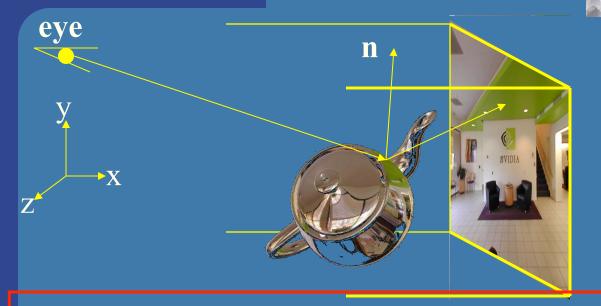




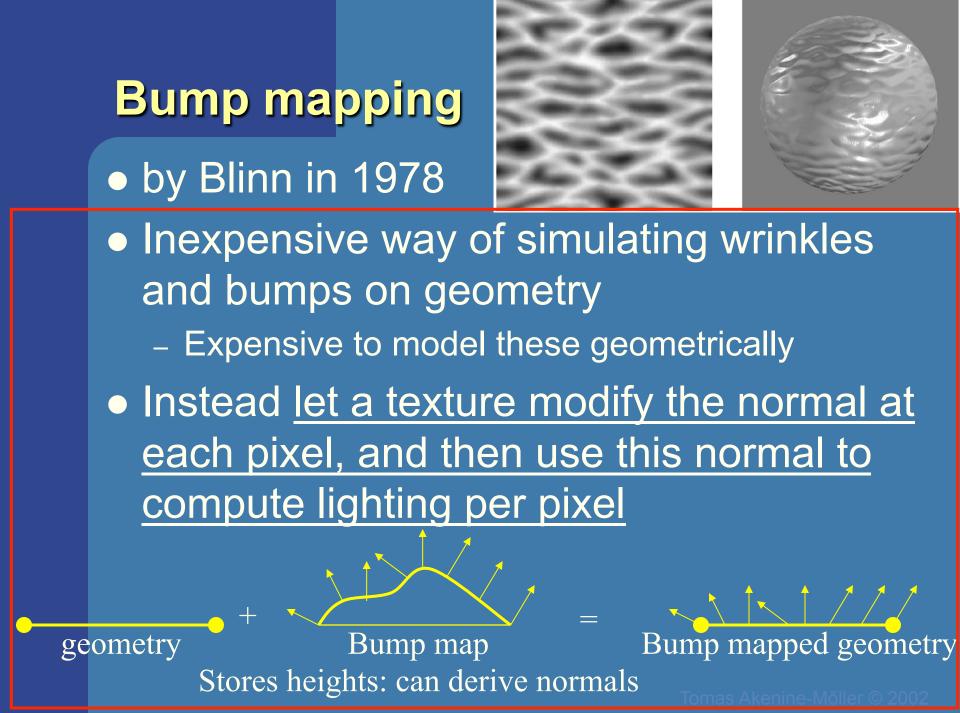
Assumes the environment is infinitely far away
Sphere mapping, or Cube mapping
Cube mapping is the norm nowadays

Modified by Ulf Assarsson 2004

Cube mapping



- Simple math: compute reflection vector, **r**
- Largest abs-value of component, determines which cube face.
 - Example: **r**=(5,-1,2) gives POS_X face
- Divide **r** by abs(5) gives (*u*,*v*)=(-1/5,2/5)
- Also remap from [-1,1] to [0,1] by (u,v) = ((u,v)+vec2(1,1))*0.5;
- Your hardware does all the work for you. You just have to compute the reflection vector.



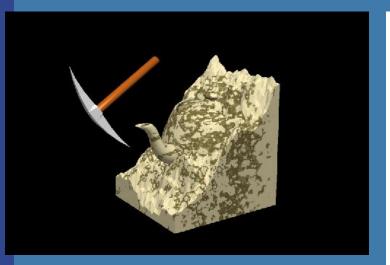
3D Textures

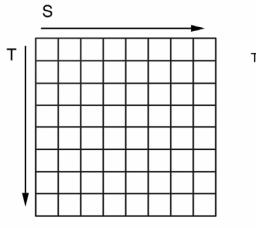
• 3D textures:

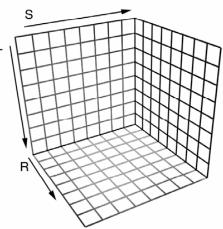




- Texture filtering is no longer trilinear
- Rather quadlinear (linear interpolation 4 times)
- Enables new possibilities
 - Can store light in a room, for example







05. Texturing:

Just know what "sprites" is and that they are very similar to a billboard

GLbyte M[64]=

{ 127,0,0,127, 127,0,0,127, 127,0,0,127, 127,0,0,127, 0,127,0,0, 0,127,0,127, 0,127,0,127, 0,127,0,0, 0,0,127,0, 0,0,127,127, 0,0,127,127, 0,0,127,0, 127,127,0,0, 127,127,0,127, 127,127,0,127, 127,127,0,0};

```
void display(void) {
  glClearColor(0.0,1.0,1.0,1.0);
  glClear(GL_COLOR_BUFFER_BIT);
  glEnable (GL_BLEND);
  glBlendFunc (GL_SRC_ALPHA,
      GL_ONE_MINUS_SRC_ALPHA);
  glRasterPos2d(xpos1,ypos1);
  glPixelZoom(8.0,8.0);
  glDrawPixels(width,height,
      GL_RGBA, GL_BYTE, M);
```

```
glPixelZoom(1.0,1.0);
glutSwapBuffers();
```

}

Sprites



Sprites (=älvor) was a technique on older home computers, e.g. VIC64. As opposed to billboards sprites does not use the frame buffer. They are rasterized directly to the screen using a

special chip. (A special bitregister also marked colliding sprites.)



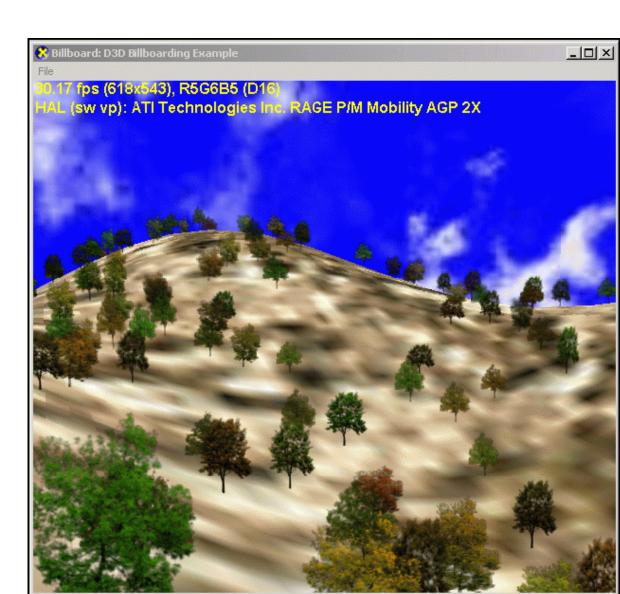
L INVADER-004 INVADER-005 U.F.D. BATTLE



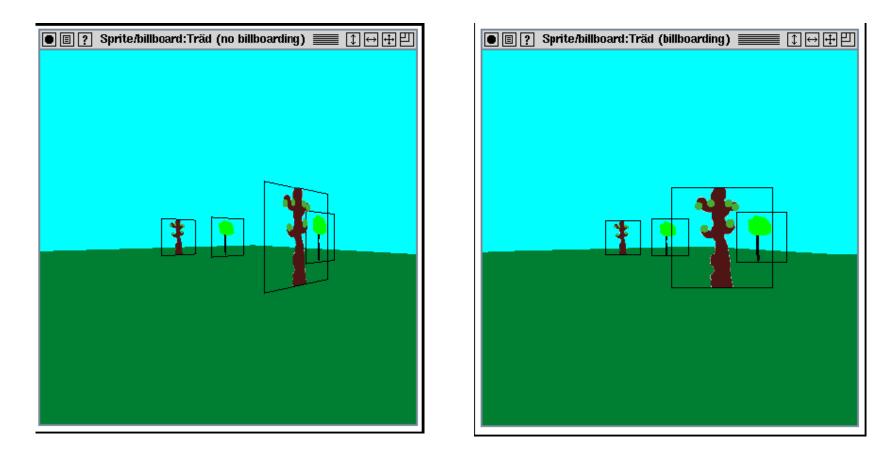


Billboards

- 2D images used in 3D environments
 - Common for trees,
 explosions,
 clouds, lens
 flares



Billboards

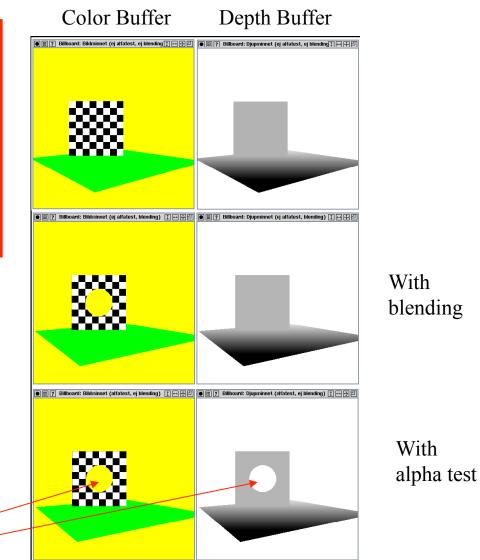


- Rotate them towards viewer
 - Either by rotation matrix or
 - by orthographic projection

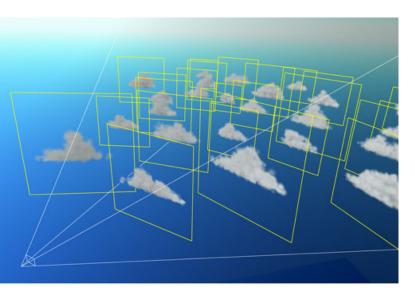
Billboards

- Fix correct transparency by
 blending AND using alpha test
 - In fragment shader: if (color.a < 0.1) discard;

If alpha value in texture is lower than this threshold value, the pixel is not rendered to. I.e., neither frame buffer nor z-buffer is updated, which is what we want to achieve.

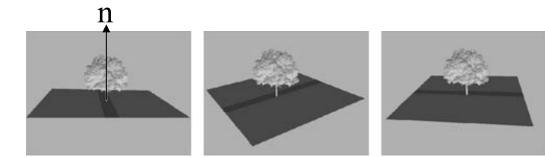


E.g. here: so that objects behind is visible through the hole





(Also called Impostors)



axial billboarding The rotation axis is fixed and disregarding the view position

Lecture 5: OpenGL

- How to use OpenGL (or DirectX)
 - Will not ask about syntax. Know how to use.
 - I.e. functionality
 - E.g. how to achieve
 - Blending and transparency
 - Fog how would you implement in a fragment shader?
 - pseudo code is enough
 - Specify a material, a triangle, how to translate or rotate an object.
 - Triangle vertex order and facing

Reflections with environment mapping

• Understand at pseudo code level!

VERTEX SHADER

in vec3 vertex; in vec3 normalIn; // The normal out vec3 normal; out vec3 eyeVector; uniform mat4 normalMatrix; uniform mat4 modelViewMatrix; uniform mat4 modelViewProjectionMatrix;

void main()

gl_Position = modelViewProjectionMatrix *vec4(vertex,1); normal = (normalMatrix * vec4(normalIn,0.0)).xyz; eveVector = (modelViewMatrix * vec4(vertex, 1)).xyz;

FRAGMENT SHADER

in vec3 normal; in vec3 eyeVector; uniform samplerCube tex1; out vec4 fragmentColor;

void main()

```
{
```

fragmentColor = texture(tex1, reflectionVector);





Buffers

- Frame buffer
 - Back/front/left/right glDrawBuffers()
 - Offscreen buffers (e.g., framebuffer objects, auxiliary buffers)

Frame buffers can consist of:

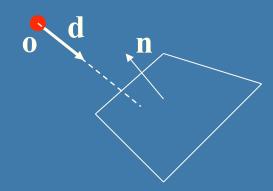
- Color buffer rgb(a)
- Depth buffer (z-buffer)
 - For correct depth sorting
 - Instead of BSP-algorithm or painters algorithm...
- Stencil buffer
 - E.g., for shadow volumes or only render to frame buffer where stencil = certain value (e.g., for masking).

Lecture 6: Intersection Tests

- 4 techniques to compute intersections:
 - Analytically
 - Geometrically e.g. ray vs box (3 slabs)
 - SAT (Separating Axis Theorem) for convex polyhedra Test:
 - 1. axes orthogonal to face of A,
 - 2. axes orthogonal to face of B
 - 3. All different axes formed by crossprod of one edge of A and one of B
 - Dynamic tests know what it means.
- E.g., describe an algorithm for intersection between a **ray** and a
 - Polygon, triangle, sphere and plane.
- Know equations for ray, sphere, cylinder, plane, triangle

Analytical: Ray/plane intersection

• Ray: **r**(*t*)=**o**+*t***d** • Plane formula: n•p + d = 0



• Replace **p** by $\mathbf{r}(t)$ and solve for t: **n**•(**o**+*t***d**) + d = 0 **n•o+***t***n•d +** d **= 0** $t = (-d - n \cdot o) / (n \cdot d)$

Here, one scalar equation and one unknown -> just solve for t.

Analytical: Ray/sphere test

- Sphere center: c, and radius r
- Ray: **r**(*t*)=**o**+*t***d**
- Sphere formula: ||**p**-**c**||=*r*
- Replace **p** by $\mathbf{r}(t)$: $||\mathbf{r}(t)-\mathbf{c}||=r$

$$(\mathbf{r}(t) - \mathbf{c}) \cdot (\mathbf{r}(t) - \mathbf{c}) - r^2 = 0$$

$$(\mathbf{o} + t\mathbf{d} - \mathbf{c}) \cdot (\mathbf{o} + t\mathbf{d} - \mathbf{c}) - r^2 = 0$$

$$(\mathbf{d} \cdot \mathbf{d})t^2 + 2((\mathbf{o} - \mathbf{c}) \cdot \mathbf{d})t + (\mathbf{o} - \mathbf{c}) \cdot (\mathbf{o} - \mathbf{c}) - r^2 = 0$$

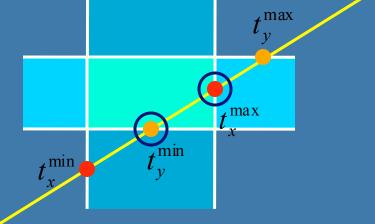
$$t^{2} + 2((\mathbf{o} - \mathbf{c}) \cdot \mathbf{d})t + (\mathbf{o} - \mathbf{c}) \cdot (\mathbf{o} - \mathbf{c}) - r^{2} = 0 \quad ||\mathbf{d}|| = 1$$

This is a standard quadratic equation. Solve for t.



Geometrical: Ray/Box Intersection (2)

 Intersect the 2 planes of each slab with the ray



Keep max of t^{min} and min of t^{max}
If t^{min} < t^{max} then we got an intersection
Special case when ray parallell to slab

Plane :
$$\pi : \mathbf{n} \cdot \mathbf{p} + d = 0$$

Point/Plane
• Insert a point x into plane equation:
 $f(\mathbf{x}) = \mathbf{n} \cdot \mathbf{x} + d = ?$
 $f(\mathbf{x}) = \mathbf{n} \cdot \mathbf{x} + d = 0$ for x's on the plane
 $f(\mathbf{x}) = \mathbf{n} \cdot \mathbf{x} + d < 0$ for x's on one side of the plane
 $f(\mathbf{x}) = \mathbf{n} \cdot \mathbf{x} + d < 0$ for x's on the other side

Negative
half spaceJPositive
half spaceJ

Sphere/Plane AABB/Plane

Plane: $\pi : \mathbf{n} \cdot \mathbf{p} + d = 0$ Sphere: $\mathbf{c} \quad r$ Box: $\mathbf{b}^{\min} \quad \mathbf{b}^{\max}$

Sphere: compute f(c) = n · c + d
f(c) is the signed distance (n normalized)
abs(f(c)) > r no collision
abs(f(c)) = r sphere touches the plane
abs(f(c)) < r sphere intersects plane

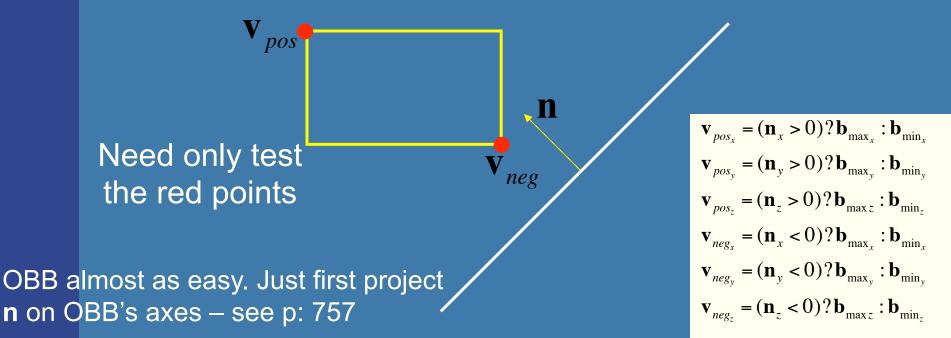
• Box: insert all 8 corners

 If all f's have the same sign, then all points are on the same side, and no collision

AABB/plane

Plane: $\pi : \mathbf{n} \cdot \mathbf{p} + d = 0$ Sphere: $\mathbf{c} \quad r$ Box: $\mathbf{b}^{\min} \quad \mathbf{b}^{\max}$

- The smart way (shown in 2D)
- Find the two vertices that have the most positive and most negative value when tested againt the plane

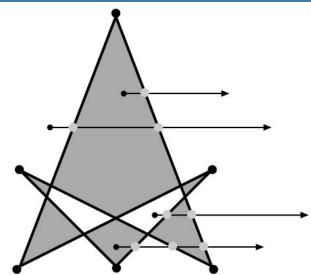


Another analytical example: Ray/ Triangle in detail

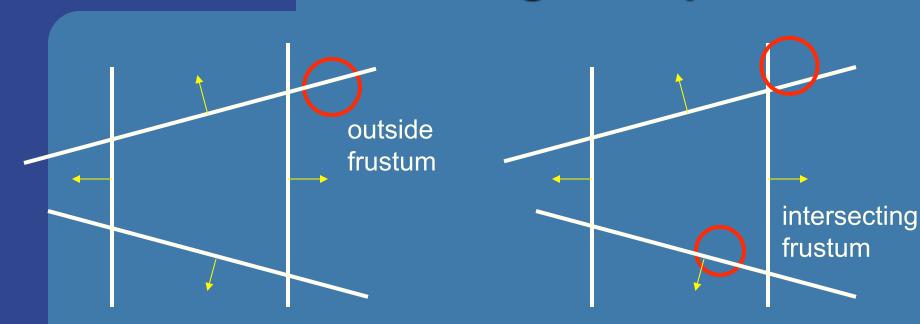
- Ray: $\mathbf{r}(t) = \mathbf{o} + t\mathbf{d}$
- Triangle vertices: \mathbf{v}_0 , \mathbf{v}_1 , \mathbf{v}_2
- A point in the triangle:
- $\mathbf{t}(u,v) = \mathbf{v}_0 + u(\mathbf{v}_1 \mathbf{v}_0) + v(\mathbf{v}_2 \mathbf{v}_0) = \mathbf{v}_0$ = $(1 - u - v)\mathbf{v}_0 + u\mathbf{v}_1 + v\mathbf{v}_2 \quad [u,v \ge 0, u + v \le 1]$
- Set t(u,v)=r(t), and solve!

$$\begin{pmatrix} | & | & | \\ -\mathbf{d} & \mathbf{v}_1 - \mathbf{v}_0 & \mathbf{v}_2 - \mathbf{v}_0 \\ | & | & | \end{pmatrix} \begin{pmatrix} t \\ u \\ v \end{pmatrix} = \begin{pmatrix} | \\ \mathbf{o} - \mathbf{v}_0 \\ | \end{pmatrix}$$

Ray/Polygon: very briefly Intersect ray with polygon plane Project from 3D to 2D How? • Find $\max(|n_x|, |n_v|, |n_z|)$ • Skip that coordinate! Then, count crossing in 2D



View frustum testing example

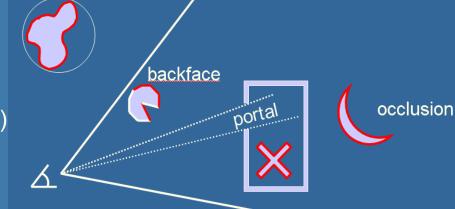


- Algorithm:
 - if sphere is outside any of the 6 frustum planes -> report "outside".
 - Else report intersect.
- Not exact test, but not incorrect, i.e.,
 - A sphere that is reported to be inside, can be outside
 - Not vice versa, so test is conservative

Lecture 7.1: Spatial Data Structures and Speed-Up Techniques

view frustum

- Speed-up techniques
 Culling
 - Backface
 - View frustum (hierarchical)
 - Portal
 - Occlusion Culling
 - Detail
 - Levels-of-detail:

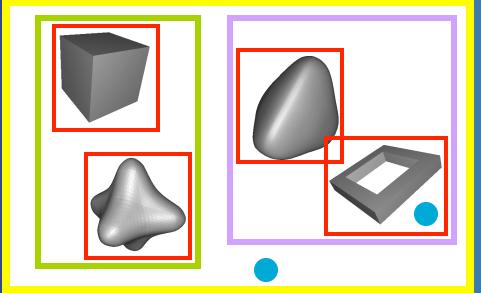


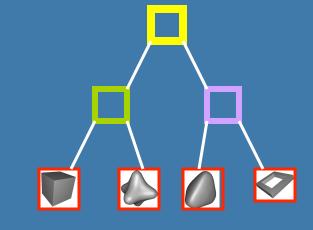
detail

 How to construct and use the spatial data structures

• BVH, BSP-trees (polygon aligned + axis aligned)

Axis Aligned Bounding Box Hierarchy - an example
Assume we click on screen, and want to find which object we clicked on





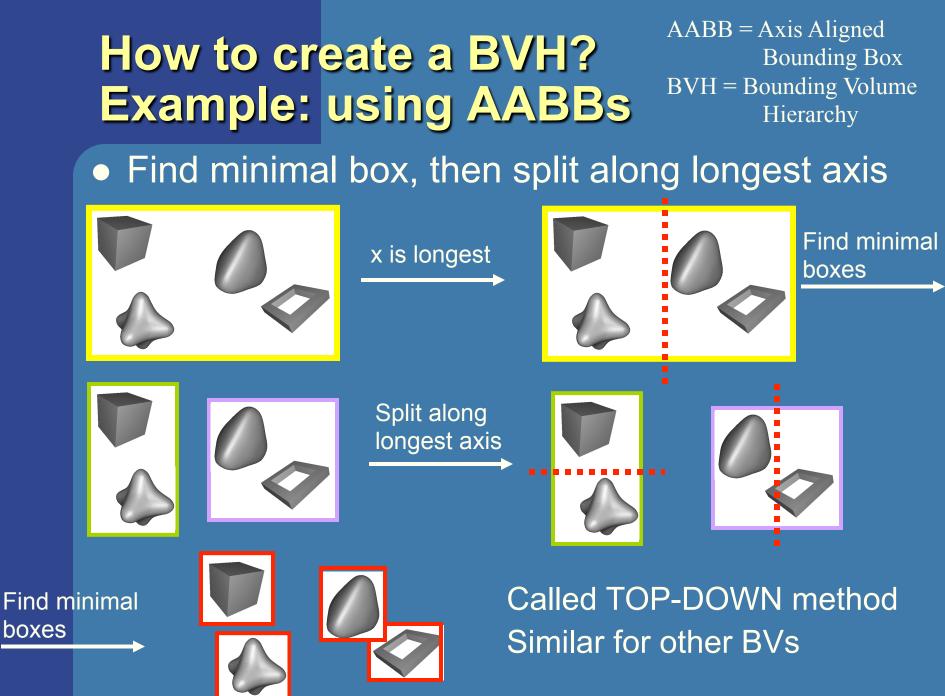
click!

1) Test the root first

2) Descend recursively as needed

3) Terminate traversal when possible

In general: get O(log n) instead of O(n)



Tomas Akenine-Mőller © 2002

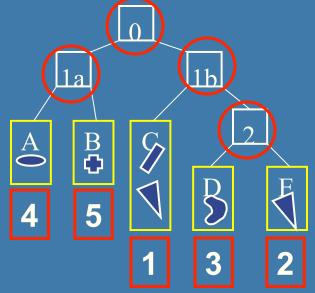
Axis-aligned BSP tree Rough sorting

- Test the planes, recursively from root, against the point of view. For each traversed node:
 - If node is leaf, draw the node's geometry
 - else

1a

- Continue traversal on the "hither" side with respect to the eye to sort front to back
- Then, continue on the farther side.





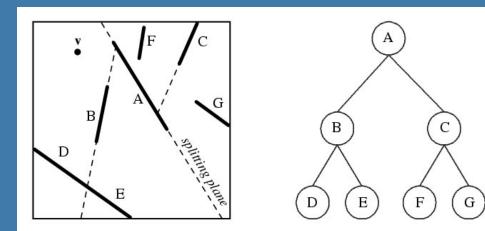
 Works in the same way for polygonaligned BSP trees --- but that gives exact sorting

Polygon-aligned BSP tree

Allows exact sorting

- Very similar to axis-aligned BSP tree
 - But the splitting plane are now located in the planes of the triangles

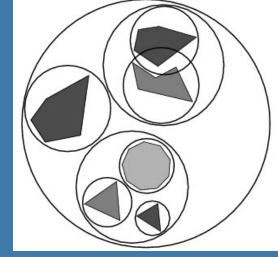
Drawing Back-to-Front { recurse on farther side of P; Draw P; Recurse on hither side of P; }// farther/hither is with respect to eye pos.

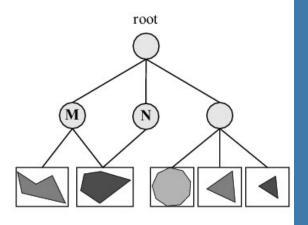


Know how to build it and how to traverse back-to-front or front-to-back with respect to the eye position (here: **v**) A Scene Graph is a hierarchical scene description – more typically a logical hierarchy (than e.g. spatial) Scene graphs

• BVH is the data structure that is used most often

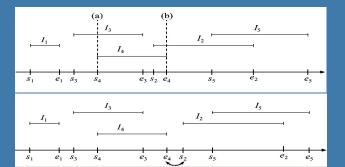
- Simple to understand
- Simple code
- However, BVH stores just geometry
 - Rendering is more than geometry
- The scene graph is an extended BVH with:
 - Lights
 - Materials
 - Transforms
 - several connections to a node
 And more





Lecture 7.2: Collision Detection

- 3 types of algorithms:
 - With rays
 - Fast but not exact
 - With BVH
 - Slower but exact
 - You should be able to write pseudo code for BVH/BVH test for coll det between two objects.
 - For many many objects.
 - why? Course pruning of "obviously" non-colliding objects
 - Sweep-and-prune





Lecture 8: Ray tracing

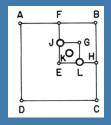
- Adaptive Super Sampling
- Jittering
- How to stop ray tracing recursion?

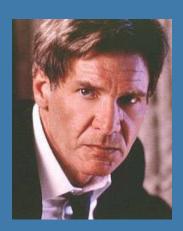


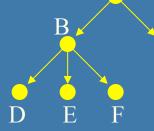
- Spatial data structures
 - Optimizations for BVHs: skippointer tree
 - Ray BVH-traversal
 - (You do not need to learn the ray traversal algorithms for Grids nor AA-BSP trees)
- Shadow cache

• Material (Fresnel: metall, dielectrics)

• Constructive Solid Geometry – how to implement







Adaptive Supersampling

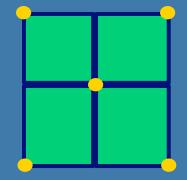
Pseudo code:

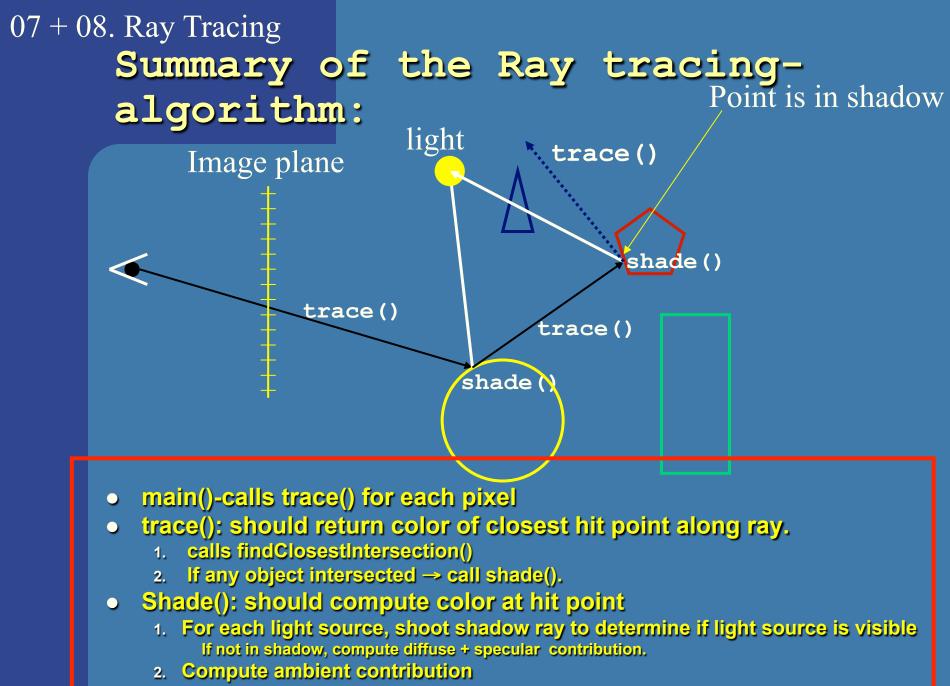
Color AdaptiveSuperSampling() {

- Make sure all 5 samples exist
 - (Shoot new rays along diagonal if necessary)
- Color col = black;
- For each quad i
 - If the colors of the 2 samples are fairly similar
 - col += $(1/4)^*$ (average of the two colors)

• Else

- col +=(1/4)* adaptiveSuperSampling(quad[i])
- return col;



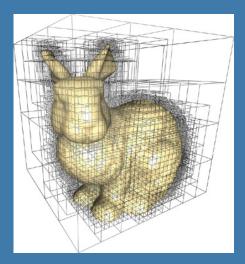


3. Call trace() recursively for the reflection- and refraction ray.

Data structures

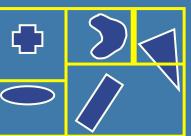
Octree



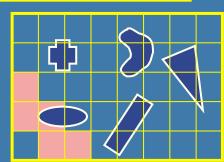


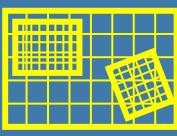
• Kd tree

• Grids Including mail boxing



Kd-tree = Axis-Aligned BSP tree with fixed recursive split plane order (e.g. x,y,z,x,y,z...)

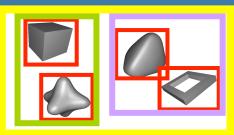




Hierarchical grid

Recursive grid

Bounding box hierarchies



2002

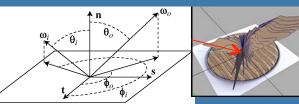
Lecture 10 – Global Illumination

• Global illumination:

$$L_o = L_e + \int_{\Omega} f_r(\mathbf{x}, \boldsymbol{\omega}, \boldsymbol{\omega}') L_i(\mathbf{x}, \boldsymbol{\omega}')(\boldsymbol{\omega}' \cdot \mathbf{n}) d\boldsymbol{\omega}'$$

- Why is not standard ray tracing enough?
- rendering eq., BRDFs
- Monte Carlo Ray Tracing
- Path tracing
- Photon mapping







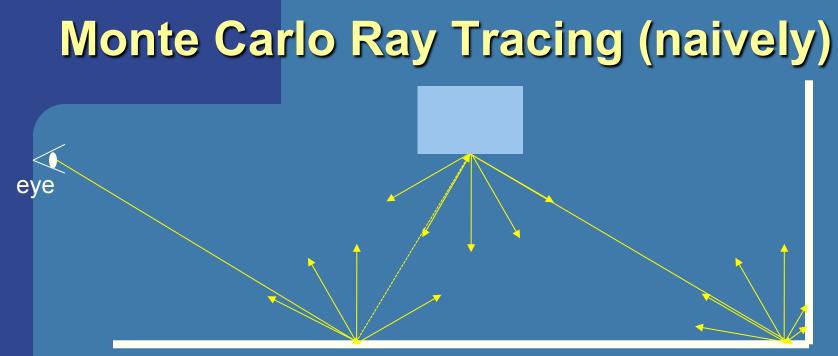


Lecture 10: What you need to know

- The rendering equation
 - Be able to explain all its components
- Path tracing
 - Why it is good, compared to naive monte-carlo sampling
 - The overall algorithm (on a high level as in these slides).
- Photon Mapping
 - The overall algorithm. See the summary slide on:
 - Creating Photon Maps...
 - Ray trace from eye...
 - Growing spheres...

- Final Gather

- Why it is good. How it works:
 - At the first diffuse hit, instead of using global map directly, sample indirect slow varying light around p by sampling the hemisphere with ~1000 rays and use the two photon maps where those rays hit a diffuse surface.
- Bidirectional Path Tracing, Metropolis Light Transport
 - Just their names. Don't need to know the algorithms.



diffuse floor and wall

 Sample <u>indirect</u> illumination by shooting sample rays over the hemisphere, at each hit.

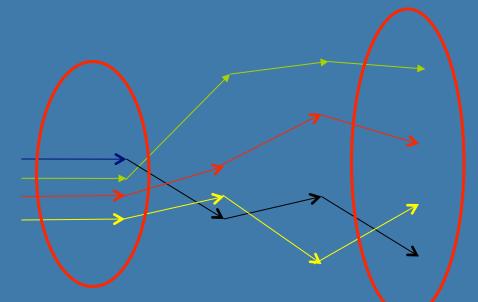
 At some recursion depth, stop and compute standard local lighting (i.e., without indirect illumination)

Monte Carlo Ray Tracing (naively)

 This gives a ray tree with most rays at the bottom level. This is bad since these rays have the lowest influence on the pixel color.

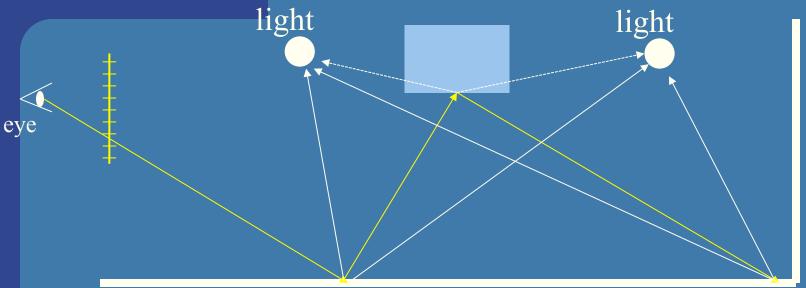
PathTracing <u>– a smarter Monte-Carlo ray-tracing method</u>

• Path Tracing instead only traces one of the possible ray paths at a time. This is done by randomly selecting only one sample direction at a bounce. Hundreds of paths per pixel are traced.



Equally number of rays are traced at each level

Path Tracing – indirect + direct illumination



diffuse floor and wall

- Shoot many paths per pixel (the image just shows one light path).
 - At each intersection,
 - Shoot one shadow ray per light source
 - at random position on light, for area/volumetric light sources
 - and randomly select one new ray direction.



Photon Mapping

• Creating Photon Maps:

 Trace photons (~100K-1M) from light source. Store them in kd-tree when they hit diffuse surface. Then, use russian roulette to decide if the photon should be absorbed or specularly or diffusively reflected. Create both global map and caustics map. For the Caustics map, we send more of the photons towards reflective/refractive objects.

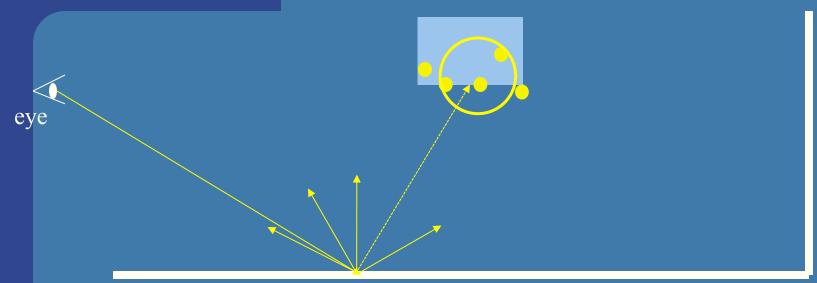
• Ray trace from eye:

- As usual: I.e., shooting primary rays and recursively shooting reflection/refraction rays, and at each intersection point p, compute direct illumination (shadow rays + shading).
- Also grow sphere around each p in caustics map to get caustics contribution and in global map to get slow-varying indirect illumination.
- If final gather is used: At the first diffuse hit, instead of using global map directly, sample indirect slow varying light around **p** by sampling the hemisphere with ~100 1000 rays and use the two photon maps where those rays hit a surface.

• Growing sphere:

Uses the kd-tree to expand a sphere around **p** until a fixed amount (e.g. 50) photons are inside the sphere. The radius is a measure of the intensity of indirect light at **p**. The BRDF at **p** could also be used to get a more accurate color and intensity value.

A modification for indirect Illumination – <u>Final Gather</u>



diffuse floor and wall

- Too noicy to use the <u>global</u> map for direct visualization
- Remember: eye rays are recursively traced (via reflections/ refractions) until a diffuse hit, p. There, we want to estimate slowvarying indirect illumination.
 - Instead of growing sphere in global map at p, Final Gather shoots 100-1000 indirect rays from p and grows sphere in the global map and also caustics map, where each of those rays end at a diffuse surface.

Lecture 11: Shadows + Reflection

- Point light / Area light
- Three ways of thinking about shadows
 - The basis for different algorithms.
- Shadow mapping
 - Be able to describe the algorithm
- Shadow volumes
 - Be able to describe the algorithm
 - Stencil buffer, 3-pass algorithm, Z-pass, Z-fail,
 - Creating quads from the silhouette edges as seen from the light source, etc
- Pros and cons of shadow volumes vs shadow maps

 Planar reflections – how to do. Why not using environment mapping?

Ways of thinking about shadows

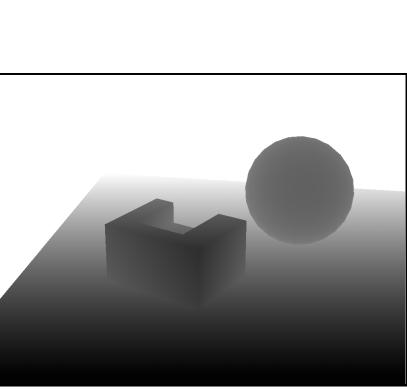
- As separate objects (like Peter Pan's shadow) This corresponds to planar shadows
- As volumes of space that are dark
 This corresponds to shadow volumes
- As places not seen from a light source looking at the scene. This corresponds to shadow maps
- Note that we already "have shadows" for objects facing away from light

Shadow Maps - Summary

Shadow Map Algorithm:

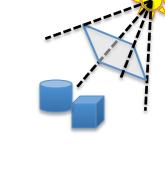
- Render a z-buffer from the light source
 - Represents geometry in light
- Render from camera
 - For every fragment:
 - Transform(warp) its 3D-pos (x,y,z) into shadow map (i.e. light space) and compare depth with the stored depth value in the shadow map
 - If depth greater-> point in shadow
 - Else -> point in light
 - Use a bias at the comparison

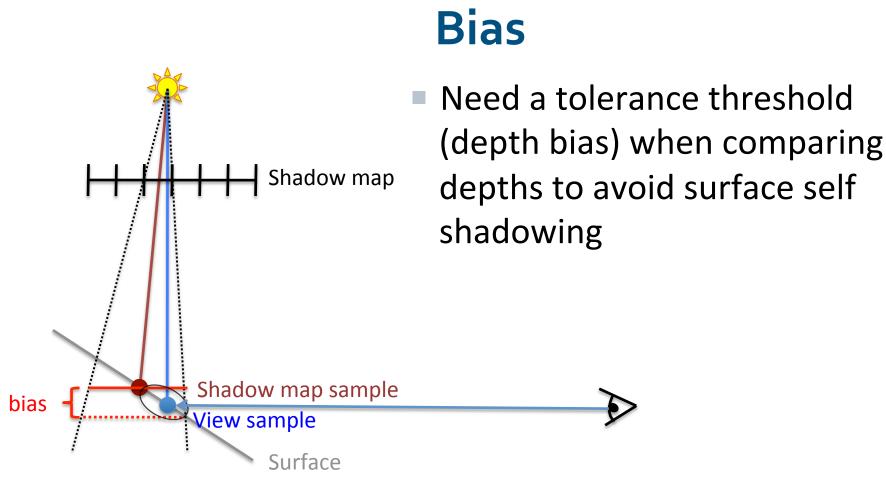
Understand z-fighting and light leaks



Shadow Map (=depth buffer)

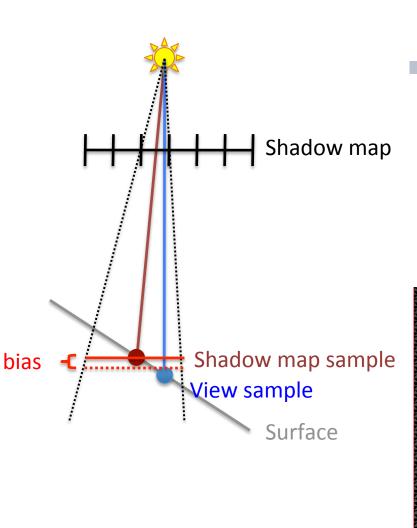
eurographics 2010





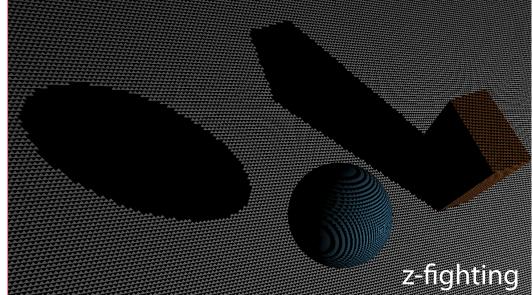


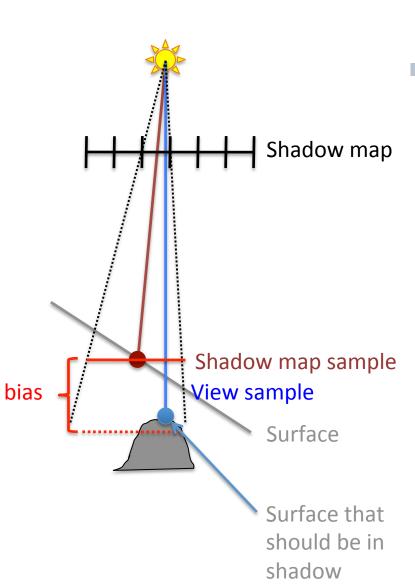
Tutorial Shadow Algorithms for Real-time Rendering



Bias

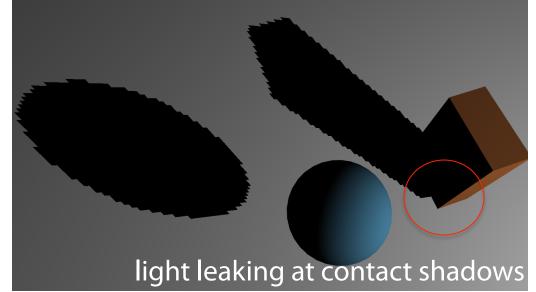
 Need a tolerance threshold (depth bias) when comparing depths to avoid surface self shadowing







 Need a tolerance threshold (depth bias) when comparing depths to avoid surface self shadowing



euro<mark>graphics 2010</mark>



Shadow volumes

Create shadow quads for all silhouette edges (as seen from the light source). (The normals are pointing outwards from the shadow volume.)

Edges between one triangle front facing the light source and one triangle back facing the light source are considered silhouette edges.



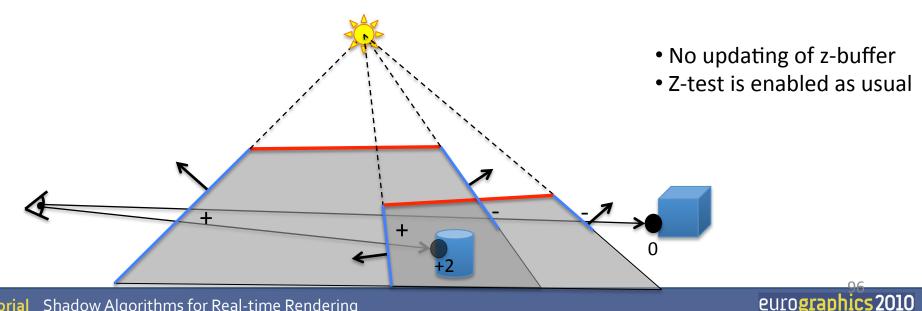


Tomas Akenine-Mőller © 2002

Shadow Volumes - concept

Perform counting with the stencil buffer

- Render front facing shadow quads to the stencil buffer
 - Inc stencil value, since those represents entering shadow volume
- Render back facing shadow quads to the stencil buffer
 - Dec stencil value, since those represents exiting shadow volume



Shadow Volumes with the Stencil Buffer

A three pass process:

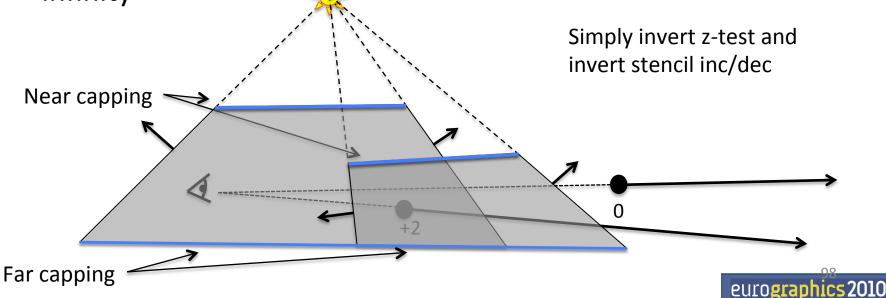
- 1st pass: Render ambient lighting
- 2nd pass:
 - Draw to stencil buffer only
 - Turn off updating of z-buffer and writing to color buffer but still use standard depth test
 - Set stencil operation to
 - » *incrementing* stencil buffer count for *frontfacing* shadow volume quads, and
 - » decrementing stencil buffer count for backfacing shadow volume quads

• **3rd pass:** Render *diffuse and specular* where stencil buffer is 0.

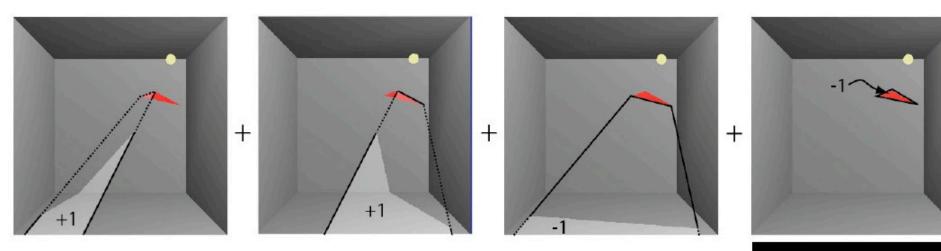


The Z-fail Algorithm

- Z-pass must offset the stencil buffer with the number of shadow volumes that the eye is inside. Problematic.
- Count to infinity instead of to the eye
 - We can choose any reference location for the counting
 - A point in light avoids any offset
 - Infinity is always in light if we cap the shadow volumes at infinity



Z-fail by example

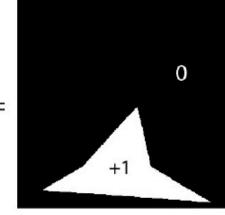


Compared to Z-pass:

Invert z-test

Invert stencil inc/dec

I.e., count to infinity instead of from eye.



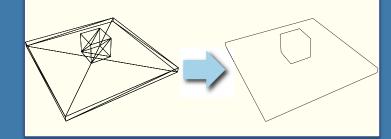
Merging Volumes

• Edge shared by two polygons facing the light creates front and backfacing quad.

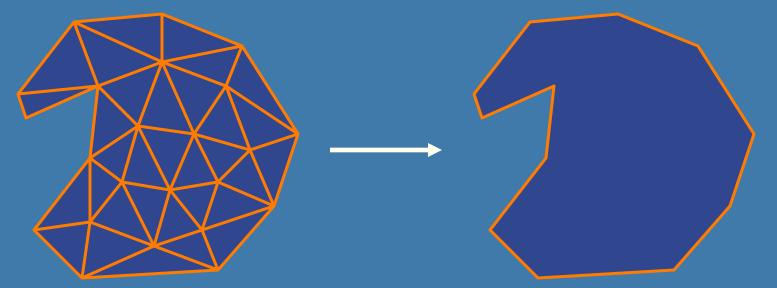
This interior edge makes two quads, which cancel out

Tomas Akenine-Mőller © 2002

Silhouette Edges



From the light's view, caster interior edges do not contribute to the shadow volume.



Finding the silhouette edge gets rid of many useless shadow volume polygons.

Tomas Akenine-Mőller © 2002

Shadow Maps vs Shadow Volumes



Shadow Maps

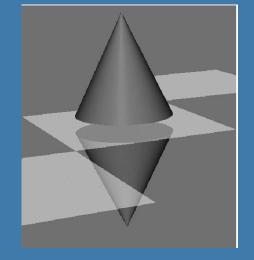
- *Good*: Handles any rasterizable geometry, **constant cost** regardless of complexity, map can sometimes be reused. **Very fast**.
- Bad: Frustum limited. Jagged shadows if res too low, biasing headaches.
 - Solution:
 - 6 SM (cube map), high res., use filtering (huge topic)

Shadow Volumes

- Good: shadows are sharp. Handles omnidirectional lights.
- Bad: 3 passes, shadow polygons must be generated and rendered → lots of polygons & fill
 - Solution: culling & clamping

Planar reflections

Two methods:



- 1. Reflecting the object:
 - If reflection plane is z=0 (else somewhat more complicated – see page 387)
 - Apply glScalef(1,1,-1);
 - Backfacing becomes front facing!
 - i.e., use frontface culling instead of backface culling
 - Lights should be reflected as well

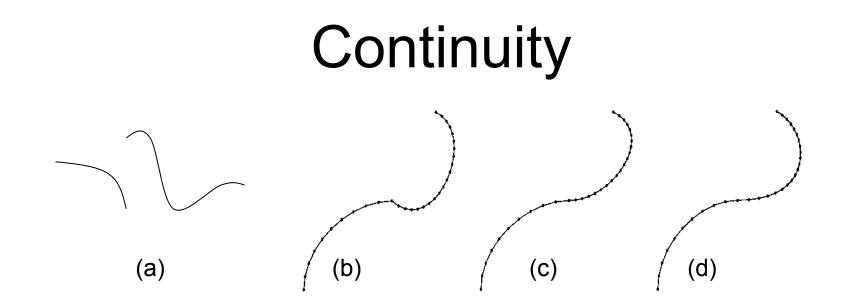
2. Reflecting the camera in the reflection plane

Planar reflections Assume plane is z=0 Then apply glScalef(1,1,-1); • Effect: Ζ

Tomas Akenine-Mőller © 2002

Planar reflections

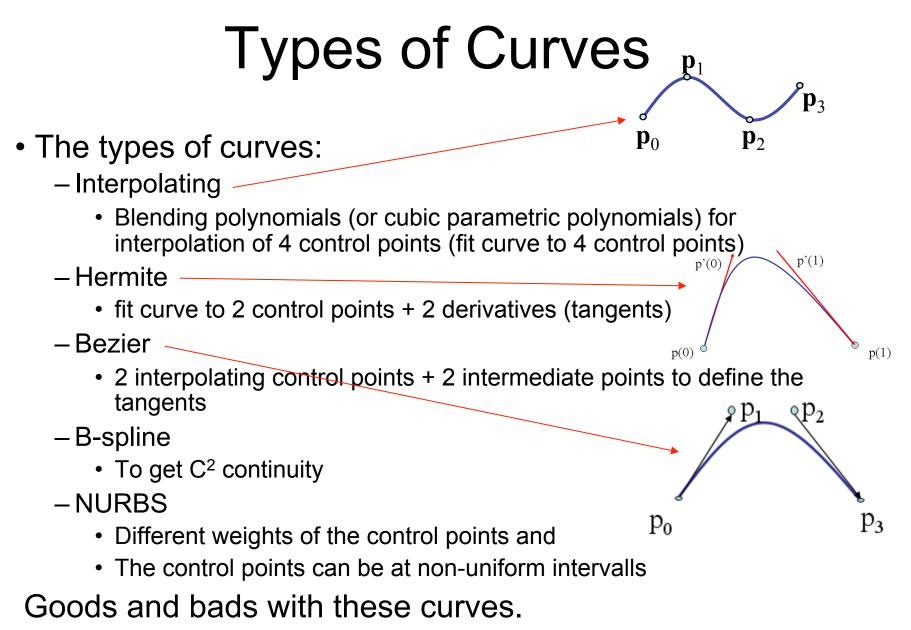
- How should you render?
- 1) the reflective ground plane polygons into the stencil buffer
- 2) the scaled (1,1,-1) model, but mask with stencil buffer
 - Reflect light pos as well
 - Use front face culling
- 3) the ground plane (semi-transparent)
 4) the unscaled model



- A) Non-continuous
- B) C⁰-continuous
- C) G¹-continuous
- D) C¹-continuous
- (C²-continuous)

See page 585-587 in Real-time Rendering, 3rd ed.

12. Curves and Surfaces:



12. Curves and Surfaces:

Splines and Basis

- If we examine the cubic B-spline from the perspective of each control (data) point, each interior point contributes (through the blending functions) to four segments
- •We can rewrite p(u) in terms of the data points as

$$p(u) = \sum B_i(u) p_i$$

defining the basis functions {B_i(u)}

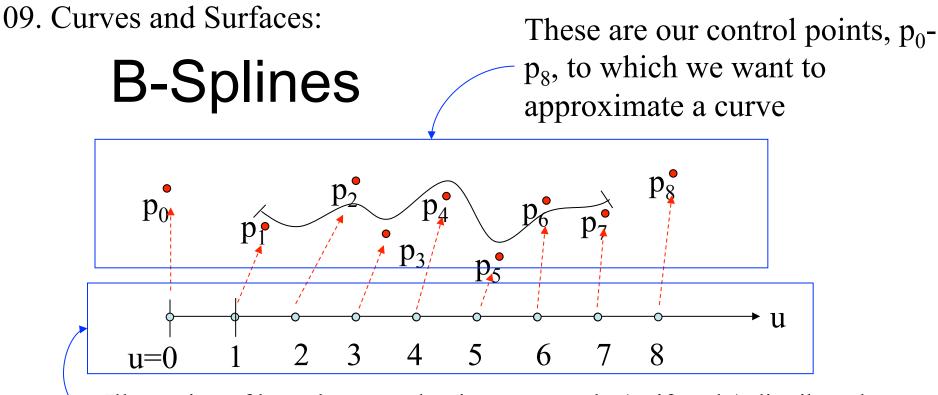


Illustration of how the control points are evenly (uniformly) distributed along the parameterisation u of the curve p(u).

In each point p(u) of the curve, for a given u, the point is defined as a weighted sum of the closest 4 surrounding points. Below are shown the weights for each point along $u=0\rightarrow 1$

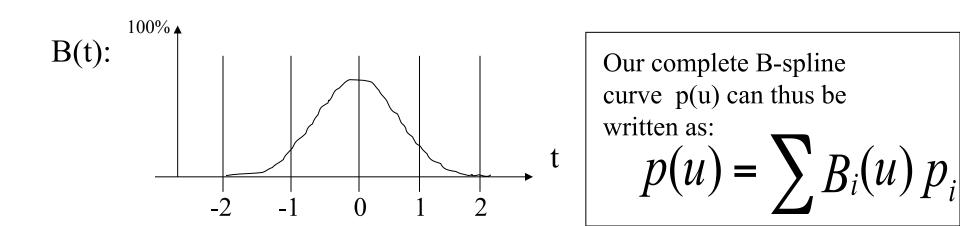
u

100%

SUMMARY

B-Splines

written as a translation of a basis function B(t). $B_{pi}(u) = B(u-i)$



12. Curves and Surfaces:

NURBS

NURBS is similar to B-Splines except that:

- The control points can have different weights, w_i, (heigher weight makes the curve go closer to that control point)
- 2. The control points do not have to be at uniform distances (u=0,1,2,3...) along the parameterisation u. E.g.: u=0, 0.5, 0.9, 4, 14,...

NURBS = Non-Uniform Rational B-Splines

The NURBS-curve is thus defined as:

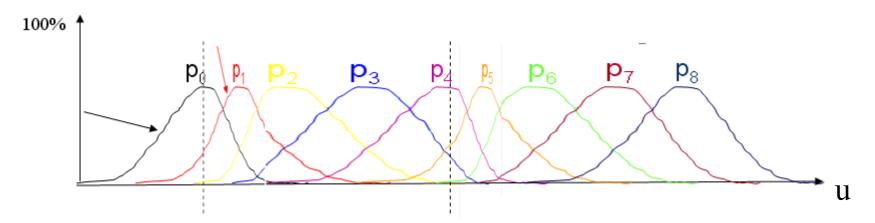
 $\mathbf{p}(u) = -$

Division with the sum of the weights, to make the combined weights sum up to 1, at each position along the curve. Otherwise, a translation of the curve is introduced (which is not desirable) 12. Curves and Surfaces:

NURBS

 Allowing control points at non-uniform distances means that the basis functions B_{pi}() are being streched and non-uniformly located.

• E.g.:



Each curve $B_{pi}()$ should of course look smooth and C^2 –continuous. But it is not so easy to draw smoothly by hand...(The sum of the weights are still =1 due to the division in previous slide)

Lecture 13:

Perspective correct interpolation (e.g. for textures)

Taxonomy:

- Sort first
- sort middle
- sort last fragment
- sort last image
- Bandwidth
 - Why it is a problem
 - How to "solve" it

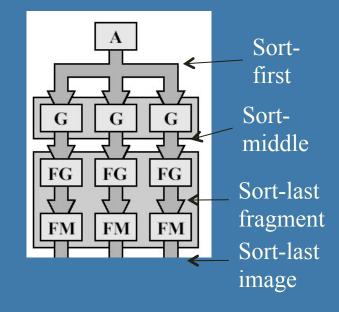
• Be able to sketch the architecture of a moder graphics card

Linearly interpolate $(u_i/w_i, v_i/w_i, 1/w_i)$ in screenspace from each triangle vertex i. Then at each pixel:

$$u_{ip} = (u/w)_{ip} / (1/w)_{ip}$$

$$v_{ip} = (v/w)_{ip} / (1/w)_{ip}$$

where ip = screen-space interpolated value between the triangle vertices.



CHALMERS

Department of Computer Engineering

