Finite Automata Theory and Formal Languages TMV027/DIT321- LP4 2015

Lecture 1 Ana Bove

March 23th 2015

Overview of today's lecture:

- Course organisation;
- Overview of the course.

People and Information

Course Responsible:

Ana Bove, bove@chalmers.se

Assistants:

Pablo Buiras, buiras@chalmers.se Simon Huber, simonhu@chalmers.se Daniel Schoepe, schoepe@chalmers.se Andrea Vezzosi, vezzosi@chalmers.se

Web Page: http://www.cse.chalmers.se/edu/course/TMV027 Accessible from CTH "studieportalen" and GU "GUL". Check it regularly for news!

Course Mailing List: fafl@lists.chalmers.se You will get registered to it next week with your CTH/GU mail address. The list is moderated.

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Course Level, Load and Examination

Level: This course is a *bachelor* course in year 1–2.

Load: 7.5 pts means ca. 20–25 hours per week!!

Note: It is important to follow the course's pace in order to pass it!

Examination:

From VT2013 the course has 2 *obligatory* parts:

- Individual weekly assignments: 1.5pts.
- Individual written exam: 6pts, no book or help allowed.
 Dates for 2015: June 3rd and August 19th.

From VT2015 the final grade is based on the performance on both parts!

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More on Assignments

- To pass the assignment part you need to get at least 50% of the sum of the points of all the weekly assignments together.
- They must be done *completely* on your own!

Note: Be aware that assignments are part of the examination of the course and they **should** be done *individually*!
Standard procedure will be followed if copied solutions are detected.

- How to submit? Via the Fire system, check course web page. https://xdat09.ce.chalmers.se/2015_faf1/login.
- Who shall submit? Students who registered VT13 or later and who have NOT passed them yet!

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Final Grade

- Students registered before VT2015: final grade is the same as the grade in the exam.
 - See course web page for information that might apply in your case.
- Students registered in VT2015:

Max. points in exam: 60, min 27 pts to pass it.

Max. points in assignments: 64, min 32 pts to pass them.

Final points (max. 76) = nr of points got in the exam + 25% of the points gathered in the assignment

Chalmers:	Final Grade	Final Pts
	3	35
	4	46
	5	57

Note: You need to pass both parts in order to pass the course!

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Lectures and Consultation Time (Check TimeEdit!)

Lectures: Ana Bove

Mondays 13:15–15:00: in HB3 (weeks 1 & 2), HC3 (week 4) and HC2 (weeks 3 and 5–8)

Tuesday 24/3 9:00-11:45: in HB3 ONLY in week 1

Thursdays 13:15-15:00: in HB3 (weeks 1-3 & 5) and HC2 (weeks 7 & 8)

Thursday 10:00-11:45: in HC2 ONLY in week 4

Note: You *MUST prepare* before each lecture in order to follow the course pace!

Consultation Time: Ana Bove

Wednesdays 15:15–17:00: in EL41 (week2) and ES53 (weeks 3–6 & 8)

Thursday 10:00–11:45: in EE (week 7)

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Exercises (Check TimeEdit!)

Exercise Sessions: VERY important!!

Come and ask questions!!!

Run by the assistants.

Thursday 26/3 10:00–11:45: for ALL students who need to recap on discrete math concepts, in HC3 (week 1).

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Mondays 15:15–17:00: in EE (weeks 2–5 & 8). 
Tuesday 15:15–17:00: in EF (week 6). 
Monday 10:00–11:45: in EE (week7).
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Tuesday 10:00–11:45: in EF (weeks 2–3, 5–8). Tuesday 15:15–17:00: in EF (week 4).

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Solutions to the Exercises

Note: There are NO solutions to exercises!!!

(This is usually the main complain in this course.)

Why?

- Expensive to create good solutions;
- Some problems have many possible solutions;
- Pedagogically not always good: you learn mostly by doing;
- Asking the teachers in case of doubt is a better way to learn;
- You need to learn how to solve problems without a solution....
 Who will pay you to solve something one already has the solution to?

If you *really* need solutions to exercises, google and you will find plenty!

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Literature and Other Material

Book: Introduction to Automata Theory, Languages, and Computation, by Hopcroft, Motwani and Ullman. Addison-Wesley. We will cover chapters 1 to 5, 7 and a bit of chapter 8.

Note: Notation in the book is sometimes different to that used in class.

Wikipedia: http://en.wikipedia.org/wiki

Youtube: http://www.youtube.com

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Comments from Course Evaluation

Preserve: The weekly assignments! But make them mandatory for each week! They were a great way to keep up with the course and to continuously refresh knowledge and get feedback.

Preserve: The consultation time, keep it as it is, it's perfect and was a very important part of the course for me.

Preserve: I also liked that there weren't any answers to the exercises; though scary at the beginning, it gave a deeper understanding of the subject of the exercise when one had to think twice and trust one's own solution. It was also a great practice for the exam and future employment.

Change: If I would redo the course, I would tried to have done the excercises before the lecture = trying to be one week ahead of the lectures. I figured it out in the end, that I was doing the excercises after the lectures = sometimes it was hard to follow the advanced parts of each topics.

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Programming Bits in the Course

The course doesn't require much programming tasks.

Still

- I will present some Haskell programs simulating certain automaton or implementing an algorithm.
 - (Some of you know Haskell, if you do not I really recommend you learn it: it is very elegant, nice and of increasing importance in industry!);
- You should implement the algorithm to improve your knowledge and understanding!

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Chinese Proverb

I hear and I forget.

I see and I remember.

I do and I understand.

Confucius

Chinese philosopher and reformer (551 BC - 479 BC)

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Automata

Dictionary definition:

Main Entry: au·tom·a·ton

Function: noun

Inflected Form(s): plural au·tom·atons or au·tom·a·ta Etymology: Latin, from Greek, neuter of automatos

Date: 1645

1 : a mechanism that is relatively self-operating;
 especially : robot

2 : a machine or control mechanism designed to follow automatically a predetermined sequence of operations or respond to encoded instructions

3 : an individual who acts in a mechanical fashion

Automata: Applications

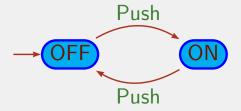
Models for ...

- Lexical analyser in a compiler;
- Software for designing circuits;
- Software for finding patterns in large bodies of text such as collection of web pages;
- Software for verifying systems with a finite number of different states such as protocols;
- Real machines like vending machines, telephones, street lights, ...;
- Application in linguistic, building of large dictionary, spell programs, search;
- Application in genetics, regular pattern in the language of protein.

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Example: on/off-switch

A very simple finite automaton:



States represented by "circles".

One state is the *starting* state, indicated with an arrow into it.

Arcs between states are labelled by observable events.

Often we need one or more *final* states, indicated with a double circle.



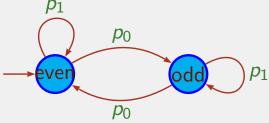
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Example: Parity Counter

The states of an automaton can be thought of as the *memory* of the machine.



Two events: p_0 and p_1 .

The machine does nothing on the event p_1 .

The machine counts the parity of the number of p_0 's.

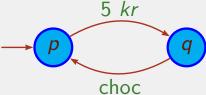
A finite-state automaton has *finite memory*!

We now would like to prove that the automata is on state even iff an even number of p_0 were pressed.

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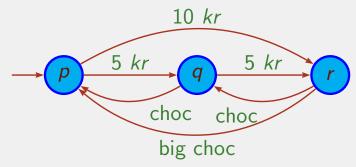
Example: Vending Machines

A simple vending machine:



What does it happen if we ask for a chocolate on p?

A more complex vending machine:



State q remembers it has already got 5 kr.

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Problem: The Man, the Wolf, the Goat and the Cabbage

A man with a wolf, a goat and a cabbage is on the left bank of a river.

There is a boat large enough to carry the man and only one of the other three things. The man wish to cross everything to the right bank.

However if the man leaves the wolf and the goat unattended on either shore, the wolf surely will eat the goat.

Similarly, if the goat and the cabbage are left unattended, the goat will eat the cabbage.

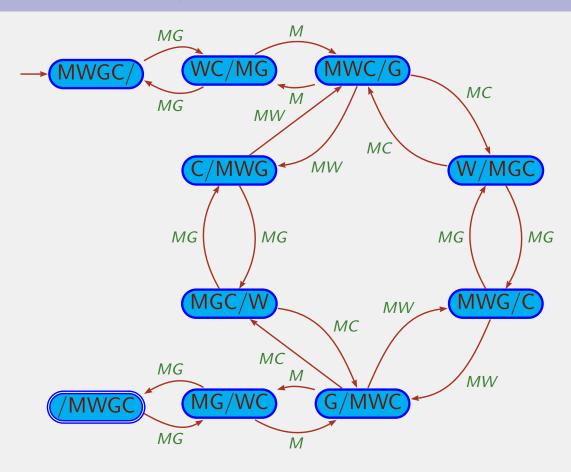
Puzzle: Is it possible to cross the river without the goat or cabbage being eaten?

How many possible solutions the problem has?

Solution: We design an automaton that models the problem with all its possible transitions, and look for paths between the initial and final state.

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Solution: The Man, the Wolf, the Goat and the Cabbage



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Formal Languages

From Wikipedia:

In mathematics, computer science, and linguistics, a formal language is a set of strings of symbols that may be constrained by rules that are specific to it.

The alphabet of a formal language is the set of symbols, letters, or tokens from which the strings of the language may be formed; frequently it is required to be finite.

The strings formed from this alphabet are called words, and the words that belong to a particular formal language are sometimes called well-formed words or well-formed formulas.

A formal language is often defined by means of a formal grammar such as a regular grammar or context-free grammar, also called its formation rule.

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Example: Formal Representation of Numbers and Identifiers in a Programming Language

A regular grammar for numbers and identifiers

A regular expression for numbers:

$$(0+1+2+3+4+5+6+7+8+9)^+$$

A regular expression for identifiers:

$$(A + ... + Z + a + ... + z)(A + ... + Z + a + ... + z + 0 + ... + 9)^*$$

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Example: Very Simple Expressions

A context-free grammar for simple expression:

$$E \rightarrow E+E \mid E-E \mid E*E \mid E/E \mid (E) \mid Nr \mid Id$$
 $Nr \rightarrow \cdots$
 $Id \rightarrow \cdots$

We might now want to prove that

- Any expression has as many "(" as ")";
- Any expression has 1 more "term" than the number of "operations".

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More Complex Examples

A better context-free grammar for simple expression:

$$E \rightarrow E+T \mid E-T \mid T$$

$$T \rightarrow T*F \mid T/F \mid F$$

$$F \rightarrow (E) \mid Nr \mid Id$$

A context-free grammar for C++ compound statements:

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\begin{array}{lll} S & \rightarrow & \{LC\} \\ LC & \rightarrow & \epsilon \mid C \; LC \\ C & \rightarrow & S \mid \text{if } (E) \; C \mid \text{if } (E) \; C \; \text{else } C \mid \\ & & \text{while } (E) \; C \mid \text{do } C \; \text{while } (E) \mid \text{for } (C \; E; E) \; C \mid \\ & & \text{case } E : C \mid \text{switch } (E) \; C \mid \text{return } E; \mid \text{goto } Id; \\ & & \text{break; } \mid \text{continue;} \\ & \vdots \end{array}
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Overview of the Course

- Formal proofs;
- Regular languages;
- Context-free languages;
- Turing machines (as much as time allows).

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Formal Proofs

Many times you will need to prove that your program/model/grammar/... is "correct" (satisfies a certain specification/property).

In particular, you won't get a complex program/model/grammar/... right if you don't understand what is going on.

Different kind of formal proofs:

- Deductive proofs;
- Proofs by contradiction;
- Proofs by counterexamples;
- Proofs by (structural) induction.

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Regular Languages

Finite automata were originally proposed in the 1940's as models of neural networks.

Turned out to have many other applications!

In the 1950s, the mathematician Stephen Kleene described these models using mathematical notation (*regular expressions*, 1956).

Ken Thompson used the notion of regular expressions introduced by Kleene in the UNIX system.

(Observe that Kleene's regular expressions are not really the same as UNIX's regular expressions.)

Both formalisms define the *regular languages*.

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Context-Free Languages

We can give a bit more power to finite automata by adding a stack that contains data.

In this way we extend finite automata into a *push down automata*.

In the mid-1950s Noam Chomsky developed the context-free grammars.

Context-free grammars play a central role in the description and design of programming languages and compilers.

Both formalisms define the *context-free languages*.

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Church-Turing Thesis

In the 1930's there has been quite a lot of work about the nature of effectively computable (calculable) functions:

- Recursive functions by Stephen Kleene;
- λ -calculus by Alonzo Church;
- Turing machines by Alan Turing.

The three *models of computation* were shown to be equivalent by Church, Kleene & (John Barkley) Rosser (1934–6) and Turing (1936-7).

The *Church-Turing thesis* states that if an algorithm (a procedure that terminates) exists then, there is an equivalent Turing machine, a recursively-definable function, or a definable λ -function for that algorithm.

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Turing Machine (ca 1936–7)

Simple theoretical device that manipulates symbols contained on a strip of tape.

It is as "powerful" as the computers we know today (in term of what they can compute).

It allows the study of *decidability*: what can or cannot be done by a computer (*halting* problem).

Computability vs complexity theory: we should distinguish between what can or cannot be done by a computer, and the inherent difficulty of the problem (tractable (polynomial)/intractable (NP-hard) problems).

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Learning Outcome of the Course

After completion of this course, the student should be able to:

- Explain and manipulate the different concepts in automata theory and formal languages;
- Have a clear understanding about the equivalence between (non-)deterministic finite automata and regular expressions;
- Acquire a good understanding of the power and the limitations of regular languages and context-free languages;
- Prove properties of languages, grammars and automata with rigorously formal mathematical methods;
- Design automata, regular expressions and context-free grammars accepting or generating a certain language;
- Describe the language accepted by an automata or generated by a regular expression or a context-free grammar;
- Simplify automata and context-free grammars;
- Determine if a certain word belongs to a language;
- Define Turing machines performing simple tasks;
- Differentiate and manipulate formal descriptions of languages, automata and grammars.

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Overview of Next Lecture

Section 1.5 in the book and more:

- Recap on logic;
- Recap on sets, relations and functions;
- Central concepts of automata theory.

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