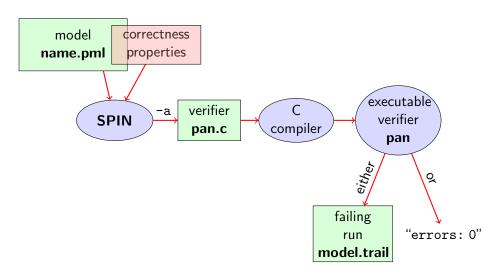
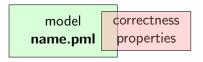
Software Engineering using Formal Methods Model Checking with Temporal Logic

Wolfgang Ahrendt

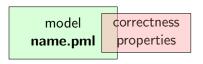
22nd September 2015

Model Checking with Spin





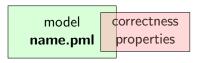
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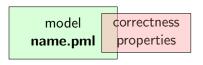
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stating properties within model using

- assertion statements
- meta labels
 - end labels
 - accept labels
 - progress labels



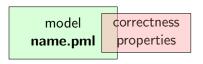
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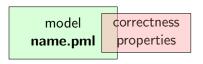
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stating properties within model using

- assertion statements
- meta labels
 - ▶ end labels
 - accept labels (briefly)
 - progress labels

stating properties outside model using

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- temporal logic formulas (today's main topic)

Preliminaries

- 1. Accept labels in Prometa \leftrightarrow Büchi automata
- 2. Fairness

Preliminaries 1: Acceptance Cycles

Definition (Accept Location)

A location marked with an accept label of the form "acceptxxx:" is called an accept location.

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Definition (Accept Location)

A location marked with an accept label of the form "acceptxxx:" is called an accept location.

Accept locations can be used to specify cyclic behavior

Definition (Acceptance Cycle)

A run which infinitely often passes through an accept location is called an acceptance cycle.

Acceptance cycles are mainly used in never claims (see below), to define forbidden infinite behavior

Preliminaries 2: Fairness

Does this PROMELA model terminate in each run? | Demo: start/fair.pml

```
byte n = 0;
bool flag = false;
active proctype P() {
 do :: flag -> break
     :: else \rightarrow n = 5 - n
  od
active proctype Q() {
  flag = true
```

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Termination guaranteed only if scheduling is (weakly) fair!

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Does this PROMELA model terminate in each run?

Demo: start/fair.pml

Termination guaranteed only if scheduling is (weakly) fair!

Definition (Weak Fairness)

A run is called weakly fair iff the following holds: each continuously executable statement is executed eventually.

Model Checking of Temporal Properties

Many correctness properties not expressible by assertions

- ▶ all properties that involve state changes
- temporal logic expressive enough to characterize many (but not all) properties

In this course: "temporal logic" synonymous with "linear temporal logic"

Today: model checking of properties formulated in temporal logic

Beyond Assertions

Locality of Assertions

Assertions talk only about the state at their location in the code

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Example

Mutual exclusion enforced by adding assertion to each critical section

```
critical++;
assert( critical <= 1 );
critical--;</pre>
```

Beyond Assertions

Locality of Assertions

Assertions talk only about the state at their location in the code

Example

Mutual exclusion enforced by adding assertion to each critical section

```
critical++;
assert( critical <= 1 );
critical--;</pre>
```

Drawbacks

- no separation of concerns (model vs. correctness property)
- changing assertions is error prone (easily out of sync)
- easy to forget assertions: correctness property might be violated at unexpected locations
- many interesting properties not expressible via assertions

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Mutual Exclusion

"critical <= 1 holds throughout any run"

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"Whenever several processes try to enter their critical section, eventually one of them does so."

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All of these are temporal properties \Rightarrow use temporal logic

Boolean Temporal Logic

Numerical variables in expressions

- ► Expressions such as i <= len-1 contain numerical variables
- Propositional LTL as introduced so far only knows propositions
- ▶ Slight generalisation of LTL required

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In Boolean Temporal Logic atomic building blocks are Boolean expressions over Prometa variables

Set For_{BTL} **of Boolean Temporal Formulas** (simplified)

▶ all global PROMELA variables and constants of type bool/bit are ∈ For_{RTI}

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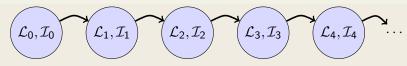
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- ▶ if P is a process and 1 is a label in P, then P@1 is ∈ For_{BTL} (P@1 reads "P is at 1")
- if ϕ and ψ are formulas $\in For_{BTL}$, then all of

$$! \phi, \quad \phi \&\& \psi, \quad \phi \mid\mid \psi, \quad \phi \rightarrow \psi, \quad \phi \Longleftrightarrow \psi$$

$$[]\phi, \quad <>\phi, \quad \phi U \psi$$

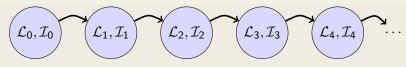
are $\in For_{RTI}$

A run σ through a Promela model M is a chain of states



- $lacksymbol{\mathcal{L}}_j$ maps each running process to its current location counter
- From \mathcal{L}_j to \mathcal{L}_{j+1} , only one of the location counters has advanced (exception: channel rendezvous)
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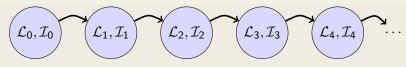
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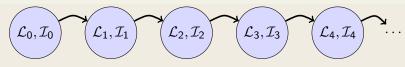


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 iff $\mathcal{L}_i(\texttt{P})$ is the location labeled with 1

Evaluating other formulas $\in For_{BTI}$ in runs σ : see previous lecture

Safety Properties

Safety Properties

- \dots are formulas of the form $[\,]\phi$
 - \blacktriangleright state that something 'good', ϕ , is guaranteed throughout each run
 - lacktriangle accordingly: [] $\neg\psi$ states that something 'bad', ψ , never happens

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Example

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TL formula [](critical <= 1)
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"it is guaranteed throughout each run that at most one process visits its critical section at any time"

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Example

```
TL formula [](critical <= 1)
```

"it is guaranteed throughout each run that at most one process visits its critical section at any time"

```
or, equivalently:
```

"it will never happen that more than one process visits its critical section"

Applying Temporal Logic to Critical Section Problem

We want to verify [](critical<=1) as a correctness property of:

```
active proctype P() {
  do :: /* non-critical activity */
        atomic {
          !inCriticalQ;
          inCriticalP = true
        critical++;
        /* critical activity */
        critical --;
        inCriticalP = false
  od
/* similarly for process Q */
```

Model Checking a Safety Property using JSPIN

1. add definition of TL formula to PROMELA file
 Example ltl atMostOne { [](critical <= 1) }
 General ltl name { TL-formula }
 can define more than one formula</pre>

- 2. load PROMELA file in JSPIN
- 3. ensure Safety is selected
- 4. select Verify
 - ▶ JSPIN always selects first formula
 - ▶ use command line ./pan -N name to select arbitrary formulas
- 5. (if necessary) select Stop to terminate too long verification

Demo: safety1.pml

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1t1 definitions not part of Ben Ari's book (SPIN≤ 6): ignore 5.3.2, etc.

Never Claims: Processes trying to show user wrong

Büchi automaton, as Promela process, for negated property

- 1. Negated TL formula translated to 'never' process
- accepting locations in Büchi automaton represented with help of accept labels ("acceptxxx:")
- 3. If one of these reached infinitely often, the orig. property is violated

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- accepting locations in Büchi automaton represented with help of accept labels ("acceptxxx:")
- 3. If one of these reached infinitely often, the orig. property is violated

Example (Never claim for <>p, simplified for readability)

```
never { /* !(<>p) */
   accept_xyz: /* passed \infty often iff !(<>p) holds */
   do
   :: (!p)
   od
}
```

Theory behind Spin

1. Represent the interleaving of all processes as a single automaton (only one process advances in each step), called \mathcal{M}

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- then ϕ holds in \mathcal{M} , otherwise we have a counterexample
- **4.** To check $\mathcal{L}^{\omega}(\mathcal{M}) \cap \mathcal{L}^{\omega}(\mathcal{NC}_{\neg \phi})$ construct intersection automaton (both automata advance in each step) and search for accepting run

Model Checking a Safety Property using Web Interface

```
1. add definition of TL formula to PROMELA file
    Example ltl atMostOne { [](critical <= 1) }
    General ltl name { TL-formula }
    can define more than one formula</pre>
```

- 2. load PROMELA file into web interface
- 3. ensure Safety is selected
- 4. enter name of LTL formula in according field
- select Verify

Demo: safety1.pml

Command Line Execution (Alt. 1)

```
Make sure ltl name { TL-formula } is in file.pml
> spin -a file.pml
> gcc -DSAFETY -o pan pan.c
> ./pan -N name
```

Demo: target/safety1.pml

Command Line Execution (Alt. 1)

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Make sure ltl name { TL-formula } is in file.pml
> spin -a file.pml
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```

Demo: target/safety1.pml

► The 'ltl <name> { <TL formula> }' construct must be part of your lab submission!

Command Line Execution (Alt. 2)

Write negated TL formula in file formulafile.PRP (first line)

```
> spin -a -F formulafile.PRP file.pml
```

- > gcc -DSAFETY -o pan pan.c
- > ./pan

Command Line Execution (Alt. 2)

Write negated TL formula in file formulafile.PRP (first line)

```
> spin -a -F formulafile.PRP file.pml
> gcc -DSAFETY -o pan pan.c
```

> ./pan

▶ some platforms have problems with -F

Liveness Properties

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- ... formulas of the form $<>\phi$
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Example

<>csp

(with csp a variable only true in the critical section of P)

"in each run, process P visits its critical section eventually"

Applying Temporal Logic to Starvation Problem

We want to verify <>csp as a correctness property of:

```
active proctype P() {
  do :: /* non-critical activity */
        atomic {
          !inCriticalQ;
          inCriticalP = true
        csp = true;
        /* critical activity */
        csp = false;
        inCriticalP = false
 od
/* similarly for process Q */
/* there, using csq
```

Model Checking a Liveness Property using JSPIN

- 1. open PROMELA file liveness1.pml
- 2. write ltl pWillEnterC { <>csp } in PROMELA file
 (as first ltl formula)
- 3. ensure that Acceptance is selected (SPIN will search for accepting cycles through the never claim)
- 4. for the moment uncheck Weak Fairness (see discussion below)
- select Verify

Verification Fails

Demo: start/liveness1.pml

Why?

Verification fails!

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Demo: start/liveness1.pml

Verification fails!

Why?

The liveness property on one process "had no chance".

Not even weak fairness was switched on!

Model Checking Liveness with Weak Fairness using ${ m JSPIN}$

Always check Weak fairness when verifying liveness

- 1. open Promela file
- 2. write ltl pWillEnterC { <>csp } in PROMELA file
 (as first ltl formula)
- **3.** ensure that Acceptance is selected (SPIN will search for accepting cycles through the never claim)
- 4. ensure Weak fairness is checked
- select Verify

Model Checking Liveness using Web Interface

1. add definition of TL formula to PROMELA file

- 2. load PROMELA file into web interface
- 3. ensure Acceptance is selected
- 4. enter name of LTL formula in according field
- 5. ensure Weak fairness is checked
- 6. select Verify

Demo: liveness1.pml

Model Checking Liveness using Spin directly

Command Line Execution (Alt. 1)

```
Make sure ltl name { TL-formula } is in file.pml
> spin -a file.pml
> gcc -o pan pan.c
> ./pan -a -f [-N name]
-a acceptance cycles, -f weak fairness
```

Demo: start/liveness1.pml

Model Checking Liveness using Spin directly

Command Line Execution (Alt. 2)

Write negated TL formula in file formulafile.PRP (first line)

```
> spin -a -F formulafile.PRP file.pml
```

```
> gcc -o pan pan.c
> ./pan -a -f
```

-a acceptance cycles, -f weak fairness

Verification fails again!

Why?

Verification fails again!

Why?

Weak fairness is too weak . . .

Definition (Weak Fairness)

A run is called weakly fair iff the following holds: each continuously executable statement is executed eventually.

Verification fails again!

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Definition (Weak Fairness)

A run is called weakly fair iff the following holds: each continuously executable statement is executed eventually.

Note that !inCriticalQ is not continuously executable!

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Why?

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Definition (Weak Fairness)

A run is called weakly fair iff the following holds: each continuously executable statement is executed eventually.

Note that !inCriticalQ is not continuously executable!

Restriction to weak fairness is principal limitation of SPIN

The only way to show liveness of our example is to rewrite the model

Temporal Model Checking without Ghost Variables

We want to verify mutual exclusion without using ghost variables

```
bool inCriticalP = false, inCriticalQ = false;
active proctype P() {
 do :: atomic {
          !inCriticalQ;
          inCriticalP = true
        /* critical activity */
cs:
        inCriticalP = false
 od
}
/* similar for process Q with same label cs: */
ltl mutualExcl { []!(P@cs && Q@cs) }
```

Demo: start/noGhost.pml

Liveness Revisited

Label expressions often remove the need for ghost variables

Liveness Revisited

Label expressions often remove the need for ghost variables

- ► Specify liveness of fair.pml using labels
- Prove termination
- Weak fairness is needed. and sufficient

Demo: target/fair.pml

Literature for this Lecture

```
Ben-Ari Chapter 5
except Sections 5.3.2, 5.3.3, 5.4.2
(ltl replaces #define and -f option of Spin)
```