

CHALMERS

## Deadline-monotonic scheduling

**Properties:**

- Uses static priorities
  - Priority is determined by urgency: the task with the shortest relative deadline receives highest priority
  - Proposed as a generalization of rate-monotonic scheduling (J. Leung and J. W. Whitehead, 1982)  
 Note that RM is a special case of DM, with  $D_i = T_i$
- Theoretically well-established
  - Exact feasibility test exists (an NP-complete problem)
  - DM is optimal among all scheduling algorithms that use static task priorities for which  $D_i \leq T_i$  (shown by J. Leung and J. W. Whitehead in 1982)

CHALMERS

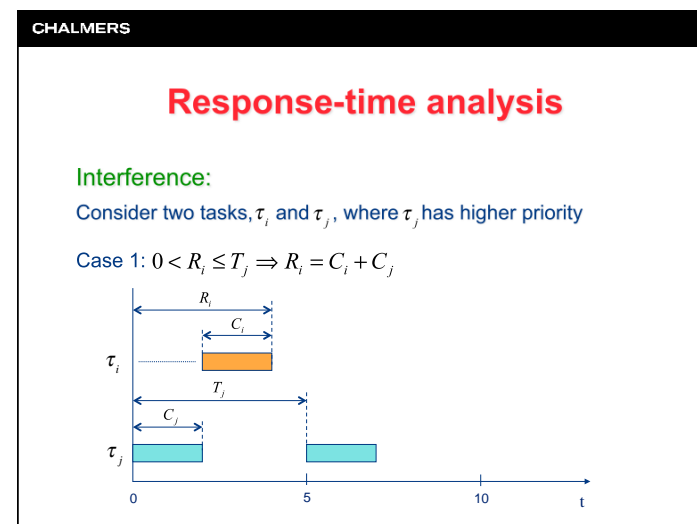
## Response-time analysis

The response time  $R_i$  for a task  $\tau_i$  represents the worst-case completion time of the task when execution interference from other tasks are accounted for.

The response time for a task  $\tau_i$  consists of:

- $C_i$  The task's uninterrupted execution time (WCET)
- $I_i$  Interference from higher-priority tasks

$$R_i = C_i + I_i$$



CHALMERS

## Response-time analysis

**Interference:**  
 Consider two tasks,  $\tau_i$  and  $\tau_j$ , where  $\tau_j$  has higher priority

Case 2:  $T_j < R_i \leq 2T_j \Rightarrow R_i = C_i + 2C_j$

The diagram shows a horizontal time axis 't' with markers at 0, 5, and 10. Task  $\tau_j$  (cyan) has a period  $T_j$  and execution time  $C_j$ . Its first instance starts at  $t=0$  and ends at  $t=C_j$ . Its second instance starts at  $t=5$  and ends at  $t=5+C_j$ . Task  $\tau_i$  (orange) has a response time  $R_i$  and execution time  $C_i$ . Its first instance starts at  $t=C_j$  and ends at  $t=C_j+C_i$ . A second instance of  $\tau_i$  starts at  $t=5+C_j$  and ends at  $t=5+C_j+C_i$ . The response time  $R_i$  is indicated as the interval from the start of the first instance to the end of the second instance.

CHALMERS

## Response-time analysis

**Interference:**  
 Task  $\tau_i$  can be preempted by higher-priority task  $\tau_j$   
 The response time for  $\tau_i$  is at most  $R_i$  time units.

If  $0 < R_i \leq T_j$ , task  $\tau_i$  can be preempted at most one time by  $\tau_j$   
 If  $T_j < R_i \leq 2T_j$ , task  $\tau_i$  can be preempted at most two times by  $\tau_j$   
 If  $2T_j < R_i \leq 3T_j$ , task  $\tau_i$  can be preempted at most three times by  $\tau_j$   
 ...

The number of interferences from  $\tau_j$  is limited by:  $\left\lceil \frac{R_i}{T_j} \right\rceil$

The total time for these interferences are:  $\left\lceil \frac{R_i}{T_j} \right\rceil C_j$

CHALMERS

## Response-time analysis

**Interference:**

- For static-priority scheduling, the interference term is

$$I_i = \sum_{\forall j \in hp(i)} \left\lceil \frac{R_i}{T_j} \right\rceil C_j$$

where  $hp(i)$  is the set of tasks with higher priority than  $\tau_i$ .

- The response time for a task  $\tau_i$  is thus:

$$R_i = C_i + \sum_{\forall j \in hp(i)} \left\lceil \frac{R_i}{T_j} \right\rceil C_j$$

CHALMERS

## Response-time analysis

**Interference:**

- The equation does not have a simple analytic solution.
- However, an iterative procedure can be used:

$$R_i^{n+1} = C_i + \sum_{\forall j \in hp(i)} \left\lceil \frac{R_i^n}{T_j} \right\rceil C_j$$

- The iteration starts with a value that is guaranteed to be less than or equal to the final value of  $R_i$  (e.g.  $R_i^0 = C_i$ )
- The iteration completes at convergence ( $R_i^{n+1} = R_i^n$ ) or if the response time exceeds some threshold (e.g.  $D_i$ )

CHALMERS

## Exact feasibility test for DM

(Sufficient and necessary condition)

A sufficient and necessary condition for deadline-monotonic scheduling, for which  $D_i \leq T_i$ , is

$$\forall i: R_i \leq D_i$$

where  $R_i$  is the response time for task  $\tau_i$

The response-time analysis and associated feasibility test was presented by M. Joseph and P. Pandya in 1986.

CHALMERS

## Exact feasibility test for DM

(Sufficient and necessary condition)

The test is valid under the following assumptions:

1. All tasks are independent.
  - There must not exist dependencies due to precedence or mutual exclusion
2. All tasks are periodic.
3. Task deadline does not exceed the period ( $D_i \leq T_i$ ).
4. Task preemptions are allowed.

CHALMERS

## Example: scheduling using DM

Problem: Assume a system with tasks according to the figure below. The timing properties of the tasks are given in the table.

- a) Calculate the task response times.
- b) Show that the tasks are schedulable using DM
- c) What is the outcome of Liu & Layland's feasibility test for RM?

Task	$C_i$	$D_i$	$T_i$
$\tau_1$	12	52	52
$\tau_2$	10	40	40
$\tau_3$	10	30	30

We solve this on the blackboard!

CHALMERS

## Extended response-time analysis

The test can be extended to handle:

- Blocking
- Start-time variations ("release jitter")
- Time offsets
- Deadlines exceeding the period
- Overhead due to context switches, timers, interrupts, ...

In this course, we only study blocking.

CHALMERS

## Extended response-time analysis

Blocking can be accounted for in the following cases:

- Blocking caused by critical regions
  - Blocking factor  $B_i$  represents the length of critical region(s) that are executed by processes with lower priority than  $\tau_i$
- Blocking caused by non-preemptive scheduling
  - Blocking factor  $B_i$  represents largest WCET (not counting  $\tau_i$  )

$$R_i = C_i + B_i + \sum_{\forall j \in hp(i)} \left\lceil \frac{R_j}{T_j} \right\rceil C_j$$

- Note that the feasibility test is now only sufficient since the worst-case blocking will not always occur at run-time.

CHALMERS

## Extended response-time analysis

Blocking using ceiling priority protocol ICPP:

priority (H) > priority (M) > priority (L)  
 H and L share resource R

CHALMERS

## Extended response-time analysis

Blocking caused by lower-priority tasks:

- When using a priority ceiling protocol (such as ICPP), a task  $\tau_i$  can only be blocked once by a task with lower priority than  $\tau_i$ .
- This occurs if the lower-priority task is within a critical region when  $\tau_i$  arrives, and the critical region's ceiling priority is higher than or equal to the priority of  $\tau_i$ .
- Blocking now means that the start time of  $\tau_i$  is delayed (= the blocking factor  $B_i$ )
- As soon as  $\tau_i$  has started its execution, it cannot be blocked by a lower-priority task.

CHALMERS

## Extended response-time analysis

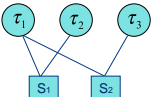
Determining the blocking factor for task  $\tau_i$ :

1. Determine the ceiling priorities for all critical regions.
2. Identify the tasks that have a priority lower than  $\tau_i$  and that calls critical regions with a ceiling priority equal to or higher than the priority of  $\tau_i$ .
3. Consider the times that these tasks lock the actual critical regions. The longest of those times constitutes the blocking factor  $B_i$ .

CHALMERS

### Example: scheduling using DM

Problem: Assume a system with tasks according to the figure below. The timing properties of the tasks are given in the table. Two semaphores  $S_1$  and  $S_2$  are used for synchronizing the tasks. The parameters  $H_{S_1}$  and  $H_{S_2}$  represent the longest time a task may lock semaphore  $S_1$  and  $S_2$ , respectively.



Task	$C_i$	$D_i$	$T_i$	$H_{S_1}$	$H_{S_2}$
$\tau_1$	2	4	5	1	1
$\tau_2$	3	12	12	1	-
$\tau_3$	8	24	25	-	2

CHALMERS

### Example: scheduling using DM

Problem: (cont'd)

Examine the schedulability of the tasks when ICPP (Immediate Ceiling Priority Protocol) is used.

- Derive the ceiling priorities of the semaphores.
- Derive the blocking factors for the tasks.
- Show whether the tasks are schedulable or not.

**We solve this on the blackboard!**