# Parallel Functional Programming Lecture 9 <br> Data Parallelism II 

## Mary Sheeran

http://www.cse.chalmers.se/edu/course/pfp

## DPH

Parallel arrays [: e:] (which can contain arrays)

## DPH

Parallel arrays [: e :] (which can contain arrays)

Expressing parallelism $=$ applying collective operations to parallel arrays

Note: demand for any element in a parallel array results in eval of all elements

## DPH array operations

```
(!:) :: [:a:] -> Int -> a
sliceP :: [:a:] -> (Int,Int) -> [:a:]
replicateP :: Int -> a -> [:a:]
mapP :: (a->b) -> [:a:] -> [:b:]
zipP :: [:a:] -> [:b:] -> [:(a,b):]
zipWithP :: (a->b->c) -> [:a:] -> [:b:] -> [:c:]
filterP :: (a->Bool) -> [:a:] -> [:a:]
concatP :: [:[:a:]:] -> [:a:]
concatMapP :: (a -> [:b:]) -> [:a:] -> [:b:]
unconcatP :: [:[:a:]:] -> [:b:] -> [:[:b:]:]
transposeP :: [:[:a:]:] -> [:[:a:]:]
expandP :: [:[:a:]:] -> [:b:] -> [:b:]
combineP :: [:Bool:] -> [:a:] -> [:a:] -> [:a:]
splitP :: [:Bool:] -> [:a:] -> ([:a:], [:a:])
```


## Parallel array comprehensions

[: forceOn p m l | p <- ps, isFar len l p:]

## Examples

```
svMul :: [:(Int,Float):] -> [:Float:] -> Float
svMul sv v = sumP [: f*(v !: i) | (i,f) <- sv :]
```

```
smMul :: [:[:(Int,Float):]:] -> [:Float:] -> Float
smMul sm v = sumP [: svMul row v | row <- sm :]
```


## Examples

```
svMul :: [:(Int,Float):] -> [:Float:] -> Float
svMul sv v = sumP [: f*(v !: i) | (i,f) <- sv :]
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```



## Barnes Hut N-body simulation

Reduces cost from $\mathrm{O}\left(\mathrm{N}^{\wedge} 2\right)$ to $\mathrm{O}(\mathrm{N} \log \mathrm{N})$

Uses octree to represent the hierarchical grouping of particles
Particles close to each other are grouped and their centre of gravity (centroid) Is calculated.

When a particle with which they should interact is sufficiently far away, then the centroid can be used.

Usually done in 3D. This DPH example is in 2D (and slightly simplified), so uses quad tree.
The Barnes Hut paper is GREAT.
Barnes, Josh, and Hut Piet. "A heirarchical $\mathrm{O}(\mathrm{N} \log \mathrm{N})$ force-calculation algorithm."
Nature. 324. (1986)
http://www.nature.com/nature/iournal/v324/n6096/pdf/324446a0.pdf (Access when on a Chalmers computer)

|  | $p_{3}$ |  | $p_{1}$ |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $p_{2}$ |  |  |  |
|  | $p_{7}$ | $p_{6}$ | $p_{4}$ |  |
| $p_{8}$ |  |  |  | $p_{5}$ |
| $p_{9}$ |  |  |  |  |

Figure 2: Subdivision of area




Having constructed such a tree, the force on any particle $p$ may be approximated by a simple recursive calculation. Start at the root cell of the tree, which contains the entire system. Let $l$ be the length of the cell currently being processed and $D$ the distance from the cell's centre-of-mass to $p$. If $l / D<\theta$, where $\theta$ is a fixed accuracy parameter $\sim 1$, then include the interaction between this cell and $p$ in the total being accumulated. Otherwise, resolve the current cell into its eight subcells, and recursively examine each one in turn. The core of the force calculation routine may be compactly expressed in SCHEME, a dialect of LISP:
(define (acceleration particle ensemble)
(cond ((singleton? ensenble) (nerton-acceleration particle (the-elenent ensenble))) ( (< (/ (diameter ensemble)
(distance particle (centroid ensenble)))
theta)
(nevton-acceleration particle (centroid ensenble)))
(else
(reduce sur-vector
(map (lambda (e) (acceleration particle e)) (subdivisions ensemble))))))

## Barnes Hut (2D) in DPH

```
-- Compute one step of the n-body simulation
oneStep :: [:Particle:] -> [:Particle:]
oneStep particles = moveParticles particles forces
    where
        tree = buildTree initialArea particles
        forces = calcForces (lengthof initialArea) tree particles
buildTree :: Area -> [:Particle:] -> Tree
calcForces :: Float -> Tree -> [:Particle:] -> [:Force:]
moveParticles :: [:Particle:] -> [:Force:] -> [:Particle:]
lengthof :: Area -> Float
```

```
moveParticles :: [:Particle:] -> [:Force:] -> [:Particle:]
moveParticles ps fs = zipWithP moveParticle ps fs
moveParticle :: Particle -> Force -> Particle
moveParticle (Particle { mass = m
                            , location = loc
                            , velocity = vel })
    force
    = Particle { mass = m
    , location = loc + vel * timeStep
    , velocity = vel + accel * timeStep }
    where
    accel = force / m
```

```
data Tree = Node Mass Location [:Tree:]
    -- Rose tree for spatial decomposition
```

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```

The only way to get parallelism
over sub-trees

```
data Tree = Node Mass Location [:Tree:]
    -- Rose tree for spatial decomposition
```

-- Perform spatial decomposition and build the tree
buildTree :: Area -> [:Particle:] -> Tree
buildTree area [: p :] = Node (mass p) (location p) [::]
buildTree area particles $=$ Node m l subtrees
where
( $\mathrm{m}, \mathrm{l}$ ) = calcCentroid subtrees
subtrees $=[$ : buildTree a ps
| a <- splitArea area
, let $\mathrm{ps}=[: p \mid \mathrm{p}<-$ particles, inArea a $\mathrm{p}:]$
, lengthP ps > 0 :]

```
data Tree = Node Mass Location [:Tree:]
    -- Rose tree for spatial decomposition
```

-- Perform spatial decomposition and build the tree
buildTree :: Area $->$ [:Particle:] $->$ Tree
buildTree area [: p :] = Node (mass p) (location

## Up to 4 areas

buildTree area particles $=$ Node m l subtrees
where
$(\mathrm{m}, \mathrm{l}) \quad=$ calcCentroid subtrees
subtrees $=[$ : buildTree a ps
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data Tree = Node Mass Location [:Tree:]
    -- Rose tree for spatial decomposition
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-- Perform spatial decomposition and build the tree
buildTree :: Area -> [:Particle:] -> Tree
buildTree area [: p :] = Node (mass p) (location p) [::]
buildTree area particles = Node m l subtrees
    where
        (m,l) = calcCentroid subtrees
        subtrees = [: buildTree a ps
                            | a <- splitArea area
                            , let ps = [:p | p <- panticles, inArea a p:]
                            , lengthP ps > 0 :]
```


## Tons of parallelism!

1) From recursive calls of parallel function buildTree 2) From nested parallel arrays
```
calcForces :: Float -> Tree -> [:Particle:] -> [:Force:]
calcForces len (Node m l ts) ps
    = let
        far_forces = [: forceon p m l | p <- ps, isFar len l p :]
        near_ps = [: p | p <- ps, not (isFar len l p) :]
        near_forces_s = [: calcForces (len / 2) t near_ps | t <- ts :]
        near_forces = [: sumForces p_forces
                            | p_forces <- transposeP near_forces_s :]
        in
        combineP [:isFar len l p | p <- ps:] far_forces near_forces
```


## Performance



Figure 6. Benchmark Runtime Performance

## Summary of example

Nestedness is essential in this example

Feels like just replacing [] by [: :] but authors caution that deciding on parallelisation needs thought and has influence on communication needed

Doesn't yet run faster than using Data.Vector, but getting there!

## Data parallelism

Perform same computation on a collection of differing data values
examples: HPF (High Performance Fortran) CUDA

Both support only flat data parallelism
Flat : each of the individual computations on (array) elements is sequential
those computations don't need to communicate parallel computations don't spark further parallel computations

# Regular, Shape-polymorphic, Parallel Arrays in Haskell 

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API for purely functional, collective operations over dense, rectangular, multi-dimensional arrays supporting shape polymorphism

ICFP 2010

## Ideas

Purely functional array interface using collective (whole array) operations like map, fold and permutations can

- combine efficiency and clarity
- focus attention on structure of algorithm, away from low level details

Influenced by work on algorithmic skeletons based on Bird Meertens formalism

Provides shape polymorphism not in a standalone specialist compiler like SAC, but using the Haskell type system

## terminology

Regular arrays
dense, rectangular, most elements non-zero
shape polymorphic
functions work over arrays of arbitrary dimension

## terminology

Regular arrays dense, rectan
shape polym
note: the arrays are purely functional and immutable
functions wo demanded at once $->$ parallelism
P processing elements, n array
elements => n/P consecutive elements on each proc. element

## But things moved on!

Repa from ICFP 2010 had ONE type of array (that could be either delayed or manifest, like in Obsidian)

A paper from the Haskell' 11 showed efficient parallel stencil convolution
http://www.cse.unsw.edu.au/~keller/Papers/stencil.pdf

## Fancier array type

```
data Array sh a
    = Array
        { arrayExtent :: sh
        , arrayRegions :: [Region sh a] }
data Region sh a
    = Region { regionRange :: Range sh
, regionGen :: Generator sh a }
data Range sh
    = RangeAll
    | RangeRects { rangeMatch :: sh }->\mathrm{ Bool
        , rangeRects :: [Rect sh] }
data Rect sh
    = Rect sh sh
data Generator sh a
    = GenManifest { genVector :: Vector a }
    | forall cursor.
        GenCursored { genMake :: sh -> cursor
        , genShift :: sh -> cursor -> cursor
        , genLoad :: cursor -> a }
```

Figure 5. New Repa Array Types

## Fancier array type



But you need to be a guru to get good performance!

## Put Array representation into the type!

The fundamental problem with Repa $1 \& 2$ is the following: at an particular point in the code, the programmer typically has a clear idea of the array representation they desire. For example, it may consist of three regions, left edge, middle, right edge, each of which is a delayed array. Although this knowledge is statically known to the the programmer, it is invisible in the types and only exposed to the compiler if very aggressive value inlining is used. Moreover, the programmer's typeless reasoning can easily fail, leading to massive performance degradation.

The solution is to expose static information about array representation to Haskell's main static reasoning system; its type system.

## Repa 3 (Haskell’12)

# Guiding Parallel Array Fusion with Indexed Types 

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Cambridge, England
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#### Abstract

We present a refined approach to parallel array fusion that uses indexed types to specify the internal representation of each array. Our approach aids the client programmer in reasoning about the performance of their program in terms of the source code. It also makes the intermediate code easier to transform at compile-time, resulting in faster compilation and more reliable runtimes. We demonstrate how our new approach improves both the clarity and performance of several end-user written programs, including a fluid flow solver and an interpolator for volumetric data.


Categories and Subject Descriptors D. 3.3 [Programming Lan-

This second version of doubleZip runs as fast as a hand-written imperative loop. Unfortunately, it is cluttered with explicit pattern matching, bang patterns, and use of the force function. This clutter is needed to guide the compiler towards efficient code, but it obscures the algorithmic meaning of the source program. It also demands a deeper understanding of the compilation method than most users will have, and in the next section, we will see that these changes add an implicit precondition that is not captured in the function signature. The second major version of the library, Repa 2, added support for efficient parallel stencil convolution, but at the same time also increased the level of clutter needed to achieve efficient code [8].

## version

I use Repa 3.2.1.1 (which works with the GHC that you get with the current Haskell platform)
cabal update
cabal install repa-3.2.1.1
cabal install repa-algorithms-3.2.1.1
cabal install bmp-1.2.1.1
cabal install repa-io-3.2.1.1
cabal install repa-examples-3.2.1.1
http://hackage.haskell.org/packages/archive/repa/3.2.1.1/doc/html/Data-Array-Repa.html

If you have a later GHC installed, you can use a later Repa, and probably get better performance.

## 10 Array representations!

- D - Delayed arrays (delayed) $\S 3.1$
- C - Cursored arrays (delayed) $\S 4.4$
- U - Adaptive unboxed vectors (manifest) $\S 3.1$
- V - Boxed vectors (manifest) $\S 4.1$
- B - Strict byte arrays (manifest) $\S 4.1$
- F - Foreign memory buffers (manifest) $\S 4.1$
- P - Partitioned arrays (meta) $\S 4.2$
- S - Smallness hints (meta) $\S 5.1 .1$
- I - Interleave hints (meta) §5.2.1
- X - Undefined arrays (meta) $\S 4.2$


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But the 18 minute presentation at Haskell'12 makes it all make sense!! Watch it!
http://www.youtube.com/watch?v=YmZtP11mBho

## Type Indexing

data family Array rep she
type index giving representation

## Type Indexing

data family Array rep she
shape

## Type Indexing

data family Array rep sh e
element type

## map

map
: : (Shape sh, Source ra) $=>$
( $\mathrm{a}->\mathrm{b}$ ) $->$ Array r sh $\mathrm{a}->$ Array $D$ sh $b$

## map

```
map
:: (Shape sh, Source r a) =>
(a -> b) -> Array r sh a -> Array D sh b
map f arr = case delay arr of ADelayed sh g ->
    ADelayed sh (f . g)
```


## Fusion

# Delayed (and cursored) arrays enable fusion that avoids intermediate arrays 

User-defined worker functions can be fused

This is what gives tight loops in the final code

## example

import Data.Array.Repa as $R$
will later see
transpose2P : : Monad m => Array U DIM2 Double $\rightarrow$ m (Array U DIM2 Double)

## example

import Data.Array.Repa as $R$
will later see

```
transpose2P :: Monad m => Array U DIM2 Double -> m (Array U DIM2 Double)
```

index type SHAPE EXTENT

## example

import Data.Array.Repa as $R$
will later see

```
transpose2P :: Monad m => Array U DIM2 Double -> m (Array U DIM2 Double)
```



## snoc lists

Haskell lists are cons lists
1:2:3:[] is the same as $[1,2,3]$

Repa uses snoc lists at type level for shape types and at value level for shapes

DIM2 = Z :. Int :. Int is a shape type

Z :. i :. $\mathrm{j} \quad$ read as ( $\mathrm{i}, \mathrm{j}$ ) is an index into a two dim. array

# more general transpose (on inner two dimensions) 

```
transpose
    :: (Shape sh, Source r e) =>
        Array r ((sh :. Int) :. Int) e
        -> Array D ((sh :. Int) :. Int) e
```


## more general transpose (on inner two dimensions) is provided

```
transpose
    :: (Shape sh, Source r e) =>
        Array r ((sh :. Int) :. Int) e
        -> Array D ((sh :. Int) :. Int) e
```

This type says an array with at least 2 dimensions.
The function is shape polymorphic

# more general transpose (on inner two dimensions) is provided 

```
transpose
    :: (Shape sh, Source r e) =>
        Array r ((sh :. Int) :. Int) e
        -> Array D ((sh :. Int) :. Int) e
```

Functions with at-least constraints become a parallel map over the unspecified dimensions (called rank generalisation)

Important way to express parallel patterns

## more general transpose (on inner two dimensions)

```
transpose
    :: (Shape sh, Source r e) =>
        Array r ((sh :. Int) :. Int) e
        -> Array D ((sh :. Int) :. Int) e
    D stands for delayed array
```


## filter?

filter :: (...) => (e -> Bool) -> Array r DIM1 e -> Array D DIM1 e
can't be shape polymorphic
the shape of the output depends on the value of the input
filtering rows in a matrix might give different lengths (but we only deal with rectangular arrays)

## filter?

filter :: (...) => (e -> Bool) -> Array r DIM1 e -> Array D DIM1 e
can't be shape polymorphic
the shape of the output depends on the value of the input
filtering rows in a matrix might give different lengths (but we only deal with rectangular arrays)

However, there are fancy operations to slice up arrays in various interesting ways

## Remember

Arrays of type (Array D sh a) or (Array C sh a) are not real arrays. They are represented as functions that compute each element on demand. You need to use computeS, computeP, computeUnboxedP and so on to actually evaluate the elements.
(quote from
http://hackage.haskell.org/packages/archive/repa/3.2.1.1/doc/html/Data-ArrayRepa.html
which has lots more good advice, including about compiler flags)

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(quote from
http://hackage.haskell.org/packages/archive/repa/3.2.1.1/doc/html/Data-ArrayRepa.html
which has lots more good advice, including about compiler flags)
computeP
$::($ Monad m, Source r2e, Target r2e, Load r1 sh e) =>
Array r1 sh e -> m (Array r2 sh e)

## Example: sorting

## bitonic sequence

inc (not decreasing) then
dec (not increasing)
or a cyclic shift of such a sequence

## Butterfly


bitonic

## Butterfly



## Making a recursive sorter (D\&C)

Make a bitonic sequence using two half-size sorters

## Batcher's sorter (bitonic)



## bitonic merger



## dee for diamond

```
dee :: (Shape sh, Monad m) => (Int }->\mathrm{ Int }->\mathrm{ Int) }->\mathrm{ (Int }->\mathrm{ Int -> Int)
        -> Int -> Array U (sh :. Int) Int -> m (Array U (sh :. Int) Int)
dee f g s arr = let sh = extent arr in computeUnboxedP $ fromFunction sh ixf
    where
        ixf (sh :. i) = if (testBit i s) then (g a b) else (f a b)
        where
            a = arr ! (sh :. i)
            b = arr ! (sh :. (i `xor` s2))
            s2 = (1::Int) `shiftL` s
```

assume input array has length a power of $2, \mathrm{~s}>=0$ in this and later functions

```
bitonicMerge
    :: (Monad m, Shape sh) =>
    Int -> Array U (sh :. Int) Int -> m (Array U (sh :. Int) Int)
bitonicMerge n = compose [dee max min (n-i) | i <- [1..n]]
```

```
compose :: Monad m => [a -> m a] -> a -> m a
compose [] arr = return arr
compose (f:fs) arr
    = do
        arr1 <- f arr
        compose fs arrl
```


## tmerge



## vee

```
vee :: (Shape sh, Monad m) => (Int -> Int -> Int) -> (Int -> Int -> Int)
    -> Int -> Array U (sh :. Int) Int -> m (Array U (sh :. Int) Int)
vee f g s arr = let (sh :. len)
    = extent arr in computeUnboxedP $ fromFunction (sh :. len) ixf
    where
    ixf (sh :. ix) = if (testBit ix s) then (g a b) else (f a b)
        where
            a = arr ! (sh :. ix)
            b = arr ! (sh :. newix)
            newix = flipLSBsTo s ix
```


## tmerge

```
tmerge
    :: (Monad m, Shape sh) =>
    Int -> Array U (sh :. Int) Int -> m (Array U (sh :. Int) Int)
tmerge n = compose $ vee min max (n-1) : [dee min max (n-i) | i <- [2..n]]
```



## Work and depth again

Can we calculate work and depth for this structure?

## Advice from Blelloch

Blelloch on programming parallel algorithms:

Start with work same as best sequential algorithm.
Work is most important.
Next reduce span.
Want work over $p$ term to dominate.

## sorter

```
tsort
    :: (Monad m, Shape sh) =>
        Int -> Array U (sh :. Int) Int -> m (Array U (sh :. Int) Int)
tsort n = compose [tmerge i | i <- [1..n]]
```


## Performance is decent!

Initial benchmarking for 2^20 Ints

Around 880 ms on 4 cores on this laptop
Compares to 1.77 seconds for Data.List.sort (which is seqential)
Still slower than Persson's non-entry from last year about a factor of 2 , which is about what you would expect when comparing Batcher's bitonic sort to quicksort

## connents

Should be very scalable
Can probably be sped up! Need to add sequentialness $)$
Similar approach might greatly speed up the FFT in repa-examples (and I found a guy running an FFT in Haskell competition)

I wonder if more standard higher order functions (without bit hackery) could be made to work well (= fast) (zipWith, interleave etc.)

Note that this approach turned a nested algorithm into a flat one
Did you notice that I didn't mention scan ?? (Repa needs one!)
Study examples written by the master

## transpose 2D array in parallel

```
transpose2P
    :: Monad m
    => Array U DIM2 Double
    -> m (Array U DIM2 Double)
transpose2P arr
    = arr `deepSeqArray
        do computeUnboxedP
        $ unsafeBackpermute new_extent swap arr
    where swap (Z :. i :. j) = Z :. j :. i
        new_extent = swap (extent arr)
```


## Matrix Multiplication $\quad(A \cdot B)_{i, j}=\sum_{k=1}^{n} A_{i, k} \cdot B_{k, j}$

| $a_{11}$ | $a_{12}$ | $a_{13}$ |
| :--- | :--- | :--- |
| $a_{21}$ | $a_{22}$ | $a_{23}$ |
| $a_{31}$ | $a_{32}$ | $a_{33}$ |
| $a_{41}$ | $a_{42}$ | $a_{43}$ |$\quad$| $b_{11}$ | $b_{12}$ |
| :--- | :--- | :--- |
| $b_{21}$ | $b_{22}$ |
| $b_{31}$ | $b_{32}$ |$\quad=$| $c_{11}$ | $c_{12}$ |
| :--- | :--- |
| $c_{21}$ | $c_{22}$ |
| $c_{31}$ | $c_{32}$ |
| $C_{41}$ | $C_{42}$ |

slide from Lippmeier's ICFP 2010 talk on Repa

```
mmultP :: Monad m
    => Array U DIM2 Double
    -> Array U DIM2 Double
    -> m (Array U DIM2 Double)
mmultP arr brr
    = [arr, brr] `deepSeqArrays`
    do trr <- transpose2P brr
    let (z :. h1 :. _) = extent arr
    let (Z :. _ :. w2) = extent brr
    computeP
    $ fromFunction (Z :. h1 :. w2)
    $ \ix -> R.sumAllS
                                $ R.zipWith (*)
                            (unsafeSlice arr (Any :. (row ix) :. All))
                            (unsafeSlice trr (Any :. (col ix) :. All))
```


## stackoverflow

is your friend

See for example
http://stackoverflow.com/questions/14082158/idiomatic-option-pricing-and-risk-using-repa-parallel-arrays?rq=1
(contains very cool 3-D plot of ghc flags to find best combination)

## Conclusions (Repa)

Based on DPH technology

Good speedups!

Neat programs

Good control of Parallelism

BUT CACHE AWARENESS needs to be tackled (see lecture later by Nick Frolov)

Array representations for parallel functional programming is an important, fun and frustrating research topic ©

## Questions to think about

Can my bitonic sorter in Repa be sped up? (I will put the code up on the web page.) (not a bad way to explore the Repa 3 API)

Can you implement a fast scan in Repa?

## Next lecture (tomorrow)

Erlang!
(more Haskell in Lennart Augustsson's guest lecture on May 2)

Feel free to mail questions

MAKE USE of Nick! He knows a lot and is happy to guide you.

