Software Engineering using Formal Methods Java Modeling Language

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Specifications as Contracts

to stress the different roles – obligations – responsibilities in a specification:

widely used analogy of the specification as a contract

"Design by Contract" methodology

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"Design by Contract" methodology

contract between caller and callee of method

callee guarantees certain outcome provided caller guarantees prerequisites

Running Example: ATM.java

```
public class ATM {
    // fields:
    private BankCard insertedCard = null;
    private int wrongPINCounter = 0;
    private boolean customerAuthenticated = false;
    // methods:
    public void insertCard (BankCard card) { ... }
    public void enterPIN (int pin) { ... }
    public int accountBalance () { ... }
    public int withdraw (int amount) { ... }
    public void ejectCard () { ... }
```

Informal Specification

very informal Specification of 'enterPIN (int pin)':

Enter the PIN that belongs to the currently inserted bank card into the ATM. If a wrong PIN is entered three times in a row, the card is confiscated. After having entered the correct PIN, the customer is regarded as authenticated.

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wrongPINCounter >= 2 and pin is incorrect

postcondition card is confiscated

user is not authenticated

Meaning of Pre/Post-condition pairs

Definition

A **pre/post-condition** pair for a method m is **satisfied by the implementation** of m if:

When m is called in any state that satisfies the precondition then in any terminating state of m the postcondition is true.

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- **3.** Terminating state may be reached by normal or by abrupt termination (cf. exceptions).

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non-termination and abrupt termination \Rightarrow next lecture

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Describing contracts of units in a mathematically precise language.

Motivation:

- higher degree of precision
- eventually: automation of program analysis of various kinds:
 - static checking
 - program verification

JML is a specification language tailored to JAVA.

General JML Philosophy

Integrate

- specification
- implementation

in one single language.

 \Rightarrow JML is not external to JAVA

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JAVA + FO Logic + pre/post-conditions, invariants

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JML/Java integration

JML annotations are attached to JAVA programs
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JML annotations are attached to JAVA programs by writing them directly into the JAVA source code files

not to confuse JAVA compiler:

JML annotations live in in special comments, ignored by JAVA, recognized by JML tools.

```
from the file ATM. java
/*@ public normal_behavior
  @ requires !customerAuthenticated;
  @ requires pin == insertedCard.correctPIN;
  @ ensures customerAuthenticated:
  0*/
public void enterPIN (int pin) {
    if ( ...
```

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from the file ATM. java
/*@ public normal_behavior
  @ requires !customerAuthenticated;
  @ requires pin == insertedCard.correctPIN;
  @ ensures customerAuthenticated:
  @*/
public void enterPIN (int pin) {
    if ( ...
Everything between /* and */ is invisible for JAVA.
```

```
/*0 public normal_behavior
    @ requires !customerAuthenticated;
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public void enterPIN (int pin) {
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/*@ public normal_behavior
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public void enterPIN (int pin) {
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```

But:

A JAVA comment with '@' as its first character it is *not* a comment for JML tools.

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/*@ public normal_behavior
  @ requires !customerAuthenticated;
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  @ ensures customerAuthenticated;
  @*/
public void enterPIN (int pin) {
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```

But:

A JAVA comment with '0' as its first character it is *not* a comment for JML tools.

JML annotations appear in JAVA comments starting with @.

```
/*@ public normal_behavior
  @ requires !customerAuthenticated;
  @ requires pin == insertedCard.correctPIN;
  @ ensures customerAuthenticated;
  @*/
public void enterPIN (int pin) {
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```

But:

A JAVA comment with '@' as its first character it is *not* a comment for JML tools.

JML annotations appear in JAVA comments starting with @.

How about "//" comments?

```
/*@ public normal_behavior
  @ requires !customerAuthenticated;
  @ requires pin == insertedCard.correctPIN;
  @ ensures customerAuthenticated; @*/
equivalent to:
//@ public normal_behavior
//@ requires !customerAuthenticated;
//@ requires pin == insertedCard.correctPIN;
//@ ensures customerAuthenticated;
```

What about the intermediate '@'s?

```
/*@ public normal_behavior
    @ requires !customerAuthenticated;
    @ requires pin == insertedCard.correctPIN;
    @ ensures customerAuthenticated;
    @*/
public void enterPIN (int pin) {
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```

Within a JML annotation, a '@' is ignored:

- ▶ if it is the first (non-white) character in the line
- ▶ if it is the last character before '*/'.

```
/*@ public normal_behavior
  0 requires !customerAuthenticated;
  0 requires pin == insertedCard.correctPIN;
  0 ensures customerAuthenticated:
  @*/
public void enterPIN (int pin) {
    if ( ...
What about the intermediate '0's?
```

Within a JML annotation, a '@' is ignored:

- ▶ if it is the first (non-white) character in the line
- if it is the last character before '*/'.
- ⇒ The blue '@'s are not required, but it's a convention to use them.

```
/*@ public normal_behavior
  @ requires !customerAuthenticated;
  @ requires pin == insertedCard.correctPIN;
  @ ensures customerAuthenticated;
  @*/
public void enterPIN (int pin) {
   if ( ...
```

This is a **public** specification case:

- 1. it is accessible from all classes and interfaces
- 2. it can only mention public fields/methods of this class

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/*@ public normal_behavior
  @ requires !customerAuthenticated;
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```

This is a **public** specification case:

- 1. it is accessible from all classes and interfaces
- 2. it can only mention public fields/methods of this class
- 2. Can be a problem. Solution later in the lecture.

```
/*@ public normal_behavior
  @ requires !customerAuthenticated;
  @ requires pin == insertedCard.correctPIN;
  @ ensures customerAuthenticated;
  @*/
public void enterPIN (int pin) {
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```

Each keyword ending with behavior opens a 'specification case'.

normal_behavior Specification Case

The method guarantees to not throw any exception

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/*@ public normal_behavior
  @ requires !customerAuthenticated;
  @ requires pin == insertedCard.correctPIN;
  @ ensures customerAuthenticated;
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public void enterPIN (int pin) {
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Each keyword ending with behavior opens a 'specification case'.

normal_behavior Specification Case

The method guarantees to not throw any exception (on the top level),

```
/*@ public normal_behavior
  @ requires !customerAuthenticated;
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  @*/
public void enterPIN (int pin) {
  if ( ...
```

Each keyword ending with **behavior** opens a 'specification case'.

normal_behavior Specification Case

The method guarantees to *not* throw any exception (on the top level), if the caller guarantees all preconditions of this specification case.

```
/*@ public normal_behavior
  @ requires !customerAuthenticated;
  @ requires pin == insertedCard.correctPIN;
  @ ensures customerAuthenticated;
  0*/
public void enterPIN (int pin) {
    if ( ...
This specification case has two preconditions (marked by requires)
 1. !customerAuthenticated
 2. pin == insertedCard.correctPIN
```

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here:
preconditions are boolean JAVA expressions
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here:
preconditions are boolean JAVA expressions
in general:
preconditions are boolean JML expressions (see below)
```

```
/*@ public normal_behavior
  @ requires !customerAuthenticated;
  @ requires pin == insertedCard.correctPIN;
  @ ensures customerAuthenticated;
  @*/
specifies only the case where both preconditions are true in pre-state
the above is equivalent to:
/*@ public normal behavior
  @ requires ( !customerAuthenticated
  0
                 && pin == insertedCard.correctPIN );
  @ ensures customerAuthenticated;
  0*/
```

```
/*@ public normal_behavior
  @ requires !customerAuthenticated;
  @ requires pin == insertedCard.correctPIN;
  @ ensures customerAuthenticated;
  @*/
public void enterPIN (int pin) {
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This specification case has one postcondition (marked by ensures)

customerAuthenticated

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/*@ public normal_behavior
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This specification case has one postcondition (marked by ensures)
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postcondition is boolean JAVA expressions
in general:
postconditions are boolean JML expressions (see below)
```

different specification cases are connected by 'also'.

```
/*@ public normal_behavior
  @ requires !customerAuthenticated;
  @ requires pin == insertedCard.correctPIN;
  @ ensures customerAuthenticated:
  0
  @ also
  0
  @ public normal_behavior
  @ requires !customerAuthenticated;
  @ requires pin != insertedCard.correctPIN;
  @ requires wrongPINCounter < 2;</pre>
  @ ensures wrongPINCounter == \old(wrongPINCounter) + 1;
  0*/
public void enterPIN (int pin) {
```

```
/*@ <spec-case1> also
  @ public normal_behavior
  @ requires !customerAuthenticated;
  @ requires pin != insertedCard.correctPIN;
  @ requires wrongPINCounter < 2;</pre>
  @ ensures wrongPINCounter == \old(wrongPINCounter) + 1;
  @*/
public void enterPIN (int pin) { ...
for the first time, JML expression not a JAVA expression
\old(E) means: E evaluated in the pre-state of enterPIN.
E can be any (arbitrarily complex) (JML) expression.
```

```
/*@ <spec-case1> also <spec-case2> also
  @ public normal_behavior
  @ requires insertedCard != null;
  @ requires !customerAuthenticated;
  @ requires pin != insertedCard.correctPIN;
  @ requires wrongPINCounter >= 2;
  @ ensures insertedCard == null;
  @ ensures \old(insertedCard).invalid:
  0*/
public void enterPIN (int pin) { ...
two postconditions state that:
'Given the above preconditions, enterPIN guarantees:
insertedCard == null and \old(insertedCard).invalid'
```

Question:

```
could it be
    @ ensures \old(insertedCard.invalid);
instead of
    @ ensures \old(insertedCard).invalid;
??
```

Specification Cases Complete?

consider spec-case-1:

- @ public normal_behavior
- @ requires !customerAuthenticated;
- @ requires pin == insertedCard.correctPIN;
- @ ensures customerAuthenticated;

what does spec-case-1 not tell about post-state?

Specification Cases Complete?

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recall: fields of class ATM:

insertedCard
customerAuthenticated
wrongPINCounter

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what does spec-case-1 not tell about post-state?

recall: fields of class ATM:

insertedCard
customerAuthenticated
wrongPINCounter

what happens with insertCard and wrongPINCounter?

Completing Specification Cases

Completing Specification Cases

```
@ public normal_behavior
@ requires !customerAuthenticated;
@ requires pin != insertedCard.correctPIN;
@ requires wrongPINCounter < 2;</pre>
 ensures wrongPINCounter == \old(wrongPINCounter) + 1;
@ ensures insertedCard == \old(insertedCard);
 ensures customerAuthenticated
          == \old(customerAuthenticated);
```

0

completing spec-case-2:

Completing Specification Cases

@ public normal_behavior @ requires insertedCard != null; @ requires !customerAuthenticated; @ requires pin != insertedCard.correctPIN; @ requires wrongPINCounter >= 2; @ ensures insertedCard == null; @ ensures \old(insertedCard).invalid; 0 ensures customerAuthenticated 0 == \old(customerAuthenticated); ensures wrongPINCounter == \old(wrongPINCounter);

completing spec-case-3:

unsatisfactory to add

@ ensures loc == \old(loc);

for all locations loc which do not change

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add assignable clause for all locations which may change

@ assignable $loc_1, \ldots, loc_n;$

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Meaning: No location other than loc_1, \ldots, loc_n can be assigned to.

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Meaning: No location other than loc_1, \ldots, loc_n can be assigned to.
Special cases:
No location may be changed:
  @ assignable \nothing;
```

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Special cases:

No location may be changed:

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Unrestricted, method allowed to change anything:

@ assignable \everything;

Specification Cases with Assignable

```
completing spec-case-1:
```

- @ public normal_behavior
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- @ requires pin == insertedCard.correctPIN;
- @ ensures customerAuthenticated;
- @ assignable customerAuthenticated;

Specification Cases with Assignable

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completing spec-case-3:
  @ public normal_behavior
  @ requires insertedCard != null;
  @ requires !customerAuthenticated;
  @ requires pin != insertedCard.correctPIN;
  @ requires wrongPINCounter >= 2;
  @ ensures insertedCard == null;
  @ ensures \old(insertedCard).invalid;
  @ assignable insertedCard,
  0
                insertedCard.invalid.
```

Assignable Groups

You can specify groups of locations as assignable, using '*'.

example:

```
@ assignable o.*, a[*] ;
```

makes all fields of object o and all locations of array a assignable.

JML Modifiers

JML extends the JAVA modifiers by additional modifiers.

The most important ones are:

- spec_public
- pure

Aim: admitting more class elements to be used in JML expressions.

in ${\tt enterPIN}$ example, ${\tt pre/post-conditions}$ made heavy use of class fields

But: public specifications can only talk about public fields.

Not desired: make all fields public.

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Not desired: make all fields public.

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different solution: use specification-only fields (not covered in this course)

JML Modifiers: pure

It can be handy to use method calls in JML annotations. Examples:

- ▶ o1.equals(o2)
- ▶ li.contains(elem)
- ▶ li1.max() < li2.min()

allowed if, and only if method is guaranteed to have no side effects.

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In JML, you can specify methods to be 'pure':

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public /*@ pure @*/ int max() { ...
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'pure' puts obligation on implementer, not to cause side effects, but allows to use method in annotations

'pure' similar to 'assignable \nothing;', but global to method

JML Expressions \neq Java Expressions

boolean JML Expressions (to be completed)

- each side-effect free boolean JAVA expression is a boolean JML expression
- ▶ if a and b are boolean JML expressions, and x is a variable of type t, then the following are also boolean JML expressions:
 - ▶ !a ("not a")
 - ▶ a && b ("a and b")
 - ▶ a || b ("a or b")

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```
!a ("not a")
a && b ("a and b")
a || b ("a or b")
a ==> b ("a implies b")
a <==> b ("a is equivalent to b")
...
...
...
...
```

Beyond boolean Java expressions

How to express the following?

▶ an array arr only holds values ≤ 2

Beyond boolean Java expressions

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Beyond boolean Java expressions

How to express the following?

- ▶ an array arr only holds values ≤ 2
- ▶ the variable m holds the maximum entry of array arr
- ▶ all created instances of class BankCard have different cardNumbers

First-order Logic in JML Expressions

JML boolean expressions extend JAVA boolean expressions by:

- implication
- equivalence

First-order Logic in JML Expressions

JML boolean expressions extend JAVA boolean expressions by:

- ► implication
- equivalence
- quantification

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   a && b ("a and b")
   a || b ("a or b")
   a ==> b ("a implies b")
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   (\forall t x; a) ("for all x of type t, a holds")
   (\exists t x; a) ("there exists x of type t such that a")
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```
!a ("not a")
   a && b ("a and b")
   a => b ("a implies b")
   a <=> b ("a is equivalent to b")
   (\forall t x; a) ("for all x of type t, a holds")
   (\exists t x; a) ("there exists x of type t fulfilling a, b holds")
   (\exists t x; a; b) ("there exists an x of type t fulfilling a, such that b")
```

JML Quantifiers

```
in
(\forall t x; a; b)
(\exists t x; a; b)
a called "range predicate"
```

JML Quantifiers

```
in
(\forall\ t\ x:\ a:\ b)
(\exists t x; a; b)
a called "range predicate"
                     those forms are redundant:
                       (\forall t x; a; b)
                            equivalent to
                     (\forall t x; a \Longrightarrow b)
                       (\exists t x; a; b)
                            equivalent to
                      (\exists t x; a && b)
```

```
(\forall t x; a; b) and (\exists t x; a; b)
widely used
pragmatics of range predicate:
a used to restrict range of x further than t
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(\forall int i,j;
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example: "arr is sorted at indexes between 0 and 9":
(\forall int i,j; 0<=i && i<j && j<10;</pre>
```

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(\forall t x; a; b) and (\exists t x; a; b)
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pragmatics of range predicate:
a used to restrict range of x further than t
example: "arr is sorted at indexes between 0 and 9":
(\forall int i, j; 0<=i && i<j && j<10; arr[i] <= arr[j])</pre>
```

How to express:

▶ an array arr only holds values ≤ 2

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(\forall int i;

How to express:

▶ an array arr only holds values ≤ 2

(\forall int i; 0 <= i && i < arr.length;

How to express:

▶ an array arr only holds values ≤ 2

```
(\forall int i; 0 <= i && i < arr.length; arr[i] <= 2)
```

How to express:

▶ the variable m holds the maximum entry of array arr

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```
(\forall int i; 0 <= i && i < arr.length; m >= arr[i])
```

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```

is this enough?

How to express:

▶ the variable m holds the maximum entry of array arr

```
(\forall int i; 0 <= i && i < arr.length; m >= arr[i])
```

```
(\exists int i; 0 <= i && i < arr.length; m == arr[i])
```

How to express:

▶ the variable m holds the maximum entry of array arr

```
arr.length > 0 ==>
(\exists int i; 0 <= i && i < arr.length; m == arr[i])</pre>
```

(\forall int i; 0 <= i && i < arr.length; m >= arr[i])

How to express:

▶ all created instances of class BankCard have different cardNumbers

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```
(\forall BankCard p1, p2;
        \created(p1) && \created(p2);
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▶ JML quantifiers range also over non-created objects

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- ▶ in KeY?

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- JML quantifiers range also over non-created objects
- same for quantifiers in KeY!
- ▶ in JML, restrict to created objects with \created
- in KeY? (⇒ coming lecture)

Generalized Quantifiers

JML offers also generalized quantifiers:

- ▶ \max
- ▶ \min
- ▶ \product
- ▶ \sum

returning the maximum, minimum, product, or sum of the values of the expressions given, where the variables satisfy the given range.

Examples (all these expressions are true):

$$(\sum i) = 0 + 1 + 2 + 3 + 4$$

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Examples (all these expressions are true):

```
(\sum int i; 0 \le i \&\& i \le 5; i) == 0 + 1 + 2 + 3 + 4
(\product int i; 0 \le i \&\& i \le 5; i) == 1 * 2 * 3 * 4
```

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(\max int i; 0 <= i && i < 5; i) == 4
```

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Examples (all these expressions are true):

```
(\sum int i; 0 <= i && i < 5; i) == 0 + 1 + 2 + 3 + 4
(\product int i; 0 < i && i < 5; i) == 1 * 2 * 3 * 4
(\max int i; 0 <= i && i < 5; i) == 4
(\min int i; 0 <= i && i < 5; i-1) == -1
```

Example: Specifying LimitedIntegerSet

```
public class LimitedIntegerSet {
  public final int limit;
  private int arr[];
  private int size = 0;
  public LimitedIntegerSet(int limit) {
    this.limit = limit;
    this.arr = new int[limit];
  public boolean add(int elem) {/*...*/}
  public void remove(int elem) {/*...*/}
  public boolean contains(int elem) {/*...*/}
  // other methods
```

Prerequisites: Adding Specification Modifiers

```
public class LimitedIntegerSet {
 public final int limit;
 private /*@ spec_public @*/ int arr[];
 private /*@ spec_public @*/ int size = 0;
  public LimitedIntegerSet(int limit) {
    this.limit = limit;
    this.arr = new int[limit];
 public boolean add(int elem) {/*...*/}
 public void remove(int elem) {/*...*/}
 public /*@ pure @*/ boolean contains(int elem) {/*...*/}
  // other methods
```

Specifying contains()

```
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public /*@ pure @*/ boolean contains(int elem) {/*...*/}
has no effect on the state, incl. no exceptions
how to specify result value?
```

```
/*@ public normal_behavior
@ ensures \result ==
```

```
/*@ public normal_behavior
@ ensures \result == (\exists int i;
@
```

```
/*@ public normal behavior
  @ requires size < limit && !contains(elem);</pre>
  @ ensures \result == true:
  @ ensures contains(elem):
  @ ensures (\forall int e:
  0
                      e != elem:
                      contains(e) <==> \old(contains(e)));
    ensures size == \old(size) + 1;
  0
  @ also
  0
  @ <spec-case2>
  0*/
public boolean add(int elem) {/*...*/}
```

```
/*@ public normal behavior
  0
   <spec-case1>
  0
  @ also
  0
  @ public normal_behavior
  @ requires (size == limit) || contains(elem);
  @ ensures \result == false;
  @ ensures (\forall int e;
  0
                      contains(e) <==> \old(contains(e)));
  @ ensures size == \old(size);
  0*/
public boolean add(int elem) {/*...*/}
```

Specifying remove()

```
/*@ public normal_behavior
  @ ensures !contains(elem);
  @ ensures (\forall int e;
  0
                      e != elem;
  0
                      contains(e) <==> \old(contains(e)));
    ensures \old(contains(elem))
  0
            ==> size == \old(size) - 1:
   ensures !\old(contains(elem))
            ==> size == \old(size):
  0
  0*/
public void remove(int elem) {/*...*/}
```

So far:

JML used to specify method specifics.

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How to specify constraints on class data?

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JML used to specify method specifics.

How to specify constraints on class data, e.g.:

- consistency of redundant data representations (like indexing)
- restrictions for efficiency (like sortedness)

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JML used to specify method specifics.

How to specify constraints on class data, e.g.:

- consistency of redundant data representations (like indexing)
- restrictions for efficiency (like sortedness)

data constraints are global:

all methods must preserve them

Consider LimitedSortedIntegerSet

```
public class LimitedSortedIntegerSet {
  public final int limit;
  private int arr[];
  private int size = 0;
  public LimitedSortedIntegerSet(int limit) {
    this.limit = limit;
    this.arr = new int[limit];
  public boolean add(int elem) {/*...*/}
  public void remove(int elem) {/*...*/}
  public boolean contains(int elem) {/*...*/}
  // other methods
```

method contains

can employ binary search (logarithmic complexity)

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- why is that sufficient?
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method remove

(accordingly)

```
recall class fields:
   public final int limit;
   private int arr[];
   private int size = 0;
sortedness as JML expression:
```

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  public final int limit;
  private int arr[];
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sortedness as JML expression:
(\forall int i; 0 < i && i < size;
                  arr[i-1] <= arr[i])
(what's the value of this if size < 2?)
```

```
recall class fields:
  public final int limit;
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sortedness as JML expression:
(\forall int i; 0 < i && i < size;
                   arr[i-1] <= arr[i])
(what's the value of this if size < 2?)
but where in the specification does the red expression go?
```

Specifying Sorted contains()

can assume sortedness of pre-state

Specifying Sorted contains()

can assume sortedness of pre-state

Specifying Sorted contains()

can assume sortedness of pre-state

```
/*@ public normal_behavior
  @ requires (\forall int i; 0 < i && i < size;</pre>
  0
                                arr[i-1] <= arr[i]):
   ensures \result == (\exists int i:
                                   0 <= i && i < size;
  0
  0
                                   arr[i] == elem):
  @*/
public /*@ pure @*/ boolean contains(int elem) {/*...*/}
contains() is pure
⇒ sortedness of post-state trivially ensured
```

Specifying Sorted remove()

```
can assume sortedness of pre-state
must ensure sortedness of post-state
/*@ public normal_behavior
  @ requires (\forall int i; 0 < i && i < size;</pre>
  0
                                 arr[i-1] <= arr[i]):
   ensures !contains(elem):
    ensures (\forall int e;
  0
                       e != elem:
                       contains(e) <==> \old(contains(e)));
  0
    ensures \old(contains(elem))
  0
             ==> size == \old(size) - 1;
    ensures !\old(contains(elem))
             ==> size == \old(size);
  0
   ensures (\forall int i; 0 < i && i < size;</pre>
  0
                                arr[i-1] <= arr[i]);
  0*/
public void remove(int elem) {/*...
SEFM: Java Modeling Language
                                                        131001
                                                               57 / 80
```

```
/*@ public normal_behavior
  @ requires (\forall int i; 0 < i && i < size;</pre>
                               arr[i-1] <= arr[i]);
  0
  @ requires size < limit && !contains(elem);
  @ ensures \result == true;
  @ ensures contains(elem);
  @ ensures (\forall int e;
  0
                      e != elem:
  0
                      contains(e) <==> \old(contains(e)));
   ensures size == \old(size) + 1;
   ensures (\forall int i; 0 < i && i < size;
                              arr[i-1] <= arr[i]):
  0
  0
  @ also <spec-case2>
  0*/
public boolean add(int elem) {/*...*/}
```

```
/*@ public normal_behavior
  @ <spec-case1> also
  @
  @ public normal_behavior
  @ requires (\forall int i; 0 < i && i < size;</pre>
                               arr[i-1] <= arr[i]):
  0
  @ requires (size == limit) || contains(elem);
  @ ensures \result == false;
  @ ensures (\forall int e;
                      contains(e) <==> \old(contains(e)));
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  @ ensures size == \old(size);
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                              arr[i-1] <= arr[i]):
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public boolean add(int elem) {/*...*/}
```

Factor out Sortedness

so far: 'sortedness' has swamped our specification

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we can do better, using

JML Class Invariant

construct for specifying data constraints centrally

Factor out Sortedness

so far: 'sortedness' has swamped our specification

we can do better, using

JML Class Invariant

construct for specifying data constraints centrally

- 1. delete blue and red parts from previous slides
- 2. add 'sortedness' as JML class invariant instead

JML Class Invariant

```
public class LimitedSorted IntegerSet {
  public final int limit;
  /*@ public invariant (\forall int i;
    0
                                 0 < i && i < size:
                                 arr[i-1] <= arr[i]):
    0
    @*/
  private /*@ spec_public @*/ int arr[];
  private /*@ spec_public @*/ int size = 0;
  // constructor and methods.
  // without sortedness in pre/post-conditions
```

JML Class Invariant

- ▶ JML class invariant can be placed anywhere in class
- ► (contrast: method contract must be in front of its method)
- custom to place class invariant in front of fields it talks about

instance invariants

can refer to instance fields of this object
 (unqualified, like 'size', or qualified with 'this', like 'this.size')
JML syntax: instance invariant

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static invariants

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cannot refer to instance fields of this object
JML syntax: static invariant

both

can refer to

- static fields
- instance fields via explicit reference, like 'o.size'

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```

static invariants

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cannot refer to instance fields of this object
JML syntax: static invariant
```

both

can refer to

- static fields
- instance fields via explicit reference, like 'o.size'

in classes: instance is default (static in interfaces)

if instance or static is omitted ⇒ instance invariant!

Static JML Invariant Example

```
public class BankCard {
  /*@ public static invariant
    @ (\forall BankCard p1, p2;
         \created(p1) && \created(p2);
         p1 != p2 ==> p1.cardNumber != p2.cardNumber)
    0*/
  private /*@ spec_public @*/ int cardNumber;
  // rest of class follows
```

Recall Specification of enterPIN()

Recall Specification of enterPIN()

```
private /*@ spec_public @*/ BankCard insertedCard = null;
private /*@ spec_public @*/ int wrongPINCounter = 0;
private /*@ spec_public @*/ boolean customerAuthenticated
                                     = false;
/*@ <spec-case1> also <spec-case2> also <spec-case3>
  0*/
public void enterPIN (int pin) { ...
last lecture:
all 3 spec-cases were normal_behavior
```

normal_behavior specification case, with preconditions *P*, forbids method to throw exceptions if pre-state satisfies *P*

normal_behavior specification case, with preconditions P,
forbids method to throw exceptions if pre-state satisfies P
exceptional_behavior specification case, with preconditions P,
requires method to throw exceptions if pre-state satisfies P

```
{\tt normal\_behavior} specification case, with preconditions P, forbids method to throw exceptions if pre-state satisfies P
```

exceptional_behavior specification case, with preconditions P, requires method to throw exceptions if pre-state satisfies P

keyword signals specifies post-state, depending on thrown exception

normal_behavior specification case, with preconditions P,

keyword signals_only limits types of thrown exception

```
forbids method to throw exceptions if pre-state satisfies P

exceptional_behavior specification case, with preconditions P, requires method to throw exceptions if pre-state satisfies P

keyword signals specifies post-state, depending on thrown exception
```

Completing Specification of enterPIN()

Completing Specification of enterPIN()

```
/*@ <spec-case1> also <spec-case2> also <spec-case3> also
  @ public exceptional_behavior
   requires insertedCard==null;
  @ signals_only ATMException;
  @ signals (ATMException) !customerAuthenticated ;
  0*/
public void enterPIN (int pin) { ...
in case insertedCard==null in pre-state
  an exception must be thrown ('exceptional_behavior')
```

- it can only be an ATMException ('signals_only')
- method must then ensure !customerAuthenticated in post-state ('signals')

signals_only Clause: General Case

an exceptional specification case can have one clause of the form

signals_only
$$E_1, \ldots, E_n$$
;

where E_1, \ldots, E_n are exception types

signals_only Clause: General Case

an exceptional specification case can have one clause of the form

signals_only
$$E_1, \ldots, E_n$$
;

where E_1, \ldots, E_n are exception types

Meaning:

if an exception is thrown, it is of type E_1 or ... or E_n

signals Clause: General Case

an exceptional specification case can have several clauses of the form

where E is exception type, b is boolean expression

signals Clause: General Case

an exceptional specification case can have several clauses of the form

where E is exception type, b is boolean expression

Meaning:

if an exception of type E is thrown, b holds in post condition

Allowing Non-Termination

by default, both:

- normal_behavior
- exceptional_behavior

specification cases enforce termination

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in each specification case, non-termination can be permitted via the clause

diverges true;

Allowing Non-Termination

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specification cases enforce termination

in each specification case, non-termination can be permitted via the clause

diverges true;

Meaning:

given the precondition of the specification case holds in pre-state, the method may or may not terminate

Further Modifiers: non_null and nullable

JML extends the JAVA modifiers by further modifiers:

- class fields
- method parameters
- method return types

can be declared as

- nullable: may or may not be null
- non_null: must not be null

non_null: Examples

```
private /*@ spec public non null @*/ String name;
implicit invariant
'public invariant name != null;'
added to class
public void insertCard(/*@ non_null @*/ BankCard card) {...
implicit precondition
'requires card != null;'
added to each specification case of insertCard
public /*@ non_null @*/ String toString()
implicit postcondition
'ensures \result != null;'
added to each specification case of toString
```

non_null is default in JML!

⇒ same effect even without explicit 'non_null's

```
private /*@ spec_public @*/ String name;
implicit invariant
'public invariant name != null;'
added to class
public void insertCard(BankCard card) {...
implicit precondition
'requires card != null;'
added to each specification case of insertCard
public String toString()
implicit postcondition
'ensures \result != null;'
added to each specification case of toString
```

nullable: Examples

To prevent such pre/post-conditions and invariants: 'nullable'

```
private /*@ spec_public nullable @*/ String name;
no implicit invariant added

public void insertCard(/*@ nullable @*/ BankCard card) {..
no implicit precondition added

public /*@ nullable @*/ String toString()
no implicit postcondition added to specification cases of toString
```

```
public class LinkedList {
    private Object elem;
    private LinkedList next;
    ....
```

In JML this means:

```
public class LinkedList {
    private Object elem;
    private LinkedList next;
    ....
```

In JML this means:

▶ all elements in the list are non_null

```
public class LinkedList {
    private Object elem;
    private LinkedList next;
    ....
```

In JML this means:

- ▶ all elements in the list are non_null
- the list is cyclic, or infinite!

```
Repair:
```

```
public class LinkedList {
    private Object elem;
    private /*@ nullable @*/ LinkedList next;
    ....
```

⇒ Now. the list is allowed to end somewhere!

non_null as default in JML only since a few years.

⇒ Older JML tutorial or articles may not use the **non_null** by default semantics.

non_null as default in JML only since a few years.

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Pitfall!

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Pitfall!

```
/*@ non_null @*/ Object[] a;
is not the same as:
/*@ nullable @*/ Object[] a; //@ invariant a != null;
```

non_null as default in JML only since a few years.

⇒ Older JML tutorial or articles may not use the **non_null** by default semantics.

Pitfall!

```
/*@ non_null @*/ Object[] a;
is not the same as:
/*@ nullable @*/ Object[] a; //@ invariant a != null;
because the first one also implicitly adds
(\forall int i; i >= 0 && i < a.length; a[i] != null)
I.e. extends non_null also to the elements of the array!</pre>
```

JML and Inheritance

All JML contracts, i.e.

- specification cases
- class invariants

are inherited down from superclasses to subclasses.

A class has to fulfill all contracts of its superclasses.

in addition, the subclass may add further specification cases, starting with also:

```
/*@ also
    @
    @ <subclass-specific-spec-cases>
    @*/
public void method () { ...
```

Tools

Many tools support JML (see http://www.jmlspecs.org).

On the course website:

web interface, implemented by Bart van Delft, to OpenJML.

Many thanks to Bart!

Literature for this Lecture

essential reading:

in KeY Book A. Roth and Peter H. Schmitt: Formal Specification. Chapter 5 only sections 5.1, 5.3, In: B. Beckert, R. Hähnle, and P. Schmitt, editors. Verification of Object-Oriented Software: The KeY Approach, vol 4334 of LNCS. Springer, 2006. (e-version via Chalmers Library)

further reading, all available at

http://www.eecs.ucf.edu/~leavens/JML/documentation.shtml:

JML Reference Manual Gary T. Leavens, Erik Poll, Curtis Clifton, Yoonsik Cheon, Clyde Ruby, David Cok, Peter Müller, and Joseph Kiniry.

JML Reference Manual

JML Tutorial Gary T. Leavens, Yoonsik Cheon.

Design by Contract with JML

JML Overview Gary T. Leavens, Albert L. Baker, and Clyde Ruby.

JML: A Notation for Detailed Design