

Answers Sequent Calculus

$$\begin{array}{c}
 \text{close } \frac{}{p \Rightarrow p, q} \quad \text{close } \frac{}{p, q \Rightarrow q} \\
 \text{impLeft } \frac{}{p, p \rightarrow q \Rightarrow q} \\
 \text{andLeft } \frac{}{p \wedge (p \rightarrow q) \Rightarrow q} \\
 \text{impRight } \frac{}{\Rightarrow (p \wedge (p \rightarrow q)) \rightarrow q}
 \end{array}$$

$$\begin{array}{c}
 \text{close } \frac{}{p \Rightarrow p, q} \quad \text{close } \frac{}{p, q \Rightarrow q} \quad \text{close } \frac{}{q, p \rightarrow q \Rightarrow q} \\
 \text{impLeft } \frac{}{p, p \rightarrow q \Rightarrow q} \\
 \text{orLeft } \frac{}{p \vee q, p \rightarrow q \Rightarrow q} \\
 \text{andLeft } \frac{}{(p \vee q) \wedge (p \rightarrow q) \Rightarrow q} \\
 \text{impRight } \frac{}{\Rightarrow ((p \vee q) \wedge (p \rightarrow q)) \rightarrow q}
 \end{array}$$

$$\begin{array}{c}
 \text{close } \frac{}{p, q \Rightarrow p, r} \quad \text{close } \frac{}{p, q \Rightarrow q, r} \quad \text{close } \frac{}{p, q, r \Rightarrow r} \\
 \text{andRight } \frac{}{p, q \Rightarrow p \wedge q, r} \\
 \text{impLeft } \frac{}{(p \wedge q) \rightarrow r, p, q \Rightarrow r} \\
 \text{impRight } \frac{}{(p \wedge q) \rightarrow r, p \Rightarrow q \rightarrow r} \\
 \text{impRight } \frac{}{(p \wedge q) \rightarrow r \Rightarrow p \rightarrow (q \rightarrow r)} \\
 \text{impRight } \frac{}{\Rightarrow ((p \wedge q) \rightarrow r) \rightarrow (p \rightarrow (q \rightarrow r))}
 \end{array}$$

$$\begin{array}{c}
 \text{close } \frac{}{p \Rightarrow p, q} \quad \text{close } \frac{}{p, q \Rightarrow q} \\
 \text{impLeft } \frac{}{p \rightarrow q, p \Rightarrow q} \\
 \text{notRight } \frac{}{p \rightarrow q \Rightarrow \neg p, q} \\
 \text{orRight } \frac{}{p \rightarrow q \Rightarrow \neg p \vee q} \\
 \text{impRight } \frac{}{\Rightarrow (p \rightarrow q) \rightarrow (\neg p \vee q)}
 \end{array}$$

$$\begin{array}{c} \text{impRight} \frac{\text{orRight} \frac{\text{notLeft} \frac{\text{andRight} \frac{\text{notRight} \frac{\text{close} \frac{}{p \Rightarrow p, \neg q}}{\Rightarrow p, \neg p, \neg q} \quad \text{notRight} \frac{\text{close} \frac{}{q \Rightarrow \neg p, q}}{\Rightarrow q, \neg p, \neg q}}{\Rightarrow p \wedge q, \neg p, \neg q}}{\neg(p \wedge q) \Rightarrow \neg p, \neg q}}{\neg(p \wedge q) \Rightarrow \neg p \vee \neg q}}{\Rightarrow \neg(p \wedge q) \rightarrow (\neg p \vee \neg q)} \end{array}$$