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{-
This is a list of selected functions from the
standard Haskell modules: Prelude Data.List
Data.Maybe Data.Char Control.Monad
-} ---------------------------------------------
-- standard type classes

class Show a where
  show :: a -> String

class Eq a where
  (==), (/=) :: a -> a -> Bool

class (Eq a) => Ord a where
  (<), (<=), (>=), (>) :: a -> a -> Bool
  max, min             :: a -> a -> a

class (Eq a, Show a) => Num a where
  (+), (-), (*)    :: a -> a -> a
  negate           :: a -> a
  abs, signum      :: a -> a
  fromInteger      :: Integer -> a

class (Num a, Ord a) => Real a where
  toRational       ::  a -> Rational

class (Real a, Enum a) => Integral a where
  quot, rem        :: a -> a -> a
  div, mod         :: a -> a -> a
  toInteger        :: a -> Integer

class (Num a) => Fractional a where
  (/)              :: a -> a -> a
  fromRational     :: Rational -> a

class (Fractional a) => Floating a where
  exp, log, sqrt      :: a -> a
  sin, cos, tan       :: a -> a

class (Real a, Fractional a) => RealFrac a where
  truncate, round :: (Integral b) => a -> b
  ceiling, floor  :: (Integral b) => a -> b

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-- numerical functions

even, odd        :: (Integral a) => a -> Bool
even n           = n `rem` 2 == 0
odd              = not . even

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-- monadic functions
sequence     :: Monad m => [m a] -> m [a]
sequence     = foldr mcons (return [])
  where mcons p q = do x <- p
                       xs <- q
                       return (x:xs)

sequence_    :: Monad m => [m a] -> m ()
sequence_ xs = do sequence xs
                  return ()

liftM   :: (Monad m) => (a1 -> r) -> m a1 -> m r
liftM f m1   = do x1 <- m1
                  return (f x1)
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-- functions on functions
id              :: a -> a
id x            = x

const           :: a -> b -> a
const x _       = x

(.)             :: (b -> c) -> (a -> b) -> a -> c
f . g           = \ x -> f (g x)

flip            :: (a -> b -> c) -> b -> a -> c
flip f x y      = f y x

($)             :: (a -> b) -> a -> b
f $  x          = f x
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-- functions on Bools

data Bool = False | True

(&&), (||)       :: Bool -> Bool -> Bool
True  && x       = x
False && _       = False
True  || _       = True
False || x       = x

not              :: Bool -> Bool
not True         = False
not False        = True
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-- functions on Maybe

data Maybe a = Nothing | Just a

isJust                  :: Maybe a -> Bool
isJust (Just a)         =  True
isJust Nothing          =  False

isNothing               :: Maybe a -> Bool
isNothing               =  not . isJust

fromJust                :: Maybe a -> a
fromJust (Just a)       =  a

maybeToList             :: Maybe a -> [a]
maybeToList Nothing     =  []
maybeToList (Just a)    =  [a]

listToMaybe             :: [a] -> Maybe a
listToMaybe []          =  Nothing
listToMaybe (a:_)       =  Just a

catMaybes               :: [Maybe a] -> [a]
catMaybes ls            = [x | Just x <- ls]

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-- functions on pairs

fst             :: (a,b) -> a
fst (x,y)       =  x

snd             :: (a,b) -> b
snd (x,y)       =  y

swap            :: (a,b) -> (b,a)
swap (a,b)      = (b,a)
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curry           :: ((a, b) -> c) -> a -> b -> c
curry f x y     =  f (x, y)

uncurry         :: (a -> b -> c) -> ((a, b) -> c
uncurry f p     =  f (fst p) (snd p)

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-- functions on lists

map :: (a -> b) -> [a] -> [b]
map f xs = [ f x | x <- xs ]

(++) :: [a] -> [a] -> [a]
xs ++ ys = foldr (:) ys xs

filter :: (a -> Bool) -> [a] -> [a]
filter p xs = [ x | x <- xs, p x ]

concat :: [[a]] -> [a]
concat xss = foldr (++) [] xss

concatMap :: (a -> [b]) -> [a] -> [b]
concatMap f = concat . map f

head, last      :: [a] -> a
head (x:_)      = x

last [x]        = x
last (_:xs)     = last xs

tail, init      :: [a] -> [a]
tail (_:xs)     = xs

init [x]        = []
init (x:xs)     = x : init xs

null            :: [a] -> Bool
null []         = True
null (_:_)      = False

length          :: [a] -> Int
length          = foldr (const (1+)) 0

(!!)            :: [a] -> Int -> a
(x:_)  !! 0     = x
(_:xs) !! n     = xs !! (n-1)

foldr         :: (a -> b -> b) -> b -> [a] -> b
foldr f z []    =  z
foldr f z (x:xs) =  f x (foldr f z xs)

foldl         :: (a -> b -> a) -> a -> [b] -> a
foldl f z []    =  z
foldl f z (x:xs) =  foldl f (f z x) xs

iterate         :: (a -> a) -> a -> [a]
iterate f x     =  x : iterate f (f x)

repeat          :: a -> [a]
repeat x        =  xs where xs = x:xs

replicate       :: Int -> a -> [a]
replicate n x   =  take n (repeat x)

cycle           :: [a] -> [a]
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cycle []          =  error "Prelude.cycle: empty list"
cycle xs          =  xs' where xs' = xs ++ xs'

tails             :: [a] -> [[a]]
tails             = iterate tail

take, drop              :: Int -> [a] -> [a]
take n _      | n <= 0 =  []
take _ []              =  []
take n (x:xs)          =  x : take (n-1) xs

drop n xs     | n <= 0 =  xs
drop _ []              =  []
drop n (_:xs)          =  drop (n-1) xs

splitAt                :: Int -> [a] -> ([a],[a])
splitAt n xs           =  (take n xs, drop n xs)

takeWhile, dropWhile :: (a -> Bool) -> [a] -> [a]
takeWhile p []         =  []
takeWhile p (x:xs)
            | p x      =  x : takeWhile p xs
            | otherwise =  []

dropWhile p []         =  []
dropWhile p xs@(x:xs')
            | p x      =  dropWhile p xs'
            | otherwise =  xs

span :: (a -> Bool) -> [a] -> ([a], [a])
span p as = (takeWhile p as, dropWhile p as)

lines, words     :: String -> [String]
-- lines "apa\nbepa\ncepa\n"
--   == ["apa","bepa","cepa"]
-- words "apa  bepa\n cepa"
--   == ["apa","bepa","cepa"]

unlines, unwords :: [String] -> String
-- unlines ["apa","bepa","cepa"]
--       == "apa\nbepa\ncepa"
-- unwords ["apa","bepa","cepa"]
--       == "apa bepa cepa"

reverse           :: [a] -> [a]
reverse           =  foldl (flip (:)) []

and, or           :: [Bool] -> Bool
and               =  foldr (&&) True
or                =  foldr (||) False

any, all          :: (a -> Bool) -> [a] -> Bool
any p             =  or . map p
all p             =  and . map p

elem, notElem     :: (Eq a) => a -> [a] -> Bool
elem x            =  any (== x)
notElem x         =  all (/= x)

lookup      :: (Eq a) => a -> [(a,b)] -> Maybe b
lookup key []     =  Nothing
lookup key ((x,y):xys)
    | key == x    =  Just y
    | otherwise   =  lookup key xys

sum, product      :: (Num a) => [a] -> a
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sum               =  foldl (+) 0
product           =  foldl (*) 1

maximum, minimum :: (Ord a) => [a] -> a
maximum [] = error "Prelude.maximum: empty list"
maximum (x:xs) = foldl max x xs

minimum [] = error "Prelude.minimum: empty list"
minimum (x:xs) = foldl min x xs

zip               :: [a] -> [b] -> [(a,b)]
zip               =  zipWith (,)

zipWith           :: (a->b->c) -> [a]->[b]->[c]
zipWith z (a:as) (b:bs)
                  =  z a b : zipWith z as bs
zipWith _ _ _     =  []

unzip             :: [(a,b)] -> ([a],[b])
unzip             =
  foldr (\(a,b) ~(as,bs) -> (a:as,b:bs)) ([],[])

nub               :: Eq a => [a] -> [a]
nub []            = []
nub (x:xs)        =
          x : nub [ y | y <- xs, x /= y ]

delete            :: Eq a => a -> [a] -> [a]
delete y []       = []
delete y (x:xs)  =
       if x == y then xs else x : delete y xs

(\\)              :: Eq a => [a] -> [a] -> [a]
(\\)              = foldl (flip delete)

union             :: Eq a => [a] -> [a] -> [a]
union xs ys       = xs ++ (ys \\ xs)

intersect         :: Eq a => [a] -> [a] -> [a]
intersect xs ys   = [ x | x <- xs, x `elem` ys ]

intersperse       :: a -> [a] -> [a]
-- intersperse 0 [1,2,3,4] == [1,0,2,0,3,0,4]

transpose         :: [[a]] -> [[a]]
-- transpose [[1,2,3],[4,5,6]]
--    == [[1,4],[2,5],[3,6]]

partition   :: (a -> Bool) -> [a] -> ([a],[a])
partition p xs =
    (filter p xs, filter (not . p) xs)

group             :: Eq a => [a] -> [[a]]
group = groupBy (==)

groupBy :: (a -> a -> Bool) -> [a] -> [[a]]
groupBy _  []     =  []
groupBy eq (x:xs) =  (x:ys) : groupBy eq zs
                where (ys,zs) = span (eq x) xs

isPrefixOf :: Eq a => [a] -> [a] -> Bool
isPrefixOf []     _      =  True
isPrefixOf _      []     =  False
isPrefixOf (x:xs) (y:ys) =  x == y
                            && isPrefixOf xs ys
isSuffixOf :: Eq a => [a] -> [a] -> Bool
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isSuffixOf x y = reverse x `isPrefixOf` reverse

sort              :: (Ord a) => [a] -> [a]
sort              = foldr insert []

insert            :: (Ord a) => a -> [a] -> [a]
insert x []       = [x]
insert x (y:xs)   =
    if x <= y then x:y:xs else y:insert x xs

-----------------------------------------
-- functions on Char

type String = [Char]

toUpper, toLower :: Char -> Char
-- toUpper 'a' == 'A'
-- toLower 'Z' == 'z'

digitToInt :: Char -> Int
-- digitToInt '8' == 8

intToDigit :: Int -> Char
-- intToDigit 3 == '3'

ord :: Char -> Int
chr :: Int  -> Char

-----------------------------------------
-- Signatures of some useful functions
-- from Test.QuickCheck

arbitrary :: Arbitrary a => Gen a
-- the generator for values of a type
-- in class Arbitrary, used by quickCheck

choose :: Random a => (a, a) -> Gen a
-- Generates a random element in the given
-- inclusive range.

oneof :: [Gen a] -> Gen a
-- Randomly uses one of the given generators

frequency :: [(Int, Gen a)] -> Gen a
-- Chooses from list of generators with weighte
-- random distribution.

elements :: [a] -> Gen a
-- Generates one of the given values.

listOf :: Gen a -> Gen [a]
-- Generates a list of random length.

vectorOf :: Int -> Gen a -> Gen [a]
-- Generates a list of the given length.

sized :: (Int -> Gen a) -> Gen a
-- construct generators that depend on the size
meter.
```