# The Synchronization Power of Coalesced Memory Accesses

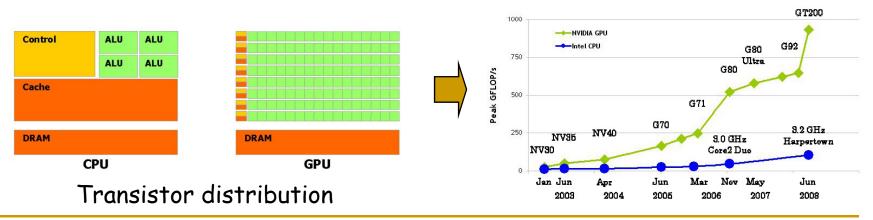
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## Problem

- Memory access mechanisms influence the system synchronization capability.
- Conventional wisdom: single-word assignment has consensus number 1

 $\Rightarrow$  stronger synch. primitives (e.g. TAS, FAA, CAS) added.

Can we make single-word assignment stronger?
 ⇒ transistors saved from strong synch. primitives can be used to enhance other functionality.



[These figures are from NVIDA CUDA Programming Guide, version 2.0] DISC'08

### What is a memory word?

A group of *n* bytes that can be stored or retrieved in a single, basic operation.
 *n* is called *word size* (in byte-addressable memory)

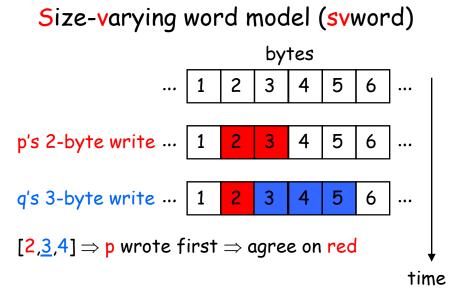


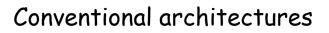
 Words of size *n* must always start at addresses that are multiples of *n*. (Alignment restriction)

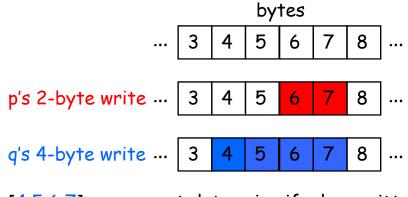
[Hamacher et al. 2002, Hennessy et al. 2003]

## Key idea 1

- Word size *n* can be any integer
  - instead of powers of 2 as in conventional architectures
  - Ex: solving 2-process consensus using 2-byte write and 3-byte write.
  - Feasibility: NVIDIA CUDA
    - int1, int2, int3, int4





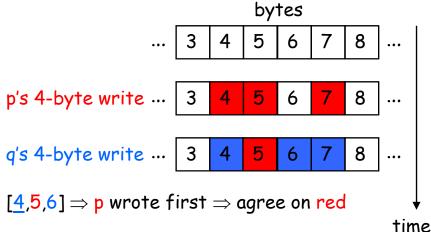


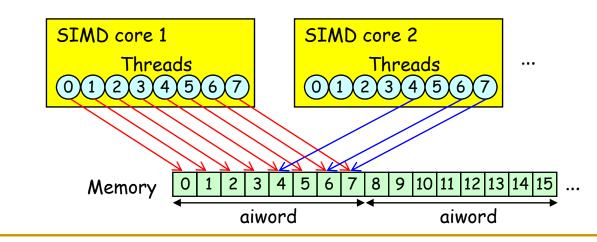
 $[4,5,\underline{6},\underline{7}] \Rightarrow q$  cannot determine if p has written!

### Key idea 2

- Some of the *n* bytes of a word may be left untouched in a single-word assignment.
  - Ex: solving 2-process consensus using 4-byte writes
  - Feasibility: NVIDIA CUDA
    - Coalesced memory accesses







#### Our main technical contributions

- Develop general models for coalesced memory accesses.
- Prove the exact consensus numbers of these models:
  - size-varying word model (svword)
  - aligned-inconsecutive word model (aiword)
  - the combination of these two models (asvword)



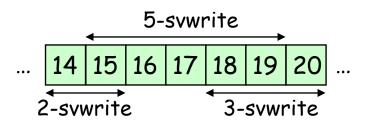
### Road-map

#### Size-varying word model (svword)

- Aligned-inconsecutive word model (aiword)
- The combination of these two models (asvword)

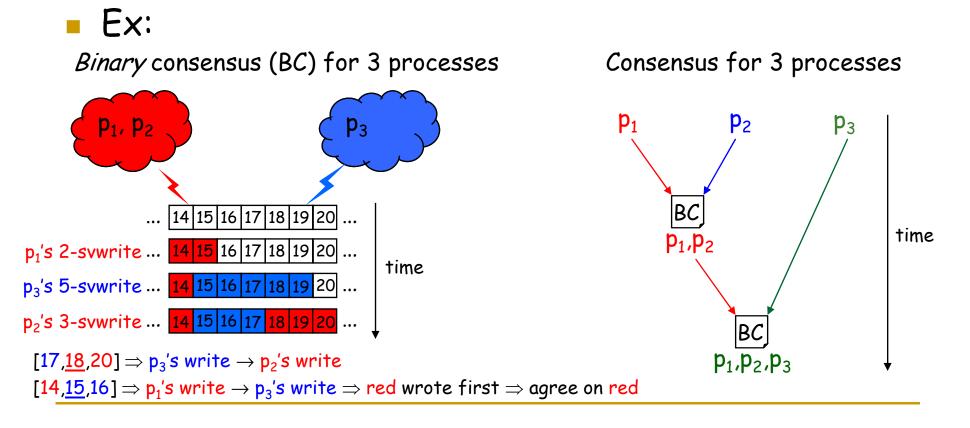
## Size-varying word model (svword)

- A syword consists of *b* consecutive memory units,
- $b \in [1, B], B$  is a constant.
  - *b*-svword for short
  - b-svwrite = b-svword assignment
- Alignment restriction:
  - Svwords of size b must start at addresses that are multiples of b.
- Ex: 2-svwrite, 3-svwrite and 5-svwrite



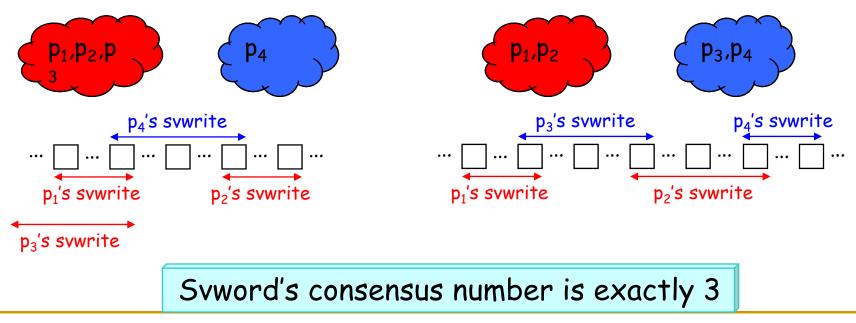
### Svword's consensus no. ≥ 3

- Idea:
  - □ 5-svwrite can partly overlap both 2-svwrite and 3-svwrite
  - $\Rightarrow$  can construct (binary) consensus objects for 3 processes



## Svword's consensus no. ≤ 3

- Idea
  - p's critical assignment must
    - write to p's private unit
    - partly overlap q's critical assignment if p's critical value ≠ q's critical value
       (Bivalency argument)
  - b-svwrite accesses consecutive units  $\Rightarrow$  each b-svwrite can partly overlap at most 2 other b-svwrites.



#### Road-map

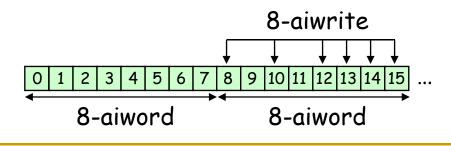
Size-varying word model (svword)

Aligned-inconsecutive word model (aiword)

The combination of these two models (asvword)

## Aligned-inconsecutive word (aiword)

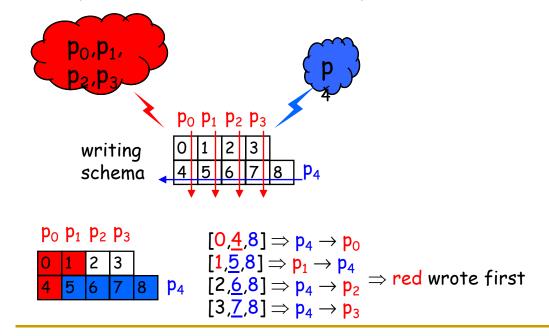
- Memory is aligned to *m*-unit words, *m* is a constant.
   *m*-aiword for short
- A read/write operation accesses an arbitrary non-empty subset of the *m* units of an aiword.
  - *m*-aiwrite = *m*-aiword assignment.
- Alignment restriction
  - $\square$  *m*-aiwords must start at addresses that are multiples of *m*.
- Ex: 8-aiwrite

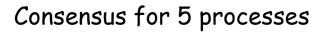


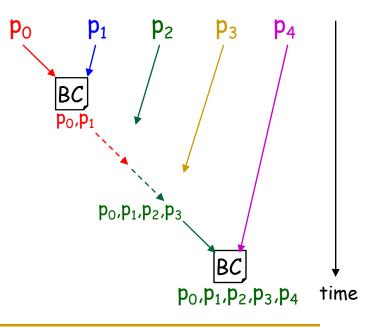
### *m*-aiword's consensus no. $\geq /(m+1)/2/$

- Idea:
  - Construct a *binary* consensus object for N=/(m+1)/2/ processes in which (N-1) processes propose the same value.
  - Construct a *multivalued* consensus object for N processes using the binary consensus object.
- Ex: 9-aiword

*Binary* consensus (BC) for 4+1 processes







### *m*-aiword's consensus no. $\leq /(m+1)/2/$

Idea:

- Lemma: p's critical assignment must atomically write to
  - $p'_i$ s own unit  $u_i$
  - shared units  $u_{i,j}$  written only by  $p_i$  and  $p_j$  where  $p'_i$ s critical value  $cv_i \neq p'_j$ s critical value  $cv_j$ .

(Bivalency argument)

⇒ solving consensus for 2 subsets  $S_1$  and  $S_2$ , where  $cv_1 \neq cv_2$ and  $n_1 + n_2 = N$ , needs to write atomically to *m* units, where  $m = N + n_1 n_2 \ge 2N - 1 \Rightarrow N \le (m+1)/2$ 

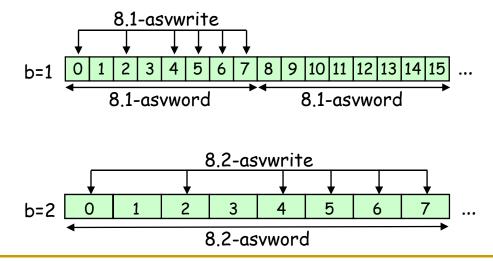
m-aiword's consensus number is exactly /(m+1)/2/

### Road-map

- Size-varying word model (svword)
- Aligned-inconsecutive word model (aiword)
- The combination of these two models (asvword)

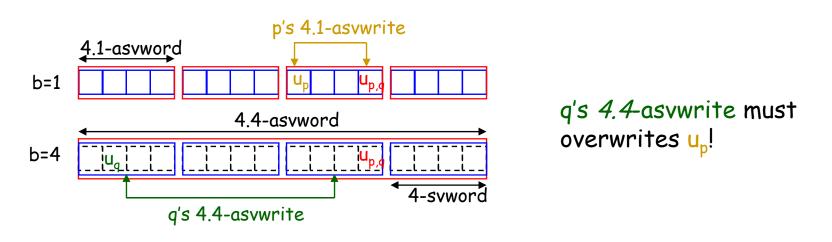
#### Asvword = aiword + svword

- An extension of *aiword*:
  - □ aiword's m units are replaced by m svwords of the same size  $b, b \in \{1, B\}$ .
  - m.b-asvword for short
  - m.b-asvwrite = m.b-asvword assignment
  - $m=t.B \text{ or } B=t.m, t \in N^*.$
- Alignment restriction
  - m.b-asywords must start at addresses that are multiples of (m.b).
- Ex: m=8, B=2:
  - 8.2-asvword vs. 8.1-asvword



## Asyword's consensus no. when $m \le B$

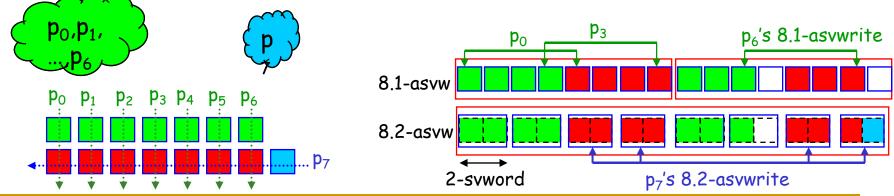
- Asvword's consensus number is |(m+1)/2|, like aiword's.
- Idea:
  - When B=t.m, t∈N\*, the combination of *m.1*-asvwrite and *m.B*-asvwrite does not provide any additional strength compared to *m*-aiwrite.
- Ex: B=m=4
  - $\square$  p and q write to  $u_p$ ,  $u_q$ ,  $u_{p,q}$  using 4.1-asymptotic and 4.4-asymptotic.



### Asvword's consensus no. when m>B

- Asvword's consensus number N
  - mB/2 if m=2tB,  $t \in N^*$
  - □ (*m*-*B*)*B*/2 if *m*=(2*t*+1)*B*
- Idea
  - Processes can atomically modify *m.B* units using *m.B*-asywrite vs. *m* units using *m*-aiwrite.
  - Avoid overwriting unintended units:
    - each B-syword contains either private units or shared units, but not both.
- Ex: m=8, B=2  $\Rightarrow$  N=8

*Binary* consensus (BC) for 7+1 processes



## Conclusions

- Develop new memory access models for coalesced memory accesses and prove their exact consensus numbers N.
  - □ size-varying word model, *b*-svword,  $b \in [1,B]$ .
    - N = 3, ∀ B ≥ 5
  - aligned-inconsecutive word model, *m*-aiword
    - N = |(m+1)/2

• the combination of these two models, *m.b*-asyword,  $b \in [1,B]$ .

$$N = \begin{cases} \left\lfloor \frac{m+1}{2} \right\rfloor & \text{if} \quad B = tm, t \in N \\ \frac{mB}{2} & \text{if} \quad m = 2tB \\ \frac{(m-B)B}{2} & \text{if} \quad m = (2t+1)B \end{cases}$$

Thanks for your attention!